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## SCF- $X\alpha$ Scattered-Wave Studies on Bonding and Ionization Potentials. 2. Higher Valence State Sulfur Compounds

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The nature of the bonding in hypervalent molecules is examined for the series  $SX_6$  ( $X = F, Cl, H$ ) as well as for  $SF_4$  and  $SOF_4$  by means of SCF- $X\alpha$  scattered-wave calculations. We refine our method of "atoms-in-molecule" population analysis to distinguish different partial wave contributions in the individual atomic regions. For the  $SX_6$  series, we discuss the correlation of electronegativity of the ligands (bond polarity) and the existence of these compounds. The bonding in  $SF_6$  is affected in a different way by the ligand s orbitals than in  $SCl_6$ , a factor not included in the original theory of hypervalency. A detailed analysis of the nature of the bonding in  $SF_6$  is made by using both the partial wave population analysis and orbital contour maps. A great similarity between the electronic structure of  $SF_4$ ,  $SOF_4$ , and  $SF_6$  is found which does not justify the usual distinction between hypervalent I ( $SF_4$ ) and hypervalent II ( $SOF_4$ ,  $SF_6$ ) bonding. We find in agreement with experiment that the axial fluorine ligands in  $SF_4$  have smaller F 1s ionization energies than the equatorial ligands. The first ionization potential of  $SOF_4$  is smaller than that of  $SF_4$  (14.5 vs. 16.2 eV).

The elements of groups 5–8 have the ability to form additional bonds beyond the number allowed by the Lewis–Langmuir valence theory when they are associated with electronegative atoms (primarily fluorines). For molecules which contain an element with its valency so expanded, Musher coined the descriptive name *hypervalent molecules*.<sup>2</sup>

There have been quite a number of suggestions to understand qualitatively the bonding of these molecules.<sup>2–9</sup> According to the perfect pairing model of Pauling<sup>4</sup> one has to invoke d-orbital participation on the central atom in constructing the appropriate orthogonal hybrid orbitals. In order to avoid the expense of a high promotional energy Dogett<sup>5</sup> introduced a simple valence-bond model without d-orbital participation by considering various valence-bond structures with charge transfer from the central atom to the ligands. This model leads to a formal charge on the central atom consistent with the fact that hypervalent molecules are mainly formed with electronegative ligands. The relation between the formal charge and the nature of the d orbitals on the central atom and thus the feasibility of the d-orbital participation in bonding have been studied by Coulson and Gianturco.<sup>6,7</sup>

Musher,<sup>2a</sup> on the other hand, gave a qualitative description of the bonding by simply using nonorthogonal hybrid orbitals on the central atom which also removes the necessity of d-orbital participation. He also discussed the molecular orbital (MO) equivalent of the theory together with CNDO/2 calculations of the simplest sulfur hydrides and fluorides.<sup>2c,d</sup> In the MO language hypervalent bonds may be characterized as three-center electron-rich bonds<sup>8</sup> with the further qualitative distinction of whether only atomic p orbitals are involved (type I) or whether sp mixing plays a significant role (type II). Chen and Hoffmann recently gave a molecular orbital analysis of the bonding in sulfuranes based on extended Hückel calculations.<sup>9</sup>

We have already reported SCF- $X\alpha$  scattered-wave studies on  $SF_6$ ,  $SeF_6$ , and  $TeF_6$ , which will be referred to as part 1.<sup>10</sup> In order to gain more insight into the bonding character of type II hypervalent sulfur compounds we have carried out SCF- $X\alpha$ -SW calculations on  $SH_6$  and  $SCl_6$  which shall be compared to our previous results in part 1 for  $SF_6$ . We have further studied the electronic structure of some hypervalent sulfur compounds of low symmetry, namely,  $SF_4$  and  $SOF_4$ . A comparison among these two and  $SF_6$  should shed some light on Musher's distinction between type I and type II hypervalent molecules.

The purpose of this paper is not only to study the structure of hypervalent molecules but to continue along the lines of part

1 and to show how detailed knowledge about the molecular orbitals of a molecule, as furnished from an SCF- $X\alpha$ -SW calculation, may be usefully reduced and correlated with the known chemistry of the molecule under study. Orbital contour maps displaying detailed features of the charge distribution in space, as well as a scheme similar to a conventional population analysis but suitably adapted to the form of SW orbitals, will be employed. To assess the reliability of these tools we will compare our findings to previous calculations of related compounds.<sup>2,11</sup> In particular a recent extensive Hartree–Fock study of the molecules  $SH_2$ ,  $SH_4$ , and  $SH_6$  which also included geometry optimization<sup>11</sup> will be used in this context.

### Scattered-Wave Population Analysis

The SCF- $X\alpha$ -SW method which we are using here has been shown to give reliable information on the electronic structure of a wide range of different molecules and clusters.<sup>11</sup> The essential features of the method are its use of the local exchange approximation, the muffin tin model for the electronic potential, and the scattered-wave (or multiple scattering) formalism to solve the one-particle Schrödinger equation. Because details of this method are well documented,<sup>12</sup> we shall not repeat them here. Two features of the SCF- $X\alpha$ -SW method should be stressed, however, as they are of special importance in connection with the following investigations. The molecular orbital wave functions are represented as rapidly converging multicenter partial wave expansions whose radial parts are found through numerical integration. Thus all of the problems of an LCAO–MO method connected with the choice of proper basis functions may be avoided. A further consequence of this multicenter expansion of the orbital wave function is a *distribution of electronic charge over different regions of space*, as defined by the muffin tin model. The SCF- $X\alpha$ -SW calculation starts with superimposed atomic distributions over the various regions of the molecule and reaches self-consistency at which point the molecular charge distribution is obtained. Thus the molecular charge distribution of each region<sup>12d</sup>—atomic (I), interatomic (II), and extramolecular (III)—and the change occurring during convergence to self-consistency provide information about the charge redistribution during formation of the bonds (see Figure 1 of part 1 for an illustration of the partitioning of space).

By analogy to the conventional Mulliken population analysis, we defined in part 1 the  $X\alpha$ -SW populations as in eq 1 and 2, where  $Q_I$  is the integrated electronic charge in the corresponding region of space and  $n_A$  and  $n_L$  are the total number of atomic spheres and the number of ligand spheres, respectively. Here,  $Z_I$  is the atomic number of atom I. In the

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$$X\alpha\text{-SW net atomic population} \equiv Q_I \quad (1a)$$

$$X\alpha\text{-SW net atomic charge} \equiv Z_I - Q_I \quad (1b)$$

$$X\alpha\text{-SW gross atomic population} \equiv Q_I + Q_{II}/n_A + Q_{III}/n_L \quad (2a)$$

$$X\alpha\text{-SW gross atomic charge} \equiv Z_I - (Q_I + Q_{II}/n_A + Q_{III}/n_L) \quad (2b)$$

case where this is the central atom the last term in eq 2 is not included in the  $X\alpha\text{-SW}$  gross atomic charge. When the distinction between the central atom and the ligands is not appropriate, e.g., in a diatomic molecule, one may define

$$X\alpha\text{-SW gross atomic charge} \equiv Z_I - Q_I - (Q_{II} + Q_{III})/n_A \quad (3)$$

