

Figure 7. Inverse molar magnetic susceptibility of $U[N(C_6H_5)_2]_4$ microcrystals, but no structure determination of these was possible.

We have found that uranium amides have a greater tendency to oligomerize than the d transition series amides. By proper choice of a bulky ligand we have been able to synthesize a monomer $U(N(C_6H_5)_2)_4$ in the solid state. The steric congestion is relieved in the oxygen-bridged product where one diphenylamide group is replaced, and the solid state structure is dimeric. In solution, $U(N(C_6H_5)_2)_4$ exhibits strong similarities to the other uranium amides. Once again the proton magnetic resonance and optical spectra indicate complexing with donating type solvents. In noncomplexing solvents, the tetrahedral structure is retained. It appears that with most of the uranium amides, the solid state structure is not necessarily the same as the solution species.

Acknowledgment. This work was done with support from the U.S. Energy Research and Development Administration.

Registry No. $U(dpa)_4$, 61900-16-1; $(UO(dpa)_3LiOEt)_2$, 62005-87-2; $U(NEt_2)_4$, 40678-59-9.

Supplementary Material Available: Formulas used in data reduction and listings of the structure factors (35 pages). Ordering information is given in any current masthead page.

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Mitridatite, $Ca_6(H_2O)_6[Fe^{III}_9O_6(PO_4)_9] \cdot 3H_2O$. A Noteworthy Octahedral Sheet Structure

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Received November 23, 1976

AIC608439

A natural single crystal of mitridatite, asymmetric unit $Ca_6(H_2O)_6[Fe^{III}_9O_6(PO_4)_9] \cdot 3H_2O$, was studied in detail by three-dimensional x-ray diffractometry. The compound is monoclinic and possesses space group Aa , $Z = 4$, $a = 17.553$ (2), $b = 19.354$ (3), $c = 11.248$ (2) Å, $\beta = 95.84$ (1)°. $R = 0.068$ ($R_w = 0.082$) for 5547 independent reflections. X-ray diffraction data to $(\sin \theta)/\lambda = 0.70$ (Mo $K\alpha_1$ radiation) were collected on a Picker FACS-1 automated diffractometer and the structure was solved by Patterson, Fourier, chemical-intuitive and least-squares refinement techniques. The underlying principle is a compact sheet of composition $[Fe^{III}_9O_6(PO_4)_9]^{12-}$ oriented parallel to the $\{100\}$ plane and located at $x \sim 1/4$ and $3/4$. It has trigonal pseudosymmetry $a = 11.25$ Å ($=c$ of mitridatite cell) and two-sided plane group $p31m$ and is locally isomorphic to a sheet of composition $[Na_9F_6(SO_4)_9]^{15-}$ found in the crystal structure of schairerite, $Na_{21}F_6Cl(SO_4)_7$, $Z = 3$. The sheet is built of octahedral Fe^{3+} -O edge-sharing nonamers decorated above, below, and in the plane by the PO_4 tetrahedra.

Introduction

Mitridatite, a basic calcium ferric phosphate, is a widely distributed although ill-defined phase in low-temperature sedimentary environments. Earlier described as crusts and nodules from the oolitic sedimentary iron ore deposits in the Kerch and Taman peninsulas, southern Russia,¹⁻³ it also occurs as a common product of weathering of exposed primary iron phosphates in pegmatites and other granitic rocks,⁴ and in ferruginous soils, marls, and sandstones which have been impregnated with organic remains. Such field evidence

suggests that the phase is quite stable and possibly one of the most important ferric phosphates formed under rather neutral conditions and ambient temperatures as prevail on the surface of the Earth. Its typical appearance as dull-green to brownish-green earthy stains and films are hardly good distinguishing characters and only the trained eye lifts it out of its undeserved obscurity in natural systems.

Mitridatite has posed some difficult problems for the investigator. Satisfactory single crystals are a great rarity and variable composition of cryptocrystalline masses is typical. The

Table I. Experimental Details of Mitridatite

(A) Crystal Cell Data	
<i>a</i> , Å	17.553 (2)
<i>b</i> , Å	19.354 (3)
<i>c</i> , Å	11.248 (2)
β , deg	95.84 (1)
Space group	<i>Aa</i>
<i>Z</i>	4
Formula	Ca ₆ (H ₂ O) ₆ [Fe ^{III} ₉ O ₆ (PO ₄) ₉]·3H ₂ O
ρ (calcd), g cm ⁻³	3.249
Specific gravity ⁴	3.24
μ , cm ⁻¹	
(B) Intensity Measurements	
Crystal size, mm	0.046(11 <i>a</i>), 0.21(11 <i>b</i>), 0.22(11 <i>c</i>)
Crystal orientation	ϕ axis = [100]
Max (sin θ)/ λ	0.70
Scan speed, deg per min	2.0
Base scan width	2.5
Background counts	Stationary, 20 s at beginning and end of scan
Radiation	Mo K α , (λ 0.7926 Å), graphite monochromator
Independent F_o	5547
(C) Refinement of the Structure	
<i>R</i>	0.068
<i>R_w</i>	0.082
Scale factor	0.900 (3)
Goodness of fit	1.00 (readjusted)
Coefficient of extinction	0.39 (11) $\times 10^{-7}$

senior investigator searched for one decade and accumulated thousands of specimens from hundreds of pegmatites distributed over six continents until the quest was rewarded. A further three years' effort was devoted to unravelling its crystal structure, which proved to be an arrangement of unusual but elegant complexity. We earlier announced preliminary results of this study⁵ and now proceed with a detailed crystal-chemical account of this fascinating phase.

Experimental Section

Preliminary crystal cell data on mitridatite, including the contents, unit cell, and space group, constituted the first formal study of the phase.⁴ In that study, the possible compositions 8[Ca₆Fe^{III}₄(OH)₆(PO₄)₄·3H₂O] or 4[Ca₆Fe^{III}₉(OH)₁₃(PO₄)₈·9H₂O] were proposed. Unusual problems were encountered including persistent twinning by rotation of $\pm\pi/3$ radians on {100}, and a pronounced pseudo-trigonal subcell with $b(\text{sub}) = b/3$ and $3^{1/2}b(\text{sub}) \approx c$. The crystal selected was described in the earlier study⁴ and originated from the White Elephant pegmatite, near Custer, S.D. Preliminary precession and Weissenberg photographs on the red-black crystal showed no evidence of twinning and revealed uniform spot shape and low mosaic spread.

Table I lists the experimental details in this study. Utilizing a Picker FACS-1 automated four-circle diffractometer, least-squares refinement of 16 high-angle reflections led to the cell parameters and estimated standard deviations in Table I. Owing to its thin tabular habit, the crystal was carefully measured and the raw intensities were corrected for absorption anisotropy, applying $6 \times 6 \times 6$ grid points and the Gaussian integral method for path lengths.⁶ Estimated errors of the intensities (σ_I) were calculated according to an earlier published procedure.⁷ For the $|F_o|$ data set, the symmetry-equivalent ($0kl$) and ($0k\bar{l}$) structure factor pairs and their errors were averaged.

Structure Determination and Refinement. Programs used in determining the structure were listed earlier.⁷ The analysis of the structure proved to be a miserable problem. Three-dimensional Patterson synthesis, $P(uvw)$, revealed a map exhibiting pronounced substructure with $b(\text{sub}) = b/3$ and $3^{1/2}b(\text{sub}) \approx c$. In addition, the vector densities of the substructure approximated trigonal symmetry, the subcell mentioned above being the orthohexagonal unit. Strong densities occur at the $u = 0$ and $1/2$ levels and we interpreted these as Fe atoms in special positions along the twofold rotor and in general positions at $x = 1/4, 3/4$ in space group $A2/a$. At this stage, we suspected local isomorphism with the crandallite, Ca[Al₃(OH)₆(P-O₃OH)(PO₄)], structure⁸ and substituted Fe for Al, Ca for Ca, and P for P for one crandallite sheet. A trial β synthesis⁹ using only those

reflections which satisfied the subcell resulted in a map with highly prolate elliptical contours, the major axes of which were parallel to a^* .

