## Characterisation of the UV, Visible and Near-IR Spectra of the Fulleride Anions $C_{60}^{1-}$ , $C_{60}^{2-}$ and $C_{60}^{3-}$ , and Theoretical Analysis of the Spectra of $C_{60}^{1+}$ , $C_{60}^{0}$ , $C_{60}^{1-}$ , $C_{60}^{2-}$ and $C_{60}^{3-}$ by Self Consistent Field-X $\alpha$ -Scattered-Wave (SCF-X $\alpha$ -SW) Calculations

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The spectra of the electrogenerated  $C_{60}^{2-}$ , and  $C_{60}^{3-}$  ions reveal intense near-IR absorption bands similar to those observed in  $C_{60}^{1-}$ ; theoretical analysis of the spectra of  $C_{60}^{2-}$  species (z = 1+, 0, 1-,2-,3-) by SCF-X $\alpha$ -SW calculations provides an explicit interpretation of the strong bands in the UV region, and establishes the nature of the characteristic near-IR bands observed for the cationic and anionic species.

As a three-dimensional delocalised molecule,  $C_{60}^{0}$  is both a vivid optical chromophore and an electron donor-acceptor. The violet or brown solutions in organic media are dominated by three intense absorption bands, centred at 32 000, 40 000 and 46 000 cm<sup>-1</sup> and are featureless in the near-IR. Interestingly, the frontier orbital  $\pi$ - $\pi$ \* promotion is optically forbidden, though this weak absorption can be located at 16300  $cm^{-1}$  (2.02 eV)<sup>†</sup> in concentrated solutions. The spectrum of  $C_{60}^{1-}$  has been reported in solution at room temperature<sup>3,4</sup> and in frozen matrices.<sup>5.6</sup> The three intense UV bands are substantially unchanged from those of  $C_{60}^{0}$ , but a new band emerges near 9300 cm<sup>-1</sup>. We now report that the  $C_{60}^{2-}$  and  $C_{60}^{3-}$  radical anions, along with the  $C_{60}^{1-}$  species, have been reversibly generated electrochemically in  $CH_2Cl_2$  at -60 °C, and in pyridine at -40 °C, and their optical spectra recorded in a cryostatted optically transparent thin-layer electrode (OTTLE) cell. Fig. 1 illustrates the highly characteristic near-IR spectra of  $C_{60}^{1-}$ ,  $C_{60}^{2-}$  and  $C_{60}^{3-}$ .

Table 1 lists the experimental spectroscopic data in the near-IR region for the anionic species.

In each case the leading band is typical of a fully allowed transition, with a rapidly diminishing vibronic progression on the blue edge of the sharp origin.<sup>7</sup> The near-IR spectrum of  $C_{60}^{3-}$  exhibits three absorption bands of comparable intensity, which is not expected for a  ${}^{4}A_{u}$  ( $t_{1u}^{3}$ ) ground state, although studies on the superconducting compound  $K_{3}C_{60}$ 

indicate that the dynamic Jahn–Teller effect is at a maximum for C<sub>60</sub><sup>3-.8</sup> Jones *et al.* have also provided ESR evidence for electron pairing in a distorted C<sub>60</sub><sup>3-</sup> ground state.<sup>9</sup> This may account for the unexpected complexity of the near-IR manifold. Our data do not exclude the possibility of specific ion pairing of C<sub>60</sub><sup>3-</sup> by electrolyte cation (Bu<sub>4</sub>N<sup>+</sup>), or with H<sup>+</sup> ions (from traces of moisture), or of labile oligomerisation. All of these could complicate the spectrum of the three-electron reduced species, as could reaction with CH<sub>2</sub>Cl<sub>2</sub>. The reductions in pyridine give identical spectra for C<sub>60</sub><sup>1-</sup> and C<sub>60</sub><sup>2-</sup> but the C<sub>60</sub><sup>3-</sup> spectrum lacks the lowest energy component. We stress that the C<sub>60</sub><sup>2-</sup>/C<sub>60</sub><sup>3-</sup> transformation was electrosynthetically reversible in both solvents.<sup>‡</sup>