For a number of questions it is helpful to have not only total atomic populations as given by eq 1 but also more detailed information concerning the relative contributions of the different atomic orbitals involved. Questions of such a nature include the amount of d-orbital participation in a molecule where their contribution to the various molecular orbitals is not singled out by the high symmetry as in octahedral molecules or the relative contribution of ligand s and p orbitals to the various  $\sigma$  bonds. Since the  $X\alpha\text{-SW}$  method<sup>12d</sup> uses in region I a partial wave expansion of the form

$$\Psi_I^{(i)}(r) = \sum_{lm} C_{lm}^{(i)} R_l^{(i)}(r_i) Y_{lm}(r_i) \quad (4)$$

where the index  $i$  refers to a specific atom  $i$ , an obvious measure for the contribution of a specific atomic orbital to the molecular orbital under consideration is given by<sup>13</sup>

$$Q_{lm}^{(i)} = 4\pi |C_{lm}^{(i)}|^2 \int_0^{b_i} [R_l^{(i)}(r_i)]^2 r_i^2 dr_i \quad (5)$$

$b_i$  denotes the radius of the corresponding atomic sphere. Of course, one has

$$Q_I \equiv Q^{(i)} = \sum_{lm} Q_{lm}^{(i)} \quad (6a)$$

and

$$1 = \sum_i Q^{(i)} + Q_{II} + Q_{III} \quad (6b)$$

If one compares the population analysis for  $X\alpha\text{-SW}$  molecular orbitals as outlined above to a conventional LCAO-type population analysis, one finds as a major difference that the latter relies on the overlap concept, whereas the former is based on an atoms-in-molecule point of view. This does not involve any bias toward a specific picture of the nature of the bonds but reflects the fundamental differences in the underlying mathematical formalisms that are used to solve the Schrödinger equation. Both methods of population analysis suffer from specific disadvantages limiting their practical value. In an LCAO-type analysis one has to arbitrarily divide the overlap density and very frequently has to face negative populations for certain orbitals (see, e.g., ref 11). While the SW approach avoids the basis set dependence found in an LCAO-type analysis, it does have some arbitrariness in the use of the atomic spheres and the assignment of the charge situated in the interatomic and the extramolecular regions. The sphere sizes occurring in the muffin tin potential are to a certain extent arbitrary parameters of the model and may only be loosely tied to the values of the corresponding covalent radii and/or determined by requiring minimal potential steps across the various boundaries of muffin tin regions. In order to eliminate the influence of the sphere sizes on our results we rely in our charge analysis more on changes between superposed atomic charges and the self-consistent molecular charge distribution or on changes in a series of related molecules. This limitation again finds its counterpart in the

current practice of LCAO-type population analysis.

## Results and Discussion

**SX<sub>6</sub> Compounds.** In part 1 we observed that a large amount of the electronic charge is drained away from the central atom to the fluorine ligands for the series of molecules SF<sub>6</sub>, SeF<sub>6</sub>, and TeF<sub>6</sub>. In an attempt to assess the importance of the electronegativity of the ligands in making hypervalent molecules of the type ML<sub>6</sub>, we varied the ligand atoms and performed SCF- $X\alpha\text{-SW}$  calculations for SH<sub>6</sub> and SCl<sub>6</sub>.

The molecules were assumed to have octahedral symmetry, of course. The bond lengths were taken from experiment (SF<sub>6</sub>) and from a previous calculation<sup>11</sup> with geometry optimization (SH<sub>6</sub>) or were determined approximately by scaling the bond length found experimentally in SCl<sub>2</sub> in the ratio of the corresponding bond length in SF<sub>2</sub> and SF<sub>6</sub> (for SCl<sub>6</sub>):  $d_{S-H} = 2.761$  au,  $d_{S-Cl} = 3.720$  au, and  $d_{S-F} = 2.956$  au. The atomic sphere radii in the muffin tin potentials were determined for SF<sub>6</sub> (cf. part 1) by requiring touching spheres and a continuous potential at the points where they are in contact.<sup>14</sup> For SH<sub>6</sub>, an additional calculation with the bond length  $d_{S-H} = 2.5$  au was performed, and in order to facilitate comparison between these two calculations for SH<sub>6</sub> and that for SF<sub>6</sub>, the same sulfur sphere radius was chosen in all three cases. We will report only the first one, as they both lead to the same conclusions for the questions to be discussed below. For SCl<sub>6</sub> the sulfur sphere radius had to be enlarged in comparison with these molecules in order to account for the increased bond length and the changed ratio of the covalent radii (1:1). The resulting sphere radii for the sulfur sphere were 1.78, 1.86, and 1.78 au for SH<sub>6</sub>, SCl<sub>6</sub>, and SF<sub>6</sub>, respectively. The ligand sphere radii are then completely determined: 0.981, 1.860, and 1.176 au for H, Cl, and F, respectively.

The values used for the atomic exchange constant  $\alpha$  were taken as determined by Schwarz ( $\alpha_{HF}$ ),<sup>15a</sup> except for H.<sup>15b</sup> In the other regions a weighted average of these values has been used. Partial waves up through  $l = 2$  were taken into account in the sulfur sphere, and through  $l = 1$  in the ligand spheres. The iterations toward self-consistency were continued until the relative change in the potential was less than  $10^{-2}$  at any point in space.

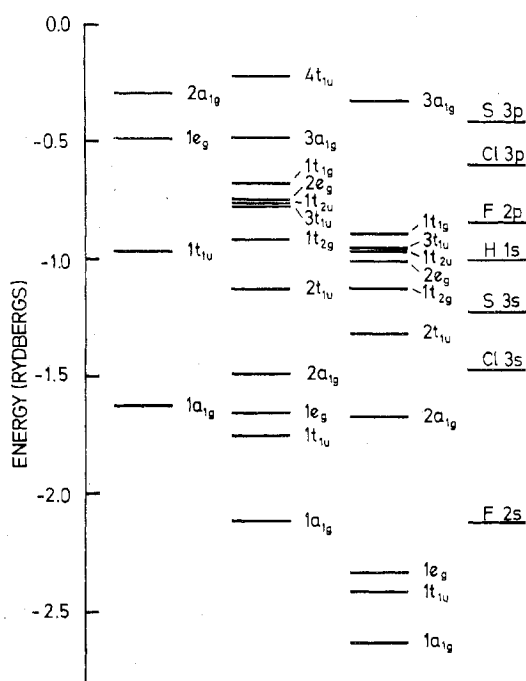
The calculated orbital energies for the valence electrons of the molecules SF<sub>6</sub> and SCl<sub>6</sub> are compared in Table I together with the normalized orbital charge distribution over the various regions of space. For SH<sub>6</sub> we find the following orbital energies:  $-1.621$  Ry ( $1a_{1g}$ ),  $-0.964$  Ry ( $1t_{1u}$ ), and  $-0.484$  Ry ( $1e_g$ ). No direct comparison with Hartree-Fock type orbital energies<sup>2c,11</sup> is possible because of the different concept of orbital energies in both the Hartree-Fock and  $X\alpha$  theory.<sup>16</sup> However, the general features in the orbital energy spectrum are the same (for SF<sub>6</sub> see part 1). In Figure 1 we compare the energies of all occupied valence orbitals together with those of the lowest unoccupied orbitals for SH<sub>6</sub>, SCl<sub>6</sub>, and SF<sub>6</sub>.

