

## Variation in the Molecular Weight Distribution of Polyvinylpyrrolidone by Ball-Milling

NOBUYOSHI KANENIWA and AKIKO IKEKAWA

*School of Pharmaceutical Sciences, Showa University<sup>1)</sup>*

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Variation in the molecular weight distribution of polyvinylpyrrolidone (PVP) by ball-milling in various kinds of atmosphere in the absence and in the presence of various kinds of organic and inorganic additives was investigated.

A line broken at several points was obtained by the logarithmic plot of  $-\log R$  versus the molecular weight of PVP,  $M_u$ , and equation (1) was applied in the limited range of  $M_u$ , respectively, where  $R$  was the ratio of the weight of the polymers of molecular weight above  $M_u$  to the total weight of the polymers, and  $k$  and  $n$  were parameters dependent on the experimental conditions and so on.

$$R = \exp(-kM_u^n) \quad (1)$$

The existence of the critical molecular weight,  $M_c$ , was observed, at the region of  $M_u$  below which  $n$  was larger than 1.0 and formation of the polymers of  $M_u$  below  $M_c$  was considered to become more difficult with a decrease of  $M_u$ . The value of  $M_c$  was below  $4 \times 10^5$  and varied remarkably by the kind of the additive and by the ball-milling atmosphere.

Theoretical consideration was made on the molecular weight distribution of the polymers formed by chain scission of polymers by application of the mechanical stress, by assuming that chain scission was produced by activation of the bonds between atoms of the main chain by the mechanical stress and that these activated bonds were distributed at random and obeyed to Poisson's distribution law. It was suggested from the consideration mentioned above and from the investigation of the value of  $n$  in equation (1) and of the variation of  $R$  with the ball-milling time that, in many cases, random chain scission was most probable and that the density of the activated bonds over a polymer of low molecular weight was approximately equal to or higher than the density over a polymer of high molecular weight.

**Keywords**—organic and inorganic additives; ball-milling atmosphere; Poisson's distribution law; the mean density of the activated bonds over a polymer,  $\gamma$ ; the critical molecular weight,  $M_c$ ; the parameter  $n$  in equation (1); the parameters,  $\gamma_1$  and  $\gamma_2$  in equation (17); random chain scission

In the previous papers, polyvinylpyrrolidone (PVP) was ball-milled in various kinds of atmosphere in the presence of various kinds of organic and inorganic additives, and it was clarified that a decrease of molecular weight of PVP by ball-milling was influenced by the presence of the additive or by the ball-milling atmosphere.<sup>2,3)</sup>

In this paper, variation in the molecular weight distribution of PVP by ball-milling was investigated, and dependence of the variation on the presence of the additive or the ball-milling atmosphere was discussed.

### Theoretical

It is well known that Rosin-Rammler's law expressed by equation (1) applies well to the particle size distribution of the crushed powders, where  $R$  is the ratio of the weight of

1) Location: Hatanodai 1-5-8, Shinagawa-ku, Tokyo.

2) N. Kaneniwa and A. Ikekawa, *Chem. Pharm. Bull.* (Tokyo), **21**, 1539 (1973).

3) N. Kaneniwa and A. Ikekawa, *Chem. Pharm. Bull.* (Tokyo), **25**, 1534 (1977).

the particles of the size above  $x$  to the total weight of the particles,  $x_e$  is the particle size for which  $R$  is equal to  $1/e$ , and  $k$  and  $n$  are the parameters dependent on the ball-milling condition and so on.<sup>4,5)</sup>

$$R = \exp(-kx^n) = \exp\{-(x/x_e)^n\} \quad (1)$$

Equation (1) is expressed by equation (2), when  $n$  is equal to 1.0.

$$R = \exp(-kx) = \exp\{-(x/x_e)\} \quad (2)$$

Gilvarry obtained equation (2) theoretically on the basis of the assumption that fracture of brittle solids was produced by activation of the flaws or cracks existent in a solid prior to application of the stress system, and that these activated points were distributed at random and obeyed to Poisson's distribution law.<sup>6)</sup>

Here, it is assumed that chain scission is produced by activation of a part of the bonds between atoms of the main chains by application of the mechanical stress to the polymers. It is also assumed that these activated bonds are distributed at random, that the density of the activated bonds over a polymer molecule is extremely small and that the activated bonds conform to Poisson's distribution law. By application of Gilvarry's discussion to the scission of the chains of the polymers by the mechanical stress under the assumptions mentioned above, equation (3) is obtained, where  $W(M)$  is the cumulative weight of the fragments with molecular weight up to  $M$  produced by applying mechanical stress to a polymer of the weight of  $W_0$ , and  $\gamma$  represents the mean density of the activated bonds over a polymer molecule.<sup>6)</sup>

$$1 - W(M)/W_0 = e^{-\gamma M} \quad (3)$$

On the other hand, equation (4) is obtained by substituting  $M$  for  $x$  in equation (1).

$$R = \exp(-kM^n) = \exp\{-(M/M_e)^n\} \quad (4)$$

In equation (4),  $R$  is the ratio of the cumulative weight of the fractions of molecular weight above  $M$  to the total weight of the polymers, and  $M_e$  is the molecular weight for which  $R$  is equal to  $1/e$ . Equation (4) is identical with equation (3), if  $n$  is equal to 1.0 and  $\gamma$  is equal to  $1/M_e$ .

In the actual case, many polymer molecules of a wide molecular weight distribution are treated mechanically at the same time. Now,  $M_i$  is the molecular weight of the polymers of the  $i$ th fraction obtained by fractionating the original polymers according to the molecular weight. The mean density of the activated bonds over a polymer is expressed as a function of  $M_i$ ,  $\gamma(M_i)$ , if the mean density depends on the molecular weight of the original polymer, though they are distributed at random on one polymer. In this case, equation (5) is applied, where  $\phi_{M_i}$  is the number of moles of the polymers of the molecular weight of  $M_i$  in the original material.

$$R = 1 - W(M)/W_0 = \frac{\sum_i \phi_{M_i} M_i e^{-\gamma(M_i) \cdot M}}{\sum_i \phi_{M_i} \cdot M_i} \quad (5)$$

## Results and Discussion

In the previous paper, the relation between molecular weight by viscometry,  $M_v$ , and intrinsic viscosity was obtained for the  $\text{KH}_2\text{PO}_4$ - $\text{Na}_2\text{HPO}_4$  buffer solution of PVP of  $M_v$  between  $7.5 \times 10^3$  and  $10^6$ , and in this paper, the value of  $M_v$  of PVP was obtained by viscometry using this relation.<sup>7)</sup>

In the previous papers, PVP K90 was ball-milled in various kinds of atmosphere in the absence of the additive or in the presence of various kinds of organic or inorganic additives,

4) K. Matsui, *Funsai*, No. 16, 68 (1971).

5) P.O. Rosin and E. Rammler, *Kolloid-Z.*, **67**, 16 (1934).

6) J.J. Gilvarry, *J. Appl. Phys.*, **32**, 391 (1961).

7) N. Kaneniwa and A. Ikekawa, *Chem. Pharm. Bull.* (Tokyo), **20**, 1536 (1972).

and a decrease of  $M_n$  by ball-milling was investigated.<sup>2,3,7)</sup> These samples were fractionated by Sepharose 6B and the mean molecular weight of PVP in the  $i$ th fraction,  $M_{ni}$ , was measured, and the variation in the molecular weight distribution of PVP was investigated.

In case of ball-milling in air, the peak in the molecular weight distribution curve shifted from the molecular weight of approximately  $10^6$  to lower molecular weight with the lapse of the ball-milling time in the presence of white alundum, *p*-hydroquinone or barbituric acid.<sup>2)</sup> This tendency was also observed in the presence of the fine powders of activated charcoal. But in case of the addition of the other powders or in the absence of the additive, the original peak at the molecular weight around  $10^6$  decreased, a new peak appeared at the lower molecular weight and increased by ball-milling.<sup>2)</sup>

The similar phenomenon was also observed in case of ball-milling in the atmosphere other than air, as shown in Fig. 1 and 2. In case of ball-milling in nitrogen in the presence of phenothiazine or ball-milling in the presence of chloranil in oxygen containing small quantity of the vapor of distilled water, the peak shifted from the molecular weight of approximately  $10^6$  to lower molecular weight with the lapse of the ball-milling time. But in the other cases, the peak at the molecular weight around  $10^6$  decreased, a new peak appeared at the lower molecular weight and increased by ball-milling. The above finding seems to suggest that there is a characteristic pattern in the way how the chains of PVP molecules are broken by ball-milling. Then, the variation of molecular weight of PVP by ball-milling was investigated.

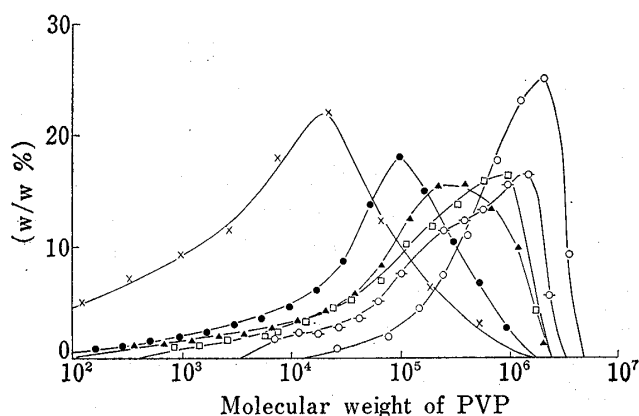


Fig. 1. Variation in Molecular Weight Distribution of PVP by Ball-Milling in Nitrogen in the Presence of 10 w/w % of Phenothiazine

$J_b=0.22, J_s=0.06^{(3)}$  (referred to Table I).

Ball-milling time (hr).

○, 0; -○-, 93; □, 115; ▲, 140; ●, 175; ×, 211.

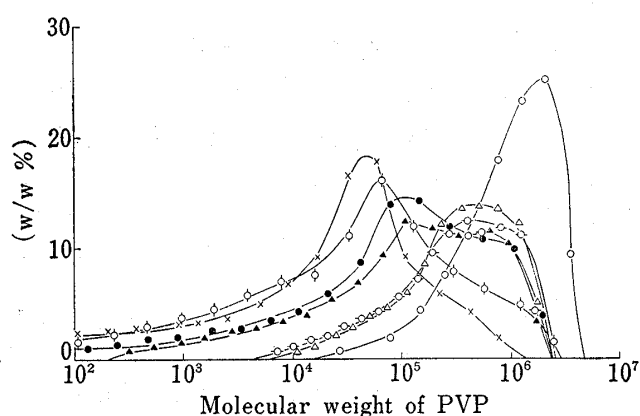


Fig. 2. Variation in Molecular Weight Distribution of PVP by Ball-Milling in Nitrogen in the Presence of 10 w/w % of Vitamin K<sub>3</sub>

$J_b=0.22, J_s=0.06^{(3)}$  (referred to Table I).

Ball-milling time (hr).

○, 0; -○-, 125; △, 145; ▲, 166; ●, 189; ○, 222; ×, 251.

