Studies of Ion Pair Solvation: Absolute Rate Constants of Propagation of the Tetraglyme-co-ordinated Living Sodium Polystyrene

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Summary Studies of anionic polymerization of styrene in tetrahydropyran in the presence of tetraglyme led to the absolute value of the equilibrium constant $K_{\rm G}$, $-S^-$, Na⁺ + glyme $\rightleftharpoons -S^-$, Na⁺ (glyme), and to the absolute value of the propagation constant of the "glymated" species

$$-S^-,Na^+$$
 (glyme) + S $\rightarrow --S^-Na^+$ (glyme), k_g .

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The addition of tri- or tetra-glyme (G) to a solution of living sodium polystyrene ($-S^-$, Na⁺) in tetrahydropyran (THP)

has a profound effect upon the rate of propagation.¹ In the absence of glyme the polymerization is propagated by two species: the rapidly growing polystyryl carbanions, $(-S^-)$, and the slowly growing ion pairs, $(-S^-, Na^+)$, the latter forming the bulk of the growing ends. Thus,

$$-S^{-} + S \rightarrow -S^{-}, \qquad k_{-}, \qquad (1)$$

$$-S^{-}, Na^{+} + S \rightarrow -S^{-}, Na^{+}, \qquad k_{\pm}, \qquad (2)$$

and

$$-S^{-}, Na^{+} \rightleftharpoons -S^{-} + Na^{+}, \qquad K_{\text{Dist}}$$
(3)

Two additional species are formed in the presence of tetraglyme (G), *viz.*,

$$-S^{-}, Na^{+} + G \rightleftharpoons -S^{-}, G, Na^{+}, K_{\beta}, \qquad (4)$$

yields the ion pairs co-ordinated with the glyme, and

$$Na^+ + G \rightleftharpoons Na^+, G, \qquad K_{Na},$$
 (5)

produces sodium ions complexed with the glyme. The $-S^{-},G,Na^+$ ion pairs are more reactive than the tight $-S^{-},Na^+$ pairs, their propagation constant being denoted by $k_{\rm G}$. The acceleration of styrene polymerization resulting from the addition of glyme is caused, therefore by: (a) the conversion of the relatively unreactive $-S^-,Na^+$ ion pairs into much more reactive $-S^-,G,Na^+$ pairs; (b) the increase in the proportion of the highly reactive $-S^-$ free ions due to the conversion of Na⁺ into Na⁺,G. The magnitude of the effect is shown in Figure 2 of ref. 1, *e.g.*, in the presence of $2 \cdot 8 \times 10^{-3}$ M-tetraglyme, the observed propagation constant increases from 150 M⁻¹ sec.⁻¹ to 3500 M⁻¹ sec.⁻¹.

The previously reported work¹ permitted us to determine the product $k_{\rm g}K_{\rm g}$. In the course of the present work we evaluated the individual constants. This was achieved by studying the polymerization at concentrations of tetraglyme sufficiently high to cause an extensive conversion of $-S^-$, Na⁺ into $-S^-$, G, Na⁺. Furthermore, extension of these studies to lower temperatures led to the determination of $\Delta H_{\rm o}$ and $\Delta S_{\rm g}$ (pertaining to equilibrium 4) and $E_{\rm g}$ (pertaining to reaction 6),

$$-S^{-},G,Na^{+} + S \rightarrow -S^{-},G,Na^{+}, k_{g}.$$
(6).

At any concentration of tetraglyme the intercept, I(G), of the line giving the observed propagation constant, k_p , as a function of [living polymers]⁻¹, is equal to $(1 - f)k_{\pm} + fk_{a}$, f being the fraction of living polymers present as $-S^-,G$, Na⁺. The intercepts may also be obtained by determining k_p as a function of $[Na^+]^{-1}$, the concentration of Na⁺ ions being varied by the addition of Na⁺, BPh₄⁻. The second method is preferred since the lines are then flatter and extrapolation more reliable (see Figure 2 of ref. 1).