Table I and Figure 1 reveal a fair similarity between the energy level spectra and spatial charge distributions of SF<sub>6</sub> and SCl<sub>6</sub>. The energy levels of SCl<sub>6</sub> are shifted upward compared with those of SF<sub>6</sub>. This is due to the fact that the chlorine s and p valence levels lie energetically much higher than those of fluorine and has important consequences for the electronic structure of SCl<sub>6</sub>. The very low-lying  $1a_{1g}$ ,  $1t_{1u}$ , and  $1e_g$  valence levels, mainly attributed to ligand s orbitals, are not included in the qualitative discussions of the bonding of hypervalent molecules<sup>2</sup> yet do contribute to sulfur-ligand bonding as may also be confirmed by detailed orbital contour maps. The  $1a_{1g}$  level plays a prominent role due to its large localization within the sulfur sphere (0.213 and 0.455 for SF<sub>6</sub> and SCl<sub>6</sub>). The sulfur 3s atomic orbital contributes significantly to bond formation through the interaction with the ligand p orbitals in order to form hypervalent molecules of type

**Table I.** SCF- $X\alpha$ -SW Orbital Energies and Normalized Charge Distributions in the Various Molecular Regions for the Valence Orbitals of  $SF_6$  and  $SCl_6$ 

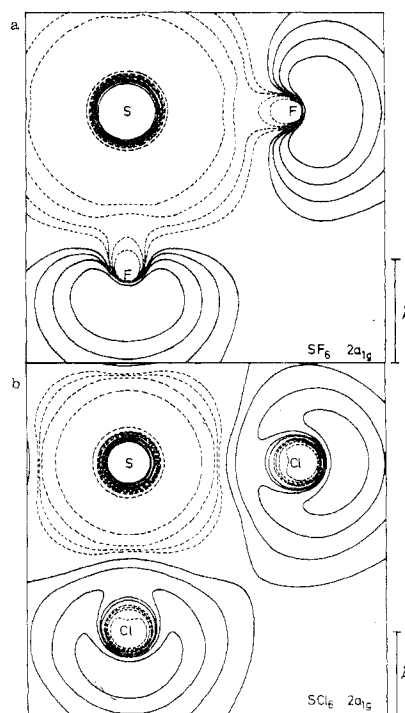
Orbital	$SF_6$					$SCl_6$				
	$-\epsilon_1^a$	S	F	INT	EXT	$-\epsilon_1^a$	S	Cl	INT	EXT
$1a_{1g}$	2.633	0.213	0.083	0.271	0.015	2.111	0.455	0.050	0.244	0.002
$1t_{1u}$	2.413	0.062	0.112	0.242	0.025	1.749	0.083	0.113	0.225	0.015
$1e_g$	2.337	0.026	0.122	0.209	0.032	1.652	0.014	0.131	0.172	0.025
$2a_{1g}$	1.665	0.361	0.072	0.161	0.057	1.484	0.231	0.093	0.172	0.040
$2t_{1u}$	1.310	0.232	0.079	0.244	0.048	1.123	0.299	0.070	0.239	0.041
$1t_{2g}$	1.123	0.031	0.094	0.365	0.041	0.913	0.018	0.088	0.415	0.036
$2e_g$	1.006	0.091	0.112	0.166	0.070	0.747	0.081	0.110	0.184	0.075
$1t_{2u}$	0.962	0.0	0.113	0.289	0.032	0.760	0.0	0.106	0.331	0.035
$3t_{1u}$	0.961	0.018	0.110	0.281	0.042	0.772	0.032	0.097	0.343	0.042
$1t_{1g}$	0.889	0.0	0.122	0.236	0.033	0.669	0.0	0.117	0.257	0.039
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$3a_{1g}^b$	0.324	0.279	0.095	0.088	0.066	0.478	0.161	0.092	0.202	0.087
$4t_{1u}$						0.218	0.352	0.066	0.187	0.063

<sup>a</sup> Energies in rydberg units (1 Ry = 13.6 eV). <sup>b</sup> Orbitals listed below the dashed line (here and in other tables) are unoccupied in the ground state of the molecule.



**Figure 1.** Comparison of the SCF- $X\alpha$ -SW orbital energies for different molecules of type  $SX_6$ . The HOMO is the  $1e_g$  orbital in  $SF_6$  and the  $1t_{1g}$  orbital in  $SCl_6$  and  $SF_6$ . The SCF- $X\alpha$  orbital energies for the various free atoms are also shown.

II.<sup>2</sup> The orbital contour map of the  $SF_6$   $2a_{1g}$  level shown in Figure 2a clearly confirms this view. This is, however, in strong contrast to the character of the corresponding  $2a_{1g}$  level of  $SCl_6$  (Figure 2b), which may be described as an antibonding sulfur  $3s$ -chlorine  $3s$  orbital. Is it possible to rationalize this finding by qualitative molecular orbital arguments? Three atomic orbitals or linear combinations thereof contribute to the molecular orbitals of symmetry  $a_{1g}$ : the sulfur  $3s$  orbital and suitable linear combinations of ligand  $s$  and  $p$  orbitals. For the sake of argument, we switch on these interactions consecutively in Figure 3. In the first stage we observe a bonding and an antibonding linear combination of sulfur  $3s$  and ligand  $s$  orbitals. By invoking this perturbational argument, it becomes clear that the interaction with the ligand  $p$  orbitals is stronger for fluorine than for chlorine so that the antibonding character of the  $2a_{1g}$  level of  $SF_6$  is overcome by the  $p_\sigma$  bonding contribution whereas in the chlorine case it is not. Therefore in contrast to the situation in  $SF_6$ , we find that the contributions of the  $1a_{1g}$  and  $2a_{1g}$  levels to sulfur-ligand



**Figure 2.** Contour plots of the  $2a_{1g}$  orbital wave function of  $SF_6$  and  $SCl_6$ . The continuous lines represent the values of the orbital with one sign; the dashed lines, the values with opposite sign. The contours near the atomic centers have been omitted: (a)  $SF_6$ ; (b)  $SCl_6$ . (Note the different scale!)

bonding do not reinforce but partially cancel each other. This effect of the ligand  $s$  orbitals is not included in the usual discussion of the electronic structure of hypervalent molecules.<sup>2</sup> Our results show that it cannot always be neglected.

The orbital contour maps for the remaining occupied orbitals of  $SF_6$  and  $SCl_6$  are rather similar after proper scaling to account for the different bond lengths. If one measures the bond strength by overlap populations, as done in a LCAO-type formalism, the assumption of equal functional character for the overlap population density, differing only by a scaling of the coordinates, would imply a reduction by a factor of roughly  $(d_{S-F}/d_{S-Cl})^3 \approx 0.5$  from  $SF_6$  to  $SCl_6$ , again pointing to weaker bonds in  $SCl_6$ . The bonding of these molecules can satisfactorily be explained without invoking the stabilizing effect of sulfur  $d$  orbitals, a view which has been expressed many times.<sup>2,8-11,12a</sup> However, even the small influence of sulfur  $d$  orbitals decreases when going from  $SF_6$  to  $SCl_6$  (see the

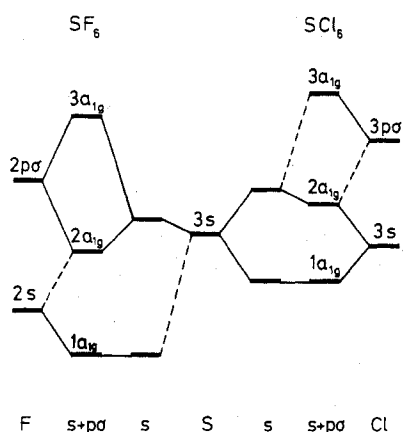


Figure 3. Interaction diagram for the  $\sigma$ -bonding orbitals in  $SF_6$  (left) and  $SCl_6$  (right). All other orbitals have been omitted. Weak interactions are indicated by dashed lines.

charge distribution in the sulfur sphere of the  $1e_g$ ,  $1t_{2g}$ , and  $2e_g$  orbitals in Table I).

Our findings concerning the electronic structure of  $SH_6$  qualitatively agree with those of earlier calculations.<sup>2,10</sup> The situation is similar to the one in  $SCl_6$ , in that the sulfur's contribution to bond formation is negligible. The fraction of charge of the  $1a_{1g}$  orbital localized in the sulfur sphere is 0.561, i.e., even larger than in the corresponding orbital of  $SCl_6$ .