### 1) A Decrease of $M_e$ by Ball-Milling

As shown in Fig. 3, a line broken at two or three points was obtained by the logarithmic plot of  $-\log R$  versus  $M_u$  obtained by equation (6).

$$M_u = (M_{\eta_i} \cdot M_{\eta_{i+1}})^{1/2} \quad (6)$$

$$M_{\eta_i} > M_{\eta_{i+1}}$$

As shown in Fig. 4,  $M_e$  obtained by reading the value of  $M_u$  for  $R$  of  $1/e$  on the  $\log(-\log R) - \log M_u$  line decreased gradually by ball-milling. In case of the addition of vitamin K<sub>3</sub>,  $M_e$  was larger than  $M_n$  at the first stage and smaller than  $M_n$  at the last stage of ball-milling. (Fig. 5). The same tendency was also observed in case of the addition of zinc oxide, activated charcoal, talc or acridine, but this tendency was not so remarkable as the tendency in Fig. 5. In the other cases,  $M_e$  was identical or parallel to  $M_n$ , and the difference between them was small.

As shown in Fig. 6, equation (7) was applied to a decrease of  $M_e$  by ball-milling in the wide range of  $M_e$ , where  $t_{ie}$  was the induction period after the lapse of which  $M_e$  began to decrease,  $t$  was the ball-milling time, and  $k_{me}$  and  $\beta_e$  were the parameters dependent on the kind of the additive, ball-milling atmosphere and so on.

$$\begin{aligned} t \leq t_{ie} & \quad -dM_e/dt = 0 \\ t > t_{ie} & \quad -dM_e/dt = k_{me}M_e^{\beta_e} \end{aligned} \quad (7)$$

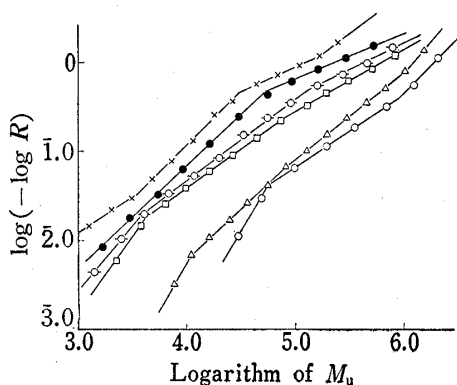


Fig. 3. Relation between  $R$  and  $M_u$  for PVP Ball-Milled in Nitrogen in the Presence of 10 v/v % of Talc

$J_b=0.22, J_s=0.06^{2.3}$  (referred to Table I).  
Ball-milling time (hr).  
○, 0; △, 72; □, 103; -○-, 133; ●, 169; ×, 201.

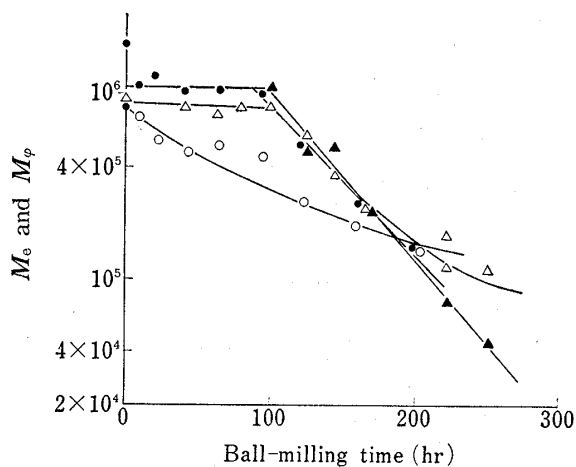


Fig. 5. Comparison of  $M_e$  with  $M_\gamma$  for PVP Ball-Milled in the Presence of 10 w/w % of Vitamin  $K_3$

$J_b=0.22, J_s=0.06^{2.3}$  (referred to Table I).  
Ball-milling atmosphere  $M_e$   $M_\gamma$   
Nitrogen ▲ △  
Air ● ○

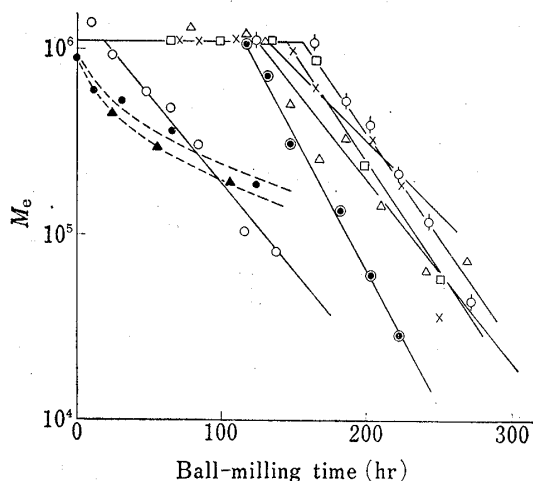


Fig. 4. Decrease of  $M_e$  of PVP by Ball-Milling in the Presence of Activated Charcoal (AC) in Various Kinds of Atmosphere

$J_b=0.22, J_s=0.06^{2.3}$  (referred to Table I).  
Kind of AC Content of AC (w/w %) Ball-milling atmosphere  
●, Absent Nitrogen.  
▲, Absent Air.  
⊙, Granules 10  $N_2(H_2O)$ .  
△, Granules 10  $N_2(H_2O_2)$ .  
□, Granules 15.1 Air.  
○, Fine powders 10 Air.  
×, Granules 15.1 Oxygen.  
⊙, Granules 10  $O_2(H_2O)$ .

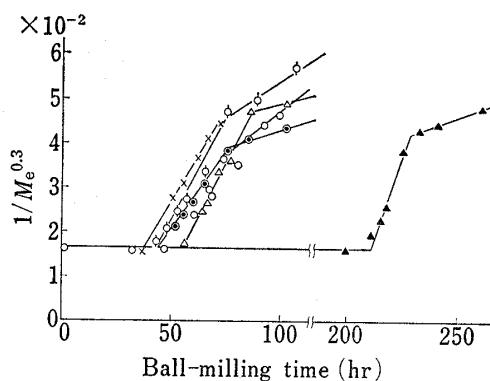


Fig. 6. Application of Equation (7) to a Decrease of  $M_e$  by Ball-Milling in the Presence of Chloranil in Various Kinds of Atmosphere

$J_b=0.43, J_s=0.03^{3.0}$  (referred to Table I).  
Weight content of chloranil (w/w %) Ball-milling atmosphere  
⊙, 5  $N_2(H_2O)$ .  
△, 5  $N_2(H_2O_2)$ .  
○, 5 Air.  
▲, 10 Air.  
×, 5  $O_2$ .  
⊙, 5  $O_2(H_2O)$ .

It was reported in the previous paper that the same relation as equation (7) was applied to a decrease of  $M_n$  by ball-milling, though the parameters  $t_i$ ,  $M_n$ ,  $k$  and  $\beta$  were in place of  $t_{ie}$ ,  $M_e$ ,  $k_{me}$  and  $\beta_e$ , respectively.<sup>2)</sup> Table I, II, III and IV show the numerical values of the parameters  $\beta_e$ ,  $t_{ie}$ ,  $k_{me}$ ,  $\beta$ ,  $t_i$  and  $k$ . The values of  $\beta$ ,  $t_i$  and  $k$  were quoted from the data in the previous papers.<sup>2,3)</sup> In case of the addition of vitamin K<sub>3</sub>,  $\beta_e$  was smaller than  $\beta$ , and this phenomenon seemed to be due to the fact in Fig. 5. In case of ball-milling in air in the presence of vitamin K<sub>3</sub>, methylene blue or phenothiazine,  $t_{ie}$  was much larger than  $t_i$ . This fact suggests that the polymers of low molecular weight formed at the first stage of ball-milling largely influence on the viscosity of the aqueous solution of the ball-milled sample. But, in the other cases, the values of  $t_{ie}$  and  $\beta_e$  were similar to those of  $t_i$  and  $\beta$ , respectively. These facts seem to suggest that the values of molecular weight obtained by viscometry reported in the previous paper<sup>7)</sup> are adequate, in spite of the wide range of molecular weight.

TABLE I. Numerical Values of  $\beta_e$ ,  $t_{ie}$ ,  $k_{me}$ ,  $\beta$ ,  $t_i$  and  $k$  for Ball-Milling of PVP in the Presence of 10 v/v % of Inorganic Additives

$$J_b^{(a)}=0.22, J_s^{(b)}=0.06^{2,3,7)}$$

Additive	Atmosphere	$\beta_e$	$t_{ie}$ (hr)	$k_{me}$ (hr <sup>-1</sup> )	$\beta$	$t_i$ (hr)	$k$ (hr <sup>-1</sup> )
Absent	Nitrogen	1.3	0	$2.3 \times 10^{-4}$	1.3	0	$3.0 \times 10^{-4}$
	Air	1.3	0	$2.7 \times 10^{-4}$	1.0	0	$1.6 \times 10^{-2}$
White alundum (type 40)	Nitrogen	1.6	0	$3.9 \times 10^{-5}$	1.3	0	$6.7 \times 10^{-4}$
	Air	1.4	0	$1.3 \times 10^{-3}$	1.5	0	$5.9 \times 10^{-5}$
Silica sands (type 3)	Nitrogen	1.0	0	$2.4 \times 10^{-2}$	1.3	0	$3.1 \times 10^{-4}$
	Air	1.5	0	$3.6 \times 10^{-5}$	1.9	0	$4.7 \times 10^{-7}$
Zinc oxide	Nitrogen	1.0	38	$2.1 \times 10^{-2}$	1.4	35	$9.3 \times 10^{-5}$
	Air	1.5	55	$4.9 \times 10^{-5}$	1.5	40	$2.6 \times 10^{-5}$
Barium sulfate	Air	1.3	34	$6.1 \times 10^{-4}$	1.4	0	$1.0 \times 10^{-4}$
Sodium chloride	Nitrogen	1.3	30	$6.1 \times 10^{-4}$	1.3	0	$3.3 \times 10^{-4}$
	Air	1.3	32	$8.3 \times 10^{-4}$	1.2	12	$2.0 \times 10^{-3}$
Granules of activated charcoal	Air	1.0	152	$2.5 \times 10^{-2}$	1.0	147	$2.4 \times 10^{-2}$
Talc	Nitrogen	1.3	42	$6.3 \times 10^{-4}$	1.4	24	$2.1 \times 10^{-4}$
	Air	1.0	66	$2.6 \times 10^{-2}$	1.0	30	$1.6 \times 10^{-2}$

a) The ratio of the apparent volume of balls in the mill to the capacity of the mill.

b) The ratio of the apparent volume of the samples in loose packing in the mill to the capacity of the mill.

