#### **Results and Discussion**

Vibrational Spectra of Oxotetrakis(fluorosulfato)tungsten(VI).—To obtain the Raman spectrum of the compound, a sample was prepared in a tube (12-mm o.d.) and sealed. A Spex 1401 double spectrometer equipped with a Model 52 argon-krypton ion laser was used. The prominent vibrational peaks are tabulated in Table I. Satisfactory infrared spectra

	Тав	le I	
	VIBRATIONAL	SPECTRA	OF
	Oxotetrakis(fluoros	ULFATO)T	ungsten(VI)
Bands,		Bands,	
<b>cm</b> <sup>-1</sup>	Assignment (tentative)	cm1	Assignment (tentative)
1464	SO <sub>2</sub> asym str	644	SO₃ sym str
1416		~ ~ ~	
		552	$SO_2$ bend
1240	SO <sub>2</sub> sym str		(bridging SO <sub>8</sub> F)
1163	SO <sub>2</sub> asym str	455	S-F wag
	$(bridging SO_3F)$		_
1044		421	S—F def
964	W=O str		
944		280	W—O str
		273	
873	S—F str	214	
853			
826		184	W-O bend modes
801		154	
707	SO <sub>8</sub> asym bend (bridging SO <sub>8</sub> F)	141	
700			

were not obtained, because of the reaction of WO- $(SO_3F)_4$  with the cell windows or the mulling agents.

The viscous nature of the compound and the large number of Raman bands, all of which were polarized, indicated the polymeric nature of the compound. Polymerization can be thought to occur *via* bridging fluorosulfate groups, as shown in Figure 1.



Figure 1.—Structure of oxotetrakis(fluorosulfato)tungsten(VI)  $(X = OSO_2F).$ 

The SO<sub>3</sub>F<sup>-</sup> ion has  $C_{sv}$  symmetry. Covalent unidentate and bidentate fluorosulfate groups are both expected to have  $C_s$  symmetry.<sup>8</sup> For the fluorosulfate ion,<sup>9</sup> the symmetric SO<sub>2</sub> stretching mode is found at 1080 cm<sup>-1</sup>, and the doubly degenerate antisymmetric stretching mode, at 1290 cm<sup>-1</sup>. The vibrational frequencies given in Table I rule out the possibility of the SO<sub>3</sub>F<sup>-</sup> ion. The SF stretching frequencies around 800–873 cm<sup>-1</sup> may be due to the fluorosulfate groups in different environments. The W=O stretching frequency has been reported at ~960 cm<sup>-1</sup> in some of the complexes of tungsten oxyhalides with phosphine oxide.<sup>10</sup> We therefore, assign the vibrational band around 944 and 964 cm<sup>-1</sup> to be due to W=O stretching motion.

### <sup>19</sup>F Nmr Spectrum of Oxotetrakis(fluorosulfato)-

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tungsten(VI).—The polymeric structure via bridging fluorosulfate groups is further supported by the <sup>19</sup>F nmr spectrum of the compound. A sample of WO- $(SO_3F)_4$  was prepared in an nmr tube having a capillary containing CCl<sub>3</sub>F. The compound was dissolved in  $S_2O_6F_2$ . Its spectra at room temperature and at  $-45^\circ$ were much alike. In a polymeric chain (Figure 1), the bridging fluorosulfate groups may either be cis or trans to each other, as has been argued for the compound SbF<sub>4</sub>(SO<sub>3</sub>F).<sup>11</sup> A peak observed at a chemical shift -42.4 ppm with respect to CCl<sub>3</sub>F may be attributed to the terminal fluorosulfate groups, while the peaks at chemical shifts -41.9, -41.6, and -41.1 ppm with respect to CCl<sub>3</sub>F may be attributed to the bridging fluorosulfate groups, which can be in different environments, *i.e.*, cis-cis, trans-trans, or cis-trans with respect to the neighboring fluorosulfate groups. It is also possible that cyclic polymers may exist.