The wealth of new spectroscopic data has encouraged us to calculate the electronic structures and transition energies for each of the species  $C_{60}^+$ ,  $C_{60}^{0}$ ,  $C_{60}^{1-}$ ,  $C_{60}^{2-}$  and  $C_{60}^{3-}$  within the SCF-X $\alpha$ -SW approximation.<sup>10,11</sup>§ Fig. 2(*a*) illustrates how the major spectral features of  $C_{60}^0$  arise as a consequence of the calculated valence-level arrangement. There is pleasing agreement with the parallel calculation of Saito and Oshiyama for  $C_{60}^{0.18}$ 

<sup>‡</sup> The solution of  $C_{60}^{0}$  in CH<sub>2</sub>Cl<sub>2</sub>-0.5 mol dm<sup>-3</sup> Bu<sub>4</sub>NBF<sub>4</sub> was cycled repeatedly through these oxidation states with no loss of spectral intensity. Ncar-IR isosbestic points were found at 8875 and 10100 cm<sup>-1</sup> for  $C_{60}^{1-/2-}$  and at 10300 and 12500 cm<sup>-1</sup> for  $C_{60}^{2-/3-}$ .

<sup>†</sup> For closed shell systems, the optical transition energy, hv, can be approximated by  $hv = (1 + \rho)\Delta E$ ,<sup>1</sup> where  $\Delta E$  is the difference between oxidation and reduction potentials, and  $\rho$  is a vibronic coupling constant, typically 0.3 or less. The reduction of  $C_{60}^{0}$  is observed at -0.45 V vs. the saturated calomel electrode, and Kadish<sup>2</sup> reports the onset of oxidation at +1.76 V, which indicates that  $\rho + 1$  is close to unity. We suggest that  $\rho$  approaches zero because internal and external reorganisation is likely to be small in such a constrained, non-polar molecule.

<sup>§</sup> The coordinates were calculated from the optimised bond lengths of Lüthi and Almlöf<sup>12</sup> (C–C 1.453 and 1.369 Å). The atomic exchange parameters were taken from Schwarz,<sup>13</sup> and the starting potential was generated from a superposition of Herman–Skillman<sup>14</sup> atomic potentials. The wavefunction was expanded using spherical harmonics up to L = 1 on carbon and L = 6 on the outer sphere. The Norman criterion<sup>15</sup> was used to determine sphere radii. A Watson sphere<sup>16</sup> of charge +1, +2, +3 and +4 was used for  $C_{60}^{0}$ ,  $C_{60}^{1-}$ ,  $C_{60}^{2-}$  and  $C_{60}^{3-}$  respectively. The potential was converged using  $D_{5h}$  symmetry, and in each case, the converged ground state potential was used to perform Slater-type transition-state calculations<sup>17</sup> for the excited states.



Fig. 1 Near-IR spectra of (a)  $C_{60}^{1-}$ , (b)  $C_{60}^{2-}$  and (c)  $C_{60}^{3-}$  in  $CH_2Cl_2$  at -60 °C

Table 1 Near-IR bands observed for  $C_{60}^{n-}$  (n = 1, 2, 3) in CH<sub>2</sub>Cl<sub>2</sub>

	v/cm <sup>-1</sup>	$\epsilon/dm^3 mol^{-1} cm^{-1}$	Configuration	
C <sub>60</sub> 1-	9 300 10 730	12 000 3 560	$5t_{1u}^1 \rightarrow 2t_{1g}^1$	
C <sub>60</sub> <sup>2-</sup>	$\frac{10\ 500}{11\ 900}$	18 750 7 688	$5t_{1u}^2 \rightarrow 5t_{1u}^1 2t_{1g}^1$	
C <sub>60</sub> <sup>3-</sup>	7 400 <i>ª</i> 10 100 11 400 12 900	6 700 8 000 8 000 11 250	$5t_{1u}^3 \rightarrow 5t_{1u}^2 2t_{1g}^1$	

<sup>a</sup> Absent in pyridine solution.