TABLE II. Numerical Values of  $\beta_e$ ,  $t_{ie}$ ,  $k_{me}$ ,  $\beta$ ,  $t_i$  and  $k$  for Ball-Milling of PVP in the Presence of 10 w/w % of Organic Additives

$$J_b=0.22, J_s=0.06^{2,3)} \text{ (referred to Table I)}$$

Additive	Atmosphere	$\beta_e$	$t_{ie}$ (hr)	$k_{me}$ (hr <sup>-1</sup> )	$\beta$	$t_i$ (hr)	$k$ (hr <sup>-1</sup> )
Vitamin K <sub>3</sub>	Nitrogen	1.0	103	$2.0 \times 10^{-2}$	1.4	104	$1.4 \times 10^{-4}$
	Air	1.0	90	$1.9 \times 10^{-2}$	1.6	0	$4.3 \times 10^{-6}$
Acridine	Nitrogen	1.0	112	$2.2 \times 10^{-2}$	1.0	115	$1.8 \times 10^{-2}$
	Air	1.0	28	$2.2 \times 10^{-2}$	1.1	0	$6.2 \times 10^{-3}$
Methylene blue	Air	1.0	60	$3.1 \times 10^{-2}$	1.1	0	$4.7 \times 10^{-3}$
Phenothiazine	Nitrogen	1.0	87	$2.2 \times 10^{-2}$	0.74	70	$5.0 \times 10^{-1}$
	Air	1.0	105	$1.1 \times 10^{-2}$	1.0	40	$9.4 \times 10^{-3}$
<i>p</i> -Hydroquinone	Nitrogen	1.0	0	$1.7 \times 10^{-2}$	1.0	0	$1.6 \times 10^{-2}$
	Air	1.5	0	$4.1 \times 10^{-5}$	1.5	0	$3.7 \times 10^{-5}$
Barbituric acid	Nitrogen	1.3	0	$1.7 \times 10^{-3}$	1.4	0	$2.1 \times 10^{-4}$
	Air	1.4	0	$2.1 \times 10^{-4}$	1.5	0	$6.6 \times 10^{-5}$

TABLE III. Numerical Values of  $\beta_e$ ,  $t_{ie}$ ,  $k_{me}$ ,  $\beta$ ,  $t_i$  and  $k$  for Ball-Milling PVP in the Presence of Activated Charcoal (AC) in Various Kinds of Atmosphere  
 $J_b=0.22, J_s=0.06^{2,3)}$  (referred to Table I)

Content of AC	Kind of AC	Atmosphere	$\beta_e$	$t_{ie}$ (hr)	$k_{me}$ (hr <sup>-1</sup> )	$\beta$	$t_i$ (hr)	$k$ (hr <sup>-1</sup> )
10% w/w	Granules	N <sub>2</sub> (H <sub>2</sub> O) <sup>a)</sup>	1.0	116	$3.4 \times 10^{-2}$	1.0	110	$2.7 \times 10^{-2}$
10% w/w	Granules	N <sub>2</sub> (H <sub>2</sub> O <sub>2</sub> ) <sup>a)</sup>	1.0	130	$2.6 \times 10^{-2}$	1.0	107	$1.7 \times 10^{-2}$
10% v/v <sup>b)</sup>	Granules	Air	1.0	152	$2.5 \times 10^{-2}$	1.0	147	$2.6 \times 10^{-2}$
10% v/v <sup>b)</sup>	Granules	O <sub>2</sub>	1.0	142	$2.2 \times 10^{-2}$	1.0	192	$2.4 \times 10^{-2}$
10% w/w	Granules	O <sub>2</sub> (H <sub>2</sub> O) <sup>a)</sup>	1.0	164	$3.0 \times 10^{-2}$	2.0	167	$1.0 \times 10^{-7}$
10% w/w	Fine powders	Air	1.0	26	$2.4 \times 10^{-2}$	1.0	0	$2.5 \times 10^{-2}$

- a) N<sub>2</sub>(H<sub>2</sub>O), in nitrogen containing the vapor of distilled water with the vapor pressure of 17 mmHg;  
 N<sub>2</sub>(H<sub>2</sub>O<sub>2</sub>), in nitrogen containing the vapor of 30 w/w of the aqueous solution of hydrogen peroxide with the vapor pressure of 15 mmHg;
- O<sub>2</sub>(H<sub>2</sub>O), in oxygen containing the vapor of distilled water with the vapor pressure of 16 mmHg.
- b) 10 v/v % = 15.1 w/w %, (v/v % by true volume).

TABLE IV. Numerical Values of  $\beta_e$ ,  $t_{ie}$ ,  $k_{me}$ ,  $\beta$ ,  $t_i$  and  $k$  for Ball-Milling PVP in the Presence of Chloranil in Various Kinds of Atmosphere  
 $J_b=0.43, J_s=0.03^{3)}$  (referred to Table I)

Weight content of chloranil (%)	Atmosphere	$\beta_e$	$t_{ie}$ (hr)	$k_{me}$ (hr <sup>-1</sup> ) <sup>a)</sup>	$\beta$	$t_i$ (hr)	$k$ (hr <sup>-1</sup> ) <sup>b)</sup>
5	N <sub>2</sub> (H <sub>2</sub> O) <sup>c)</sup>	1.2	44	$2.2 \times 10^{-3}$	1.2	45	$4.3 \times 10^{-3}$
5	N <sub>2</sub> (H <sub>2</sub> O <sub>2</sub> ) <sup>c)</sup>	1.4	55	$3.5 \times 10^{-3}$	1.1	56	$3.8 \times 10^{-3}$
5	Air	1.2	55	$3.5 \times 10^{-3}$	1.2	47	$3.8 \times 10^{-3}$
5	O <sub>2</sub>	1.5	39	$2.9 \times 10^{-3}$	1.3	37	$3.8 \times 10^{-3}$
5	O <sub>2</sub> (H <sub>2</sub> O) <sup>c)</sup>	1.3	44	$3.0 \times 10^{-3}$	1.3	37	$3.8 \times 10^{-3}$
10	Air	1.2	209	$4.4 \times 10^{-3}$	1.2	210	$4.8 \times 10^{-3}$

- a) The values of  $k_{me}$  are those for the case of the mean value of  $\beta_e$  of 1.30.
- b) The values of  $k$  are those for the case of the mean value of  $\beta$  of 1.25.
- c) N<sub>2</sub>(H<sub>2</sub>O), in nitrogen containing the vapor of distilled water with the vapor pressure of 22 mmHg;  
 N<sub>2</sub>(H<sub>2</sub>O<sub>2</sub>), in nitrogen containing the vapor of 30 w/w % of the aqueous solution of hydrogen peroxide with the vapor pressure of 13 mmHg;  
 O<sub>2</sub>(H<sub>2</sub>O), in Oxygen containing the vapor of distilled water with the vapor pressure of 22 mmHg.

TABLE V. Numerical Values of  $n$  for PVP Ball-Milled in the Absence of the Additive  
 $J_b=0.22, J_s=0.06^{7)}$  (referred to Table I)

		Atmosphere						
		Nitrogen		Air		Oxygen		
$t$	L	$n$	$t$	L	$n$	$t$	L	$n$
0	$1.2 \times 10^6 \leq M_u$	1.2	21	$1.3 \times 10^6 \leq M_u$	1.1	21	$1.2 \times 10^6 \leq M_u$	1.0
	$5.2 \times 10^4 \leq M_u \leq 1.2 \times 10^6$	0.86		$4.2 \times 10^4 \leq M_u \leq 1.3 \times 10^6$	0.63		$4.2 \times 10^4 \leq M_u \leq 1.2 \times 10^6$	0.65
	$M_u \leq 5.2 \times 10^4$	1.9		$M_u \leq 4.2 \times 10^4$	1.6		$M_u \leq 4.2 \times 10^4$	1.4
11	$1.2 \times 10^6 \leq M_u$	1.1	54	$1.2 \times 10^6 \leq M_u$	0.84	54	$1.2 \times 10^6 \leq M_u$	0.84
	$4.1 \times 10^4 \leq M_u \leq 1.2 \times 10^6$	0.76		$3.4 \times 10^4 \leq M_u \leq 1.2 \times 10^6$	0.57		$4.2 \times 10^4 \leq M_u \leq 1.2 \times 10^6$	0.55
	$M_u \leq 4.1 \times 10^4$	1.4		$M_u \leq 3.4 \times 10^4$	1.9		$M_u \leq 4.2 \times 10^4$	1.6
30	$10^6 \leq M_u$	1.1	103	$1.2 \times 10^6 \leq M_u$	0.64	100	$1.2 \times 10^6 \leq M_u$	0.75
	$4.0 \times 10^4 \leq M_u \leq 10^6$	0.71		$4.8 \times 10^4 \leq M_u \leq 1.2 \times 10^6$	0.48		$3.5 \times 10^4 \leq M_u \leq 1.2 \times 10^6$	0.46
	$M_u \leq 4.0 \times 10^4$	1.4		$M_u \leq 4.8 \times 10^4$	1.9		$M_u \leq 3.5 \times 10^4$	2.0
67	$10^6 \leq M_u$	0.96						
	$4.0 \times 10^4 \leq M_u \leq 10^6$	0.51						
	$M_u \leq 4.0 \times 10^4$	1.7						
123	$6.7 \times 10^5 \leq M_u$	0.62						
	$3.8 \times 10^4 \leq M_u \leq 6.7 \times 10^5$	0.41						
	$M_u \leq 3.8 \times 10^4$	1.6						

$t$ ; Ball-milling time (hr), L; The range of  $M_u$ .

TABLE VI. The Numerical Values of  $n$  for PVP Ball-Milled in the Presence of the Inorganic Additives $J_b=0.22, J_s=0.06^{2,3}$  (referred to Table I)

Additive	Atmosphere					
	Nitrogen			Air		
	$t$	L	$n$	$t$	L	$n$
White alundum	9		0.69	7		0.98
	21		0.63	31	$1.2 \times 10^5 \leq M_u$	0.73
	46	$1.3 \times 10^4 \leq M_u$	0.73		$M_u \leq 1.2 \times 10^5$	1.1
		$M_u \leq 1.3 \times 10^4$	0.49	61	$10^5 \leq M_u$	0.83
	98	$10^5 \leq M_u$	0.66		$M_u \leq 10^5$	1.1
		$1.1 \times 10^4 \leq M_u \leq 10^5$	0.93	103		0.70
	$M_u \leq 1.1 \times 10^4$	0.61				
Silica sands	15	$3.6 \times 10^4 \leq M_u$	0.73	14	$3.4 \times 10^5 \leq M_u$	1.2
		$M_u \leq 3.6 \times 10^4$	1.3		$M_u \leq 3.4 \times 10^5$	1.7
	36	$3.5 \times 10^4 \leq M_u$	0.61	53	$9.1 \times 10^4 \leq M_u$	0.68
		$M_u \leq 3.5 \times 10^4$	1.4		$M_u \leq 9.1 \times 10^4$	1.5
	56	$2.4 \times 10^4 \leq M_u$	0.49	100	$9.5 \times 10^4 \leq M_u$	0.60
		$M_u \leq 2.4 \times 10^4$	1.4		$M_u \leq 9.5 \times 10^4$	1.4
	75	$4.2 \times 10^4 \leq M_u$	0.53	202	$8.5 \times 10^4 \leq M_u$	0.38
		$M_u \leq 4.2 \times 10^4$	1.6		$M_u \leq 8.5 \times 10^4$	1.8
	100	$3.3 \times 10^4 \leq M_u$	0.42			
		$M_u \leq 3.3 \times 10^4$	1.6			
	129	$2.0 \times 10^4 \leq M_u$	0.36			
		$M_u \leq 2.0 \times 10^4$	1.8			
160	$2.0 \times 10^4 \leq M_u$	0.33				
	$M_u \leq 2.0 \times 10^4$	1.4				
201	$7.0 \times 10^4 \leq M_u$	0.31				
	$M_u \leq 7.0 \times 10^4$	0.66				
Zinc oxide	15	$5.0 \times 10^4 \leq M_u$	0.87	59	$5.4 \times 10^4 \leq M_u$	0.99
		$M_u \leq 5.0 \times 10^4$	1.1		$M_u \leq 5.4 \times 10^4$	2.1
	36	$5.5 \times 10^4 \leq M_u$	1.2	80	$4.0 \times 10^4 \leq M_u$	0.89
		$M_u \leq 5.5 \times 10^4$	1.6		$M_u \leq 4.0 \times 10^4$	2.6
	56	$1.1 \times 10^5 \leq M_u$	1.1	106	$3.0 \times 10^4 \leq M_u$	0.63
		$M_u \leq 1.1 \times 10^5$	1.7		$M_u \leq 3.0 \times 10^4$	1.2
	75	$8.0 \times 10^4 \leq M_u$	0.78	172	$5.0 \times 10^4 \leq M_u$	0.44
		$M_u \leq 8.0 \times 10^4$	1.7		$M_u \leq 5.0 \times 10^4$	0.99
	100	$2.8 \times 10^4 \leq M_u$	0.47	201	$5.0 \times 10^4 \leq M_u$	0.44
		$M_u \leq 2.8 \times 10^4$	1.0		$M_u \leq 5.0 \times 10^4$	1.2
	129	$4.6 \times 10^4 \leq M_u$	0.55			
		$M_u \leq 4.6 \times 10^4$	1.6			
160	$2.7 \times 10^4 \leq M_u$	0.43				
	$M_u \leq 2.7 \times 10^4$	1.4				
201	$2.4 \times 10^4 \leq M_u$	0.40				
	$M_u \leq 2.4 \times 10^4$	1.5				
Barium sulfate	8	$1.1 \times 10^5 \leq M_u$	1.1			
		$M_u \leq 1.1 \times 10^5$	1.8			
	33	$7.0 \times 10^4 \leq M_u$	0.89			
		$M_u \leq 7.0 \times 10^4$	1.6			
	55	$7.0 \times 10^4 \leq M_u$	0.74			
		$M_u \leq 7.0 \times 10^4$	1.3			
	78	$6.4 \times 10^4 \leq M_u$	0.62			
		$M_u \leq 6.4 \times 10^4$	1.5			
101	$8.6 \times 10^4 \leq M_u$	0.52				
	$M_u \leq 8.6 \times 10^4$	1.3				
202	$4.0 \times 10^4 \leq M_u$	0.40				
	$M_u \leq 4.0 \times 10^4$	1.2				