To summarize,  $SCl_6$  and  $SH_6$  are expected to have much weaker bonds than  $SF_6$ . Also the steric situation around the sulfur atom is worse in  $SCl_6$  than in  $SF_6$ . Unfortunately, we are not able to use total energies<sup>17</sup> in our argument on the existence of  $SCl_6$  (for the discussion of the stability of  $SH_6$ , see ref 11). Since the bond strength is 58 kcal/mol in  $Cl_2$  (vs. 37 kcal/mol in  $F_2$ ), it appears improbable that the total energy of  $SCl_6$  lies above that of  $SCl_4 + Cl_2$ .<sup>18</sup> In turn  $SCl_4$  dissociates already at  $\sim -30^\circ C$  into  $SCl_2 + Cl_2$ .<sup>19</sup>

Let us now examine the total charge distributions in the atomic, interatomic, and extramolecular regions of each molecule  $SX_6$ :  $Q_S$ ,  $Q_X$ ,  $Q_{INT}$ , and  $Q_{EXT}$ . These charges are listed in Table II together with  $\Delta Q_i = Q_i^{mol} - Q_i^{atom}$  where  $Q_i^{mol}$  and  $Q_i^{atom}$  are the charge of a molecule in region  $i$  and the superimposed atomic charges in that region, respectively. From Table II we notice that every molecular electronic charge is contracted. Among the three,  $SH_6$  undergoes the least change while the charge redistribution in  $SF_6$  is quite significant. The net gain of electronic charge on the ligand side, defined by

$$\Delta = \sum_{i \text{ all ligands}} \Delta Q_i - \Delta Q_S \quad (7)$$

may be taken as a measure of the bond polarity. It describes how much more effective the ligands are in attracting the charge in regions II and III than is the central atom. This concept brings to mind a recently proposed formalism to determine the charge distribution in transition metal complexes via game theory.<sup>20</sup> Obviously, the  $\Delta$  values of 0.653, 1.036, and 1.650 correlate with the electronegativity values of H, Cl, and F.<sup>19</sup> According to the above discussion on the stability

Table II. Electronic Charges and Charge Differences (Molecular vs. Superposed Atomic Charges) in Different Molecular Regions for the  $SX_6$  Series

Molecule	$Q_S$	$Q_X$	$Q_{INT}$	$Q_{EXT}$
$SH_6$	13.443	0.473	4.613	1.104
$SCl_6$	14.344	14.800	13.123	1.731
$SF_6$	13.671	7.023	12.303	1.886

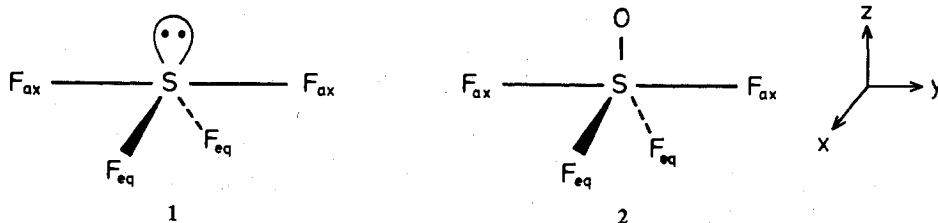
  

Molecule	$\Delta Q_S$	$\Delta Q_X$	$\Delta Q_{INT}$	$\Delta Q_{EXT}$	$\Delta$ (ligand net gain)
$SH_6$	0.115	0.128	-0.226	-0.659	0.653
$SCl_6$	0.494	0.255	-0.735	-1.291	1.036
$SF_6$	0.702	0.392	-2.066	-0.994	1.650

of  $SCl_6$  and  $SF_6$ , one might expect binding energies in the same ordering:  $SH_6 < SCl_6 < SF_6$ . The energies of the highest occupied molecular orbitals (HOMO) would also correlate with this relationship (see Figure 1). Therefore, the calculated  $\Delta$  values imply that the  $Cl_6$  lattice, not to mention the  $H_6$  lattice, has less strength to withdraw the electronic charge from the sulfur atom than does the  $F_6$  lattice. If charge removal of a sufficient amount is prerequisite for the formation of hypervalent molecules,<sup>2a,6</sup> the nonexistence of  $SH_6$  and  $SCl_6$  may be partially inferred from the resulting  $\Delta$  values.<sup>18</sup>

As a final comment on the population analysis of these compounds it should be noted that neither the net charges of the sulfur atom (2.557, 1.656, and 2.329 for  $SH_6$ ,  $SCl_6$ , and  $SF_6$ , respectively) nor the gross charges (1.898, -0.219, 0.571), as calculated according to eq 1 and 2 from the data in Table II, show any reasonable sizes or trends. This is a rather disappointing result which shows that the partitioning of space, necessary to establish the muffin tin approximation of the potential, bears a strong influence on any attributed atomic charges. Trends do show up, however, when considering differences  $\Delta Q_i$  or "second" differences, such as  $\Delta$ . It is also of value to compare the d-component populations ( $\sum_m Q_{2m}^S$  as defined in eq 5) in the sulfur sphere for the various  $SX_6$ -type molecules. The corresponding numbers are 0.344, 0.488, and 0.653 for  $SH_6$ ,  $SCl_6$ , and  $SF_6$ , respectively. They correspond to 10, 11, and 18% of the total valence charge in the sulfur sphere of  $SH_6$ ,  $SCl_6$ , and  $SF_6$ , respectively. These values show an interesting trend with the above inferred relative stability of the molecules, even if one takes the different sphere sizes into account. The value for  $SH_6$  found from an LCAO-MO wave function<sup>21</sup> (0.244) lies below that found from the  $X\alpha$ -SW orbital wave function. When comparing this to  $X\alpha$ -SW populations, one should, however, keep in mind that the two values have been determined in rather different ways.

**The Molecules  $SF_4$  and  $SOF_4$ .** The molecule sulfur tetrafluoride,  $SF_4$ , is the prototype of a type I hypervalent molecule.<sup>2a</sup> Its geometry may be idealized as a trigonal bipyramid with a sulfur lone pair in one of the equatorial positions (1).<sup>22</sup> The two equatorial S-F bonds are 2.920 au ( $F_{eq}SF_{eq} = 101.5^\circ$ ), somewhat shorter than the S-F bond in  $SF_6$  (2.956 au). The axial fluorine atoms are bonded to sulfur via hypervalent bonds which are significantly longer (3.111 au;  $F_{ax}SF_{ax} = 187^\circ$ ). The two axial fluorines are bent somewhat to the side of the two equatorial ones. The molecule thionyl tetrafluoride  $SOF_4$  (2) has roughly the same geometry with an oxygen occupying the third equatorial position. The



**Table III.** SCF-X $\alpha$ -SW Orbital Energies and Normalized Charge Distributions in the Various Molecular Regions for the Valence Orbitals of SF<sub>4</sub>