Acknowledgment.—This work was performed in part under contract with the office of Naval Research. The authors thank Dr. J. W. Macklin and Mr. B. J. Nist for taking the Raman and <sup>19</sup>F nmr spectra, respectively.

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# Tetra-*n*-butylammonium Salts of $B_5H_8^-$ and $B_6H_8^-$ and Decomposition Products of the Anions

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#### Received July 12, 1971

The deprotonation of pentaborane $(9)^{1-3}$  and hexa $borane(10)^{3,4}$  has been established and the physical properties and thermal stabilities of the alkali metal salts have been reported.<sup>3</sup> In our studies of the  $B_5H_8^$ and  $B_{\delta}H_{9}^{-}$  anions, we have found that the tetra-*n*butylammonium salts are thermally more stable than their alkali metal counterparts. Furthermore they are readily soluble in nonbasic solvents such as methylene chloride, while the alkali metal salts are insoluble. In view of the possible advantages afforded by tetran-butylammonium salts, we report herein metathesis reactions for the preparation of  $(n-C_4H_9)_4NB_5H_8$  and  $(n-C_4H_9)_4NB_6H_9$  and the thermal decomposition products of these anions. We also wish to report that the previously claimed (CH<sub>3</sub>)<sub>4</sub>N-*i*-B<sub>5</sub>H<sub>8</sub><sup>2,3</sup> was in fact a mixture of decomposition products of (CH<sub>3</sub>)<sub>4</sub>NB<sub>5</sub>H<sub>8</sub>.

#### Results and Discussion

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the following metathesis reactions in which KI precipitated from solution and the borate salt was isolated from the filtrate

$$(n-C_4H_9)_4NI + KB_5H_8 \xrightarrow{CH_2C_{12}-THF} KI + (n-C_4H_9)_4NB_5H_8$$
 (1)

$$(n-C_4H_9)_4NI + KB_6H_9 \xrightarrow{CH_0Cl_0-THF} KI + (n-C_4H_9)_4NB_6H_9 \quad (2)$$

A similar metathesis procedure has been used to prepare  $(n-C_4H_9)_4NB_6H_9$  from  $NH_4B_6H_9$ ,<sup>5</sup> however, for quantities of  $(n-C_4H_9)_4NB_6H_9$  larger than 2 or 3 mmol, reaction 2 represents the preferred procedure.

The <sup>11</sup>B nmr spectrum of  $(n-C_4H_9)_4NB_5H_8$  at low temperature (0 to  $-50^{\circ}$ ) consists of doublets at 16.3 ppm (J = 135 Hz) and 52.6 ppm (J = 152 Hz) and for  $(n-C_4H_9)_4NB_6H_9$  the <sup>11</sup>B nmr spectrum (0 to  $-30^\circ$ ) consists of doublets at -10.0 ppm (J = 120 Hz) and 49.0 ppm (J = 140 Hz). (Chemical shifts are with respect to  $BF_3 \cdot Et_2O$ .) These values are slightly lower than those reported for the alkali metal salts in THF.<sup>3</sup> The boron-11 nmr spectra of tetra-n-butylammonium salts show the same general temperature dependence as reported for the alkali metal  $B_5H_8^-$  and  $B_6H_9^$ salts.<sup>3</sup> That is, with decreasing temperature there is a loss of resolution and broadening of the basal peaks while apical peaks sharpen. Sharpening of apical peaks of pyramidal boranes has been suggested by Onak and Leach<sup>6</sup> as being due to loss of coupling between the apical and basal borons due to more effective and rapid nuclear quadrupolar relaxation of the basal borons.