**Fig. 2** Transitions contributing to the observed electronic spectra of  $C_{60}^{0}$  and its ions: (*a*) transitions in the UV for  $C_{60}^{0}$  and all derivatives; (*b*) additional transitions for  $C_{60}^{n-}$  arising from promotion from the partially occupied  $t_{1u}$  orbital and (*c*) additional transitions for  $C_{60}^{1+}$  arising from promotions into the partially occupied  $4h_u$  orbital.  $\longrightarrow$  indicates forbidden transition. Approximate transition energies (× 10<sup>3</sup> cm<sup>-1</sup>) are shown under relevant arrows. 1 Ry ≈ 13.61 eV.

**Table 2** Energies/cm<sup>-1</sup> of transitions shown in Fig. 2(a, b)

	$C_{60}^{+}$	C <sub>60</sub>	$C_{60}^{1-}$	$C_{60}^{2-}$	$C_{60}^{3-}$
$4h_{\mu} \rightarrow 5g_{\sigma}$	45 300	45 500	45 800	46 000	46 200
$6h_g \rightarrow 5t_{1u}$	44 500	44 200	43 900	43 600	43 300
$4g_0 \rightarrow 5t_{2u}$	40 300	40 400	40 500	40 700	40 900
$7h_{e} \rightarrow 5t_{2u}$	39 800	40 000	40 100	40 200	40 300
$4h_{u} \rightarrow 8h_{a}$	31 600	31 700	31 700	31 800	31 900
$7h_a \rightarrow 5t_{1u}$	25 500	25 500	25 600	25 600	25 700
$4h_{\mu}^{\mu} \rightarrow 2t_{1\mu}$	24 900	24 900	24 900	24800	24 800
$4h_{\mu} \rightarrow 5t_{1\mu}^{2a}$	16 500	16 500	16600	16600	16700
$5t_{1\mu} \rightarrow 8h_{\alpha}$			15 200	15 200	15 200
$5t_{1u} \rightarrow 2t_{1g}$			8 300	8 200	8 100

<sup>a</sup> Optically forbidden.

Figs. 2(*b* and *c*) show that low-energy (near-IR) transitions are readily anticipated in both  $C_{60}^{n-}$  and  $C_{60}^{1+}$ .

In the 46000 to 40000 cm<sup>-1</sup> region, where two bands are seen, Fig. 2(*a*) shows four possible transitions. The observed band at 46000 cm<sup>-1</sup> coincides with the  $4h_u \rightarrow 5g_g$  transition, while that at 40000 cm<sup>-1</sup> coincides with the  $7h_g \rightarrow 5t_{2u}$  and  $4g_g \rightarrow 5t_{2u}$  transitions (Table 2), but the possibility of a contribution from the  $6h_g \rightarrow 5t_{1u}$  transition to one of these bands cannot be excluded.¶

The band found at 32 000 cm<sup>-1</sup> can be assigned to the 4h<sub>u</sub>  $\rightarrow$  8h<sub>g</sub> transition. The optically forbidden frontier orbital gap transition from 4h<sub>u</sub>  $\rightarrow$  5t<sub>1u</sub> is calculated to occur at 16 500 cm<sup>-1</sup>, which coincides well with experiment. Between these features, the experimental spectrum of C<sub>60</sub><sup>0</sup> displays only a very sharp, weak band at 24 800 cm<sup>-1</sup>, and a much broader, weaker feature in the region 16 000 to 22 000 cm<sup>-1</sup>. The calculations predict two allowed transitions at 25 000 cm<sup>-1</sup>, due to the 4h<sub>u</sub>  $\rightarrow$  2t<sub>1g</sub> and 7h<sub>g</sub>  $\rightarrow$  5t<sub>1u</sub> transitions. Since only