Orbital	$-\epsilon_i^a$	S	F <sub>ax</sub>	F <sub>eq</sub>	INT	EXT
1a <sub>1</sub>	2.638	0.119	0.052	0.262	0.245	0.007
1b <sub>1</sub>	2.546	0.039	0.0	0.360	0.232	0.008
1b <sub>2</sub>	2.435	0.033	0.393	0.0	0.165	0.016
2a <sub>1</sub>	2.416	0.026	0.326	0.072	0.161	0.017
3a <sub>1</sub>	1.723	0.455	0.068	0.093	0.205	0.018
2b <sub>1</sub>	1.330	0.201	0.016	0.250	0.246	0.021
2b <sub>2</sub>	1.288	0.193	0.199	0.075	0.234	0.026
4a <sub>1</sub>	1.265	0.218	0.045	0.179	0.318	0.016
1a <sub>2</sub>	1.152	0.015	0.091	0.241	0.304	0.017
5a <sub>1</sub>	1.115	0.055	0.048	0.285	0.257	0.020
3b <sub>2</sub>	1.101	0.039	0.189	0.147	0.268	0.026
3b <sub>1</sub>	1.086	0.001	0.002	0.353	0.268	0.015
4b <sub>1</sub>	1.007	0.003	0.344	0.032	0.224	0.021
6a <sub>1</sub>	1.003	0.016	0.331	0.046	0.200	0.028
4b <sub>2</sub>	0.993	0.008	0.257	0.122	0.224	0.011
2a <sub>2</sub>	0.988	0.001	0.274	0.109	0.230	0.004
6a <sub>1</sub>	0.897	0.210	0.263	0.016	0.204	0.029
-----						
5b <sub>1</sub>	0.481	0.388	0.019	0.081	0.378	0.034
8a <sub>1</sub>	0.300	0.262	0.045	0.094	0.336	0.125
5b <sub>2</sub>	0.225	0.365	0.144	0.005	0.266	0.072

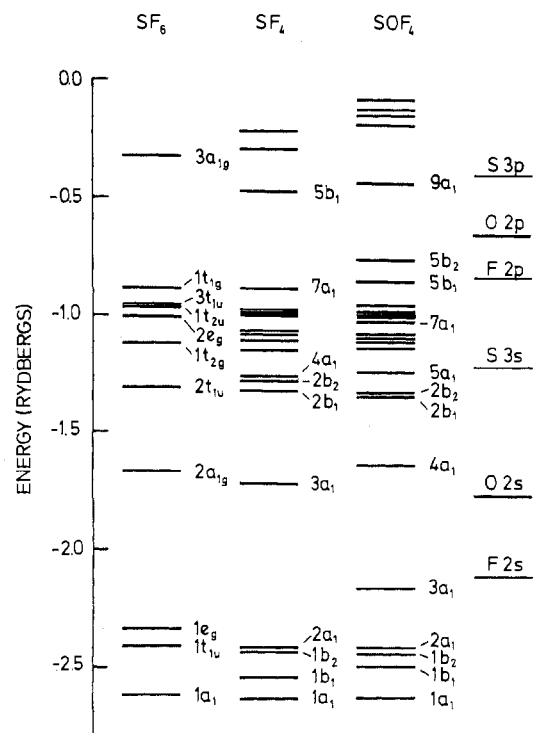
<sup>a</sup> Energies in rydbergs.

fluorine bond lengths and angles differ slightly from those in SF<sub>4</sub>.<sup>23</sup> The geometry used was as follows:<sup>23a</sup>  $d_{S-O} = 2.687$  au,  $d_{S-F_{ax}} = 3.027$  au,  $d_{S-F_{eq}} = 2.908$  au,  $F_{eq}SF_{eq} = 123^\circ$ ,  $F_{ax}SF_{ax} = 183^\circ$ .

A number of molecular orbital calculations of SF<sub>4</sub><sup>2c,24</sup> or the related sulfurane SH<sub>4</sub><sup>9,11,25</sup> have appeared by now. A detailed molecular orbital analysis of bonding aspects, geometrical distortions, and substituent site preferences has been given recently.<sup>9</sup> Here, we are interested in a comparison of the electronic structures of SF<sub>4</sub>, SOF<sub>4</sub>, and SF<sub>6</sub> and in the difference between type I (SF<sub>4</sub>) and type II (SOF<sub>4</sub>, SF<sub>6</sub>) hypervalent molecules.

Both molecules SF<sub>4</sub> and SOF<sub>4</sub> are of C<sub>2v</sub> symmetry.<sup>22,23</sup> The irreducible representations of this group are labeled a<sub>1</sub>, a<sub>2</sub>, b<sub>1</sub>, and b<sub>2</sub>. With the exception of a<sub>2</sub> for which only two nonbonding orbitals occur, every irreducible representation has a basis in s and p type functions on all the centers. Therefore, even from symmetry arguments,<sup>26</sup> the question of d-orbital participation will not be relevant for these molecules. To improve the orbital wave functions and to be consistent with the calculation of SF<sub>6</sub> we included partial waves with  $l = 2$  in the sulfur sphere. We come back to a quantitative discussion later on.

There is some ambiguity about how to choose the sphere radii in these low-symmetry molecules. The equatorial S-F bonds have approximately the same length as those in SF<sub>6</sub>. We therefore require the continuity of the potential along these bonds. For touching spheres and centering the outer sphere on the sulfur atom, all other radii are then determined by geometry. The resulting atomic radii in SF<sub>4</sub> (and the corresponding values in SOF<sub>4</sub>) are for sulfur 1.758 (1.753) au, for the equatorial fluorine atoms 1.162 (1.155) au, and for the axial fluorine atoms 1.353 (1.274) au. This leads to a rather small oxygen radius of 0.934 au leaving a large amount of the oxygen charge in the intersphere region. We thus decided to do an additional calculation with overlapping sulfur and oxygen spheres.<sup>27</sup> We enlarged the radius of the oxygen sphere in several calculations to a maximum of 1.20 au, a value which has been used for even shorter carbon-oxygen bonds.<sup>28</sup> None of the conclusions to be drawn depend critically on this parameter. We therefore present detailed results only for the calculation with overlapping spheres. The resulting energy levels are shown in Figure 4 together with those of the SF<sub>6</sub> molecule. Table III lists the charge distribution and energies

**Figure 4.** Comparison of the SCF-X $\alpha$ -SW orbital energies for the molecules SF<sub>6</sub>, SF<sub>4</sub>, and SOF<sub>4</sub>. For the sake of clarity only those levels are labeled which are discussed in the text. The highest occupied orbital is the 7a<sub>1</sub> level in SF<sub>4</sub> and the 5b<sub>2</sub> level in SOF<sub>4</sub>.**Table IV.** SCF-X $\alpha$ -SW Orbital Energies and Normalized Charge Distributions in the Various Molecular Regions for the Valence Orbitals of the Molecule SOF<sub>4</sub> (Overlapping Sulfur and Oxygen Spheres)

