

Studies on the Proton Magnetic Resonance Spectra in Aromatic Systems. III.<sup>1)</sup>  
Discussions on the Substituent Shielding Parameter and  
 $\pi$ -Electron Charge Density

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(Received July 24, 1967)

The revised substituent shielding parameter has been proposed in *ortho* and *meta*  $^1\text{H}$  shift for estimating the  $\pi$ -electron charge densities in substituted benzene series, and, also the resonance contribution has been proved to be a dominant factor in determining the *meta*  $^1\text{H}$  shift.

The  $\pi$ -electron charge density calculated from simple sum rule of the revised shielding parameter showed passable agreement with those from HMO treatment.

In the previous communication,<sup>1)</sup> the authors examined the correlations among substituent shielding parameter in mono-substituted benzene series *vs.*  $\pi$ -electron charge density and proposed the revised shielding parameter appropriate to obtain  $\pi$ -electron charge density without mathematical treatment. These parameters have been proved reliable for  $\pi$ -electron charge density estimation in poly-substituted benzene series.

In the present study, the authors examined the correlations among revised substituent shielding parameter and  $\pi$ -electron density, *etc.* and estimated the revised shielding parameter for each substituent.

### Discussion

#### 1) On the Substituent Shielding Parameter and $\pi$ -Electron Charge Density

Formerly, Corio and Dailey<sup>3)</sup> estimated the aromatic ring  $^1\text{H}$  chemical shift in *ortho*, *meta* and *para* positions, and a few years ago, Martin, Dailey,<sup>4)</sup> Spiesecke, Schneider,<sup>5)</sup> and Diehl<sup>6)</sup> obtained more accurate results from their advanced experiments. And, for the physical organic treatment of above parameters, the correlations *vs.* Hammett constants  $\sigma_I$  and  $\sigma_R$  have been investigated from several groups of workers.<sup>6-9)</sup>

Recently, Schaefer, *et al.*<sup>10)</sup> have estimated from their elegant experiment the magnitude of aromatic  $^1\text{H}$  chemical shift per one  $\pi$ -electron as below:

$$\delta = 10.7 \pm 0.2 \text{ ppm}/e \cdot \Delta\rho$$

where  $\delta = ^1\text{H}$  chemical shift

$\Delta\rho =$  excess charge density

- 1) Y. Sasaki and M. Suzuki, *Chem. Pharm. Bull.* (Tokyo), **15**, 1429 (1967).
- 2) Location: Toneyama, Toyonaka, Osaka.
- 3) P.L. Corio and B.P. Dailey, *J. Am. Chem. Soc.*, **78**, 3043 (1956).
- 4) J.S. Martin and B.P. Dailey, *J. Chem. Phys.*, **39**, 1722 (1963).
- 5) H. Spiesecke and W.G. Schneider, *J. Chem. Phys.*, **37**, 731 (1961).
- 6) P. Diehl, *Helv. Chim. Acta*, **44**, 829 (1961).
- 7) Y. Yukawa, *et al.*, *Memories of Sci. and Ind. Res. Inst. Osaka University*, **17**, 185 (1960).
- 8) R.W. Taft Jr., *J. Phys. Chem.*, **64**, 1805 (1960).
- 9) Y. Yukawa and Y. Tsuno, *Bull. Chem. Soc. Japan*, **32**, 960 (1963).
- 10) T. Schaefer and W.G. Schneider, *Can. J. Chem.*, **4**, 966 (1963).

And the derived charge density from above equation has been compatible with those from HMO calculation in electron releasing substituent groups—for example, anisole, aniline, *etc.* In our previous treatment<sup>1)</sup>, the revised shielding parameters have been estimated from following reasons.

i)  $d_p$ —The shielding parameter in *para* position—is mainly controled from the resonance factor transmitted by  $\pi$ -electron framework, and in this position the contribution of inductive factor transmitted through 5  $\sigma$ -bonds could be ignored.<sup>5)</sup>

ii)  $d_m$ —The magnitude of which is within  $\pm 0.2$  ppm—is dependent on inductive, resonance and magnetic anisotropy effects to a certain extent, and in some molecule—for instance, nitrobenzene—the contribution from “electric field effect”<sup>11)</sup> shows good coincidence. Consequently, the contribution from  $\pi$ -electron charge in  $d_m$  has been neglected in view of  $\rho_m/\rho_p$  relation.

iii)  $d_o$ —The shielding parameter in *ortho* position—is controled mainly from the resonance effect as well as magnetic anisotropy effect, *etc.* and in this case, the inductive contribution transmitted through 3  $\sigma$ -bonds remains unsettled.

