

Communications to the Editor

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CHARACTERIZATION OF NOVEL SUBSTITUENT ENTROPY CONSTANT
BY CLUSTER ANALYSIS

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Eighteen kinds of current QSAR parameters were analysed by the cluster analysis, and divided into 4 groups, namely, cluster 1 = σ_i , $|\sigma_i|$, σ_m , F; cluster 2 = σ_π , σ_p , R; cluster 3 = MR, Pr, Vw, $\sigma_{s\circ}$, ΔS° , π , Es, Mw; cluster 4 = $|\sigma_\pi|$, i , μ . Of the eight kinds of parameters belonging to cluster 3, MR, Pr, and Vw can be substituted by $\sigma_{s\circ}$, whereas π (aromatic group) and Es are expressed by the linear combination of σ_i , σ_π and $\sigma_{s\circ}$.

KEYWORDS ——— substituent entropy constant $\sigma_{s\circ}$; QSAR analysis; cluster analysis; substituent constant; regression analysis; nonlinear mapping

In the previous works¹⁾ on the studies of QSAR analysis, we have proposed a substituent entropy constant $\sigma_{s\circ}$ and approved the utility of this parameter as a quadratic form, where the biological response BR of the drug was expressed as Eq.1.

$$BR = a(\sigma_{s\circ})^2 + b\sigma_{s\circ} + c|\sigma_i| + d|\sigma_\pi| + e \quad (1)$$

This communication dealt with the characterization of $\sigma_{s\circ}$ using the cluster analysis and nonlinear mapping (NLM) of the eighteen kinds of current QSAR parameters including $\sigma_{s\circ}$. The results show that they are classifiable into four clusters (Table 1). Eighteen-space coordinates of QSAR parameters are displayed in two-dimensional space using the NLM method²⁾ (Fig.1).

Table I. Cluster Analysis of the Eighteen Kinds of QSAR Parameters

cluster 1	σ_i ³⁾ $ \sigma_i $ σ_m F ⁴⁾	σ -inductive or field effect
cluster 2	σ_π ³⁾ σ_p R ⁴⁾	π -resonance effect
cluster 3	MR ⁵⁾ Pr ⁵⁾ Vw ⁵⁾ Es Mw ⁵⁾ ΔS° $\sigma_{s\circ}$ π ⁵⁾	steric effect (entropy/term)
cluster 4	$ \sigma_\pi $ i ⁶⁾ μ ⁶⁾	others

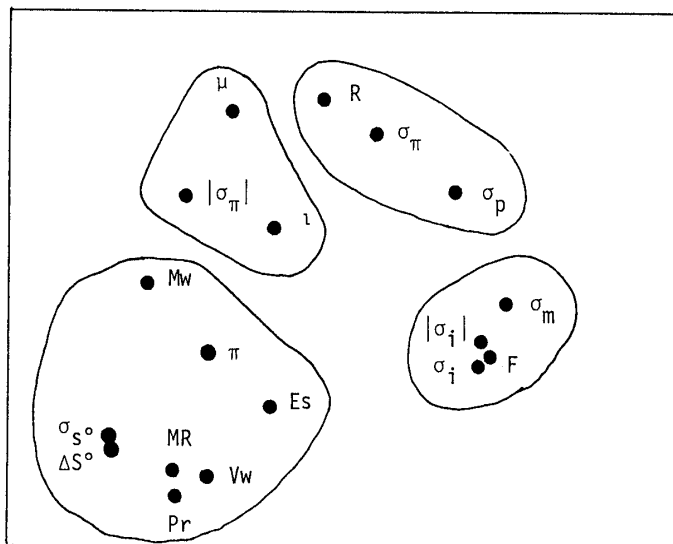


Fig.1. Nonlinear Map of Eighteen Kinds of Current QSAR Parameters

Of the eight kinds of empirical parameters belonging to cluster 3, π and Es are taken as the parameters related to the energy term, but others are not. Consequently, the two parameters should be analysed by the linear combination of the enthalpy and entropy parameters, e.g. σ_i , σ_π ³⁾ and σ_{s° . π of aromatic compounds was analysed in the previous works.¹⁾ In this communication, we report the analysis of the aliphatic π .