<sup>¶</sup> Preliminary calculations of oscillator strengths have been performed (Noodleman's procedure<sup>19</sup> which indicate that the intensities of the 7h<sub>g</sub>  $\rightarrow$  5t<sub>2u</sub> and 4g<sub>g</sub>  $\rightarrow$  5t<sub>2u</sub> transitions are negligible. This leads us to assign the two bands at 46 000 and 40 000 cm<sup>-1</sup> to the 4h<sub>u</sub>  $\rightarrow$  5g<sub>g</sub> and 6h<sub>g</sub>  $\rightarrow$  5t<sub>1u</sub> transitions.

one band is observed, we conclude that only one of these transitions has non-negligible intensity. There is the possibility of considerable configuration interaction between the T<sub>1u</sub> states arising from the two almost isoenergetic excited configurations,  $4h_u^{92}t_{1g}^{1}$  and  $7h_g^{95}t_{1u}^{1}$ , which may affect both energies and intensities in this region of the spectrum.<sup>20</sup>

The near-IR spectrum of  $C_{60}^{1-}$  defines the energy interval between the 5 =  $t_{1u}^1$  and 2 =  $t_{1g}^1$  configurations as 9300 cm<sup>-1</sup>, thereby approximately thereby empirically mapping the frontier orbital gap of the anion (Fig. 2(b)). In view of the excellent agreement between the SCF-X $\alpha$ -SW calculations and the observed spectrum in the range 15 000-50 000 cm<sup>-1</sup>, it is reassuring that for each of the radical anions  $C_{60}^{n-}$  (n = 1,2,3), a new absorption band system is predicted at about 8200  $cm^{-1}$  (Table 2). No other well-defined new features are observed for the anions, but there is a marked increase in intensity in the region of 17000 cm<sup>-1</sup>, which may reflect the  $5t_{1u} \rightarrow 8h_g$  transition.

The spectrum of the  $C_{60}^{1+}$  cation in the UV region has not been reported. We predict that bands similar to those observed in the neutral and anionic species will be observed in the region  $15\,000-50\,000$  cm<sup>-1</sup>, but there will be additional features due to transitions into the now partially occupied  $4h_{\rm u}$ orbital [Fig. 2(c)], occuring at 28050, 38000, 40700 and 48900 cm<sup>-1</sup>. The strong band observed in the near-IR at 10 200 cm<sup>-1</sup> has been assigned to the  $7h_g \rightarrow 4h_u$  transition,<sup>5</sup> in accord with our calculations, which predict the transitions from the almost isoenergetic 7hg and 4gg orbitals into 4hu orbital to lie in the near-IR region at 9010 and 9450 cm<sup>-1</sup>, respectively.

The invariance of the major spectral features and of the calculated transition energies across the series  $C_{60}{}^0$  to  $C_{60}{}^3$ indicates that the relative ordering of orbitals is insensitive to charge. The measured frontier orbital separations,  $7h_g \rightarrow 4h_u$ (in  $C_{60}^{1+}$ ) and  $5t_{1u} \rightarrow 2t_{1g}$  (in  $C_{60}^{1-}$ ) will therefore be very similar to the corresponding separations in  $C_{60}^{0}$ , where the those transitions are not directly observable, but the  $4h_u \rightarrow$ 5t<sub>10</sub> transition is. Compiling this empirical information regarding energy level separations indicates that both the  $7h_g \rightarrow 5t_{1u}$ and  $4h_u \rightarrow 2t_{1g}$  separations are close to 25000 cm<sup>-1</sup>, as predicted by the calculations. This lends further weight to our assignment of the band at 24800 cm<sup>-1</sup>.

In summary, the electronic spectra of  $C_{60}^{1-}$ ,  $C_{60}^{2-}$  and  $C_{60}^{3-}$  have been observed in the 5000–50 000 cm<sup>-1</sup> range in solution, that of  $C_{60}^{3-}$  showing unexpected complexity in the

near-IR region, and MO calculations have led to a new and self consistent assignment of the spectrum of  $C_{60}^{0}$  and its several known ions.

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<sup>||</sup> The oscillator strength for  $4h_u \rightarrow 2t_{1g}$  is calculated to be negligible, supporting the conclusion of Leach et al.21 that the band at 24 800  $cm^{-1}$  is due to  $7h_g \rightarrow 5t_{1u}$  transition.