Additive	Atmosphere					
	Nitrogen			Air		
	<i>t</i>	L	<i>n</i>	<i>t</i>	L	<i>n</i>
Sodium chloride	9	$1.3 \times 10^5 \leq M_u$	1.2	8	$8.0 \times 10^4 \leq M_u$	1.0
		$M_u \leq 1.3 \times 10^5$	1.7		$M_u \leq 8.0 \times 10^4$	2.0
	18	$2.0 \times 10^5 \leq M_u$	1.1	33	$7.2 \times 10^4 \leq M_u$	0.96
		$M_u \leq 2.0 \times 10^5$	1.5		$M_u \leq 7.2 \times 10^4$	2.2
	36	$2.0 \times 10^5 \leq M_u$	0.85	55	$7.0 \times 10^4 \leq M_u$	0.90
		$M_u \leq 2.0 \times 10^5$	1.0		$M_u \leq 7.0 \times 10^4$	1.8
	57	$7.0 \times 10^4 \leq M_u$	0.72	75	$5.0 \times 10^4 \leq M_u$	0.53
		$M_u \leq 7.0 \times 10^4$	1.0		$M_u \leq 5.0 \times 10^4$	1.2
	75	$8.0 \times 10^4 \leq M_u$	0.79	105	$5.0 \times 10^4 \leq M_u$	0.54
		$M_u \leq 8.0 \times 10^4$	1.6		$M_u \leq 5.0 \times 10^4$	1.4
	95	$9.0 \times 10^4 \leq M_u$	0.65	131	$4.8 \times 10^4 \leq M_u$	0.66
		$M_u \leq 9.0 \times 10^4$	1.2		$M_u \leq 4.8 \times 10^4$	1.6
	121	$5.0 \times 10^4 \leq M_u$	0.57	199	$2.5 \times 10^4 \leq M_u$	1.1
		$M_u \leq 5.0 \times 10^4$	2.1		$M_u \leq 2.5 \times 10^4$	3.0
	153	$1.1 \times 10^5 \leq M_u$	0.38			
	$4.0 \times 10^4 \leq M_u \leq 1.1 \times 10^5$	0.83				
	$M_u \leq 4.0 \times 10^4$	2.1				
201	$3.5 \times 10^4 \leq M_u$	0.54				
	$1.6 \times 10^4 \leq M_u \leq 3.5 \times 10^4$	1.3				
	$M_u \leq 1.6 \times 10^4$	2.8				
Talc	72	$8.0 \times 10^4 \leq M_u$	0.99	72		0.86
		$M_u \leq 8.0 \times 10^4$	1.1			
	103	$6.0 \times 10^4 \leq M_u$	0.73	106	$10^4 \leq M_u$	0.56
		$M_u \leq 6.0 \times 10^4$	0.86		$M_u \leq 10^4$	1.3
	133	$8.0 \times 10^4 \leq M_u$	0.60	131	$1.2 \times 10^4 \leq M_u$	0.49
		$M_u \leq 8.0 \times 10^4$	0.96		$M_u \leq 1.2 \times 10^4$	1.4
	169	$5.0 \times 10^4 \leq M_u$	0.52	166	$1.3 \times 10^4 \leq M_u$	0.35
		$M_u \leq 5.0 \times 10^4$	1.1		$M_u \leq 1.3 \times 10^4$	1.2
	201	$4.3 \times 10^4 \leq M_u$	0.57	204	$1.9 \times 10^4 \leq M_u$	0.31
		$M_u \leq 4.3 \times 10^4$	1.1		$M_u \leq 1.9 \times 10^4$	1.2

TABLE VII. The Numerical Values of *n* for PVP Ball-Milled in the Presence of Organic Additives

$J_b = 0.22, J_s = 0.06^{2,3}$  (referred to Table I)

Additive	Atmosphere					
	Nitrogen			Air		
	<i>t</i>	L	<i>n</i>	<i>t</i>	L	<i>n</i>
Vitamin K <sub>3</sub>	125	$2.5 \times 10^4 \leq M_u$	0.91	8	$10^5 \leq M_u$	1.0
		$M_u \leq 2.5 \times 10^4$	1.9		$2.0 \times 10^4 \leq M_u \leq 10^5$	0.73
	145	$3.0 \times 10^4 \leq M_u$	1.0		$M_u \leq 2.0 \times 10^4$	1.4
		$M_u \leq 3.0 \times 10^4$	2.3	21	$10^5 \leq M_u$	0.84
	166		0.59		$10^4 \leq M_u \leq 10^5$	0.52
	189	$10^5 \leq M_u$	0.59		$M_u \leq 10^4$	1.5
		$4.6 \times 10^4 \leq M_u \leq 10^5$	0.78	41	$10^4 \leq M_u$	0.87
		$M_u \leq 4.6 \times 10^4$	0.42		$M_u \leq 10^4$	3.3
	222	$9.2 \times 10^4 \leq M_u$	0.39	65	$5.6 \times 10^4 \leq M_u$	0.75
		$2.4 \times 10^4 \leq M_u \leq 9.2 \times 10^4$	0.55		$10^4 \leq M_u \leq 5.6 \times 10^4$	0.55
		$M_u \leq 2.4 \times 10^4$	0.40		$M_u \leq 10^4$	1.6
	251	$8.2 \times 10^4 \leq M_u$	0.46	95	$5.5 \times 10^4 \leq M_u$	0.76
		$1.6 \times 10^4 \leq M_u \leq 8.2 \times 10^4$	0.75		$M_u \leq 5.5 \times 10^4$	1.1
		$M_u \leq 1.6 \times 10^4$	0.32	123	$3.2 \times 10^4 \leq M_u$	0.52
					$M_u \leq 3.2 \times 10^4$	0.67



Additive	Atmosphere						
	Nitrogen			Air			
	<i>t</i>	<i>L</i>	<i>n</i>	<i>t</i>	<i>L</i>	<i>n</i>	
Acridine				160	$3.2 \times 10^4 \leq M_u$	0.47	
					$M_u \leq 3.2 \times 10^4$	0.69	
				200	$4.0 \times 10^4 \leq M_u$	0.43	
					$M_u \leq 4.0 \times 10^4$	0.77	
		125	$2.1 \times 10^5 \leq M_u$	0.89	8	$1.6 \times 10^5 \leq M_u$	1.2
			$M_u \leq 2.1 \times 10^5$	0.66		$M_u \leq 1.6 \times 10^5$	2.4
		145	$1.3 \times 10^5 \leq M_u$	0.90	22	$8.2 \times 10^4 \leq M_u$	1.2
			$M_u \leq 1.3 \times 10^5$	0.70		$M_u \leq 8.2 \times 10^4$	2.8
		166		0.79	43	$8.0 \times 10^4 \leq M_u$	0.91
		198	$1.5 \times 10^5 \leq M_u$	0.75		$M_u \leq 8.0 \times 10^4$	1.6
			$4.5 \times 10^4 \leq M_u \leq 1.5 \times 10^5$	0.78	74	$5.0 \times 10^4 \leq M_u$	0.70
			$M_u \leq 4.5 \times 10^4$	0.50		$M_u \leq 5.0 \times 10^4$	1.6
		222	$1.2 \times 10^5 \leq M_u$	0.56	101	$4.6 \times 10^4 \leq M_u$	0.52
			$2.5 \times 10^4 \leq M_u \leq 1.5 \times 10^4$	0.74		$M_u \leq 4.6 \times 10^4$	1.5
			$M_u \leq 2.5 \times 10^4$	0.56	207	$2.8 \times 10^4 \leq M_u$	0.73
		251	$6.5 \times 10^4 \leq M_u$	0.55		$M_u \leq 2.8 \times 10^4$	3.3
		$1.4 \times 10^4 \leq M_u \leq 6.5 \times 10^4$	0.97				
		$M_u \leq 1.4 \times 10^4$	0.67				
Methylene blue				8	$8.0 \times 10^4 \leq M_u$	1.1	
					$M_u \leq 8.0 \times 10^4$	1.5	
				43	$1.1 \times 10^5 \leq M_u$	1.2	
					$M_u \leq 1.1 \times 10^5$	1.5	
				74	$1.1 \times 10^5 \leq M_u$	1.1	
					$M_u \leq 1.1 \times 10^5$	1.4	
				101	$8.0 \times 10^4 \leq M_u$	0.70	
					$M_u \leq 8.0 \times 10^4$	2.0	
Phenothiazine				207	$7.5 \times 10^4 \leq M_u$	0.61	
					$M_u \leq 7.5 \times 10^4$	1.5	
		93	$3.0 \times 10^5 \leq M_u$	0.90	21	$2.8 \times 10^4 \leq M_u$	0.97
			$8.0 \times 10^4 \leq M_u \leq 3.0 \times 10^5$	0.60		$M_u \leq 2.8 \times 10^4$	1.7
			$M_u \leq 8.0 \times 10^4$	0.86	41	$7.3 \times 10^4 \leq M_u$	1.0
		115	$8.4 \times 10^4 \leq M_u$	0.72		$M_u \leq 7.3 \times 10^4$	1.5
			$10^4 \leq M_u \leq 8.4 \times 10^4$	0.62	65		1.0
			$M_u \leq 10^4$	0.86	95	$4.8 \times 10^4 \leq M_u$	1.1
		140	$6.4 \times 10^4 \leq M_u$	0.73		$M_u \leq 4.8 \times 10^4$	1.9
			$M_u \leq 6.4 \times 10^4$	0.54	123	$2.3 \times 10^4 \leq M_u$	0.85
		175	$4.0 \times 10^4 \leq M_u$	0.75		$M_u \leq 2.3 \times 10^4$	2.0
			$M_u \leq 4.0 \times 10^4$	0.56	160		1.2
	211		0.50	200	$5.1 \times 10^4 \leq M_u$	0.72	
					$M_u \leq 5.1 \times 10^4$	1.3	
<i>p</i> -Hydroquinone				10	$1.2 \times 10^5 \leq M_u$	1.2	
					$M_u \leq 1.2 \times 10^5$	2.4	
		7	$1.3 \times 10^5 \leq M_u$	1.4	19	$1.2 \times 10^5 \leq M_u$	1.3
			$M_u \leq 1.3 \times 10^5$	2.3		$M_u \leq 1.2 \times 10^5$	2.0
		20	$4.0 \times 10^5 \leq M_u$	1.3	42	$1.8 \times 10^5 \leq M_u$	1.3
			$6.0 \times 10^4 \leq M_u \leq 4.0 \times 10^5$	0.93		$M_u \leq 1.8 \times 10^5$	3.9
			$M_u \leq 6.0 \times 10^4$	2.3	65		0.89
		35	$9.0 \times 10^4 \leq M_u$	1.1	93		1.1
			$M_u \leq 9.0 \times 10^4$	1.7	200	$5.5 \times 10^4 \leq M_u$	1.1
		72	$6.0 \times 10^4 \leq M_u$	0.52		$M_u \leq 5.5 \times 10^4$	1.7
			$M_u \leq 6.0 \times 10^4$	0.91			
		100	$10^5 \leq M_u$	0.50			
			$M_u \leq 10^5$	1.2			
		150	$1.2 \times 10^5 \leq M_u$	0.47			
		$M_u \leq 1.2 \times 10^5$	1.1				
	203	$3.3 \times 10^4 \leq M_u$	0.58				
		$M_u \leq 3.3 \times 10^4$	1.4				