Properties of the Solid Salts.-The tetra-n-butylammonium salts of  $B_5H_8^-$  and  $B_6H_9^-$  are fine white crystalline materials which are soluble not only in tetrahydrofuran and 1,2-dimethoxyethane as are the alkali metal salts3 but also in methyl chloride, methylene chloride, and chloroform. They precipitate from these solvents upon addition of diethyl ether or pentane. In the solid state these salts are appreciably more thermally stable at room temperature than the potassium salts and could be "fingerprinted" by means of infrared spectroscopy and X-ray powder patterns.

The first sign of decomposition of  $(n-C_4H_9)_4NB_5H_8$ appears in the infrared spectrum 8 hr after isolation of the compound at room temperature; a shoulder appears near the original B-H terminal stretch. Even 24 hr later the very weak absorption at 1780 cm<sup>-1</sup>, tentatively assigned to the bridge hydrogen stretching motion, is still in evidence whereas, for KB3H8, decomposition becomes evident from its infrared spectrum within 15 min after warming the isolated solid to room temperature.3 X-Ray powder pattern data suggest essentially total decomposition of KB<sub>5</sub>H<sub>8</sub> within 24 hr. On the other hand, infrared and X-ray powder pattern data of  $(n-C_4H_9)_4NB_5H_8$  still show evidence of the presence of some of the tetra-n-butylammonium salt after a period of 4 days.

There is no change in the infrared spectrum of (n- $C_4H_9)_4NB_6H_9$  (Nujol mull) over a period of 5 days at room temperature while  $KB_6H_9$  is extensively decomposed after this period under the same conditions.

The primary decomposition products of the solid salts are the same as those of the salts in solution and

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are discussed below in the section on thermal decomposition in solution.

Treatment of solid  $(n-C_4H_9)_4NB_5H_8$  with liquid HCl produced the parent hydride B3H9 in 96% yield. On the other hand attempts to regenerate B<sub>6</sub>H<sub>10</sub> from solid (n-C4H9)4NB6H9 with liquid HCl did not yield  $B_{6}H_{10}$  quantitatively. The volatile product contained approximately half of the boron in the system and consisted of about 75 mol % B<sub>5</sub>H<sub>9</sub> and 25 mol % B<sub>6</sub>H<sub>10</sub>. The remaining solid was not characterized. Essentially the same results were obtained in (CH<sub>3</sub>)<sub>2</sub>O. The yield of  $B_6H_{10}$  obtained was significantly lower than from the reaction of HCl with  $KB_6H_9$  in  $(CH_3)_2O^3$ .

Thermal Decomposition in Solution.-Monitoring the <sup>11</sup>B nmr spectrum of KB<sub>5</sub>H<sub>8</sub> in THF and (n- $C_4H_9$ )<sub>4</sub>NB<sub>5</sub>H<sub>8</sub> in CH<sub>2</sub>Cl<sub>2</sub> showed that decomposition begins at about 20°. On the average, samples were completely decomposed in 30 hr at room temperature. When  $B_{\delta}H_{\vartheta}$  is present in the solution (5 mol %), decomposition is accelerated and becomes evident at  $-10^{\circ}$ . Analogous salts of  $B_6H_9^-$  are significantly more stable. Only slight decomposition is evident after 24 hr at ambient temperature and decomposition is not complete even after 5 days.

The primary decomposition products of KB<sub>5</sub>H<sub>8</sub> and  $(n-C_4H_9)_4NB_5H_8$  in solution are  $BH_4^-$ ,  $B_3H_8^-$ , and  $B_9H_{14}$ . In the case of the THF solution of  $KB_5H_8$ , tetrahydroborate(1-) precipitated as the potassium salt and was identified by X-ray powder pattern and infrared spectra. The  $B_9H_{14}^-$  anion was also isolated as the tetramethylammonium salt. An authentic sample of (CH<sub>3</sub>)<sub>4</sub>NB<sub>9</sub>H<sub>14</sub> was prepared.<sup>7</sup> Its <sup>11</sup>B nmr spectrum was in agreement with that reported for  $CsB_9H_{14}^8$ and also with that of the material isolated from the decomposition products. The X-ray powder pattern and infrared spectrum of the authentic sample of  $(CH_3)_4NB_9H_{14}$  were identical with those of  $(CH_3)_4$ - $NB_9H_{14}$  which was isolated from the decomposition product. The previously reported  $i-B_3H_8^{-2,3}$  was found to be a mixture of  $B_3H_8^-$  and  $B_9H_{14}^-$ . A doublet at -10.3 ppm (J = 130 Hz) and one arm of a doublet or triplet at 36.7 ppm (the other being hidden by the absorption due to  $B_3H_8^{-}$ ) cannot be assigned to any known species at the present time.