Centric tests were not conclusive; we assumed the elliptical contours resulted from an acentric arrangement and repeated the β synthesis in space group Aa . Displacements in the contours away from $x = 1/4$ resulted in more uniform spherical shapes and a new set of parameters led to $R = 0.33$ for the substructure. It was then apparent that trial bond distances between the Fe atoms indicated an edge-sharing octahedral sheet structure, not a corner-sharing sheet as found in crandallite. Guided by bond distances, intuition, and the chemical analysis, we assigned nine nonequivalent Fe atoms at $x \sim 1/4$, three P at $x \sim 1/4$, three P at $x \sim 0.11$, three P at $x \sim 0.39$, three Ca at $x \sim 0.08$, and three Ca at $x \sim 0.42$ and repeated the β synthesis with all reflections for the full mitridatite cell. Although $R = 0.50$ at this stage, it was possible to locate all oxygens associated with the FeO₆ octahedra and PO₄ tetrahedra. A trial β synthesis led to $R = 0.33$ after slight readjustment of the atomic coordinate parameters. At this stage, blocked least-squares refinement of these coordinates (B set to 1.0 \AA^{-2}) led to convergence at $R = 0.22$. A difference Fourier synthesis revealed six oxygens coordinated to Ca only and three oxygens in open spaces and we assumed these to be water molecules. Further convergence was rapid.

Four cycles of scale factor, s ($F_o = sF_c$), coefficient of secondary extinction,¹⁰ atomic coordinate parameter, isotropic thermal vibration parameter refinements led to excellent convergence at $R = 0.068$ and $R_w = 0.082$, where,

$$R = \frac{\sum ||F_o| - |F_c||}{\sum |F_o|}$$

$$R_w = \left[\frac{\sum_w (|F_o| - |F_c|)^2}{\sum_w F_o^2} \right]^{1/2}$$

The final cycle minimized $\sum_w w||F_o| - |F_c||^2$ where $w = \sigma^{-2}(F)$. The "goodness of fit", $S = \sum_w w||F_o| - |F_c||^2 / (n - m)$, where n = number of independent F 's and m = number of parameters, was set at 1.00 in the final refinement and w adjusted such that $\sigma^{-2}(F) = \sigma^2(F(\text{old})) + kF_o^2$. The total number of parameters was $m = 302$, so the independent data to variable parameter ratio is about 18:1.

We employed scattering curves¹¹ for Ca²⁺, Fe³⁺, P⁵⁺, and O¹⁻ and applied anomalous dispersion corrections¹² to Fe, P, and Ca.

A final difference synthesis revealed a low profile with no evidence of remaining non-hydrogen atoms and it was not possible to directly ascertain the hydrogen atom locations, doubtless owing to the rather dense matrix and pronounced pseudosymmetry of mitridatite. Atomic coordinate parameters and isotropic thermal vibration parameters are presented in Table II. It is seen that the thermal parameters range between 0.58 and 0.69 Å⁻² for Fe, 0.78 and 1.09 Å⁻² for Ca, 0.53 and 0.61 Å⁻² for P, and 0.34 and 2.4 Å⁻² for O, typical values for a dense and well-ordered crystal structure. Pertinent bond distances and angles are given in Table III.

The condensed discussion above can hardly convey the unusual complexity of the structure study which spanned 3 years and which required at least 50 β syntheses. Indeed 9 Fe, 6 P, 6 Ca, and 24 O²⁻ approximate in position those found in a sheet of crandallite and dictate the substructure. The essential difficulty, however, was in assigning correct phase angles for the majority of structure factors which were relatively weak and which were mainly influenced by the additional 3 P, 18 O²⁻, and 9 OW (=H₂O) atoms in the asymmetric unit. These latter amount to 28% of the total scattering matter, too great for correct phasing by the substructure reflections and too small for location on the $P(uvw)$ map. The correct formula for an asymmetric unit of mitridatite is Ca₆(H₂O)₆[Fe^{III}₉O₆(PO₄)₉]·3H₂O.

Description of the Structure

The Octahedral Sheet. The underlying structural principle for mitridatite is an elegant compact sheet of composition [Fe^{III}₉O₆(PO₄)₉]¹²⁻ (Figure 1) oriented parallel to the {100} plane and situated at $x \sim 1/4$ and $3/4$. The complex cell of low symmetry masquerades a pronounced trigonal pseudosymmetry with two-sided plane group $p31m$, $a = 11.25 \text{ \AA}$ ($=c$ of the mitridatite cell). The sheet is built up of octahedral edge-sharing nonamers each defining a trigonal ring which fuse

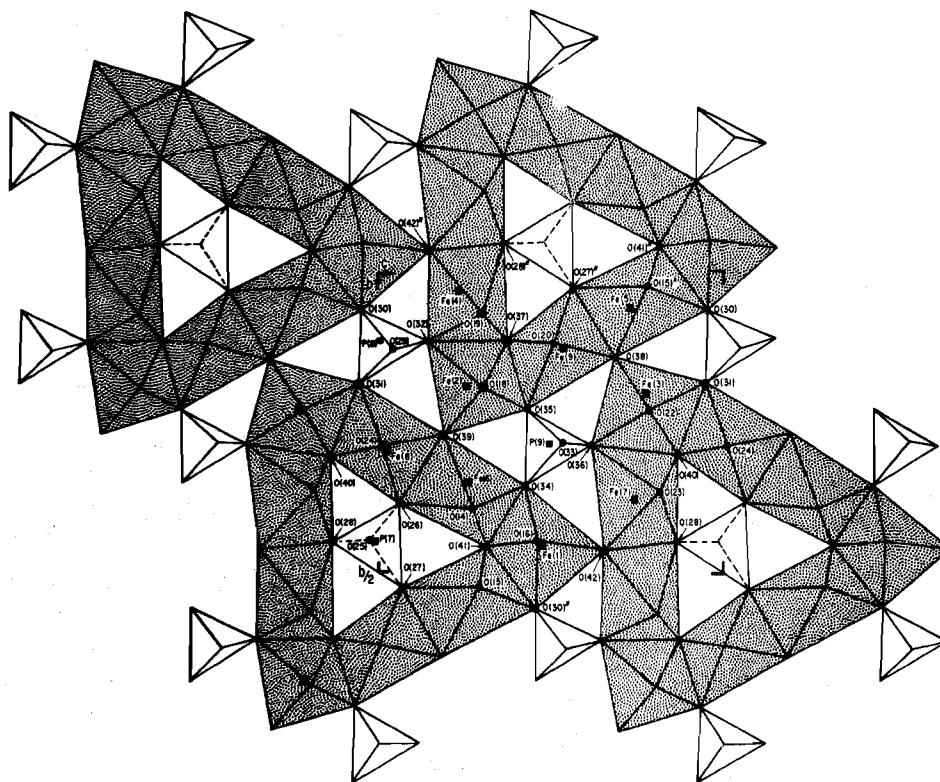


Figure 1. The $[\text{Fe}_9\text{O}_6(\text{PO}_4)_9]^{12-}$ sheet in mitridatite. Atoms are labeled to conform with Table II.

at their extreme trigonal corners to the edge midpoints of symmetry equivalent nonamers. These nonamers have composition $M_9\phi_{36}$ (where M = octahedral center and ϕ = vertex) and constitute an asymmetric unit of structure, the condensed octahedral sheet having composition $M_9\phi_{33}$. The point of condensation is an oxo anion (O^{2-}) which is bonded to three Fe^{3+} ions. In addition, each nonamer possesses three corners in its interior, also comprised of oxo anions, which are also bonded to three Fe^{3+} ions. At the center of each nonamer is a (PO_4) tetrahedron along a pseudotrigonal axis which is linked at three of its corners to octahedra and we refer to its center as P(a). It is located at the origin of the $p31m$ pseudocell. The assembled sheet has a second kind of pseudotrigonal axis which also passes through (PO_4) tetrahedra, the centers of which we designate P(b). They are located at $1/3^2/3z$ and $2/3^1/3z$ positions of the $p31m$ pseudocell. Finally, (PO_4) tetrahedra link at three of their corners to triangular groupings of octahedral vertices above and below the sheet and these we call P(c). Thus, the sheet formula can be written, $[\text{Fe}^{\text{III}}_9\text{O}_6(\text{P}(\text{a})\text{O}_4)(\text{P}(\text{b})\text{O}_4)_2(\text{P}(\text{c})\text{O}_4)_6]^{12-}$.

