



Table 1 Test conditions and selected results

Runs with $\alpha = 90^\circ$									
Run	$M_\infty$	$Re_\infty/m$ ( $\times 10^{-6}$ )	$Re_{ns}$	$T_0$ (K)	$T_{\text{wwd}}$ (K)	$T_{\text{wwd}}$ $T_{\text{lee}}$	$St_{\text{lee}}$ $\times 10^4$	$St_{\text{af}}$ $\times 10^3$	$\Delta/\delta \times 10^2$ (See note “a”, below)
2	12.8	1.85	570	2570	233	1.0	5.05	1.95	0.93
3	11.9	5.34	1710	2580	233	1.0	3.28	1.23	0.96
26	12.3	1.77	510	2410	478	1.62	5.61	2.54	1.00
27	11.8	5.21	1720	2640	794	2.72	3.79	1.59	1.32
28	12.2	1.67	510	2560	800	2.72	7.20	3.04	1.28
29	11.7	0.36	120	2540	800	2.72	13.4	6.02	1.27
30	15.7	1.90	360	2580	800	2.72	6.76	3.25	1.18
31	11.8	5.29	1750	2660	478	1.62	3.34	1.24	1.19
Runs with $\alpha = 30^\circ$									
1	12.3	1.85	570	2570	233	1.0	2.51	1.04	0.82
32	12.3	1.88	580	2540	811	2.72	3.87	1.56	1.20

<sup>a</sup> Boundary-layer parameters shown are for  $\phi = 90^\circ$  (Fig. 1).

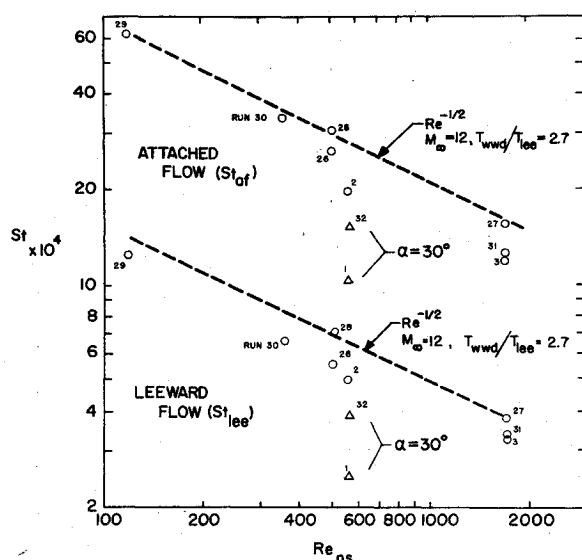


Fig. 2 Variation of Stanton numbers for attached flow at  $\phi = 90^\circ$  and for separated region ( $0 \leq \phi \leq 60^\circ$ ) with Reynolds number  $Re_{ns}$ .

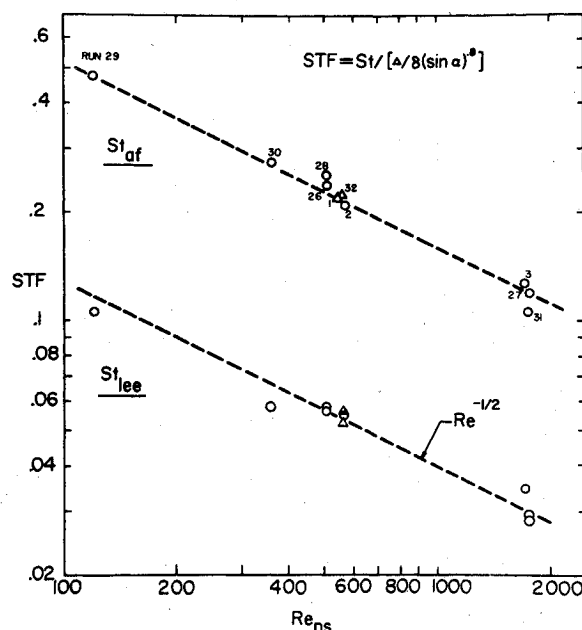


Fig. 3 Correlation of characteristic Stanton numbers with Reynolds number  $Re_{ns}$ . Data for  $\alpha = 30^\circ$  denoted by triangles.

runs 1 and 32 display, for a  $30^\circ$  angle of attack, the effect of an increase in  $T_{wwd}/T_{lee}$  from 1.0 to 2.72. In all these runs the approach Mach number was nominally 12. It is observed that heat transfer levels are lowered significantly as  $T_{wwd}/T_{lee}$  is decreased to unity; furthermore the effect of a smaller angle of attack is also to decrease heat transfer rates.