In conclusion, as the so-called shielding parameter does not always reflect  $\pi$ -electron charge density, we can't correlate both directly.

## 2) $\pi$ -Electron Charge Density and Revised Shielding Parameter

Formerly,  $\pi$ -electron charge densities in monosubstituted benzene series have been calculated by HMO method from several groups of workers.<sup>12-19)</sup> In the preceding communication,<sup>1)</sup>  $\rho_o/\rho_p$ <sup>20)</sup> and  $\rho_m/\rho_p$  relations have been examined and definite correlations have been confirmed. On the other hand,  $d_o/d_p$ <sup>21)</sup> relation shows nearly the same gradient with  $\rho_o/\rho_p$ , especially in electron releasing substituent groups. Consequently, in the above case, we are able to assume  $d_o/d_p, \rho_o/\rho_p$ . Nevertheless, in electron attracting substituent group,  $d_o/d_p$  relation deviates markedly in the low field site, and the deviations from above extention line have been attributed to sum of factors other than  $\pi$ -electron charge. Moreover,  $d_m/d_p$  relation seems to be irregular, but general trend is somewhat interesting. Then, if  $d_o/d_p, d_m/d_p$  relations were revised approximately equal to  $\rho_o/\rho_p, \rho_m/\rho_p$  the following correlations would be satisfied. Namely,

$$d_o/d_p \doteq \rho_o/\rho_p$$

$$d_m/d_p \doteq \rho_m/\rho_p$$

According to the above assumption, the substituent shielding parameter for  $\rho$  value estimation has been revised in the previous study.<sup>1)</sup>

In this work, the correlations among these shielding parameter— $d_p$  and revised  $d_o$ —and  $\sigma_\pi$ <sup>22)</sup> have been examined, and a linear relation, comparable with those from several calculated  $\pi$ -electron density  $\rho_{\text{calcd}}$ ,<sup>14,19,23)</sup> has been observed (*cf.* Fig. 1,2).

- 11) A.D. Puckingham, *Can. J. Chem.*, **38**, 300 (1960).
- 12) K. Fukui, T. Yonezawa, C. Nagata, H. Kato, A. Imamura, K. Morokuma, “Introduction to Quantum Chemistry,” Kagaku Dojin, Kyoto, 1964, p. 152, 177, 624.
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- 14) H. Baba and H. Suzuki, *J. Chem. Phys.*, **32**, 1706 (1960).
- 15) C. Sandorfy, *Bull. Soc. Chim. France*, **16**, 615 (1949).
- 16) K. Nishimoto and R. Fujishiro, *Bull. Chem. Soc. Japan*, **31**, 1036 (1958).
- 17) A. Azumi, “Quantum Chemistry,” Baifukan, Tokyo, 1960, p. 248.
- 18) A. Streitwieser, “Molecular Orbital Theory for Organic Chemists,” John-Wiley and Sons, 1961, p. 353.
- 19) T.K. Wu and B.P. Dailey, *J. Chem. Phys.*, **41**, 2796 (1964).
- 20)  $\rho = \pi$ -electron charge density;  $o = ortho$ ,  $m = meta$ ,  $p = para$ , respectively.
- 21)  $d =$  substituent shielding parameter;  $o = ortho$ ,  $m = meta$ ,  $p = para$ , respectively.
- 22) Y. Yukawa and Y. Tsuno, *Nippon Kagaku Zasshi*, **86**, 873 (1965).
- 23) K. Nishimoto, *Theoretica Chimica Acta*, **7**, 207 (1967).