The nonamer can be directly related to the central girdle of the well-known Keggin molecule, of which $[\text{PW}_{12}\text{O}_{40}]^{3-}$ is an example, by removing the trigonal edge-sharing caps above and below the molecule resulting in $[\text{PW}_6\text{O}_{28}]$. It is topologically identical to the central girdle of the related $[\text{PMo}_9\text{O}_{31}(\text{H}_2\text{O})_3]^{3-}$ polyanion which has been shown¹³ to be related to the Keggin molecule. Rewriting this polyanion $[(\text{PMo}_6\text{O}_{28})\text{Mo}_3\text{O}_3(\text{H}_2\text{O})_3]$, mitridatite's isomorphous region can be written $[\text{P}(\text{a})\text{Fe}_6\text{O}_{28}]$; it is obtained by removing the three octahedra at the extreme trigonal corners of the nonamer (Figure 2).

The sheet in mitridatite appeared quite new to us until a local isomorphism was discovered between it and the seemingly unrelated schairerite structure,¹⁴ $\text{Na}_{21}\text{F}_6\text{Cl}(\text{SO}_4)_7$, $P31m$, $Z = 3$, $a = 12.20 \text{ \AA}$, $c = 19.26 \text{ \AA}$. This latter compound is based on the compression of seven trigonal sheets within the c -axial repeat, one of which is geometrically isomorphous to mitridatite. In schairerite, the isomorphous sheet has composition

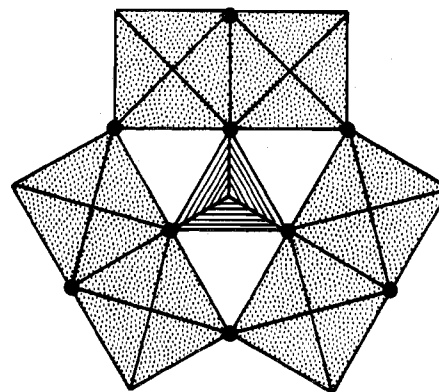


Figure 2. The $[\text{PFe}_6\text{O}_{28}]$ central girdle found in the Keggin molecule and in mitridatite.

$[\text{Na}_9\text{F}_6(\text{SO}_4)_9]^{15-}$ and conserves every geometrical detail of the mitridatite sheet including the orientations of the tetrahedra. The remaining six sheets in schairerite share local isomorphisms with the curious crystal structure of lāngbanite, $\text{Mn}^{\text{II}}_4\text{Mn}^{\text{III}}_9\text{Sb}^{\text{V}}\text{Si}^{\text{IV}}_2\text{O}_{24}$, $P31m$, $Z = 3$, $a = 11.57 \text{ \AA}$, $c = 11.12 \text{ \AA}$. Our presently unpublished results show that lāngbanite possesses four sheets in the c -axial repeat, two of which are isomorphous to sheets in schairerite, viz., $\text{Mn}^{\text{II}}_{12}\text{Mn}^{\text{III}}_9\text{Sb}^{\text{V}}_3$ - $[\text{Mn}^{\text{III}}_9\text{O}_{24}(\text{SiO}_4)_3]_2$. The composition in brackets constitutes the isomorphous region and the remaining cations are organized in an ordered way according to the sheet of the familiar brucite, $\text{Mg}(\text{OH})_2$, structure type.

Perhaps most intriguing is the fact that mitridatite is a collapsed version of the crystal structure of the well-known alunite structure type and the crandallite isotype.^{8,15} The comparison is best made by following the trigonal idealizations of the structures in Figure 3. The alunite structure type is built of a corner-linked octahedral sheet which is based on three-membered and six-membered octahedral rings (Figure 3a). The octahedral centers define the vertices of the well-known Kagomé net. If alternate three-membered octahedral

