The Entropy Inhibition of a Gas-phase S_N2 Reaction

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The observed rate constant for proton transfer is much larger than that for the S_N^2 gas-phase reaction between protonated methanol and ammonia, which is reproduced reasonably by the theoretical Gibbs free energy change.

The recent development of ion cyclotron resonance and high pressure mass spectrometry makes the measurement of gas-phase S_N2 reactions feasible. The S_N2 reaction involving positive ions is of particular mechanistic interest. The combination of methanol and protonated methanol has been reported to proceed *via* the typical S_N2 mechanism with Walden inversion.¹

In the present work, the kinetics of a gas-phase reaction between protonated methanol and ammonia are investigated *via* an ion-trapping method.² The potential energy surface is searched by *ab initio* MO calculations. The aim of this work is to compare gas-phase reactivity during proton transfer (equation 1) and during the S_N2 reaction (equation 2) under low pressure (1.17 × 10⁻⁴ mmHg) and high temperature (403 K) conditions.

Apparently, from the reaction enthalpy, ΔH_r , the more exothermic reaction, $S_N 2$, is preferred over proton transfer. However, the rate constants $[k_1 \text{ and } k_2 = (11 \pm 1) \times 10^{-10}$

$$CH_{3}OH_{2}^{+} + NH_{3} - \underbrace{\binom{k_{1}}{k_{1}}}_{S_{N}^{2}} CH_{2}O + CH_{3}NH_{3}^{+} (2) (-151.7) \\ (1) (2) \underbrace{\binom{k_{2}}{k_{2}}}_{S_{N}^{2}} H_{2}O + CH_{3}NH_{3}^{+} (2) (-151.7) \\ (9) (8) \end{array}$$

Proton affinities (PA) (CH₃OH) = 732.2 and 761 kJ/mol from refs. 3 and 4 were used, respectively. The values in square brackets denote theoretical ΔH_r values calculated in this work.



Figure 1. Normalised ion intensities *versus* reaction time observed in a CH₃OH/NH₃ mixture at [CH₃OH]/[NH₃] = 3.27, [CH₃OH] = 4.67 × 10¹² molecule/cm³, temp. = 403 K, electron energy = 30 eV. Mass number (*m*/*z*) and possible ions are indicated. The disappearance rate constants² for the reactions of CH₃OH₂⁺ with NH₃ and CH₃OH were estimated from the slopes of semi-logarithmic plots of the relative ion intensity for the CH₃OH₂⁺. The disappearance rate constant to form (CH₃)₂OH⁺¹ by the reaction of CH₃OH₂⁺ with CH₃OH was determined to be $(0.46 \pm 0.1) \times 10^{-10} \text{ cm}^3/(\text{molecule s})$, in agreement with the value of ~0.5 × 10⁻¹⁰ cm³/(molecule s) reported by Bowers.¹

cm³/(molecule s) and $k_2 \leq 10^{-11}$ cm³/(molecule s)] derived from Figure 1 show the opposite trend. To examine the origin of the very slow rate of the $S_N 2$ reaction, the potential energy diagrams of equations (1) and (2) are drawn in Figure 2. In the course of proton transfer, a stable hydrogen bonded complex (5) is formed. Its Gibbs free energy (G) level is almost the same as that of the product, which indicates that the large value of k_1 is due to there being no point along the reaction path at which ΔG is significantly positive during the dissociation [(5) \rightarrow (10) + (11)].

Under the experimental conditions of low pressure and high temperature, the decrease of the translational entropy (S_{trans}) by ion-dipole complex formation is significantly large.[†] The decrease leads to destabilisation according to the second law of thermodynamics. This trend is obviously shown in equation (2). While the electronic energy (E_T) levels are all below the level of the reactant, the G levels have the larger energy barrier. Even the ion-dipole complex energy level is higher than that of the reactant.

The substantially large rate of equation (1) is attributed both to the large electronic stabilisation energy during the transformation $(1) + (2) \rightarrow (5)$ and to the entropy stabilisation



Figure 2. The potential energy diagram of the electronic energy, $E_{\rm T}$, and the Gibbs free energy, G (pressure = 1.17×10^{-4} mmHg and temp. = 403 K), for equations (1) and (2). $E_{\rm T}$ is calculated with the MP3/6-31+G*//RHF/3-21G method, using the GAUSSIAN 82 program.⁵ On the basis of the 3-21G optimised geometries, the vibrational frequencies are calculated at the RHF/3-21G level. The stationary points with respect to E_{T} 's have been sought along the minimum-energy path of the partial optimisation. Although the strict method of the 'intrinsic reaction co-ordinate' is not used, the presence or the absence of all the stationary points along and near the path has been checked. By the use of the MP3/6-31 + G* E_T , 3-21G geometries, and 3-21G frequencies (scaled down by 0.9 as recommen ded^6), G is evaluated through the standard equations of statistical dynamics.⁷ Energies in the figure stand for the stabilising (<0) or destabilising (>0) values in kJ/mol relative to those of reactants (1) and (2). Values in parentheses denote differences between two adjacent levels. TS refers to the transition state of the S_N^2 reaction (2) with the sole imaginary frequency, 302.1 cm⁻¹. Bond distances in the structural formulae are in Å.

[†] $S_{\text{trans}} = R$ {3/2 ln M + 5/2 ln T - ln P - 1.1650}; R is the gas constant, M is the relative molecular mass, T is temp., and P is pressure. In the process of the ion-dipole complex formation, $\Delta S_{\text{trans}} = S_{\text{trans}}$ (3) - S_{trans} (1) - S_{trans} (2). Under high T (403 K) and low P (1.17 × 10⁻⁴ mmHg) conditions, $-\Delta S_{\text{trans}}$ becomes large (275.6 J mol⁻¹ K⁻¹), which is referred to as a 'decrease' in the text.

 $-T\Delta S$ in $\Delta G = \Delta H - T\Delta S$ during (5) \rightarrow (10) + (11). However, when different experimental conditions (high pressure and low temperature) were applied to the present system, the $S_N 2$ reaction (equation 2) competed with the proton transfer reaction (equation 1). In this case, the G energy level becomes close to the E_T level, and equation (1) suffers destabilisation during the transformation (5) \rightarrow (10) + (11).

This work demonstrates that the gas-phase $S_N 2$ reaction is controlled by the entropy factor as well as by the enthalpy change. Basically, the $S_N 2$ ion-dipole complex does not have enough electronic stabilising energy to overcome the $-T\Delta S$ barrier. The reactivity of the $S_N 2$ reaction should be examined as a function of pressure and temperature.

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