Orbital	$-\epsilon_i^a$	S	O	F <sub>ax</sub>	F <sub>eq</sub>	INT	EXT
1a <sub>1</sub>	2.631	0.191	0.023	0.100	0.161	0.255	0.008
1b <sub>1</sub>	2.499	0.053	0.0	0.344	0.246	0.012	
1b <sub>2</sub>	2.449	0.047	0.001	0.366	0.0	0.200	0.019
2a <sub>1</sub>	2.421	0.038	0.017	0.205	0.157	0.204	0.017
3a <sub>1</sub>	2.166	0.209	0.400	0.071	0.010	0.219	0.010
4a <sub>1</sub>	1.647	0.315	0.125	0.052	0.104	0.225	0.024
2b <sub>1</sub>	1.357	0.234	0.014	0.019	0.211	0.268	0.024
2b <sub>2</sub>	1.332	0.234	0.017	0.206	0.033	0.234	0.035
5a <sub>1</sub>	1.250	0.170	0.266	0.321	0.091	0.286	0.032
1a <sub>2</sub>	1.146	0.024	0.0	0.125	0.182	0.335	0.026
3b <sub>2</sub>	1.117	0.028	0.047	0.202	0.084	0.326	0.026
6a <sub>1</sub>	1.104	0.046	0.043	0.023	0.274	0.296	0.023
3b <sub>1</sub>	1.088	0.027	0.025	0.018	0.287	0.315	0.022
7a <sub>1</sub>	1.035	0.075	0.098	0.230	0.066	0.197	0.038
4b <sub>1</sub>	1.011	0.003	0.004	0.282	0.073	0.258	0.025
4b <sub>2</sub>	1.006	0.009	0.003	0.141	0.210	0.271	0.015
8a <sub>1</sub>	0.997	0.029	0.061	0.314	0.007	0.239	0.029
2a <sub>2</sub>	0.968	0.000	0.0	0.222	0.152	0.229	0.023
5b <sub>1</sub>	0.865	0.047	0.427	0.030	0.046	0.350	0.025
5b <sub>2</sub>	0.772	0.011	0.487	0.075	0.0	0.332	0.019
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9a <sub>1</sub>	0.450	0.289	0.014	0.073	0.173	0.163	0.040
6b <sub>1</sub>	0.201	0.388	0.137	0.012	0.095	0.231	0.031
10a <sub>1</sub>	0.160	0.219	0.113	0.026	0.051	0.353	0.162
11a <sub>1</sub>	0.133	0.031	0.021	0.005	0.011	0.398	0.518
6b <sub>2</sub>	0.092	0.420	0.019	0.153	0.017	0.153	0.067

<sup>a</sup> Energies in rydbergs.

for the occupied valence orbitals and the lower unoccupied orbitals of SF<sub>4</sub>. In Table IV the same is done for the molecule SOF<sub>4</sub>.

In the following molecular orbital analysis we shall make use of these data, orbital contour maps and a partial wave population analysis (see above) from which the general shape

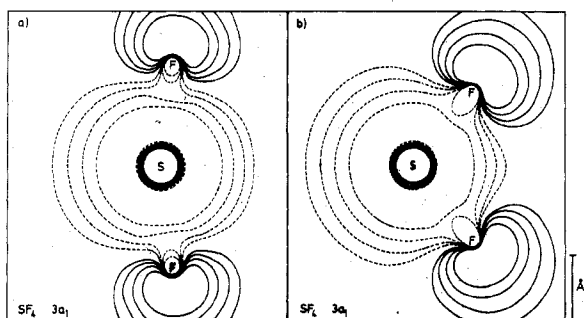


Figure 5. Contour plots of the  $3a_1$  orbital in  $SF_4$  showing the interaction of the sulfur  $3s$  atomic orbital and the ligand orbitals. The set of contour values is the same as those in Figure 2: (a) plane defined by the axial ligands,  $F_{ax}SF_{ax}$ ; (b) plane defined by the equatorial ligands,  $F_{eq}SF_{eq}$ .

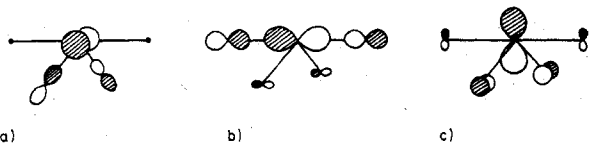


Figure 6. Schematic representation of those orbitals of  $SF_4$  which show the sulfur  $3p$  contribution to bonding: (a) the  $2b_2$  orbital; (b) the  $2b_1$  orbital; (c) the  $4a_1$  orbital.

of the orbitals may be inferred as well.

At first sight, one discovers from Figure 4 a large similarity between the energy level schemes of all three molecules  $SF_6$ ,  $SF_4$ , and  $SOF_4$ . The levels  $1a_1$ ,  $1b_1$ ,  $1b_2$ , and  $2a_1$  are mainly derived from fluorine  $2s$  orbitals as may be seen from their energies and the population analysis. The first three of them contribute to sulfur-fluorine bonding, the  $1a_1$  level with a strong  $3s$  character in the sulfur sphere very much so, whereas the  $2a_1$  orbital is largely a nonbonding in-phase combination of the two axial F  $2s$  orbitals. These findings parallel the situation found in  $SF_6$  (see above). This is true also for the  $3a_1$  level (cf.  $2a_{1g}$  in  $SF_6$ ) whose localization in the sulfur sphere has increased to 0.455 in agreement with the expectation for type I hypervalent bonding. But, nevertheless, it contributes to sulfur-fluorine bonding much in the same way as does the corresponding  $2a_{1g}$  level in  $SF_6$ . This may be seen by comparing the contour map of this orbital (see Figure 2a) to the two contour maps in Figure 5 which show the  $3a_1$  orbital in the planes defined by  $F_{ax}SF_{ax}$  and  $F_{eq}SF_{eq}$ . The next three levels,  $2b_1$ ,  $2b_2$ , and  $4a_1$ , may formally be derived from the  $2t_{1u}$  level in  $SF_6$  when going from  $O_h$  symmetry to  $C_{2v}$  in  $SF_4$ . Their shapes are sketched out in Figure 6 to show how the  $3p$  orbitals of sulfur participate in the bonding with the fluorine  $2p$  orbitals. Some small contributions of  $\pi$  bonding are found in the orbitals  $2b_1$  and  $4a_1$ . The next eight orbitals on the energy scale ( $1a_2-2a_2$ ) are nonbonding and delocalized over the ligands.

The HOMO ( $7a_1$ ) lies somewhat separated in energy. There has been some controversy whether it should contain mainly the sulfur lone pair<sup>9</sup> or should be delocalized over the axial ligands<sup>2c,11</sup> containing the extra electrons of the electron-rich hypervalent bond. In our calculation we find it to be a combination of both (see Figure 7a), thus partially confirming the prediction made by Chen and Hoffmann.<sup>9</sup> Of course, the sulfur lone pair will be smeared out over several levels in a molecular orbital approach. However, we find an appreciable localization of  $p_z$  character only in the  $4a_1$  (0.192) and  $7a_1$  orbitals (0.116).

Comparing the axial and the equatorial sulfur-fluorine bonds one notices that the orbitals describing the axial bonds ( $1b_2$ ,  $2b_2$ ) lie energetically higher than the corresponding ones for the equatorial bonds ( $1b_1$ ,  $2b_1$ ). In addition, there is the

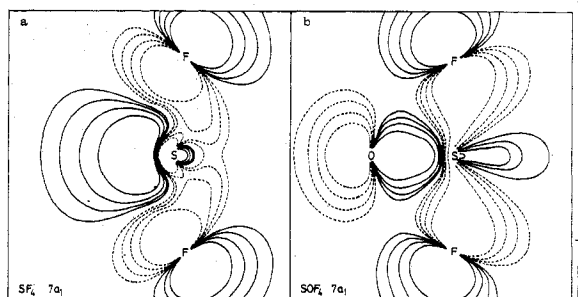


Figure 7. Contour plots of the HOMO  $7a_1$  in  $SF_4$  and the orbital  $7a_1$  in  $SOF_4$  derived from it. The planes shown are the same in both cases, defined by the axial fluorine atoms and the third equatorial position which is empty in  $SF_4$  and occupied by oxygen in  $SOF_4$ : (a)  $SF_4$ ; (b)  $SOF_4$ .

$4a_1$  orbital which reinforces the latter bonds. Both observations are consistent with the equatorial bonds being stronger than the axial ones.