Additive	Atmosphere					
	Nitrogen			Air		
	<i>t</i>	L	<i>n</i>	<i>t</i>	L	<i>n</i>
Barbituric acid	7		0.75	8		1.3
	20		0.60	23		1.0
	35	$5.7 \times 10^4 \leq M_u$	0.57	42		0.78
		$M_u \leq 5.7 \times 10^4$	0.84	62		0.74
	47	$5.5 \times 10^4 \leq M_u$	0.51	91		0.53
		$M_u \leq 5.5 \times 10^4$	0.78	200		1.2
	72	$4.0 \times 10^4 \leq M_u$	0.68			
		$M_u \leq 4.0 \times 10^4$	1.7			
	121	$4.1 \times 10^4 \leq M_u$	0.62			
		$M_u \leq 4.1 \times 10^4$	1.7			
	151	$3.8 \times 10^4 \leq M_u$	0.69			
		$M_u \leq 3.8 \times 10^4$	2.2			
	203	$3.5 \times 10^4 \leq M_u$	0.77			
		$M_u \leq 3.5 \times 10^4$	2.8			

TABLE VIII. The Numerical Values of *n* for PVP Ball-Milled in the Presence of Activated Charcoal (AC) in Various Kinds of Atmosphere

$J_b=0.22, J_s=0.06^{2,3)}$  (referred to Table I)

	Kind of AC Granules Content of AC 10% Atmosphere N <sub>2</sub> (H <sub>2</sub> O)				Kind of AC Granules Content of AC 10% Atmosphere N <sub>2</sub> (H <sub>2</sub> O <sub>2</sub> )		
	<i>t</i>	L	<i>n</i>		<i>t</i>	L	<i>n</i>
118	$1.5 \times 10^6 \leq M_u$		1.2	78	$1.8 \times 10^6 \leq M_u$		1.3
	$M_u \leq 1.5 \times 10^6$		0.68		$M_u \leq 1.8 \times 10^6$		0.81
131	$8.4 \times 10^5 \leq M_u$		1.2	115	$1.4 \times 10^6 \leq M_u$		1.3
	$1.1 \times 10^4 \leq M_u \leq 8.4 \times 10^5$		0.57		$4.8 \times 10^4 \leq M_u \leq 1.4 \times 10^6$		0.75
	$M_u \leq 1.1 \times 10^4$		0.85		$M_u \leq 4.8 \times 10^4$		1.0
146	$4.5 \times 10^5 \leq M_u$		1.2	127	$1.5 \times 10^6 \leq M_u$		1.2
	$2.0 \times 10^4 \leq M_u \leq 4.5 \times 10^5$		0.56		$2.0 \times 10^4 \leq M_u \leq 1.5 \times 10^6$		0.57
	$M_u \leq 2.0 \times 10^4$		1.6		$M_u \leq 2.0 \times 10^4$		0.99
162	$4.5 \times 10^5 \leq M_u$		1.2	145	$10^6 \leq M_u$		1.3
	$2.0 \times 10^4 \leq M_u \leq 4.5 \times 10^5$		0.56		$2.3 \times 10^4 \leq M_u \leq 10^6$		0.57
	$M_u \leq 2.0 \times 10^4$		1.8		$M_u \leq 2.3 \times 10^4$		1.2
181	$2.4 \times 10^5 \leq M_u$		0.70	164	$4.6 \times 10^4 \leq M_u$		0.50
	$2.0 \times 10^4 \leq M_u \leq 2.4 \times 10^5$		0.51		$M_u \leq 4.6 \times 10^4$		1.4
	$M_u \leq 2.0 \times 10^4$		1.4	184	$1.1 \times 10^6 \leq M_u$		1.2
202	$2.5 \times 10^5 \leq M_u$		0.71		$2.5 \times 10^4 \leq M_u \leq 1.1 \times 10^6$		0.51
	$1.2 \times 10^4 \leq M_u \leq 2.5 \times 10^5$		0.44		$M_u \leq 2.5 \times 10^4$		1.3
	$M_u \leq 1.2 \times 10^4$		1.5	211	$10^6 \leq M_u$		1.0
221	$10^4 \leq M_u$		0.46		$3.3 \times 10^4 \leq M_u \leq 10^6$		0.51
	$M_u \leq 10^4$		1.6		$M_u \leq 3.3 \times 10^4$		1.8
				241	$3.2 \times 10^4 \leq M_u$		0.44
					$M_u \leq 3.2 \times 10^4$		1.8
				269	$1.2 \times 10^6 \leq M_u$		0.73
					$4.2 \times 10^4 \leq M_u \leq 1.2 \times 10^6$		0.49
					$M_u \leq 4.2 \times 10^4$		2.0

Kind of AC Granules Content of AC 15.1% Atmosphere Air			Kind of AC Fine powders Content of AC 10% Atmosphere Air		
<i>t</i>	L	<i>n</i>	<i>t</i>	L	<i>n</i>
65		0.88	8	$1.5 \times 10^5 \leq M_u$	1.0
98		0.77		$M_u \leq 1.5 \times 10^5$	1.9
130		0.81	22	$1.4 \times 10^5 \leq M_u$	0.99
164		0.72		$M_u \leq 1.4 \times 10^5$	1.4
198	$2.1 \times 10^4 \leq M_u$	0.72	46	$1.4 \times 10^5 \leq M_u$	1.1
	$M_u \leq 2.1 \times 10^4$	2.3		$M_u \leq 1.4 \times 10^5$	1.5
251	$2.6 \times 10^4 \leq M_u$	0.57	63	$1.7 \times 10^5 \leq M_u$	0.72
	$M_u \leq 2.6 \times 10^4$	1.4		$M_u \leq 1.7 \times 10^5$	1.6
			80	$1.8 \times 10^5 \leq M_u$	0.64
				$M_u \leq 1.8 \times 10^5$	1.5
			113	$7.3 \times 10^4 \leq M_u$	1.1
				$M_u \leq 7.3 \times 10^4$	2.5
			136	$7.3 \times 10^4 \leq M_u$	0.90
				$M_u \leq 7.3 \times 10^4$	2.7

Kind of AC Granules Content of AC 15.1% Atmosphere Oxygen			Kind of AC Granules Content of AC 10% Atmosphere O <sub>2</sub> (H <sub>2</sub> O)		
<i>t</i>	L	<i>n</i>	<i>t</i>	L	<i>n</i>
69	$7.5 \times 10^5 \leq M_u$	1.1	122	$1.3 \times 10^6 \leq M_u$	1.2
	$3.0 \times 10^4 \leq M_u \leq 7.5 \times 10^5$	0.91		$1.7 \times 10^4 \leq M_u \leq 1.3 \times 10^6$	0.74
	$M_u \leq 3.0 \times 10^4$	1.4		$M_u \leq 1.7 \times 10^4$	1.2
82	$3.0 \times 10^4 \leq M_u$	0.89	164	$1.3 \times 10^6 \leq M_u$	1.2
	$M_u \leq 3.0 \times 10^4$	1.2		$2.8 \times 10^4 \leq M_u \leq 1.3 \times 10^6$	0.70
112	$3.0 \times 10^4 \leq M_u$	0.90		$M_u \leq 2.8 \times 10^4$	1.2
	$M_u \leq 3.0 \times 10^4$	1.4	184	$8.2 \times 10^5 \leq M_u$	1.4
148	$7.2 \times 10^5 \leq M_u$	1.0		$2.1 \times 10^4 \leq M_u \leq 8.2 \times 10^5$	0.69
	$M_u \leq 7.2 \times 10^5$	0.80		$M_u \leq 2.1 \times 10^4$	1.9
164	$4.7 \times 10^5 \leq M_u$	1.4	202	$4.4 \times 10^5 \leq M_u$	1.8
	$1.3 \times 10^4 \leq M_u \leq 4.7 \times 10^5$	0.73		$5.2 \times 10^4 \leq M_u \leq 4.4 \times 10^5$	0.90
	$M_u \leq 1.3 \times 10^4$	1.4		$M_u \leq 5.2 \times 10^4$	2.5
204	$1.7 \times 10^4 \leq M_u$	0.70	221	$6.2 \times 10^5 \leq M_u$	1.1
	$M_u \leq 1.7 \times 10^4$	1.7		$2.4 \times 10^4 \leq M_u \leq 6.2 \times 10^5$	0.55
224	$2.0 \times 10^4 \leq M_u$	0.62		$M_u \leq 2.4 \times 10^4$	1.8
	$M_u \leq 2.0 \times 10^4$	1.8	241	$6.0 \times 10^5 \leq M_u$	0.94
248	$8.0 \times 10^3 \leq M_u$	0.72		$1.4 \times 10^4 \leq M_u \leq 6.0 \times 10^5$	0.48
	$M_u \leq 8.0 \times 10^3$	2.8		$M_u \leq 1.4 \times 10^4$	1.6
			271	$2.4 \times 10^5 \leq M_u$	0.94
				$1.4 \times 10^4 \leq M_u \leq 2.4 \times 10^5$	0.52
				$M_u \leq 1.4 \times 10^4$	1.8

## 2) Relation between *R* and *M<sub>u</sub>*

A line broken at several points was obtained by the logarithmic plot of  $(-\log R)$  versus  $M_u$ , as shown in Fig. 3. The value of  $M_u$  at the broken point and the gradient of each of the straight lines in the range of various molecular weights,  $n$ , are shown in Table V, VI, VII, VIII and IX. These Tables show the existence of the critical molecular weight,  $M_c$ , at the region of molecular weight above which,  $n$  is around or below 1.0, and at the region of molecular weight below which,  $n$  is larger than 1.0. The value of  $M_c$  in the absence of the additive was influenced little by the ball-milling atmosphere.