2) Runs 27, 28, and 29 display, for  $T_{wwd}/T_{lee} = 2.72$ , the influence of a 15-fold increase in  $Re_{ns}$ . The nominal approach Mach number was 12 for these runs. The Stanton number variation with Reynolds number appears to confirm the existence of both a laminar boundary layer and a laminar near wake for these approach flow conditions.

3) Runs 28 and 30 indicate, for  $T_{wwd}/T_{lee} = 2.72$ , the effect of an increase in approach Mach number from 12 to 16. This effect is seen to be small, which is not unexpected for a blunt body in hypersonic flow.

The influence of  $\alpha$  on windward heat transfer has been correlated previously<sup>5</sup> with a power-law relationship, viz.,  $St \sim (\sin \alpha)^n$  where  $1 \leq n \leq 1.5$ . Although limited, the present data for  $\alpha = 30^\circ$  suggest an exponent of  $n = 0.8$ . Correlation of the effect of  $T_{wwd}/T_{lee}$  is facilitated through the recognition that any variation in surface temperature affects the shape of the stagnation temperature profile within the viscous wall layer prior to separation. One can therefore devise an integral thickness parameter which reflects the difference between the actual  $T_0$  profile and some baseline profile, such as the Crocco profile in which stagnation temperature is proportional to velocity. Current boundary-layer computations, which are summarized in Table 1, suggest that the effect of the windward to leeward temperature ratio can be correlated by  $St \sim \Delta/\delta$  (see Nomenclature).

The foregoing correlation proposals are incorporated in the parameter  $STF = St / [\Delta/\delta(\sin \alpha)^n]$  which is shown as a function of  $Re_{ns}$  in Fig. 3. The correlation lines are given by  $STF_{lee}(Re)^{1/2} = 1.24$  and  $STF_{af}(Re)^{1/2} = 5.16$ . Dispersion of the data is characterized by mean deviations of 6% and standard deviations of 8%. Relative values of two levels of heat transfer in Fig. 3 are of interest although the actual ratios are known to be configuration dependent. The correlation equations show that  $St_{lee} \approx 0.24 St_{af}$  which compares with a value of 0.6 from Chapman's early theoretical model<sup>7</sup> for negligible boundary layer prior to separation.

## References

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<sup>3</sup>Penland, J.A., "Aerodynamic Characteristics of a Circular Cylinder at Mach Number 6.86 and Angles-of-Attack up to 90°," NACA, RML54A14, Washington, D.C., March 1954.

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<sup>5</sup>Beckwith, I.E. and Gallagher, J.J., "Local Heat Transfer and Recovery Temperature on a Yawed Cylinder at a Mach Number of 4.15 and High Reynolds Number," NASA TR R-104, Washington, D.C., 1961.

<sup>6</sup>Bertin, J.J., Lamb, J.P., Zickler, J.L., and Goodrich, W.D., "Flow Field Measurements for Space-Shuttle Related Cylindrical Configurations in Hypersonic Streams," AIAA Paper 72-294, San Antonio, Texas, 1972; see also "Heat Transfer Measurements for Cylindrical Configurations in Hypersonic Streams," *Journal of Spacecraft and Rockets*, Vol. 10, March 1973, pp. 217-218.

<sup>7</sup>Chapman, D.R., "A Theoretical Analysis of Heat Transfer in Regions of Separated Flow," NACA, TN 3792, Washington, D.C., Oct. 1956.

## Asymmetric Shock-Wave Oscillations on Spiked Bodies of Revolution

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### Nomenclature

$D$	= overall model diameter
$F$	= frequency
$p_1, p_2$	= pressure sensed by transducers 1 and 2
$p_{ns}$	= pressure downstream of normal shock
$p_\infty$	= stream static pressure
$S$	= Strouhal number
$T_o$	= wind-tunnel supply temperature
$u_\infty$	= freestream flow speed
$x$	= coordinate in stream direction
$y$	= coordinate normal to $x$
$(\quad)$	= time-averaged quantities
$\langle \quad \rangle$	= root-mean-square quantities