Table II. Mitridatite Atomic Coordinate Parameters^a

	x	y	z	B, Å ²		x	y	z	B, Å ²
Fe(1)	0.2500	0.46266 (8)	0.5000	0.60 (2)	P(5)	0.3889 (2)	0.1192 (1)	0.3965 (3)	0.58 (4)
Fe(2)	0.2465 (1)	0.20013 (8)	0.2917 (2)	0.58 (2)	O(17)	0.4739 (5)	0.1166 (4)	0.4165 (7)	0.95 (12)
Fe(3)	0.2468 (1)	0.22755 (8)	0.7935 (2)	0.60 (2)	O(18)	0.3602 (5)	0.1863 (4)	0.3271 (6)	0.66 (11)
Fe(4)	0.2434 (1)	0.04173 (8)	0.2716 (2)	0.60 (2)	O(19)	0.3568 (5)	0.0559 (4)	0.3205 (7)	0.88 (12)
Fe(5)	0.2456 (1)	0.05241 (8)	0.7703 (2)	0.62 (2)	O(20)	0.3542 (5)	0.1186 (4)	0.5190 (7)	0.87 (12)
Fe(6)	0.2487 (1)	0.37474 (8)	0.2725 (2)	0.69 (2)	P(6)	0.3943 (2)	0.3085 (1)	0.8955 (3)	0.57 (4)
Fe(7)	0.2517 (1)	0.38608 (8)	0.7719 (2)	0.65 (2)	O(21)	0.4811 (5)	0.3098 (4)	0.9072 (7)	0.82 (11)
Fe(8)	0.2504 (1)	0.29595 (8)	0.0397 (2)	0.64 (2)	O(22)	0.3628 (5)	0.2430 (4)	0.8255 (7)	0.83 (11)
Fe(9)	0.2401 (1)	0.12921 (8)	0.5377 (2)	0.60 (2)	O(23)	0.3626 (5)	0.3736 (4)	0.8265 (7)	0.95 (12)
Ca(1)	0.5807 (2)	0.0376 (1)	0.8212 (2)	0.97 (6)	O(24)	0.3638 (5)	0.3075 (4)	1.0209 (7)	0.77 (11)
Ca(2)	0.5820 (2)	0.1717 (1)	0.3670 (2)	0.78 (5)	P(7)	0.2067 (2)	0.4590 (1)	1.0165 (3)	0.56 (4)
Ca(3)	0.5762 (2)	0.3737 (1)	0.8394 (2)	0.91 (5)	O(25)	0.1230 (6)	0.4449 (5)	0.9905 (8)	1.45 (14)
Ca(4)	0.4155 (2)	0.2880 (1)	0.2319 (2)	0.88 (6)	O(26)	0.2489 (5)	0.3993 (4)	1.0927 (6)	0.34 (10)
Ca(5)	0.4157 (2)	0.4858 (1)	0.6851 (2)	1.09 (6)	O(27)	0.2286 (5)	0.5276 (4)	1.0880 (7)	0.99 (13)
Ca(6)	0.4125 (2)	0.1551 (1)	0.7090 (2)	0.95 (5)	O(28)	0.2453 (5)	0.4637 (4)	0.8979 (7)	0.60 (11)
P(1)	0.1052 (2)	0.2863 (1)	0.1836 (3)	0.53 (4)	P(8)	0.2871 (2)	0.1280 (1)	1.0370 (3)	0.57 (4)
O(1)	0.0198 (5)	0.2852 (4)	0.1686 (7)	1.17 (12)	O(29)	0.3720 (6)	0.1190 (5)	1.0593 (8)	1.41 (14)
O(2)	0.1369 (5)	0.2206 (4)	0.2533 (7)	0.97 (13)	O(30)	0.2501 (5)	0.0688 (5)	0.9587 (7)	1.15 (13)
O(3)	0.1382 (5)	0.3498 (4)	0.2549 (7)	0.95 (12)	O(31)	0.2579 (5)	0.1954 (4)	0.9751 (7)	0.77 (11)
O(4)	0.1401 (5)	0.2863 (4)	0.0616 (6)	0.58 (11)	O(32)	0.2472 (5)	0.1265 (4)	1.1557 (7)	0.82 (11)
P(2)	0.1054 (2)	0.4618 (1)	0.6459 (3)	0.61 (4)	P(9)	0.2876 (2)	0.2942 (1)	0.5364 (3)	0.60 (4)
O(5)	0.0191 (5)	0.4578 (4)	0.6282 (7)	1.06 (12)	O(33)	0.3724 (6)	0.2845 (5)	0.5560 (8)	1.45 (14)
O(6)	0.1351 (5)	0.5279 (4)	0.7148 (7)	0.81 (12)	O(34)	0.2595 (4)	0.3581 (4)	0.4598 (6)	0.62 (11)
O(7)	0.1390 (5)	0.3988 (4)	0.7194 (7)	0.81 (11)	O(35)	0.2478 (5)	0.2303 (4)	0.4726 (7)	0.94 (12)
O(8)	0.1398 (5)	0.4613 (4)	0.5235 (7)	1.02 (12)	O(36)	0.2515 (5)	0.3014 (4)	0.6550 (7)	0.98 (12)
P(3)	0.1018 (2)	0.1440 (1)	0.6894 (2)	0.56 (4)	O(37)	0.2137 (4)	0.1142 (4)	0.3709 (6)	0.59 (11)
O(9)	0.0162 (5)	0.1466 (5)	0.6800 (7)	1.17 (13)	O(38)	0.2726 (5)	0.1452 (4)	0.7107 (7)	0.82 (11)
O(10)	0.1371 (5)	0.2082 (4)	0.7602 (7)	1.02 (12)	O(39)	0.2771 (5)	0.2827 (4)	0.2143 (6)	0.68 (11)
O(11)	0.1326 (5)	0.0775 (4)	0.7547 (7)	0.98 (12)	O(40)	0.2205 (4)	0.3138 (4)	0.8757 (6)	0.47 (10)
O(12)	0.1312 (5)	0.1444 (4)	0.5626 (7)	1.14 (13)	O(41)	0.2191 (4)	0.4639 (4)	0.3250 (6)	0.51 (10)
P(4)	0.3932 (2)	0.4660 (1)	0.3548 (3)	0.57 (4)	O(42)	0.2773 (5)	0.4650 (4)	0.6680 (7)	0.81 (11)
O(13)	0.4792 (5)	0.4691 (4)	0.3607 (7)	0.74 (11)	OW(1)	0.4990 (6)	0.2693 (5)	0.4121 (8)	1.35 (13)
O(14)	0.3629 (5)	0.3976 (4)	0.2918 (7)	0.75 (11)	OW(2)	0.4856 (6)	0.3789 (5)	0.6597 (8)	1.84 (15)
O(15)	0.3584 (5)	0.5290 (4)	0.2855 (7)	0.75 (11)	OW(3)	0.4981 (5)	0.0616 (5)	0.6506 (7)	1.14 (13)
O(16)	0.3654 (5)	0.4667 (4)	0.4820 (7)	0.72 (11)	OW(4)	0.4926 (6)	0.1928 (5)	0.1842 (8)	1.49 (14)
					OW(5)	0.5022 (6)	0.4707 (4)	0.8748 (8)	1.17 (13)
					OW(6)	0.4891 (6)	0.1222 (5)	0.8916 (8)	1.81 (16)
					OW(7)	0.4275 (6)	0.4509 (5)	0.0628 (9)	1.64 (15)
					OW(8)	0.5775 (6)	0.3798 (6)	0.4874 (9)	2.18 (17)
					OW(9)	0.5812 (7)	0.2132 (6)	0.0080 (9)	2.39 (18)

^a Estimated standard errors in parentheses refer to the last digit.

rings are collapsed together to form an edge-sharing system, the mitridatite configuration obtains (Figure 3b). The six-membered rings now become triangular regions which receive the P(a)O₄ and P(b)O₄ tetrahedra. A further collapse (Figure 3c) leads to the edge-sharing Kagomé sheet of octahedra, well-known as a slice of spinel along the {111} plane and found as an entity in the crystal structure of chloritoid,¹⁶ Fe₂-Al(OH)₄[Al₃O₂(SiO₄)₂]. This is the densest sheet possible since it is a section of the cubic close-packing (-c). Thus, a progressive sequence of sheets of increasing density can be conceived, beginning with the iron phosphate isotype of alunite, lusungite:

	Sheet	% collapse (area)
Lusungite	[Fe ₉ (OH) ₆ (P(c)O ₄) ₆] ⁹⁻	0.0
Mitridatite	[Fe ₉ O ₆ (P(a)O ₄) ₂ (P(b)O ₄) ₂ (P(c)O ₄) ₆] ¹²⁻	16.1
Hypothetical	[Fe ₉ O ₆ (P(a)O ₄) ₃ (P(b)O ₄) ₃] ³⁻	35.1

To assess the degree of collapse based on the area of the cells, the cell length of the hypothetical condensed structure, 3-[M₃O₂(TO₄)₂], was derived by isomorphic substitution of Fe³⁺ for Al³⁺ in chloritoid. It is noted that mitridatite affords a reduction of about 16% in area and the hypothetical sheet composition an additional 19%. Among phosphates, the hypothetical sheet has yet to be found although it appears in

bermanite, Mn^{II}(H₂O)₄[□Mn^{III}₂(OH)₂(PO₄)₂], if the ordered vacancy, □, is included.¹⁷

In all three structures, the loci of the Fe atoms are approximately the same which accounts for similar substructure reflections. Thus, the progressive condensation of the sheets outlined above is an interesting example of oxygen rearrangements about the same configuration of metal centers. The P(c)O₄ tetrahedra in the lusungite and mitridatite structures are also approximately isomorphic as seen in Figure 4, the tetrahedra for the former represented by the isomorphic crandallite parameters.⁸ Although mitridatite was earlier suggested to be related in some way to the alunite structure,¹⁸ the contradiction of a decrease in area when an increase was expected through isomorphic substitution of Al³⁺ by Fe³⁺ can now be understood; mitridatite is a new type chemically and structurally, topologically distinct from but related to alunite.

The Alkaline Earth-Water Layer. A thick assembly of CaO₅(H₂O)₂ polyhedra and water molecules occurs as open sheets parallel to {100} at about $x \sim 0$ and $1/2$. A polyhedral diagram about $x \sim 1/2$ is featured in Figure 5. All six nonequivalent CaO₅(H₂O)₂ polyhedra possess approximately the same geometry; each Ca is coordinated to four phosphate oxygens, one oxo anion, and two water molecules, defining a distorted octahedron with an additional coordination sphere above the midpoint of one of the octahedral faces. In Figure 6, the polyhedron is featured with its vertices classified ac-