The relation $f/(1-f) = K_0[G]$ coupled with the inequality $k_0 \gg k_{\pm}$ leads to the equation

$$\frac{1}{I(G) - I(O)} = \frac{1}{k_G} + \frac{1}{k_G K_G}.$$
 [G]⁻¹,

where I(O) is the intercept of the line obtained in the absence of tetraglyme. A plot of $1/{I(G) - I(O)}$ against $[G]^{-1}$ is

TABLE

Equilibrium constant K_G for the reaction



exemplified by Figure 1 and its slope and intercept give eventually $k_{\rm g}$ and $K_{\rm g}$. Thus, the experiments performed

at 25°, 0°. -20° , and -45° led to the data summarized in the Table. Moreover, at lower temperatures $k_{\rm G}$ could be determined directly from the asymptotes of the plots of



I(G) against [G] as shown in Figures 2a and b. Figure 2c shows in more detail the results obtained at 25°. The

initial slope and the asymptote permit us to evaluate $k_{\rm g}$ and K_{α} .



FIGURE 2c. The lower scale refers to the lower curve.





FIGURE 4

The van't Hoff plot (log $K_{\mathfrak{g}}$ against 1/T) and the Arrhenius plot (log k_0 against 1/T) are shown in Figures 3 and 4, respectively. From these $\Delta H_{g} = -6.5$ kcal./mole, $\Delta S_{g} =$ -13 e.u., and $E_{g} = 1.2$ kcal./mole.

Closely similar values of $\Delta H_{\mathfrak{g}}$ and $K_{\mathfrak{g}}$ were obtained in other systems. For example, for

Biphenylide, $Na^+ + G \rightleftharpoons$ Biphenylide, G, Na^+

 $\Delta H_{\rm G} = -6.0$ kcal./mole and $K_{\rm G}$ (at 21°) = 75 m⁻¹ in THP,² and -4.6 kcal./mole and 145 M⁻¹, respectively, in methyltetrahydrofuran;² for

Fluorenyl⁻,Na⁺ + G \rightleftharpoons Fluorenyl⁻,G,Na⁺ in THF³

 $\Delta H_{\rm G} = -7.0$ kcal./mole and $K_{\rm G}$ (at 25°) = 125 M⁻¹; for

Naphthalenide, $Na^+ + G \rightleftharpoons Naphthalenide, G, Na^+$ in THP4

 $K_{\rm G}$ (at 25°) is about 200 M⁻¹. Apparently, the nature of anion and of solvent only slightly affects thermodynamics of tetraglyme co-ordination with the Na⁺ ion of a tight ion pair.

The reactivity of -S⁻,G,Na⁺, measured by the value of $k_{\rm Q}$, should be compared with those of "solvent separated" polystyryl sodium ion pairs. In tetrahydrofuran (THF) and in dimethoxyethane (DME) sodium ions become fully coordinated with solvent molecules⁵ and their association with the anions yields the solvent separated pairs, provided the solvation shell is not squeezed out. The propagation constants of $-S^{-}(THF)_{n}Na^{+}$ and $-S^{-},(DME)_{m},Na^{+}$ ion pairs^{6,7} are ca. $30,000 \text{ M}^{-1} \text{ sec.}^{-1}$ and $20,000 \text{ M}^{-1} \text{ sec.}^{-1}$, respectively, at 25°. Critical review of the relevant calculations convinces us that, in spite of some assumptions introduced in the derivation, these rate constants are substantially higher than $K_{\rm G}$ (ca. 4000 M⁻¹ sec.⁻¹). Hence, the "glymated" -S-,G,Na+ ion pair, albeit loose, is appreciably less reactive than the loose living sodium polystyrene ion pairs solvated by THF or DME. Recent e.s.r. studies of 'glymated'' loose ion pairs⁴ justify this result and show them to be tighter than the "solvent separated" pairs.

Finally, the unusually low value of $E_{\mathbf{G}}$ calls for comment. We tentatively suggest that -S-,G,Na+ exists in two isomeric forms-a less reactive, which predominates at higher temperatures, and a more reactive which becomes abundant at lower temperatures. Evidence for such two isomers was first reported by Slates and Szwarc² for sodium biphenylide and more recently confirmation of this phenomenon was obtained from the e.s.r. studies⁴ of glymated sodium naphthalenide ion pairs.

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