TABLE IX. Numerical Values of  $n$  for PVP Ball-Milled in the Presence of Chloranil

$J_b=0.43, J_s=0.03^3$  (referred to Table I)

Content of chloranil 5% Atmosphere $N_2(H_2O)$			Content of chloranil 5% Atmosphere $N_2(H_2O_2)$			Content of chloranil 5% Atmosphere Air		
$t$	L	$n$	$t$	L	$n$	$t$	L	$n$
43	$5.5 \times 10^5 \leq M_u$	1.2	55	$1.1 \times 10^6 \leq M_u$	1.6	31	$7.8 \times 10^6 \leq M_u$	0.99
	$1.6 \times 10^4 \leq M_u \leq 5.5 \times 10^5$	0.65		$6.0 \times 10^4 \leq M_u \leq 1.1 \times 10^6$	0.98		$1.3 \times 10^4 \leq M_u \leq 7.8 \times 10^5$	0.73
	$M_u \leq 1.6 \times 10^4$	1.5		$M_u \leq 6.0 \times 10^4$	2.2		$M_u \leq 1.3 \times 10^4$	1.1
51	$1.3 \times 10^4 \leq M_u$	0.68	62	$4.7 \times 10^5 \leq M_u$	0.93	47	$4.7 \times 10^5 \leq M_u$	0.93
	$M_u \leq 1.3 \times 10^4$	1.4		$1.1 \times 10^4 \leq M_u \leq 4.7 \times 10^5$	0.63		$8.6 \times 10^3 \leq M_u \leq 4.7 \times 10^5$	0.53
55	$2.5 \times 10^4 \leq M_u$	0.70		$M_u \leq 1.1 \times 10^4$	1.2		$M_u \leq 8.6 \times 10^3$	1.2
	$M_u \leq 2.5 \times 10^4$	1.3	66	$6.0 \times 10^5 \leq M_u$	0.92	61	$6.4 \times 10^4 \leq M_u$	0.75
59	$3.8 \times 10^4 \leq M_u$	0.64		$1.6 \times 10^4 \leq M_u \leq 6.0 \times 10^5$	0.64		$M_u \leq 6.4 \times 10^4$	0.98
	$M_u \leq 3.8 \times 10^4$	1.3		$M_u \leq 1.6 \times 10^4$	1.0	67	$8.0 \times 10^4 \leq M_u$	0.62
64	$4.5 \times 10^4 \leq M_u$	0.58	69	$2.9 \times 10^4 \leq M_u$	1.2		$M_u \leq 8.0 \times 10^4$	1.3
	$M_u \leq 4.5 \times 10^4$	1.4		$M_u \leq 2.9 \times 10^4$	1.6	73	$7.7 \times 10^4 \leq M_u$	0.35
73	$5.0 \times 10^4 \leq M_u$	0.56	75	$3.5 \times 10^4 \leq M_u$	1.1		$M_u \leq 7.7 \times 10^4$	1.4
	$M_u \leq 5.0 \times 10^4$	1.8		$M_u \leq 3.5 \times 10^4$	1.9	81	$9.5 \times 10^4 \leq M_u$	0.35
85	$5.0 \times 10^4 \leq M_u$	0.57	84	$2.8 \times 10^4 \leq M_u$	0.58		$2.5 \times 10^4 \leq M_u \leq 9.5 \times 10^4$	1.6
	$M_u \leq 5.0 \times 10^4$	1.7		$M_u \leq 2.8 \times 10^4$	1.3		$M_u \leq 2.5 \times 10^4$	1.1
101	$5.3 \times 10^4 \leq M_u$	0.36	102	$4.1 \times 10^4 \leq M_u$	0.69	91	$5.2 \times 10^4 \leq M_u$	0.28
	$M_u \leq 5.3 \times 10^4$	1.6		$M_u \leq 4.1 \times 10^4$	1.4		$1.4 \times 10^4 \leq M_u \leq 5.2 \times 10^4$	1.8
							$M_u \leq 1.4 \times 10^4$	1.4
						99	$4.8 \times 10^4 \leq M_u$	0.25
							$1.4 \times 10^4 \leq M_u \leq 4.8 \times 10^4$	1.8
							$M_u \leq 1.4 \times 10^4$	1.5

Content of chloranil 10% Atmosphere Air			Content of chloranil 5% Atmosphere $O_2$			Content of chloranil 10% Atmosphere $O_2(H_2O)$		
$t$	L	$n$	$t$	L	$n$	$t$	L	$n$
199	$1.4 \times 10^6 \leq M_u$	1.4	36	$1.4 \times 10^6 \leq M_u$	1.3	42	$5.5 \times 10^4 \leq M_u$	1.2
	$8.4 \times 10^4 \leq M_u \leq 1.4 \times 10^6$	0.78		$2.5 \times 10^4 \leq M_u \leq 1.4 \times 10^6$	0.74		$1.8 \times 10^4 \leq M_u \leq 5.5 \times 10^4$	0.75
	$M_u \leq 8.4 \times 10^4$	1.8		$M_u \leq 2.5 \times 10^4$	1.4		$M_u \leq 1.8 \times 10^4$	1.8
210	$9.0 \times 10^5 \leq M_u$	1.2	47	$1.8 \times 10^6 \leq M_u$	1.2	47	$2.8 \times 10^4 \leq M_u$	0.84
	$7.8 \times 10^4 \leq M_u \leq 9.0 \times 10^5$	0.78		$2.8 \times 10^4 \leq M_u \leq 1.8 \times 10^6$	0.70		$M_u \leq 2.8 \times 10^4$	1.6
	$M_u \leq 7.8 \times 10^4$	1.4		$M_u \leq 2.8 \times 10^4$	1.6	51	$6.0 \times 10^4 \leq M_u$	0.73
215	$7.4 \times 10^4 \leq M_u$	0.81	50	$10^6 \leq M_u$	0.73		$M_u \leq 6.0 \times 10^4$	1.3
	$M_u \leq 7.4 \times 10^4$	1.3		$3.5 \times 10^4 \leq M_u \leq 10^6$	0.57	56	$8.0 \times 10^4 \leq M_u$	0.67
218	$3.8 \times 10^5 \leq M_u$	2.1		$M_u \leq 3.5 \times 10^4$	0.89		$M_u \leq 8.0 \times 10^4$	1.3
	$9.0 \times 10^4 \leq M_u \leq 3.8 \times 10^5$	1.3	55	$2.0 \times 10^4 \leq M_u$	0.47	64	$8.7 \times 10^4 \leq M_u$	0.58
	$M_u \leq 9.0 \times 10^4$	2.2		$M_u \leq 2.0 \times 10^4$	0.63		$M_u \leq 8.7 \times 10^4$	1.4
224	$2.0 \times 10^5 \leq M_u$	1.3	61	$5.6 \times 10^4 \leq M_u$	0.52	75	$5.2 \times 10^4 \leq M_u$	0.40
	$M_u \leq 2.0 \times 10^5$	0.72		$M_u \leq 5.6 \times 10^4$	0.91		$M_u \leq 5.2 \times 10^4$	1.1
232	$1.2 \times 10^5 \leq M_u$	0.39	65	$6.0 \times 10^4 \leq M_u$	0.44	88	$5.7 \times 10^4 \leq M_u$	0.29
	$3.6 \times 10^4 \leq M_u \leq 1.2 \times 10^5$	0.83		$M_u \leq 6.0 \times 10^4$	0.86		$M_u \leq 5.7 \times 10^4$	1.2
	$M_u \leq 3.6 \times 10^4$	1.4	72	$6.3 \times 10^4 \leq M_u$	0.39	107		2.8
241	$1.2 \times 10^5 \leq M_u$	0.50		$M_u \leq 6.3 \times 10^4$	0.84			
	$4.0 \times 10^4 \leq M_u \leq 1.2 \times 10^5$	0.61						
	$M_u \leq 4.0 \times 10^4$	1.5						
261	$4.9 \times 10^4 \leq M_u$	0.39						
	$M_u \leq 4.9 \times 10^4$	1.4						

### 2)-i The Value of $M_c$ in the Presence of Inorganic Additives

In case of ball-milling in nitrogen,  $n$  was around or below 1.0 in all the range of molecular weight in the presence of white alundum or talc. The value of  $M_c$  in the presence of silica sands was approximately identical with the value in the absence of the additive. But in the presence of the other additives,  $M_c$  was larger than the value in the absence of the additive at the first stage after the lapse of the induction period and decreased gradually by ball-milling.

In case of ball-milling in air,  $n$  was around or below 1.0 in all the range of molecular weight in the presence of white alundum. The value of  $M_c$  in the presence of talc or the granules of activated charcoal was smaller than the value in the absence of the additive. The value of  $M_c$  in the presence of zinc oxide was nearly identical with the value in the absence of the additive. The value of  $M_c$  in the presence of the other additives at the first stage of ball-milling was larger than the value in the absence of the additive.

### 2)-ii The Value of $M_c$ in the Presence of Organic Additives

In case of ball-milling in nitrogen,  $M_c$  was approximately identical with the value in the absence of the additive at the first stage after the lapse of the induction period, but  $n$  was below 1.0 in all the range of  $M_u$  for PVP ball-milled for more than 50 hours from the time of the induction period in the presence of vitamin K<sub>3</sub>. In the presence of acridine or phenothiazine,  $n$  was smaller than 1.0 in all the range of  $M_u$ , and the same tendency was observed at the first stage of ball-milling in the presence of barbituric acid. But, in the presence of *p*-hydroquinone,  $M_c$  was larger than the value in the absence of the additive.

In case of ball-milling in air in the presence of vitamin K<sub>3</sub>,  $n$  was around or below 1.0 in all the range of  $M_u$  after the lapse of the induction period. In the presence of acridine or methylene blue,  $M_c$  was larger than the value in the absence of the additive at the first stage after the lapse of the induction period and decreased gradually by ball-milling. In the presence of phenothiazine,  $M_c$  was nearly identical with the value in the absence of the additive, and in the presence of *p*-hydroquinone,  $M_c$  was larger than the value in the absence of the additive. A straight line was obtained by the logarithmic plot of  $-\log R$  versus  $M_u$  in the presence of barbituric acid, and  $n$  was larger than 1.0 at the first stage of ball-milling.

### 2)-iii Influence of the Ball-Milling Atmosphere on $M_c$

In case of ball-milling in various kinds of atmosphere in the presence of the granules of activated charcoal,  $n$  was around or below 1.0 in all the range of  $M_u$  at the first stage, and  $M_c$  was smaller than or nearly identical with the value in the absence of the additive for PVP ball-milled for more than 20 hours from the time of the induction period. In the presence of the fine powders of activated charcoal in air,  $M_c$  was larger than the value in the absence of the additive. (Table VIII)

In the presence of chloranil in various kinds of atmosphere,  $M_c$  was nearly identical or smaller than the value in the absence of the additive at the first stage of ball-milling from the time of the induction period (Table IX).

Equation (8) is obtained by differentiating equation (4) with ball-milling time,  $t$ .

$$-\partial R/\partial M_u = nkM_u^{(n-1)}R \quad (8)$$

In equation (8),  $-\partial R/\partial M_u$  is the ratio of the weight of the polymers of molecular weight between  $M_u$  and  $M_u + \partial M_u$  to the total weight of the polymers. When  $n$  is larger than 1.0,  $-1/R(\partial R/\partial M_u)$  decreases with a decrease of  $M_u$ . Accordingly, it is considered that the weight of the polymers in each fraction decreases with a decrease of molecular weight in the range of  $M_u$  below  $M_c$ .