It is well known that the shock-wave configuration in front of "spiked" axisymmetric bodies in supersonic flow can be unstable.<sup>1,2</sup> This instability arises primarily in cases where the forebody geometry has a forward-facing step such as those found in supersonic inlet diffusers with conical centerbodies, or on blunt bodies with drag-reducing spikes. For certain ranges of forebody geometry and flow parameters<sup>3-5</sup> these configurations do not allow a steady-state shock shape capable of satisfying the momentum and continuity equations. As a result, the shock structure oscillates harmonically with a Strouhal number based on body diameter and stream speed which, characteristically, is of order 0.2. This oscillation has been termed a "catastrophic" or "E-oscillation." Until recently, the shock motion was thought limited to one degree of freedom in the radial direction; that is, the shock has been observed to move in an expanding-collapsing fashion symmetrically about the body axis. In this

Note, we report observations which imply a more complex motion such as would result from two or more degrees of freedom. Time-averaged and instantaneous surface pressure data presented should be of some interest also since they control the time-averaged drag, and since their prediction by theory is difficult at this juncture.

Experiments were performed in the Aeronutronic Ford Supersonic Wind Tunnel with a model, sketched in Fig. 1, which consisted of a sphere-cone-cone cylinder. In units of the cylinder afterbody diameter  $D$ , the hemisphere at the model tip had a  $0.05 D$  diam. The cone following it had a half-angle of  $20^\circ$  and the second cone a half-angle of  $80^\circ$ . The model was positioned at zero incidence in continuous flow at Mach  $3.02 \pm 0.02$  and supply temperature  $T_o$  of  $100^\circ\text{F}$ . The Reynolds number based on  $D$  and freestream properties varied from 40,000 to 150,000 and the model wall temperature was nearly equal to  $T_o$ .

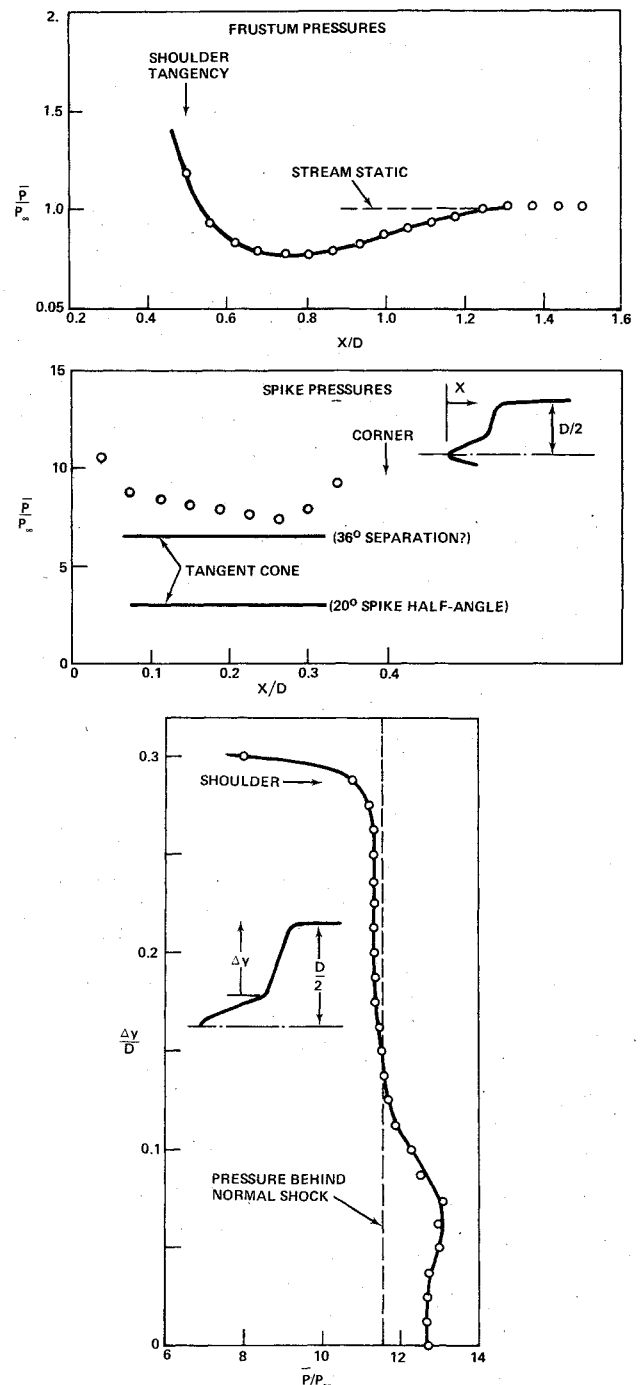


Fig. 1 Time-averaged surface pressure distribution over the spike, front "face" and frustum of the model.

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Index categories: Supersonic and Hypersonic Flow; Shock Waves and Detonations.

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