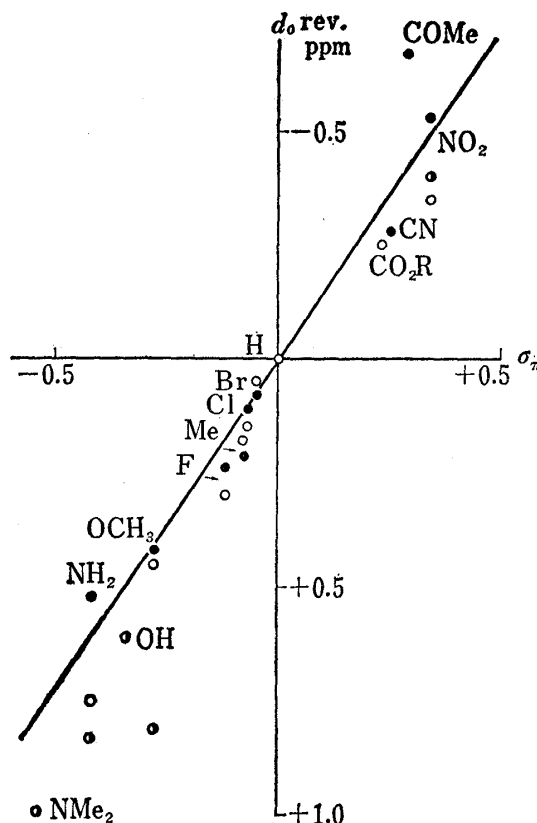
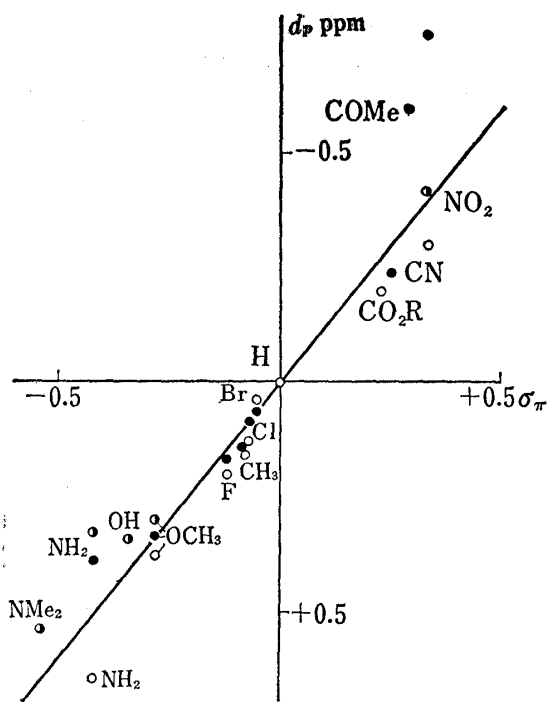


Fig. 1

Fig. 2

○ :  $d_p$  and  $d_o$  rev.,<sup>1)</sup> respectively      ● : T.K. Wu, B.P. Dailey<sup>19)</sup>  
 △ : H. Baba, S. Suzuki<sup>14)</sup>                      ● : K. Nishimoto<sup>23)</sup>  
 All shifts except shielding parameters are calculated by the following equation.  
 $\delta = 10.7 \times \Delta\rho$  ppm where  $\Delta\rho =$  calculated excess charge  
 The lines from the least square method in  $d_p$  and  $d_o$  rev.<sup>1)</sup> are slid to pass the origin. The deviations from the line in  $d_p$  and  $d_o$  rev. are corrected, and the shielding parameters in Table I are estimated.

In the next place,  $d_m/d_p$  relation shown in the previous communication<sup>1)</sup> signifies an interesting evidence—namely, even in *meta* position, the resonance contribution in the opposite direction should be taken into account, contrary to the results of HMO calculation. This conclusion has been confirmed also in *para*-substituted anisole and toluene, 1-substituted 3,4-dimethoxybenzene (cf. Fig. 3,4), respectively.