The results are as follows⁷⁾;

$$\pi = 11.42 \sigma_{s^\circ} - 0.90 \quad r = 0.937^{**} \quad SE = 0.098 \quad (2)$$

$n = 22$ MeR R = H, F, OH, OMe, Cl, Br, Me, Et, n-Pr, n-Bu, n-Am, n-Oct, i-Bu, t-Bu, i-Pr, CF₃, Ph, PhCH₂, PhCH₂CH₂, Cyclopentyl, Cyclohexyl, Ph(CH₂)₃

$$Es = -10.56 \sigma_{s^\circ} - 2.35 \sigma_\pi^{**} - 0.08 \quad (3)$$

$$r = 0.925 \quad F = 20.99^{**} \quad SE = 0.14$$

$n = 10$ PhR R = H, Me, Et, t-Bu, OH, OMe, NH₂, NMe₂, F, NO₂

$|\sigma_\pi|$ denotes the contribution of a weak interaction, σ_π indicates a strong one.

On the other hand, the entropy parameter σ_{s° or ΔS° is thermodynamically most applicable to cluster 3, so we analysed the non-energy parameters with respect to σ_{s° and obtained these results:

$$Vw = 3.855 \sigma_{s^\circ} - 0.020 \quad r = 0.941^{**} \quad SE = 0.025 \quad (4)$$

$n = 12$ PhR R = H, Me, Et, n-Pr, i-Pr, t-Bu, Ph, CH=CH₂, F, Cl, Br, I

$$MR = 87.82 \sigma_{s^\circ} + 0.26 \quad r = 0.853^{**} \quad SE = 0.95 \quad (5)$$

$n = 13$ PhR R = H, Me, Et, n-Pr, NMe₂, t-Bu, F, Cl, Br, I, C≡CH, OMe, NO₂

$$Pr = 888.8 \sigma_{s^\circ} - 3.8 \quad r = 0.876^{**} \quad SE = 6.8 \quad (6)$$

$n = 12$ PhR R = H, Me, Et, Ph, C≡CH, CH=CH₂, F, Cl, Br, I, CN, NO₂

The details of this work will be published in a subsequent paper.

EXPERIMENTAL

1. Cluster Analysis

Cluster Analysis was carried out by the farthest neighbor method using Euclidean distances calculated from the contribution ratio matrix of eighteen kinds of QSAR parameters.

2. Nonlinear Mapping (NLM)

NLM was carried out using the same data as for the cluster analysis. Two-dimensional space coordinates were obtained by our own programs using the SIMPLEX method⁸⁾ and the Davidson-Fletcher-Powell method⁹⁾ for minimization of the stress and by the NEC GDSP-6 system for plotting two-dimensional space coordinates.

3. Regression Analysis

The regression analysis were carried out using the program NEC TSS LIBRARY TSS/LIB-6 and our own programs coded in BASIC language. The values of SE are obtained from the equation $SE = [S_{se}/(n-k)(n-k-1)]^{1/2}$, where n = number of observations, k = number of independent variables and S_{se} = sum of squares of residuals.

4. Calculation

All numerical treatments were carried out with a NEAC S-900 computer at the Computation Center, Osaka University; a FACOM M-200 computer at the Computation Center, Kyoto University; a HITAC M-200H computer at the Computation Center, Tokyo University and a personal computer NEC PC8001.

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- 5) MR:molar refructivity, Pr:parachor, Vw:van der Waals volume, Mw:molecular weight, π :hydrophobic substituent constant.
All the values of these parameters, E_s , σ_p and σ_m are cited from references.¹⁰⁾
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- 7) All regression coefficients in this communication passed the t-test (p=0.01).
**: The null hypothesis, H_0 , is abandoned (p=0.01). $H_0: r = 0$ or $a_1 = a_2 = \dots = 0$.
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