The results of our molecular orbital calculation of  $SF_4$  support the conclusions from simple MO theoretical arguments<sup>9</sup> concerning the energy level scheme and the general aspects of bonding. They do not justify the distinction made by the theory of hypervalent molecules<sup>2a,c</sup> into different hybridization schemes since the relative contribution of the sulfur  $3s$  orbital to the ligand bonding varies only slightly in going from  $SF_6$  to  $SF_4$ . The agreement with the calculations by Koutecky and Musher<sup>2c</sup> using the CNDO/2 method is very qualitative.<sup>29</sup> They found the bonding levels in the order  $4a_1 < 2b_1 < 2b_2$ , a much stronger S-F  $\pi$  bond (judging qualitatively from their figures), and a HOMO without any sulfur lone-pair contribution. Since the method employed is quite different from ours, the above differences are not unexpected. The agreement between the present work and other simplified treatments<sup>24</sup> is also rather qualitative.

The level structure of  $SOF_4$  differs from that of  $SF_4$  mainly through the (additional) levels  $3a_1$ ,  $5b_1$ , and  $5b_2$ . The extreme localization of the  $5b_1$  and  $5b_2$  levels clearly discriminates these highest lying occupied molecular orbitals as describing oxygen lone pairs. The  $7a_1$  HOMO of  $SF_4$  underwent a remarkable stabilization in  $SF_4O$  ( $\Delta\epsilon_1 = -0.138$  Ry) where the  $7a_1$  orbital shows most of its former character (see Figure 7b). The strong oxygen-sulfur bond is usually taken as a double bond.<sup>30</sup> The levels  $3a_1$  (mainly O  $2s-S$   $3s$ ),  $5a_1$  (mainly O  $2p-S$   $3p$ ), and  $7a_1$  show bonding character between oxygen and sulfur whereas the  $4a_1$  orbital is oxygen-sulfur antibonding. The contribution of the fluorine ligands to various other levels in  $SOF_4$  remains more or less unchanged from that in  $SF_4$ .

Photoelectron measurements have been reported only for the fluorine  $1s$  levels in  $SF_4$ .<sup>31</sup> We do find the axial fluorine atoms to have smaller ionization energies (678.5 vs. 683.9 eV) from transition-state calculations<sup>16</sup> in agreement with the expected larger negative charge on the axial fluorine atoms. However, the quantitative agreement with experiment (692.9 vs. 695.3 eV) is rather poor. It might possibly be improved by localizing the "hole" on a definite ligand atom.<sup>32</sup> No experimental valence-shell photoelectron spectra are available for either  $SF_4$  or  $SOF_4$ . We therefore carried out transition-state calculations<sup>16</sup> only for the orbitals of  $a_1$  symmetry. The relaxation downward in energy is rather uniform and amounts to approximately 4 eV. This leads to first ionization potentials of 16.2 and 14.5 eV for  $SF_4$  and  $SOF_4$ , respectively. The general structure of the spectra should parallel that of the corresponding one-electron energies as shown in Figure 4.

Let us now turn to the charge distribution and population analysis of these compounds. The relevant data are collected in Table V. Again we notice that charge contraction occurs

Table V. Electronic Charges and Charge Differences in Different Molecular Regions of SF<sub>4</sub>, SOF<sub>4</sub>, and SF<sub>6</sub>

Molecule	Q <sub>S</sub>	Q <sub>F<sub>ax</sub></sub>	Q <sub>F<sub>eq</sub></sub>	Q <sub>O</sub>	Q <sub>INT</sub>	Q <sub>EXT</sub>
SF <sub>4</sub>	13.276	7.796	7.286		7.969	0.590
SOF <sub>4</sub>	13.554	7.291	6.845	4.985	12.782	0.396
SOF <sub>4</sub> <sup>a</sup>	13.581	7.429	6.985	6.118	10.568	0.903
SF <sub>6</sub> <sup>b</sup>	13.671		7.023		12.303	1.886

Molecule	Δ (ligand net gain)					
	ΔQ <sub>S</sub>	ΔQ <sub>F<sub>ax</sub></sub>	ΔQ <sub>F<sub>eq</sub></sub>	ΔQ <sub>O</sub>	ΔQ <sub>INT</sub>	ΔQ <sub>EXT</sub>
SF <sub>4</sub>	0.406	0.526	0.706		-2.201	-0.650
SOF <sub>4</sub>	0.674	0.311	0.335	0.645	-1.248	-1.372
SOF <sub>4</sub> <sup>a</sup>	0.701	0.449	0.475	0.515	-2.181	-0.865
SF <sub>6</sub> <sup>b</sup>	0.702		0.392		-2.066	-0.994

<sup>a</sup> Overlapping-sphere parameterization. <sup>b</sup> All fluorine atoms are equivalent, of course.

in each atomic region of these molecules (cf. Table II and part 1) and that the ligands accumulate more than does the central sulfur atom (net gain  $\Delta > 0$ ). The axial fluorine atoms in SF<sub>4</sub> have a larger amount of charge associated with them than the equatorial ligands. The analysis of photoelectron spectra<sup>31</sup> and the population analysis of LCAO-MO wave function<sup>2c,24</sup> show the same trend. It is interesting to note that the charge increase in the equatorial fluorine spheres is larger although their size is smaller. In other words, more electronic charge contraction occurs around the equatorial bond regions. Following the findings in part 1, the equatorial S-F bonds are predicted to be stronger than the axial bonds, which is in agreement with our analysis of the individual MO's, other calculations,<sup>9,24d</sup> and experiment.<sup>22,30,33</sup>

In the case of SOF<sub>4</sub>, the charge distribution on the fluorine atoms of the two different environments shows the same trends as found in SF<sub>4</sub>. The fact that the charge increase in the oxygen sphere is larger than that in the fluorine spheres may be considered as due to the double-bond character of the sulfur-oxygen bond. In the overlapping sphere parametrization these differences tend to be equalized.

The ligand net gain  $\Delta$  in SF<sub>4</sub> is quite large whereas  $\Delta$  values for SOF<sub>4</sub> and SF<sub>6</sub> are rather comparable. The same relation is observed in the X $\alpha$ -SW gross charges on sulfur: 1.130 in SF<sub>4</sub>, 0.657 in SOF<sub>4</sub>, and 0.571 in SF<sub>6</sub>. The gross charges on the fluorine atoms in SF<sub>4</sub> are -0.537 (axial) and -0.028 (equatorial). The ligand charge in SF<sub>6</sub> (-0.095) lies between them as was found in other calculations.<sup>24d-f,31</sup> The difference between axial and equatorial ligand charges is, however, rather large and partly due to the different sphere sizes. It has been concluded from LCAO calculations<sup>11,24</sup> that the sulfur charge increases with the number of ligands. Neither X $\alpha$ -SW net nor gross charges show this trend as a comparison of the results for SF<sub>4</sub> and SF<sub>6</sub> reveals, although the sulfur sphere sizes of these molecules are quite comparable (1.758 vs. 1.780 au). One might be tempted to speculate whether the fact that the electronic charge of the sulfur atom is more easily drained in SX<sub>4</sub> than in SX<sub>6</sub> by the electronegative atoms X may be one reason why SCl<sub>6</sub> does not exist but SCl<sub>4</sub> does.