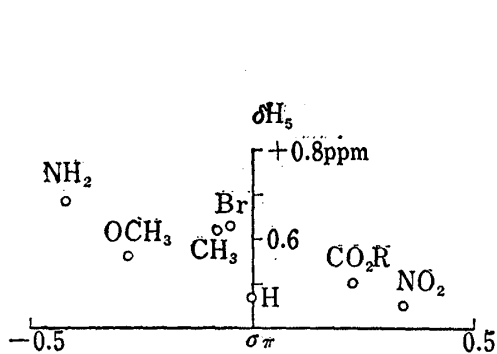


Fig. 3. H-5 Shift in 1-Substituted 3,4-Dimethoxybenzene Series vs.  $\sigma_\pi$

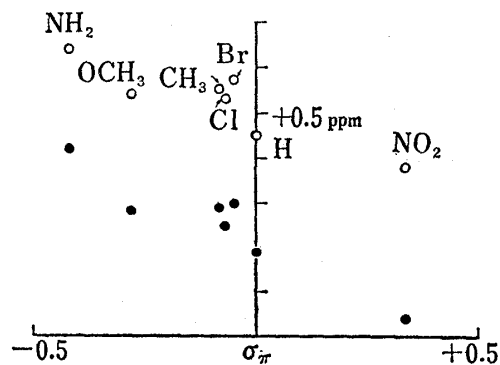
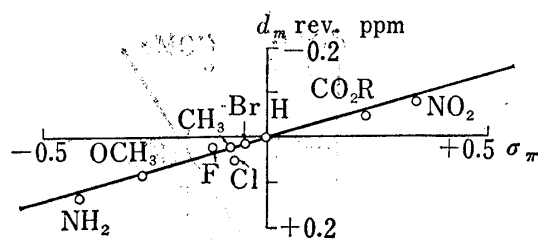


Fig. 4. H-2 and H-6 Shift in *para*-Substituted Anisole (○), Toluene (●) Series vs.  $\sigma_\pi$

Then we have examined the linear correlation among  $d_m/d_p$  and estimated the revised *meta* shielding parameter  $d_m$  rev. (cf. Table I), which is also linear with  $\sigma_\pi$  (cf. Fig. 5).

Fig. 5.  $d_m$  rev. vs.  $\sigma_\pi$ 

Thus, from the correlation among  $d_p$ ,  $d_o$  rev. and  $d_m$  rev. vs.  $\sigma_\pi$ , we are able to propose tentatively the revised three parameters for each substituent groups by interpolation as below (cf. Table I).

These mutual correlations described above are summarized graphically in the following (cf. Fig. 6).

TABLE I. Revised Shielding Parameter (ppm)

	$d_o$ rev.	$d_m$ rev.	$d_p$ rev.		$d_o$ rev.	$d_m$ rev.	$d_p$ rev.
$N(CH_3)_2$	+0.78	+0.15	+0.65	$C_6H_5$	+0.13	+0.03	+0.11
$NH_2$	+0.61	+0.12	+0.50	$NO_2$	-0.49	-0.09	-0.40
$OH$	+0.58	+0.09	+0.41	$COCH_3$	-0.42	-0.08	-0.34
$OCH_3$	+0.43	+0.08	+0.34	$SO_2CH_3$	-0.40	-0.08	-0.33
$CH_3$	+0.12	+0.03	+0.10	$SO_2NH_2$	-0.37	-0.07	-0.31
$C_2H_5$	+0.11	+0.02	+0.09	$CN$	-0.36	-0.07	-0.30
$t-C_4H_9$	+0.08	+0.02	+0.07	$CF_3$	-0.34	-0.06	-0.29
$F$	+0.17	+0.04	+0.15	$CO_2R$	-0.33	-0.06	-0.27
$Cl$	+0.11	+0.02	+0.09	$SOCH_3$	-0.16	-0.03	-0.13
$Br$	+0.08	+0.02	+0.07	$N^+Me_3$	-0.19	-0.03	-0.15

The shielding parameters— $d_o$  rev.,  $d_m$  rev. and  $d_p$  rev. which are not determined from experimental shift, have been estimated by interpolation in Fig. 1, 2 and 5.

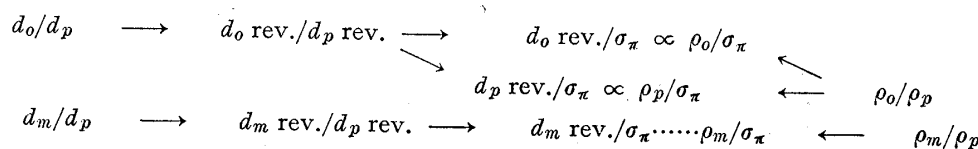


Fig. 6

As illustrated in Fig. 1 and 2, the correspondence among  $d_p$  rev. and  $d_o$  rev. in Table I vs. shift calculated from excess charge in HMO treatment<sup>14,19,23</sup>) has been compared, and apparent discrepancies have been observed in the latter, though the general trends are very similar.

In conclusion, the correlation  $d_o$  rev./ $\sigma_\pi$ ,  $d_p$  rev./ $\sigma_\pi$  are nearly proportional with those of  $\rho_o/\sigma_\pi$ ,  $\rho_p/\sigma_\pi$ , but it is self-evident that  $d_m$  rev./ $\sigma_\pi$  is not with  $\rho_m/\sigma_\pi$  (cf. Fig. 1,2). Namely, in the present step, these discrepancies are somewhat apparent, but will be settled by the more refined calculation in the near future.