Ca(1) (Continued)		Ca(2) (Continued)		Ca(3) (Continued)	
O(3)'-O(41)'	2.698 (11) ^c	O(4)''-O(40)'	2.692 (10) ^c	O(6)'''-O(37)'	2.699 (11) ^c
O(11)''-O(41)'	2.743 (11) ^c	O(7)''-O(40)'	2.709 (11) ^c	O(2)''-O(37)'	2.729 (11) ^c
O(8)''-O(41)'	2.749 (11) ^d	O(10)''-O(40)'	2.762 (11) ^c	O(12)''-O(37)'	2.779 (11) ^c
OW(3)-OW(6)	2.973 (11) ^d	OW(1)-OW(4)	2.951 (12) ^d	OW(2)-OW(5)	2.992 (11) ^d
O(13)''-OW(6)	2.986 (12)	O(17)''-OW(1)	2.988 (12)	O(6)'''-OW(5)	3.088 (12)
O(13)''-OW(3)	3.011 (11)	O(4)''-OW(1)	3.044 (12)	O(21)-OW(2)	3.096 (12)
O(3)''-OW(3)	3.126 (12)	O(17)''-OW(4)	3.047 (11)	O(21)''-O(12)'	3.140 (12)
O(11)'''-O(13)''	3.184 (12)	O(7)''-OW(4)	3.114 (13)	O(21)''-OW(5)	3.162 (12)
O(3)''-OW(6)	3.213 (13)	O(10)''-OW(1)	3.134 (13)	O(6)'''-OW(2)	3.192 (13)
O(8)''-OW(6)	3.317 (13)	O(10)''-OW(4)	3.224 (13)	O(2)''-OW(2)	3.361 (13)
O(8)''-O(13)''	3.473 (12)	O(4)''-O(17)	3.706 (13)	O(2)''-O(21)	3.433 (12)
O(11)'''-OW(3)	3.692 (13)	O(4)''-O(10)'	3.707 (13)	O(12)''-OW(5)	3.685 (13)
O(3)''-O(8)'	3.711 (13)	O(7)''-O(10)'	3.718 (13)	O(2)''-O(6)'''	3.754 (13)
O(8)''-O(11)'''	3.760 (13)	O(7)''-O(17)	3.835 (13)	O(2)''-O(12)'	3.789 (13)
O(3)''-O(11)'''	4.408 (14)	O(4)''-O(7)'	4.421 (14)	O(6)'''-O(12)'	4.522 (14)
Average	3.270	Average	3.270	Average	3.295
Ca(4)		Ca(5)		Ca(6)	
g		Ca(5)-O(5)'''	2.265 (9)	Ca(6)-O(1)'	2.294 (9)
g' Ca(4)-O(9)'	2.297 (9)	Ca(5)-O(42)	2.451 (9)	Ca(6)-O(38)	2.465 (9)
a Ca(4)-O(39)	2.420 (8)	Ca(5)-O(23)	2.900 (8)	Ca(6)-O(15)''	2.786 (8)
e Ca(4)-O(18)	2.485 (8)	Ca(5)-O(19)''	2.356 (8)	Ca(6)-O(22)	2.368 (8)
e Ca(4)-O(14)	2.434 (8)	Ca(5)-O(16)	2.392 (8)	Ca(6)-O(20)	2.381 (8)
e Ca(4)-O(24)	2.482 (8)	Ca(5)-OW(5)	2.507 (9)	Ca(6)-OW(6)	2.424 (10)
h Ca(4)-OW(1)	2.405 (9)	Ca(5)-OW(2)	2.437 (10)	Ca(6)-OW(3)	2.483 (9)
h Ca(4)-OW(4)	2.380 (10)	Average	2.473	Average	2.457
Average	2.415	O(16)-O(42)	2.724 (11) ^c	O(22)-O(38)	2.708 (11) ^c
O(18)-O(39)	2.616 (11) ^c	O(19)''-O(42)	2.738 (11) ^c	O(20)-O(38)	2.755 (11) ^c
O(14)-O(39)	2.776 (11) ^c	O(23)-O(42)	2.828 (11) ^c	O(15)''-O(38)	2.789 (11) ^c
O(24)-O(39)	2.821 (10) ^c	OW(2)-OW(5)	2.992 (11) ^d	OW(3)-OW(6)	2.973 (11) ^d
OW(1)-OW(4)	2.951 (12) ^d	O(23)-OW(2)	3.003 (13)	O(1)''-OW(3)	2.994 (13)
O(18)-OW(4)	2.960 (12)	O(19)''-OW(5)	3.047 (13)	O(20)-OW(3)	3.006 (12)
O(18)-OW(1)	2.993 (12)	O(23)-OW(5)	3.093 (13)	O(15)''-OW(6)	3.063 (13)
O(9)''-OW(1)	3.117 (12)	O(5)'''-OW(5)	3.141 (12)	O(15)''-OW(3)	3.078 (12)
O(9)''-OW(4)	3.137 (13)	O(16)-OW(2)	3.238 (12)	O(1)''-OW(6)	3.174 (12)
O(9)''-O(24)	3.190 (12)	O(5)'''-OW(2)	3.241 (13)	O(22)-OW(6)	3.256 (13)
O(9)''-O(14)	3.199 (12)	O(5)'''-O(16)	3.348 (12)	O(15)''-O(20)	3.457 (11)
O(14)-O(24)	3.512 (11)	O(9)''-O(23)	3.529 (12)	O(1)''-O(22)	3.464 (11)
O(24)-OW(4)	3.546 (13)	O(5)'''-O(19)''	3.757 (13)	O(1)''-O(20)	3.708 (13)
O(14)-OW(1)	3.612 (13)	O(16)-O(19)''	4.197 (14)	O(15)''-O(22)	4.166 (14)
O(14)-O(18)	4.109 (14)	O(16)-O(23)	4.278 (14)	O(20)-O(22)	4.195 (14)
O(18)-O(24)	4.173 (14)	Average	3.277	Average	3.252
Average	3.247				
P(1)		P(2)		P(3)	
g P(1)-O(1)	1.492 (9)	P(2)-O(5)	1.510 (9)	P(3)-O(9)	1.496 (10)
g'		P(2)-O(7)	1.554 (8)	P(3)-O(11)	1.551 (9)
e P(1)-O(2)	1.567 (9)	P(2)-O(6)	1.557 (8)	P(3)-O(10)	1.568 (9)
e P(1)-O(3)	1.547 (9)	P(2)-O(8)	1.559 (8)	P(3)-O(12)	1.566 (8)
e P(1)-O(4)	1.559 (7)	Average	1.545	Average	1.545
Average	1.541	O(6)-O(7)	2.499 (12)	O(9)-O(11)	2.513 (13)
O(2)-O(3)	2.501 (12)	O(7)-O(8)	2.514 (11)	O(11)-O(12)	2.516 (11)
O(3)-O(4)	2.502 (11)	O(6)-O(8)	2.517 (11)	O(9)-O(10)	2.519 (13)
O(2)-O(4)	2.509 (11)	O(5)-O(7)	2.519 (12)	O(9)-O(12)	2.523 (13)
O(1)-O(2)	2.510 (13)	O(5)-O(8)	2.527 (12)	O(10)-O(11)	2.530 (12)
O(1)-O(3)	2.533 (12)	O(5)-O(6)	2.556 (12)	O(10)-O(12)	2.535 (11)
O(1)-O(4)	2.535 (11)	Average	2.522	Average	2.523
Average	2.515				
P(4)		P(5)		P(6)	
g		P(5)-O(17)	1.488 (9)	P(6)-O(21)	1.515 (8)
g' P(4)-O(13)	1.505 (9)	P(5)-O(19)	1.565 (9)	P(6)-O(22)	1.564 (8)
e P(4)-O(14)	1.570 (8)	P(5)-O(18)	1.572 (8)	P(6)-O(23)	1.553 (8)
e P(4)-O(15)	1.539 (8)	P(5)-O(20)	1.563 (8)	P(6)-O(24)	1.558 (8)
e P(4)-O(16)	1.559 (8)	Average	1.547	Average	1.547
Average	1.543	O(17)-O(20)	2.499 (12)	O(21)-O(23)	2.509 (12)
O(13)-O(15)	2.489 (11)	O(17)-O(19)	2.514 (12)	O(22)-O(24)	2.526 (11)
O(15)-O(16)	2.510 (11)	O(18)-O(19)	2.526 (12)	O(22)-O(23)	2.529 (12)
O(14)-O(16)	2.521 (11)	O(17)-O(18)	2.532 (12)	O(21)-O(24)	2.531 (11)
O(13)-O(14)	2.523 (11)	O(18)-O(20)	2.536 (11)	O(23)-O(24)	2.531 (11)
O(13)-O(16)	2.532 (11)	O(19)-O(20)	2.547 (11)	O(21)-O(22)	2.538 (12)
O(14)-O(15)	2.546 (11)	Average	2.526	Average	2.527
Average	2.520				