The decomposition of  $B_6H_9^-$  in solution yields primarily B11H14-, identified by 11B nmr spectra and X-ray powder pattern, and BH4-, identified by its infrared spectrum and X-ray powder pattern.

It is of interest to note that the decomposition products of  $B_5H_8^-$  observed in this investigation are in accord with products reported from the reaction of  $B_5H_9$ with BH4- in a recent investigation.9 It was suggested9 that the reaction between  $B_5H_9$  and  $BH_4^-$  is essentially different from that involving  $B_{\delta}H_{9}$  and  $H^{-}$  since no  $B_5H_8$  was observed in the reaction with  $BH_4$ . On the other hand it is possible that the following sequence occurred

$$B_{5}H_{9} + BH_{4} \longrightarrow H_{2} + B_{5}H_{3} \longrightarrow B_{6}H_{11} + H_{2}$$

since the existence of B<sub>6</sub>H<sub>11</sub><sup>--</sup> is now established.<sup>10</sup> However, under the conditions reported for the <sup>11</sup>B nmr spec-

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(9) C. G. Savory and M. G. H. Wallbridge, Inorg. Chem., 10, 419 (1971). (10) H. D. Johnson, and S. G. Shore, J. Amer. Chem. Soc., 92, 3789 (1971). tra (0 and  $25^{\circ}$ )<sup>9</sup> B<sub>6</sub>H<sub>11</sub><sup>-</sup> would go undetected, since we have found that it decomposes above  $-15^{\circ}$  to form similar decomposition products as B<sub>5</sub>H<sub>8</sub><sup>-</sup>.

#### Experimental Section

A conventional vacuum line system was used in handling airsensitive materials. Infrared spectra were recorded on a Perkin-Elmer 457 spectrometer. X-Ray powder patterns were obtained using a Debye-Scherrer camera and Cu K $\alpha$  radiation. Boron-11 nmr spectra were obtained on a Varian Associates HA-100 spectrometer with a 32.1-MHz probe.

Materials.—Potassium hydride was obtained from ROC/RIC as a 50% suspension in mineral oil. The mineral oil was removed by washing with pentane. Pentaborane(9) was obtained from Callery Chemical Co. Hexaborane(10) was prepared according to the literature.<sup>11</sup> Tetra-*n*-butylammonium iodide was obtained from Matheson Coleman and Bell.

**Preparation** of  $(n-C_4H_9)_4B_5H_8$  and  $(n-C_4H_9)_4B_6H_9$ .—In a standard drybox 2.00 mmol (0.738 g) of  $(n-C_4H_9)_4NI$  and 2.00 mmol (0.08 g) of KH were weighed in a reaction vessel containing a Teflon-covered magnetic stir bar. The vessel was attached to the vacuum line and approximately 3 ml of dry THF was condensed in and KB5H8 or KB6H9 was prepared as described elsewhere.<sup>3</sup> The reaction mixture was frozen and 6 ml of methylene chloride was condensed in. The mixture was stirred and allowed to warm to  $-22.5^{\circ}$  at which temperature it was kept for 30 min. Diethyl ether was added to precipitate the salt. The mixture was frozen and transferred under nitrogen to an extractor and filtered at  $-78^{\circ}$ . Under nitrogen a new vessel was placed under the extractor and the precipitate was washed with CH<sub>2</sub>Cl<sub>2</sub> dissolving the borate salt. The product on the frit was identified by its X-ray powder pattern as KI. A portion of the solution was tipped into an nmr tube side arm attached to the vessel, which was sealed and removed. The remainder of the compound was precipitated with ether and filtered. The infrared spectrum of  $(n-C_4H_9)_4NB_5H_8$  showed an absorption in the B-H terminal region at 2500 cm<sup>-1</sup> and a very weak, very broad peak in the B-H-B stretching region centered at 1780 cm<sup>-1</sup>.