Baramboim investigated a decrease of molecular weight of several kinds of polymers by the mechanical treatment and found that the molecular weight approached to the limited

value between  $4 \times 10^3$  and  $1.1 \times 10^4$ .<sup>8)</sup> It was reported in the previous paper that the molecular weight of PVP varied from  $9.7 \times 10^5$  to a lower value and approached to  $4 \times 10^3$  by ball-milling.<sup>7)</sup> But an appreciable decrease of molecular weight was not observed by ball-milling PVP of  $7.5 \times 10^3$  of mean molecular weight, even after ball-milling for 200 hours.<sup>9)</sup> In many cases in the absence and in the presence of various kinds of the additives, the molecular weight distribution of PVP approached to the narrow distribution with the peak of a fixed low molecular weight by ball-milling, as reported in the previous papers<sup>2,7,9)</sup> and as shown in Fig. 1 and 2. Blundel, *et al.* also found the similar phenomenon by investigating molecular weight distribution of the polyethylene crystals degraded by nitric acid etching, and considered that there was a surprising regularity in the break-down pattern, indicative of certain discrete length which must be related to the way the chains were arranged in the crystals.<sup>10)</sup> These findings are considered to be related to the existence of  $M_c$ .

### 3) Variation of R with the Ball-Milling Time

The values of  $(-\log R)$  for  $10^6$ ,  $5 \times 10^5$ ,  $10^5$ ,  $5 \times 10^4$  and  $10^4$  of  $M_u$  were obtained by reading the values on the  $\log(-\log R)-\log M_u$  line. As shown in Fig. 7, equation (9) was applied to the variation of  $R$  with the ball-milling time,  $t$ , where  $k_t$ ,  $k_t'$ ,  $\gamma_1$  and  $\gamma_2$  were parameters dependent on the ball-milling condition and so on, and  $t_c$  was the time at which the line obtained by the logarithmic plot of  $(-\log R)$  versus  $(t-t_c)$  broke.

$$\begin{aligned} t < t_c & \quad R = \exp \{-k_t(t-t_c)^{\gamma_1}\} \\ t \geq t_c & \quad R = \exp \{-k_t'(t-t_c)^{\gamma_2}\} \end{aligned} \quad (9)$$

Table X, XI, XII, XIII and XIV show the numerical values of the parameters  $t_c$ ,  $\gamma_1$  and  $\gamma_2$ . When a straight line was obtained by the logarithmic plot of  $(-\log R)$  versus  $(t-t_c)$ , the gradient of the line was considered to be  $\gamma_2$  (Fig. 8).

In case of ball-milling in nitrogen in the presence of white alundum or barbituric acid,  $\gamma_2$  decreased with a decrease of  $M_u$ . In the presence of sodium chloride in nitrogen or in the presence of the granules of activated charcoal in air,  $\gamma_2$  was independent of  $M_u$ . But, in the other cases,  $\gamma_2$  increased with a decrease of  $M_u$  in the range of  $M_u$  above  $5 \times 10^4$ .

Equation (10) was obtained by differentiating equation (9) with ball-milling time,  $t$ .

$$-\partial R/\partial t = \gamma_2 \cdot k_t'(t-t_c)^{(\gamma_2-1)} R \quad (10)$$

In equation (10),  $-\partial R/\partial t$  is the ratio of the weight of the polymers whose molecular weight varies from the value above  $M_u$  to the value below  $M_u$  by the mechanical treatment for the

TABLE X. Numerical Values of  $\gamma_1$ ,  $\gamma_2$  and  $t_c$  for Ball-Milling PVP in the Absence of the Additive  
 $J_b=0.22$ ,  $J_s=0.067$  (referred to Table I)

$M_u$	Atmosphere								
	Nitrogen			Air			Oxygen		
	$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$t_c$ (hr) <sup>a)</sup>	$\gamma_1$	$\gamma_2$
$10^6$	56	0	0.47			0.24	53	—	0.50
$5 \times 10^5$	43	0.04	0.46			0.28	53	—	0.53
$10^5$	42	0.25	0.77	51	0.37	0.52	53	—	0.74
$5 \times 10^4$	55	0.40	0.90	53	0.38	0.63	53	—	0.86
$10^4$							53	—	0.37

a) The value of  $\gamma_1$  in case of ball-milling in oxygen could not be obtained, as the data were not sufficient for the calculation. But the same tendency as observed in nitrogen or air was also obtained for  $\gamma_1$  in oxygen.

8) N.K. Baramboim, *Dokl. Akad. Nauk SSSR*, **114**, 568 (1957); *Zhur. Fiz. Khim.*, **32**, 433 (1958).

9) N. Kaneniwa and A. Ikekawa, *Yakuzai-gaku*, **31**, 201 (1971).

10) D.J. Blundell, A. Keller, and I.M. Ward, *Polymer Letters*, **4**, 781 (1966).

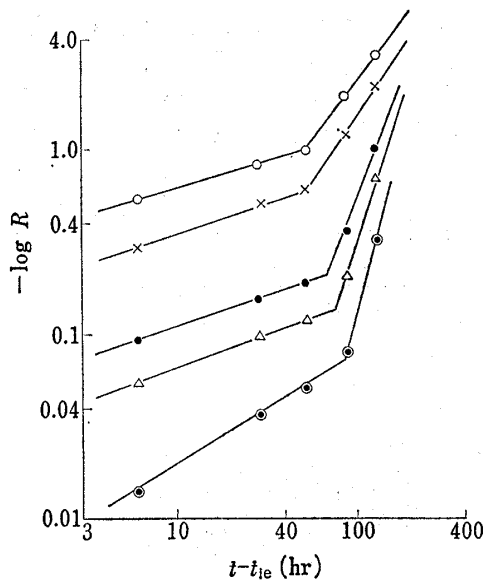


Fig. 7. Relation between  $R$  and Ball-Milling Time for Ball-Milling PVP in Nitrogen in the Presence of 10% of Phenothiazine

$t_{ie}=87$  (hr),  $J_b=0.22$ ,  $J_s=0.06^{(3)}$  (referred to Table I).  
 $M_u$ :  $\circ$ ,  $10^6$ ;  $\times$ ,  $5 \times 10^5$ ;  $\bullet$ ,  $10^5$ ;  $\Delta$ ,  $5 \times 10^4$ ;  $\odot$ ,  $10^4$ .

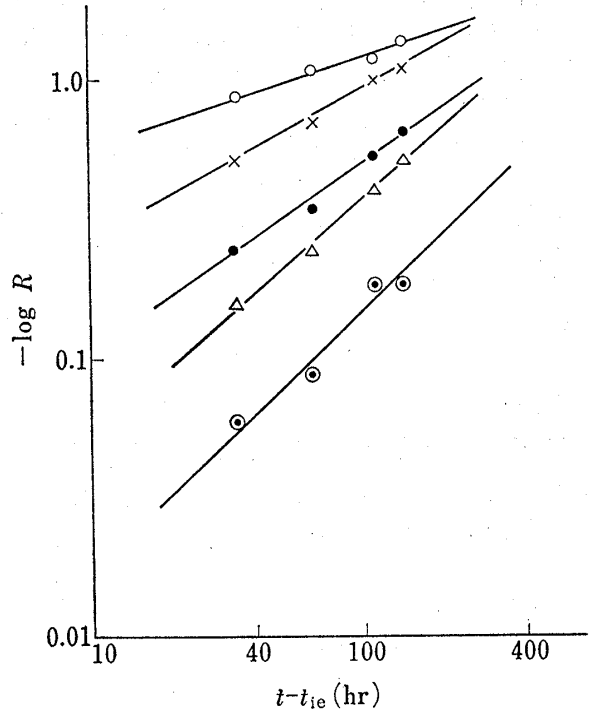


Fig. 8. Relation between  $R$  and Ball-Milling Time for Ball-Milling PVP in Air in the Presence of 10% v/v of Talc

$t_{ie}=66$  (hr),  $J_b=0.22$ ,  $J_s=0.06^{(3)}$  (referred to Table I).  
 $M_u$ :  $\circ$ ,  $10^6$ ;  $\times$ ,  $5 \times 10^5$ ;  $\bullet$ ,  $10^5$ ;  $\Delta$ ,  $5 \times 10^4$ ;  $\odot$ ,  $10^4$ .

TABLE XI. The Numerical Values of  $\gamma_1, \gamma_2$  and  $t_c$  for Ball-Milling PVP in the Presence of Inorganic Powders  
 $J_b=0.22$ ,  $J_s=0.06^{(2,3)}$  (referred to Table I)

Additive	White alundum						Silica sands		Zinc oxide			Air
	Atmosphere	Nitrogen		Air		Nitrogen	Air	Nitrogen		Air		
		$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$t_c$ (hr)			$\gamma_1$	$\gamma_2$		$t_c$ (hr)	
$M_u$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$\gamma_2$	$\gamma_2$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$\gamma_2$
$10^6$	21	0.36	1.0	30	0.37	0.81	0.46	0.53	108	0.20	0.98	0.43
$5 \times 10^5$	24	0.38	1.1	30	0.49	0.90	0.59	0.74	126	0.50	1.1	0.53
$10^5$	26	0.51	0.99	48	0.72	1.3	0.86	1.1			1.2	0.84
$5 \times 10^4$			0.73	42	0.62	1.5	0.97	1.1			1.6	0.90
$10^4$			0.75	41	0.51	2.1	1.6				1.5	

Additive	Barium sulfate	Sodium chloride				Talc	
		Air	Nitrogen		Air	Nitrogen	Air
			$t_c$ (hr)	$\gamma_1$			
$M_u$	$\gamma_2$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$\gamma_2$	$\gamma_2$	$\gamma_2$
$10^6$	0.66	145	0.29	2.3	0.77	0.85	0.30
$5 \times 10^5$	0.76	125	0.35	1.7	0.99	1.0	0.57
$10^5$	0.98	115	0.55	1.9	1.5	1.4	0.70
$5 \times 10^4$	1.8	95	0.53	1.7	1.6	1.5	0.88
$10^4$	2.0			2.7	0.18	1.5	0.90

TABLE XII. The Numerical Values of  $\gamma_1$ ,  $\gamma_2$  and  $t_c$  for Ball-Milling PVP in the Presence of 10% of Organic Powders $J_b=0.22$ ,  $J_s=0.06^{2,3}$  (referred to Table I)

$M_u$	Additive		Vitamin K <sub>3</sub>				Acridine			Methylene blue	Phenothiazine					
	Atmosphere	$t_c$ (hr)	Nitrogen		Air	Nitrogen		Air	Air	Nitrogen			Air			
			$\gamma_1$	$\gamma_2$	$\gamma_2$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$\gamma_2$	$\gamma_2$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$
$10^6$		150	0	0.83	0.42	152	0.12	0.78	0.73	1.1	140	0.29	1.3	155	—	0.35
$5 \times 10^5$		150	0	1.1	0.47	157	0.09	1.2	0.84	1.2	140	0.34	1.5	155	—	0.87
$10^5$				1.3	0.66	154	0	1.6	1.4	1.2	160	0.33	2.9	155	—	1.3
$5 \times 10^4$				1.3	0.66	157	0	1.7	1.7	1.3	160	0.36	3.0	155	—	1.4
$10^4$				1.2	0.66	146	0.14	1.6	2.4		170	0.65	3.5			0.76