A detailed analysis of the X $\alpha$ -SW orbital wave functions shows that the fractions of s (28%) and p (72%) valence electron populations in the fluorine atoms stay remarkably constant regardless of the ligand type (axial vs. equatorial) and the molecule (SF<sub>4</sub>, SOF<sub>4</sub>, and SF<sub>6</sub>). The corresponding analysis of the sulfur valence electrons is given in Table VI. Again, SOF<sub>4</sub> and SF<sub>6</sub> look rather similar, where the s population in SF<sub>4</sub> has been increased at the expense of the d orbital contribution. This effect is almost exclusively a consequence of the strong localization of the "sulfur 3s" orbital 3a<sub>1g</sub> in SF<sub>4</sub>. It may be interpreted as a somewhat smaller mixing of the

Table VI. Population Analysis (Absolute and Relative) of the Valence Electrons Located in the Sulfur Sphere for SF<sub>4</sub>, SOF<sub>4</sub>, and SF<sub>6</sub>

Molecule	s	p	d	Total
SF <sub>4</sub>	1.320 (40%)	1.658 (51%)	0.298 (9%)	3.276
SOF <sub>4</sub> <sup>a</sup>	1.148 (32%)	1.852 (52%)	0.581 (16%)	3.581
SF <sub>6</sub>	1.148 (31%)	1.870 (51%)	0.653 (18%)	3.671

<sup>a</sup> Overlapping-sphere parameterization.

sulfur 3s with the ligand orbitals in this compound. This difference may therefore be ultimately traced back to Musher's distinction between type I (SF<sub>4</sub>) and type II (SOF<sub>4</sub>, SF<sub>6</sub>) bonding. However, two such separate theoretical concepts only obscure the large similarities in the electronic structure of these molecules as our discussion has brought out.

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**Registry No.** SH<sub>6</sub>, 51715-67-4; SCl<sub>6</sub>, 38158-58-6; SF<sub>6</sub>, 2551-62-4; SF<sub>4</sub>, 7783-60-0; SOF<sub>4</sub>, 13709-54-1.

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## Microwave Spectrum, Structure, and Dipole Moment of 1,7-Dicarba-closo-octaborane(8), C<sub>2</sub>B<sub>6</sub>H<sub>8</sub>

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The microwave spectrum of 1,7-dicarba-closo-octaborane(8), C<sub>2</sub>B<sub>6</sub>H<sub>8</sub>, has been observed and the rotational spectra of nine isotopic species have been assigned. Coordinates of all boron atoms were accurately located and boron-boron bond lengths were determined. The results support those of earlier x-ray diffraction studies and confirm that the slightly distorted *D*<sub>2d</sub> geometry of the C<sub>2</sub>B<sub>6</sub> unit exists in the gas phase. The bond distances are B<sub>2</sub>-B<sub>3</sub> = 1.813 Å, B<sub>2</sub>-B<sub>5</sub> = 1.843 Å, B<sub>2</sub>-B<sub>6</sub> = 1.685 Å, B<sub>3</sub>-B<sub>4</sub> = 1.886 Å, B<sub>3</sub>-B<sub>6</sub> = 1.880 Å, and B<sub>5</sub>-B<sub>6</sub> = 1.949 Å. The molecular dipole was measured to be  $\mu = 1.40 \pm 0.01$  D.

### Introduction

The structure of the carborane 1,7-C<sub>2</sub>B<sub>6</sub>H<sub>8</sub> has been the topic of much discussion. Williams and Gerhart proposed a dodecahedral structure similar to that of B<sub>8</sub>Cl<sub>8</sub><sup>1</sup> based on the mass spectrum and <sup>11</sup>B NMR data.<sup>2</sup> More recently, proton NMR and <sup>11</sup>B NMR analyses of the C, C'-dimethyl derivative have indicated the equivalence of the methyl groups and their adjacent carbon atoms.<sup>3</sup> These data are consistent with a square-antiprismatic structure. Single-crystal x-ray diffraction studies have shown the structure to consist of a dodecahedron which is distorted toward a square antiprism.<sup>4</sup> These results indicate a molecule with C<sub>2</sub> symmetry which exhibits chirality. To confirm that this molecule retains its distorted chiral structure in the gas phase the microwave spectrum was investigated and the structure of the boron atoms was determined. The dipole moment was also obtained.

### Experimental Section

Previously, the carborane 1,7-C<sub>2</sub>B<sub>6</sub>H<sub>8</sub> had been prepared by the pyrolysis of 1,3-dicarbanidonorborane(13), C<sub>2</sub>B<sub>7</sub>H<sub>13</sub>, in diphenyl ether. By using an improved synthesis described by Dunks and Hawthorne,<sup>5</sup> the yield of 1,7-C<sub>2</sub>B<sub>6</sub>H<sub>8</sub> has been doubled. A 60% yield is obtained by slow, low-pressure pyrolysis of C<sub>2</sub>B<sub>7</sub>H<sub>13</sub>. The original sample of C<sub>2</sub>B<sub>6</sub>H<sub>8</sub> was kindly provided by T. Onak. The sample was stored in a Pyrex tube in liquid nitrogen without further purification. No problems involving impurity or decomposition were encountered. The microwave spectrum between 8 and 40 GHz was observed at dry ice temperature and at pressures between 10 and 50 mTorr. A standard 100-kHz Stark-modulated spectrometer was used in this investigation. Frequency measurements were calibrated by using a General Radio Co. standard frequency multiplier, Type 1112-A, with a Hewlett-Packard HP5245L electronic counter. Stark effects were studied by D.C. biasing the 100-kHz square wave. The effective waveguide spacing was determined by measuring the Stark shifts of the *J* = 1 ← 0 transitions of carbonyl sulfide.

### Spectra

Initial predictions of the rotational constants were made using the skeletal structural parameters of 1,7-B<sub>6</sub>H<sub>8</sub>C<sub>2</sub>-

Table I. Rotational Constants<sup>a</sup> of the Isotopic Species of 1,7-C<sub>2</sub>B<sub>6</sub>H<sub>8</sub>

Isotopic species	Rel intens <sup>b</sup>	A, MHz	B, MHz	C, MHz
Normal	1	3885.03	3124.79	3091.11
2- <sup>10</sup> B	0.47	3902.60	3168.02	3129.77
3- <sup>10</sup> B	0.47	3932.73	3148.87	3102.46
5- <sup>10</sup> B	0.47	3936.42	3148.20	3102.41
2,4- <sup>10</sup> B	0.11	3950.88	3195.05	3137.75
2,5- <sup>10</sup> B	0.11	3954.51	3187.74	3145.86
2,6- <sup>10</sup> B	0.11	3954.40	3195.58	3138.62
3,5- <sup>10</sup> B	0.11	3984.03	3178.81	3107.45
3,6- <sup>10</sup> B	0.11	3985.41	3159.25	3126.70

<sup>a</sup> Uncertainties are 0.04 MHz or less. <sup>b</sup> The natural abundance ratio of <sup>10</sup>B:<sup>11</sup>B is 19:81.

(CH<sub>3</sub>)<sub>2</sub>.<sup>4</sup> Such predictions indicated that C<sub>2</sub>B<sub>6</sub>H<sub>8</sub> is a near-prolate symmetric rotor with the principal axes directed as shown in Figure 1. The point symmetry of the molecule is C<sub>2</sub>; the C<sub>2</sub> axis is coincident with the inertial *c* axis and passes through the midpoints of the B(3)-B(4) bond and the B(5)-B(6) bond. The dipole moment of the parent species lies only along the *c*-axis direction, however small *a* and *b* dipole components are present in certain species when the axes are rotated upon isotopic substitution. Nevertheless, only *c*-type transitions were observable for all boron isotopic species.

Most of the boron isotopic species exist in sufficient concentrations to be observed in natural abundance. Assignment of a value of 1 to the intensity of the normal species gives relative intensities of various substituted boron isotopes as listed in Table I. Most species were assigned on the basis of Stark effects and relative intensities. The relative intensity pattern for the isotopic species is consistent with the relative abundance of the isotopes of a molecule belonging to a C<sub>2</sub> point group. In principle, the variation in intensities due to nuclear spin statistics can also be used; however calculations reveal the differences are too small to be useful. Four doubly substituted species and the <sup>13</sup>C species were too weak to be observed.