Table III (Continued)

P(7)		P(8)		P(9)				
f P(7)-O(25)	1.494 (11)	P(8)-O(29)	1.496 (10)	P(9)-O(33)	1.495 (10)			
c P(7)-O(26)	1.578 (8)	P(8)-O(30)	1.547 (9)	P(9)-O(35)	1.558 (9)			
c P(7)-O(28)	1.559 (8)	P(8)-O(31)	1.542 (8)	P(9)-O(34)	1.559 (8)			
c P(7)-O(27)	1.580 (9)	P(8)-O(32)	1.570 (8)	P(9)-O(36)	1.541 (8)			
Average	1.553	Average	1.539	Average	1.538			
O(25)-O(28)	2.506 (13)	110.3 (5)	O(31)-O(32)	2.454 (11)	104.1 (4)	O(35)-O(36)	2.466 (11)	105.4 (5)
O(26)-O(27)	2.509 (11)	105.2 (5)	O(30)-O(31)	2.460 (12)	105.6 (5)	O(34)-O(36)	2.472 (11)	105.8 (4)
O(27)-O(28)	2.514 (11)	106.4 (5)	O(30)-O(32)	2.485 (11)	105.8 (5)	O(34)-O(35)	2.488 (11)	105.9 (4)
O(26)-O(28)	2.516 (10)	106.7 (4)	O(29)-O(30)	2.512 (13)	111.3 (5)	O(33)-O(36)	2.517 (13)	112.0 (5)
O(25)-O(26)	2.544 (13)	111.8 (5)	O(29)-O(32)	2.545 (13)	112.2 (5)	O(33)-O(35)	2.519 (13)	111.2 (5)
O(25)-O(27)	2.605 (13)	115.9 (5)	O(29)-O(31)	2.590 (12)	117.0 (5)	O(33)-O(34)	2.587 (12)	115.8 (5)
Average	2.532	109.4	Average	2.508	109.3	Average	2.508	109.4
Hydrogen Bonds								
h→f								
OW(1)→O(33)	2.895 (13)	OW(3)-OW(7)''-O(9)'''	99.2 (4)	OW(5)''-O(25)'-OW(3)	75.1 (4)			
OW(2)→O(33)	2.860 (13)	OW(3)-OW(7)''-OW(5)''	85.9 (4)	OW(6)''-O(29)''-OW(4)''	76.6 (4)			
OW(3)→O(25)'	2.978 (13)	OW(5)''-OW(7)''-O(9)'''	100.6 (4)	OW(1)-O(33)-OW(2)	75.6 (4)			
OW(4)→O(29)''	2.809 (13)	Average	95.2	Average	75.8			
OW(5)''→O(25)'	2.880 (13)	OW(6)''-OW(9)''-OW(4)''	84.0 (4)	i→g'				
OW(6)→O(29)''	2.929 (13)	OW(6)''-OW(9)''-O(21)'''	85.2 (4)	OW(7)''→O(9)'''	2.703 (13)			
Average	2.892	OW(4)''-OW(9)''-O(21)'''	90.6 (4)	OW(8)→O(13)	2.737 (13)			
d(O-H...O) pred _e	2.60	Average	86.6	OW(9)''→O(21)'	2.732 (14)			
Δp _o = +0.66 ^f		OW(1)-OW(8)-OW(2)	83.8 (4)	Average	2.724			
h→i								
OW(1)→OW(8)	2.638 (14)	OW(1)-OW(8)-O(13)	93.7 (4)	d(O-H...O) pred _e	2.74			
OW(2)→OW(8)	2.644 (14)	OW(2)-OW(8)-O(13)	89.3 (4)	Δp _o = +0.30 ^f				
OW(3)→OW(7)''	2.618 (13)	Average	88.9					
OW(4)→OW(9)''	2.671 (14)							
OW(5)''→OW(7)''	2.627 (13)							
OW(6)→OW(9)''	2.646 (15)							
Average	2.641							
d(O-H...O) pred _e	2.76							
Δp _o = +0.24 ^f								

^a Estimated standard deviations refer to the last digit. ^b Fe-Fe oxygen octahedral shared edges. ^c Fe-Ca oxygen polyhedral shared edges. ^d Ca-Ca oxygen polyhedral shared edges. ^e $e' = 1/2 + x, 1/2 - y, 1/2 + z$; $e'' = x, 1/2 + y, 1/2 + z$; $e''' = 1/2 + x, -y, z$ applied to coordinates in Table II. ^f Valence units.

cording to four kinds of oxygens (see under Bond Distances). The first, O_g, corresponds to apical P(c)O₄ oxygens. The P(c)-O_g distances are among the shortest for all six non-equivalent Ca atoms. The second type, O_e, corresponds to basal P(c)O₄ oxygens which are, in addition, bonded to the Fe atoms. These are arranged in a manner similar to that found in the alunite structure type. The third, O_a (or O_b), which is the additional coordinating sphere above the midpoint of the octahedral face, corresponds to an oxo anion in the octahedral sheets. Thus, Ca:P(c):O²⁻ (oxo-) = 1:1:1. Finally, there exist two water molecules, O_h. These water molecules define a shared OW-OW' edge which is shared by two Ca atoms resulting in Ca₂O₁₀(H₂O)₂ dimers. The arrangement of these dimers in Figure 5 results in a destruction of trigonal symmetry, thus leading to the monoclinic cell in mitridatite. Note that the orthohexagonal unit is related by $3^{1/2}b \sim c$ which is the orthogonal expression of the trigonal pseudosymmetry. From these observations, it is tempting to suggest that a trigonal modification may exist in nature, differing from mitridatite in the manner in which the interlayer large cations are organized.

Hydrogen Bonds. A hydrogen bond network is proposed on geometrical grounds since it was not possible to resolve hydrogen atom positions on a difference synthesis. Figure 5 shows these bonds and the model proposed is entirely consistent with bond distances and tetrahedral geometry. Three sets of clustered configurations occur which are each geometrically equivalent. The apical oxygens, O(25), O(29), and O(33) to P(7), P(8), and P(9), respectively, each receive two bonds from water molecules bonded to the Ca atoms. In addition, OW(7) through OW(9), which participate in hydrogen bonding only,

each receive two bonds from the aforementioned water molecules and donate one bond to a phosphate oxygen, the composite defining the base of a tetrahedral configuration. The remaining hydrogen is weakly bonded to a PO₄ tetrahedral base above (or below) the layer. Thus, OW(7), OW(8), and OW(9) duplicate in their arrangement the complementary pattern found for P(7), P(8), and P(9), respectively.

The atomic arrangement described above explains many physical properties noted for mitridatite. The perfect basal cleavage, parallel to {100}, is the plane of the water molecules and the octahedral sheets. Mitridatite is extremely pleochroic, deep greenish-brown for vibrations parallel to the sheets and pale greenish-yellow for vibrations normal to the sheets.⁴ In addition, the indexes of refraction in the sheets ($n_{\beta,\gamma} \sim 1.85$) are considerably greater than the index normal to the sheets ($n_{\alpha} \sim 1.78$). These phenomena arise from the short Fe-Fe separations in the plane of the sheets owing to extensive edge sharing and it is predicted that the compound will possess extensive antiferromagnetic character with an anomalously low magnetic moment per Fe atom. Indeed, Rossman¹⁹ found $\mu = 3.54 \mu_B$ for jarosite at 298 K, and with the much shorter Fe-Fe separations found in mitridatite the magnetic moment is expected to be even further reduced in that mineral owing to spin coupling across shared edges.