Analyses.—Boron and hydrolyzable hydrogen analyses for  $(n-C_4H_9)_4NB_5H_8$  and  $(n-C_4H_9)_4NB_6H_9$  were carried out by acid hydrolysis. Anal. Calcd for  $(n-C_4H_9)_4NB_6H_5$ : B, 17.76%; H, 12.00 mol/mol of sample. Found: B, 17.14%; H, 11.64 mol/mol of sample. Calcd for  $(n-C_4H_9)_4NB_6H_9$ : B, 20.49%; H, 14.00 mol/mol of sample. Found: B, 20.37%; H, 13.37 mol/mol of sample.

**X-Ray Powder Patterns.**— $(n-C_4H_9)_4NB_5H_8$ : d (Å) = 10.8 (s), 8.63 (m), 7.46 (m), 6.71 (m), 5.38 (m), 5.01 (w), 4.75 (m), 4.47 (w), 4.29 (s), 4.15 (w), 3.78 (w). ( $n-C_4H_9)_4NB_6H_9$ : d (Å) = 10.0 (m), 9.12 (m), 8.22 (m), 7.70 (m), 7.16 (m), 6.79 (s), 6.19 (w), 5.82 (vw), 5.31 (m), 4.77 (s), 4.53 (s), 4.29 (m), 4.05 (m), 3.79 (m), 3.49 (w), 3.39 (w).

**Regeneration of B**<sub>5</sub>**H**<sub>9</sub> and **B**<sub>6</sub>**H**<sub>10</sub>.—Into a test tube type vessel was placed 0.154 g (0.505 mmol) of  $(n-C_4H_9)_4NB_5H_8$ . Approximately 1 ml of liquid HCl was condensed in at  $-196^\circ$ . The vessel was warmed to  $-111^\circ$  and the solution was stirred for 45 min. The mixture was fractionated and 0.485 mmol (96%) of B<sub>5</sub>H<sub>9</sub> was recovered.

Reaction of  $(n-C_4H_9)_4NB_6H_9$  with liquid HCl was carried out using a similar procedure. Regeneration of  $B_6H_{10}$  was also attempted in  $(CH_3)_2O$ . In a vessel 0.321 g (1.52 mmol) of  $(n-C_4H_9)_4NB_6H_9$  was weighed. About 3 ml of dimethyl ether and 1.55 mmol of HCl passed through  $P_2O_5$  were condensed in at  $-196^\circ$ . The vessel was warmed to  $-78^\circ$  and stirred overnight. Fractionation of the volatiles yielded  $B_5H_9$  and  $B_6H_{10}$  in both procedures.  $B_5H_9$  and  $B_6H_{10}$  were condensed in on excess KH in  $(CH_3)_2O$  at  $-78^\circ$ . The  $H_2$  evolved was collected and measured as 0.785 mmol representing 52% of the original  $B_6H_9^-$ . The solid residue in the vessel was dissolved in  $CH_2Cl_2$  and the <sup>11</sup>B nmr showed the presence of  $B_6H_9^-$  and  $B_8H_8^-$ .