### 3) Simple Sum Rule of Revised Shielding Parameter and $\pi$ -Electron Charge Density

In the previous papers of this series,<sup>24</sup>) the ring  $^1H$  chemical shift in poly-substituted benzene series has been shown by simple sum of substituent shielding parameter. Namely, the perturbation among substituent affects little in estimating ring  $^1H$  chemical shift. From above fact, the following schemes are proposed.

$$\begin{array}{l}
 d_A = \pi\text{-Factor A} + \text{Another Factor A} \\
 d_B = \pi\text{-Factor B} + \text{Another Factor B} \\
 \vdots \\
 d_Z = \pi\text{-Factor Z} + \text{Another Factor Z}
 \end{array}$$

$$d_{(A+B+\dots+Z)} = \pi\text{-Factor}(A+B+\dots+Z) + \text{Another Factor}(A+B+\dots+Z)$$

where  $d_A, d_B, \dots, d_Z$  = shielding parameter of substituent, A, B, ..., Z.  $\pi$ -Factor A, B, ..., Z = re-

24) Y. Sasaki, M. Suzuki, T. Hibino, and K. Karai, *Chem. Pharm. Bull.* (Tokyo), **15**, 599 (1967); Y. Sasaki, M. Suzuki, A. Shimazu (Hoshi), and A. Misaki, *ibid.*, **15**, 1083 (1967).

vised shielding parameter of substituent, A, B,..., Z, Another Factor A, B,..., Z=contribution other than  $\pi$ -electron charge density.

In the following, we have compared both  $\pi$ -electron densities from revised shielding parameter and HMO method in several series of compounds (*cf.* Table II, III, IV, V, VI), and the apparent discrepancies have been observed in *meta* position.

TABLE II.  $\pi$ -Electron Densities in Methoxybenzene Series

OCH <sub>3</sub> position	H position	$\rho_{\text{calcd}}^{25)}$	$\rho_{\text{nmr}}$	OCH <sub>3</sub> position	H position	$\rho_{\text{calcd}}^{25)}$	$\rho_{\text{nmr}}$	
1	2, 6	1.040	1.042	1, 2, 4	3	1.079	1.088	
	3, 5	0.998	1.008		5	1.066	1.079	
	4	1.030	1.032		6	1.037	1.050	
1, 2	3, 6	1.040	1.048	2, 4, 6	1, 3, 5	1.109	1.112	
	4, 5	1.025	1.039		1, 2, 3, 4	5, 6	1.064	1.087
1, 3	2	1.082	1.080	1, 2, 3, 5	4, 6	1.106	1.120	
	4, 6	1.068	1.072		1, 2, 4, 5	3, 6	1.078	1.095
	5	0.996	1.015			2, 3, 4, 5, 6	1	1.104
1, 4	2, 3, 5, 6	1.037	1.048					
1, 2, 3	4, 6	1.066	1.080					
	5	1.024	1.047					

TABLE III.  $\pi$ -Electron Densities in Mono-substituted Benzene Series

Substituent		$\rho_{\text{calcd}}^{19)}$	$\rho_{\text{nmr}}$	Substituent		$\rho_{\text{calcd}}^{19)}$	$\rho_{\text{nmr}}$
NH <sub>2</sub>	<i>p</i>	1.03667	1.0467	Br	<i>p</i>	1.00542	1.0065
	<i>m</i>	0.99773	1.0112		<i>m</i>	0.99964	1.0019
	<i>o</i>	1.04843	1.0635		<i>o</i>	1.00728	1.0075
OCH <sub>3</sub>	<i>p</i>	1.03063	1.0318	I	<i>p</i>	1.00331	1.004
	<i>m</i>	0.9902	1.0075		<i>m</i>	0.99982	1.000
	<i>o</i>	1.04138	1.0403		<i>o</i>	1.00423	1.004
F	<i>p</i>	1.01583	1.0140	NO <sub>2</sub>	<i>p</i>	0.92860	0.9618
	<i>m</i>	0.99875	1.0037		<i>m</i>	0.99499	0.9916
	<i>o</i>	1.02270	1.0159		<i>o</i>	0.95045	0.9542
CH <sub>3</sub>	<i>p</i>	1.01331	1.0094	CHO	<i>p</i>	0.95269	0.976
	<i>m</i>	0.99888	1.0028		<i>m</i>	1.00146	1.000
	<i>o</i>	1.01982	1.0112		<i>o</i>	0.94596	0.972
Cl	<i>p</i>	1.0075	1.0084				
	<i>m</i>	0.99947	1.0019				
	<i>o</i>	1.01042	1.0103				