Bond Distances and Angles

Nomenclature. Owing to the pronounced pseudosymmetry of mitridatite, it is convenient to arrange the polyhedral bond distances and bond length-bond strength variations according to structurally similar regions. The apical oxygens on PO₄ groups are indexed sequentially: for P(*n*) it is O(4*n* - 3), *n*

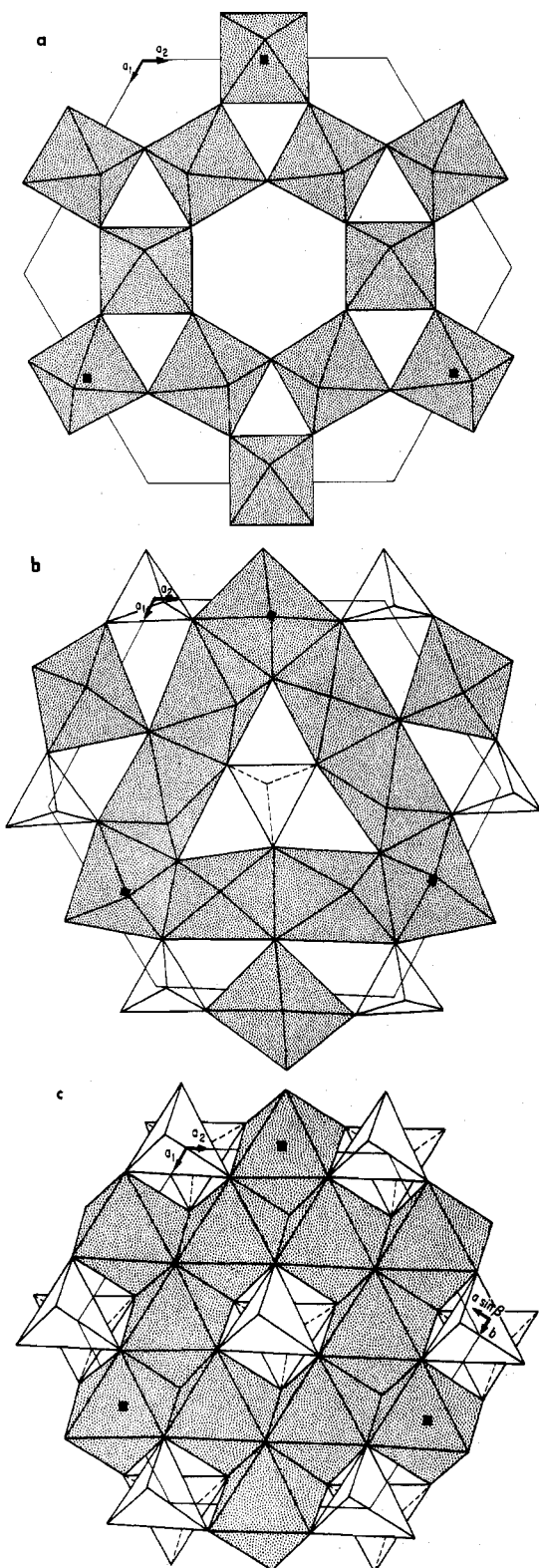


Figure 3. Sequence of progressively condensed octahedral sheets in (a) the alunite structure type, (b) mitridatite, and (c) hypothetical [Fe^{III}₉O₆(PO₄)₆]³⁻. For orientation, refer to the three solid squares on each diagram.

= 1–9. The oxo anions are O(37)–O(42). There are two kinds of Fe atoms: three at the extreme pseudotrigonal corners (Fe(1) through Fe(3)) and the remaining six which comprise the central girdle (Fe(4) through Fe(9)). For true trigonal *p31m* symmetry the atoms within the groupings would be equivalent. The first six P atoms, P(1) through P(6), are also related to each other by pseudosymmetry, and P(7) through

P(9) are in geometrically similar environments. Finally, all six nonequivalent calcium atoms, Ca(1) through Ca(6), are related to each other in a pseudosymmetrical way. Thus, in Table III, the Fe–O, P–O, and Ca–O distances are arranged consistently, grouped according to the distinct kinds of oxygens. The O–O' edge distances, however, are arranged in order of increasing distances following the more conventional procedure since we want to assess shared edge effects on these distances.

Ten kinds of oxygens are discerned and the first five are labeled in Figure 7. O_a and O_b are closely related and each is bonded to three Fe and one Ca. The O_a's are distributed at the triangular corners inside the nonamer and O_b's are the links between nonamers. The O_c oxygens correspond to the base of P(7) inside the nonamer and O_d are the bases of P(8) and P(9). Each of these bonds to two Fe and one P atom. The O_e oxygens are the bases of P(1) through P(6), akin to the alunite structure type, and link to Fe as termini above and below the sheets. They receive one bond from Fe, one from P, and one from Ca. The O_f's correspond to the apical oxygens of P(7) through P(9) and receive two hydrogen bonds (H_a) and one P bond. O_g are the apical oxygens of P(1) through P(6), similar to those found in the alunite structure type. There are two kinds: O_g receives one Ca and one P bond and O_g' receives an additional hydrogen bond from OW(7) through OW(9). The O_h's are OW(1) through OW(6) and each receives two Ca bonds and provides two hydrogen atom donors (H_d). Finally, O_i corresponds to OW(7) through OW(9) and each receives two hydrogen bonds (H_a) and donates two hydrogen bonds (H_d). One of the latter points to the base of P(7) through P(9) and is a weak bond: all O–H...O bonds are longer than 3.2 Å to any oxygen.

Figures 1, 4, and 5 afford the labeling of atoms; those unprimed indexes refer to the atomic positions in Table II, the primed indexes corresponding to positions generated by point set equivalence.

Assessment of Bond Length–Bond Strength Variations. Baur²⁰ has discussed the empirical relationships between bond length (*d*) and bond strength (*s*) for ionic inorganic crystals. For mineral structures, it is expected that the sum of bond strengths of cations about an anion, *p_x*, varies only slightly from the formal charge of that anion with reversed sign. Deviations (Δp_x) of a considerable degree should correlate with corresponding deviations in individual bond distance (Δd) with respect to the polyhedral average. The bond strength is evaluated $s = z/N_c$, where *z* is the formal charge of the cation and *N_c* is the coordination number of that cation. Therefore, $p_x = \sum_i s_i$ for the *i* cations surrounding (coordinated to) the anion. For hydrogen bonds, the hydrogen atom donor (H_d) bond is given $s = 5/6$ and a hydrogen atom acceptor (H_a) bond $s = 1/6$, suggested on empirical grounds by Baur.²⁰ Finally, Baur's fourth rule is invoked: "The lengths of the hydrogen bonds formed between pairs of anions vary inversely with Δp , the difference of the *p_x*-values received by the donor and acceptor atoms of the hydrogen bond: $\Delta p = p_{\text{donor}} - p_{\text{acceptor}}$."