Decomposition of  $B_8H_8^-$  and  $B_6H_8^-$ .—A solution of  $KB_5H_8^{3,4}$ in tetrahydrofuran (ca. 0.5 M) was stirred at room temperature for 2 days. The solution was filtered and the solid on the frit was identified as  $BH_4^-$  by its infrared spectrum and X-ray powder pattern. As much tetrahydrofuran as possible was removed under vacuum. The vessel was removed from the vacuum line and a solution containing excess (CH<sub>3</sub>)<sub>4</sub>NCl in water was added to the gummy residue. The solution was stirred and filtered.

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The solid isolated was identified as  $(CH_3)_4NB_9H_{14}$  by its <sup>11</sup>B nmr spectrum<sup>8</sup> and comparison of its infrared spectrum and X-ray powder pattern with those of an authentic sample. The yield of  $(CH_3)_4NB_9H_{14}$  ranged from 0.15 to 0.20 mmol/mmol of  $KB_5H_8$ . The X-ray powder pattern of  $(CH_3)_4NB_9H_{14}$  has the following d (Å) values: 7.18 (vw), 6.03 (w), 5.04 (vs), 4.12 (vw), 4.00 (vw), 3.56 (w), 3.19 (m). Concentration of the solution yielded another precipitate which was identified as  $B_3H_8^-$  by its infrared spectrum and <sup>11</sup>B nmr spectrum.

Solutions of KB<sub>6</sub>H<sub>9</sub> in tetrahydrofuran (*ca.* 1 *M*) were allowed to stir at room temperature for 2 weeks. Filtration of the solution and identification of the solid product by its infrared spectrum and X-ray powder pattern showed KBH<sub>4</sub>. The boron-11 nmr spectrum of the resulting solution showed a doublet at 16.2 ppm (J = 138 Hz) which compares favorably with the literature value for B<sub>11</sub>H<sub>14</sub>.<sup>12,13</sup> Addition of dioxane to the solution precipitated a solid which exhibited the same infrared spectrum and X-ray powder pattern as an authentic sample of KB<sub>11</sub>H<sub>14</sub> prepared in dioxane by the method previously reported for B<sub>11</sub>H<sub>14</sub><sup>-</sup> salts.<sup>12</sup> The X-ray powder pattern of KB<sub>11</sub>H<sub>14</sub> which has not been previously reported contains the following *d* (Å) values: 8.39 (m), 6.37 (m), 5.56 (m), 5.07 (s), 4.32 (m), 4.20 (s), 3.58 (m), 3.10 (vw), 2.98 (w), 2.80 (m), 2.70 (w), 2.56 (m), 2.49 (w), 2.41 (w), 2.36 (w).

Solutions of the tetrabutylammonium salts of these boranes in methylene chloride were monitored by <sup>11</sup>B nmr. The  $B_{\delta}H_8^-$  salt was completely decomposed in 30 hr. The  $B_{6}H_9^-$  species was completely decomposed after 2 weeks. The <sup>11</sup>B nmr spectra of the decomposition products of these salts appeared identical with those of their potassium counterparts.

Acknowledgments.—We wish to thank the National Science Foundation for its financial support. V. T. B. also wishes to thank the Stauffer Chemical Co. for financial support.

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## Preparation of B-Tris(cyclopentadienyl)-N-trimethylborazines and B-Tris(methylcyclopentadienyl)-N-trimethylborazines

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#### Received July 15, 1971

Two reports have previously appeared concerning cyclopentadienyl reactions with borazines.<sup>1,2</sup> In view of their brevity, it was of interest to investigate the reactions of certain cyclopentadienides and methylcyclopentadienides with both *B*-trichloro-*N*-trimethylborazine and *B*-trichloroborazine in order to develop a preparative technique for obtaining cyclopentadienylsubstituted borazines. We were able to prepare methylcyclopentadienyl and cyclopentadienyl derivatives of *B*-trichloro-*N*-trimethylborazine while we were unsuccessful in similar attempts with *B*-trichloroborazine.

#### **Experimental Section**

General Information.—All preparations involved standard drybox and high-vacuum procedures with particular care being

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