TABLE IV.  $\pi$ -Electron Densities in Symmetrically *para*-Disubstituted Benzene Series

Substituent	$\rho_{\text{calcd}}^{19)}$	$\rho_{\text{nmr}}$	Substituent	$\rho_{\text{calcd}}^{19)}$	$\rho_{\text{nmr}}$
NH <sub>2</sub>	1.04536	1.0747	Br	1.00689	1.0094
OCH <sub>3</sub>	1.03879	1.0477	I	1.00403	1.005
F	1.02134	1.0192	NO <sub>2</sub>	0.95315	0.9458
CH <sub>3</sub>	1.01855	1.0140	CHO	0.95069	0.967
Cl	1.00984	1.0122			

25) A. Zweig, J.E. Lehnsen, J.E. Lancaster, and M.T. Neglia, *J. Am. Chem. Soc.*, **85**, 3940 (1963).

TABLE V.  $\pi$ -Electron Densities in Hydroxy Substituted Benzene Series

OH position	H position	$\rho_{\text{calcd}}$		$\rho_{\text{nmr}}$
		J.C. Schug J.C. Deck <sup>26)</sup>	R. Fujishiro K. Nishimoto <sup>27)</sup>	
1	2, 6	1.0990	1.075 <sup>28)</sup>	1.0532
	3, 5	0.9968	0.990	1.0084
	4	1.0831	1.038	1.0383
1, 4	2, 6, 3, 5	1.0928	1.036	1.0626
1, 2	3, 6	1.1187	1.038	1.0626
	4, 5	1.0768	1.026	1.0467
1, 3	2	1.2117	1.107	1.1082
	4, 6	1.1711	1.024	1.0925
	5	0.9928	1.030	1.0169
1, 2, 3	4, 6	1.1704		1.1090
	5	1.0694		1.0552
1, 3, 5	2, 4, 6		1.103	1.1485
1, 2, 4, 5	3, 6		1.037	1.1252

TABLE VI.  $\pi$ -Electron Densities in Cyano Substituted Benzene Series

CN position	H position	$\rho_{\text{calcd}}$		$\rho_{\text{nmr}}$
		H.E. Popkie J.B. Moffat <sup>29)</sup>		
1	2, 6	0.9892		0.9764
	3, 5	0.9880		0.9935
	4	0.9904		0.9720
1, 2	3, 6	0.9878		0.9599
	4, 5	0.9891		0.9655
1, 3	2	0.9790		0.9332
	4, 6			0.9383
	5	0.9963		0.9869
1, 4	2, 3, 5, 6	0.9878		0.9599
1, 2, 4, 5	3, 6	0.9771		0.9195

### Conclusion

In substituted benzene series, the  $\pi$ -electron charge density estimated from the revised substituent shielding parameter showed good correspondence with those from HMO method, except *meta* position, and in the present step it is concluded that  $\pi$ -electronic effect is a dominant factor in determining the ring  $^1\text{H}$  shift, and the contribution from the so-called "electric field effect" in *meta* position is doubtful. In addition, the anomalous *meta*  $^1\text{H}$  shifts observed in halogen series are somewhat puzzling.

**Acknowledgement** The authors express their grateful thanks to Prof. Dr. Y. Yukawa and Assoc. Prof. Dr. Y. Tsuno, Scientific and Industrial Research Institute, Osaka University, Assoc. Prof. Dr. K. Nishimoto, Dept. of Chemistry, Faculty of Science, Osaka City University and Assoc. Prof. Dr. T. Ikenoue, Chemical Institute of Non-Aqueous Solutions, Tohoku University for their valuable advice and criticism.

26) J.C. Schug and J.C. Deck, *J. Chem. Phys.*, **37**, 2618 (1962). HMO

27) R. Fujishiro and K. Nishimoto, *Bull. Chem. Soc. Japan*, **32**, 699 (1959). HMO

28) K. Nishimoto, *Theoret. Chim. Acta*, **5**, 74 (1966). S.C.F.

29) H.E. Popkie and J.B. Moffat, *Can. J. Chem.*, **43**, 624 (1965). S.C.F.