$M_u$	Additive		<i>p</i> -Hydroquinone				Barbituric acid									
	Atmosphere	$t_c$ (hr)	Nitrogen		Air		Nitrogen			Air						
			$\gamma_1$	$\gamma_2$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$			
$10^6$				0.49	34	0.21	1.7	46	0.32	1.6			0.62			
$5 \times 10^5$		40	0.52	1.5	32	0.19	1.8	48	0.37	1.6			0.81			
$10^5$				1.5	20	0.09	1.8	46	0.58	1.3	68	1.3	2.3			
$5 \times 10^4$				1.8	18	0.55	2.0	54	0.72	1.2	90	1.1	2.6			
$10^4$				2.8			0.50			0.23						

TABLE XIII. The Numerical Values of  $\gamma_1$ ,  $\gamma_2$  and  $t_c$  for Ball-Milling PVP in the Presence of Activated Charcoal (AC) in Various Kinds of Atmosphere $J_b=0.22$ ,  $J_s=0.06^{2,3}$  (referred to Table I)

$M_u$	Kind of AC Content of AC Atmosphere	Granules 10% N <sub>2</sub> (H <sub>2</sub> O)		Granules 10% N <sub>2</sub> (H <sub>2</sub> O <sub>2</sub> )	Granules 15.1% Air	Fine powders 10% Air	Granules 15.1% O <sub>2</sub>	Granules 10% O <sub>2</sub> (H <sub>2</sub> O)	
		$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$\gamma_2$	$\gamma_2$	$\gamma_2$	$\gamma_2$	
		$\gamma_2$	$\gamma_1$	$\gamma_2$	$\gamma_2$	$\gamma_2$	$\gamma_2$	$\gamma_2$	
$10^6$				0.53	0.36	1.0	0.70	0.37	0.98
$5 \times 10^5$		162	0.55	1.1	0.43	1.0	0.96	0.68	0.97
$10^5$		166	0.51	1.4	0.48	1.1	1.5	1.1	1.3
$5 \times 10^4$		166	0.54	1.8	0.51	1.0	1.1	1.1	1.3
$10^4$		163	0.21	2.6	0	1.5		0.96	1.5

TABLE XIV. The Numerical Values of  $\gamma_1$ ,  $\gamma_2$  and  $t_c$  for Ball-Milling PVP in the Presence of Chloranil in Various Kinds of Atmosphere $J_b=0.43$ ,  $J_s=0.03^3$  (referred to Table I)

$M_u$	Content of chloranil Atmosphere	5%	5%	5%	10%		5%	5%			
		N <sub>2</sub> (H <sub>2</sub> O)	N <sub>2</sub> (H <sub>2</sub> O <sub>2</sub> )	Air	Air		O <sub>2</sub>	O <sub>2</sub> (H <sub>2</sub> O)			
		$\gamma_2$	$\gamma_2$	$\gamma_2$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$	$\gamma_2$	$t_c$ (hr)	$\gamma_1$	$\gamma_2$
$10^6$		0.68	—	0.32				0.66	54	0.40	0.55
$5 \times 10^5$		0.67	—	0.56		1.5		0.69	56	0.43	0.79
$10^5$		0.98	1.0	1.0	227	1.4	0.68	0.91	59	0.57	1.1
$5 \times 10^4$		0.98	1.1	1.5	224	2.2	0.86	0.99	62	0.42	2.4
$10^4$		0.47	0.61	0.80			0.39	0.99	64	0.39	—



time,  $\partial t$ , to the total weight of the polymers. The value of  $-(1/R)(\partial R/\partial t)$  increases with the lapse of the ball-milling time when  $\gamma_2$  is larger than 1.0, and decreases when  $\gamma_2$  is smaller than 1.0. Equation (10) seems to suggest that the mean density of the activated bonds on a polymer molecule,  $\gamma$ , increases with a decrease of molecular weight of PVP, when  $\gamma_2$  increases with a decrease of  $M_u$ , and that the opposite is the case when  $\gamma_2$  decreases with a decrease of  $M_u$ .

TABLE XV. The Numerical Values of  $M_c$ , and  $n_o$ ,  $R_{r1}$  and  $R_{r2}$  for Ball-Milling PVP in the Presence of Inorganic or Organic Powders

$J_b=0.22$ ,  $J_s=0.06^{2,3,7}$  (referred to Table I)

Additive	Atmosphere	$M_c$	$n_o$	$R_{r1}$	$R_{r2}$
Absent	Nitrogen	$(4-6) \times 10^4$	0.9		1.9
Absent	Air	$(3-5) \times 10^4$	0.7		2.6
Absent	Oxygen	$(3-4) \times 10^4$	0.7		1.7
White alundum	Nitrogen		0.7-0.8		0.72
White alundum	Air		1.0	1.7	1.8
Silica sands	Nitrogen	$(2-4) \times 10^4$	0.9		2.1
Silica sands	Air	$3.5 \times 10^5$	1.0-1.2		1.4
Zinc oxide	Nitrogen	$(5-6) \times 10^4$	1.1-1.2		1.6
Zinc oxide	Air	$(4-6) \times 10^4$	1.0		2.1
Barium sulfate	Air	$7 \times 10^4$	0.9-1.1		2.8
Sodium chloride	Nitrogen	$2 \times 10^5$	0.9-1.0	1.8	0.74
Sodium chloride	Air	$(7-8) \times 10^4$	1.0		2.1
Talc	Nitrogen		1.0-1.2		1.7
Talc	Air		0.9		2.9
Vitamin K <sub>3</sub>	Nitrogen	$(2.5-3) \times 10^4$	0.9-1.0		2.2
Vitamin K <sub>3</sub>	Air		0.7-1.0		1.6
Acridine	Nitrogen		0.6-1.0		2.2
Acridine	Air	$8 \times 10^4$	1.0		2.3
Methylene blue	Air	$10^5$	1.1		1.2
Phenothiazine	Nitrogen		0.6-1.0	1.2	2.3
Phenothiazine	Air	$(2-5) \times 10^4$	0.9-1.0		4.0
<i>p</i> -Hydroquinone	Nitrogen	$(1-2) \times 10^5$	1.0-1.4		1.2
<i>p</i> -Hydroquinone	Air	$(1-2) \times 10^5$	1.2-1.3		1.2
Barbituric acid	Nitrogen		0.8	2.3	0.76
Barbituric acid	Air		1.2-1.3		4.3

TABLE XVI. The Numerical Values of  $M_c$ ,  $n_o$ ,  $R_{r1}$  and  $R_{r2}$  for Ball-Milling PVP in the Presence of Activated Charcoal (AC) or Chloranil

Additive	Content of additive (%)	Atmosphere	$M_c$	$n_o$	$R_{r1}$	$R_{r2}$
AC (Granules)	10	N <sub>2</sub> (H <sub>2</sub> O)	$(1-2) \times 10^4$	0.7	1.0 <sup>a)</sup>	3.4
AC (Granules)	10	N <sub>2</sub> (H <sub>2</sub> O <sub>2</sub> )		0.6-1.1 <sup>b)</sup>		1.4
AC (Granules)	15.1	Air		0.8		1.0
AC (Fine powders)	10	Air	$1.4 \times 10^5$	1.0		1.5
AC (Granules)	15.1	O <sub>2</sub>	$(1-2) \times 10^4$	0.8-1.0		3.2
AC (Granules)	10	O <sub>2</sub> (H <sub>2</sub> O)	$(2-3) \times 10^4$	0.7-0.9		1.3
Chloranil	5	N <sub>2</sub> (H <sub>2</sub> O)	$(1-2.5) \times 10^4$	0.7		1.4
Chloranil	5	N <sub>2</sub> (H <sub>2</sub> O <sub>2</sub> )	$10^4$	0.6-1.0		—
Chloranil	5	Air		0.9-1.0		4.7
Chloranil	10	Air	$(7-8) \times 10^4$	0.8	1.5 <sup>a)</sup>	
Chloranil	5	O <sub>2</sub>	$(2-3.5) \times 10^4$	0.8		1.5
Chloranil	5	O <sub>2</sub> (H <sub>2</sub> O)	$(3-9) \times 10^4$	0.9	1.1	4.3

a) In these cases, the ratio of  $\gamma_1$  for PVP of  $M_u$  of  $5 \times 10^4$  to  $\gamma_1$  for PVP of  $M_u$  of  $5 \times 10^5$  was shown for the data of  $\gamma_1$  for PVP of  $M_u$  of  $10^6$  could not be obtained.

b) The value of  $n_o$  was approximately 0.6 for PVP of molecular weight,  $M_u$ , above  $2 \times 10^4$  and 1.1 for PVP of  $M_u$  below  $2 \times 10^4$ .

AC,  $J_b=0.22$ ,  $J_s=0.06^{2,3}$ ; Chloranil,  $J_b=0.43$ ,  $J_s=0.03^{3)}$  (referred to Table I).

#### 4) Discussion on the Way How the Chains are broken

Though equation (5) is very complicated, it is suggested from this equation that, in case of the random chain scission, the parameter  $n$  in equation (4) is larger than 1.0, when  $\gamma(M_i)$  increases with an increase of  $M_i$ , and that  $n$  is smaller than 1.0 in the opposite case. The parameter  $n$  varied with the ball-milling time, as shown in Table V, VI, VII, VIII and IX. The value of  $n$  in the range of  $M_u$  above  $M_c$  after ball-milling for an infinitely short time from the time of the induction period,  $n_0$ , was obtained by extrapolating the  $\log n - (t - t_{ie})$  curve. Table XV and XVI show the numerical values of  $n_0$  and the ratio of the value of  $\gamma_1$  or  $\gamma_2$  for PVP of  $M_u$  of  $5 \times 10^4$  to the value for PVP of  $M_u$  of  $10^6$ ,  $R_{\gamma_1}$  or  $R_{\gamma_2}$ , respectively. The following suggestion seems to be reasonable from the comparison of  $n_0$  and  $R_{\gamma_1}$  or  $R_{\gamma_2}$ .

In case of ball-milling in air in the presence of barbituric acid,  $n_0$  was little larger than 1.0 and  $R_{\gamma_2}$  was larger than 1.0. In this case, the probability of chain scission at the center of a polymer may be a little higher than the probability near the end of a polymer. But, in the other cases,  $n_0$  was around or below 1.0, and  $R_{\gamma_1}$  and  $R_{\gamma_2}$  were approximately equal to or larger than 1.0. In case of ball-milling in nitrogen in the presence of white alundum,  $n_0$  was smaller than 1.0, and  $\gamma_1$  increased with a decrease of  $M_u$ , as shown in Table XI. In these cases, random chain scission is most probable and the value of  $\gamma$  for PVP of low molecular weight seems to be approximately equal to or larger than the value for PVP of high molecular weight.

Roughly speaking, the following tendency was observed. The peak in the molecular weight distribution curve of PVP shifted from approximately  $10^6$  to lower molecular weight by ball-milling and the value of  $\beta_e$  was large, when  $R_{\gamma_2}$  was around or below 1.0 or when the probability of chain scission at the center seemed to be a little larger than the probability near the end of a polymer.

#### Experimental

The ball-milled samples reported in the previous papers were used.<sup>2,3,7)</sup> The molecular weight distribution of PVP in the supernatant obtained by centrifugal separation of  $\text{KH}_2\text{PO}_4 \cdot \text{Na}_2\text{HPO}_4$  buffer solution (pH: 6.3, ionic strength; 0.05) of the ball-milled sample was investigated by gel permeation method and by viscometry reported in the previous papers.<sup>2,7)</sup>