Bond length–bond strength variations are important in assessing the role of water. In Table IV, the Δd and Δp_O are arranged according to the kind of oxygen. If more than one cation of a given kind coordinates to an anion the distance deviations were averaged. Inspection immediately shows that no hydroxyl (OH⁻) anions occur in the structure; O_a, O_b, O_f, O_g, and O_g' treated as O²⁻ are all undersaturated ($\Delta p_O = -0.21$ to -0.46) and the individual distances are all considerably shorter than average. The reverse would be true if OH⁻ anions were present. O_c and O_d are considerably oversaturated ($\Delta p_O = +0.25$) and, consequently, the bond distances are longer than average. The agreement in distance deviations predicted from Baur's results of regression analyses²⁰ is quite acceptable. The O_e oxygens are nearly neutral ($\Delta p_O = +0.04$); deviations in

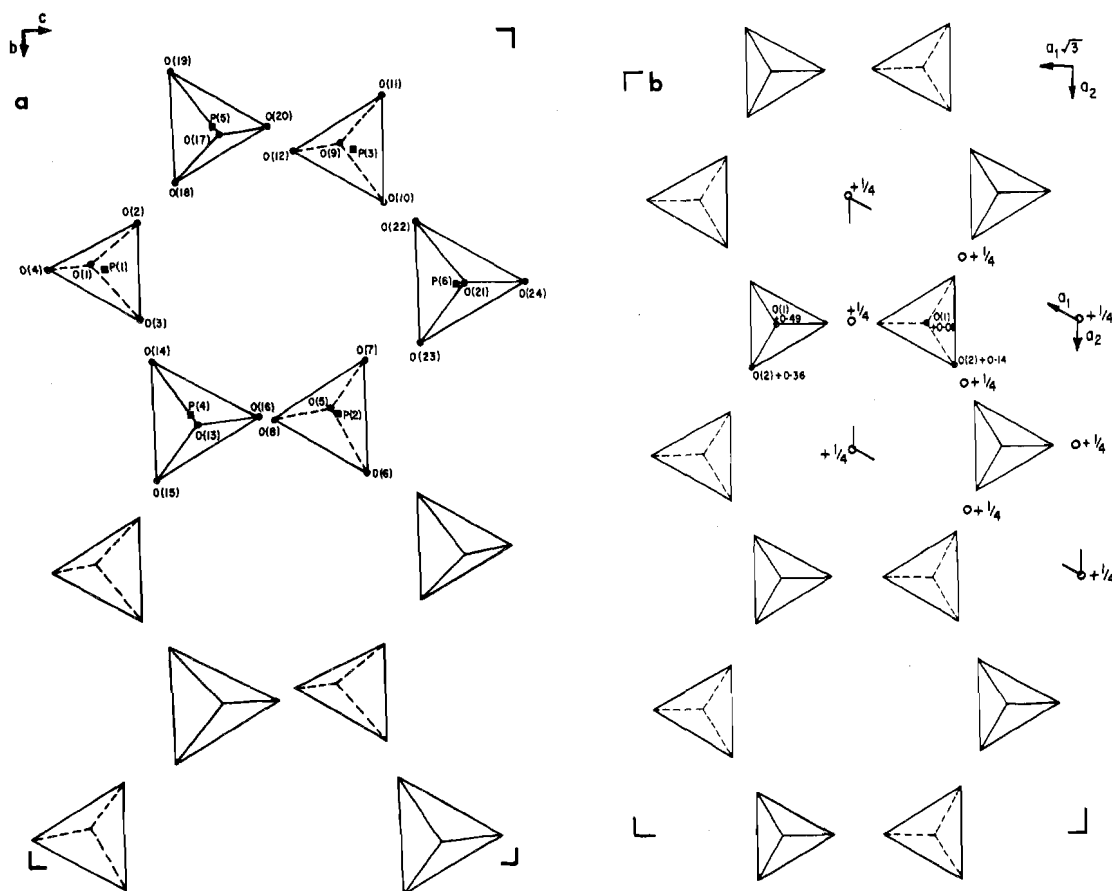


Figure 4. The $P(c)O_4$ tetrahedral isomorphisms between (a) mitridatite and (b) crandallite. The tetrahedra in (a) are those above and below $x = 1/4$ and adopt the atom labels according to Table II. The tetrahedra in (b) were drawn from atom coordinates⁸ which were inverted and translated $+3/4$ on z to facilitate comparison with (a). The crandallite cell is outlined and the inversion centers are drawn as open circles.

Δd are generally smaller than found for the more undersaturated and oversaturated oxygens. When the individual deviations are substantial for one cation (inspect O(6) and O(10)) they are compensated by the others. This analysis is extended to the water molecules of the type O_h and O_i . Here it is noted that $O_h \rightarrow O_f$ type bonds are all longer than predicted by Baur's regression analysis;²⁰ these are balanced by the Ca– O_h bonds which are all shorter than predicted.

Since there are no contradictions, an unambiguous formula can be written for mitridatite. O_a and O_b must be accepted as oxo anions (O^{2-}) and there are no "acid" phosphate groups, hence the asymmetric unit is $Ca_6(H_2O)_6[Fe^{III}_9O_6(PO_4)_3] \cdot 3H_2O$ with the three water molecules after the period participating in hydrogen bonding only.

Bond Distances and Angles. Both bond strength sum deviations from local electrostatic neutrality and shared polyhedral edges account for patterns in individual bond distance deviations from polyhedral averages. P– O_b , O_g' range from 1.49 to 1.51 Å, about 0.03 to 0.05 Å shorter than their polyhedral averages. Ca– O_b , O_g' are also considerably foreshortened, ranging from 0.12 to 0.22 Å below the averages. These are well-understood from the principles discussed above.

Owing to cation–cation repulsions across shared edges, O–O' distances associated with these edges are considerably foreshortened. Thus, in Table III, all such edges are the shortest for their polyhedra. The effect is most pronounced for the Fe–Fe' cation pairs, but is clearly evident for Fe–Ca and Ca–Ca pairs as well. The Ca atoms are arranged above and below the O_a and O_b oxygens and the $CaO_5(H_2O)_2$ polyhedra share three of their edges with the FeO_6 octahedra. These edges are identified as those which emanate from the seventh coordinating oxygen (O_a or O_b) which lies above the octahedral face (Figure 6). It is noted that the octahedral face

below the oxygen has edges which are the longest for the $CaO_5(H_2O)_2$ polyhedra. This clearly arises from the strain induced by the ${}^2_6[Fe_9O_{33}]$ octahedral sheets above and below owing to the rigid capping $P(c)O_4$ tetrahedra.

The nonamer itself is severely strained since it is a trigonal edge-sharing ring built of octahedra. Thus, the angles Fe(5)–Fe(1)–Fe(6) = 67.6 (1)°, Fe(4)–Fe(2)–Fe(9) = 67.8 (1)°, and Fe(7)–Fe(3)–Fe(8) = 69.1 (1)° are highly acute; for perfect octahedra these would each be 90°. Geometrically, it is impossible to construct the ${}^2_6[Fe_9O_{33}]$ sheet from octahedra and for this reason mitridatite is an unusual case of a complex oxide arrangement where distorted octahedra are implicit in its structure topology and geometry.

Isotypes and Derivative Structures

Two isotypes of mitridatite are known, arseniosiderite and robertsite, and their structure cell data are summarized in Table V. Arseniosiderite obtains from isomorphic replacement of (PO_4) by (AsO_4) , resulting in slightly larger cell parameters. The most pronounced dilation is along the a direction since the contribution in this direction by the larger (AsO_4) tetrahedra is not constrained by the relatively rigid ${}^2_6[Fe_9O_{33}]$ sheets. Robertsite is particularly interesting since it is the ${}^2_6[Mn^{III}_9O_{33}]$ analogue of mitridatite and we anticipate a pronounced Jahn–Teller distortion of the octahedra owing to high spin $Mn^{3+}(3d^4)$ in an octahedral oxide field. Assuming that the distortion leads to apically elongated tetragonal bipyramidal coordination, we now predict the direction of distortion in the crystal structure. In studies on pinakioleite²¹ ($Mg_2Mn^{III}O_2(BO_3)$), braunite²² ($Mn^{II}Mn^{III}_2SiO_{12}$), and bermanite¹⁷ ($Mn^{II}(H_2O)_4[Mn^{III}_2(OH)_2(PO_4)_2]$), it was noted that averages of four equatorial $Mn^{3+}-O^{2-}$ bonds range from 1.92 to 1.96 Å and the two apical $Mn^{3+}-O^{2-}$ bonds range from

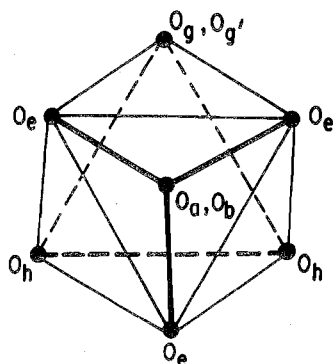


Figure 6. Labeling of the $\text{CaO}_5(\text{H}_2\text{O})_2$ oxygens according to their type. Shared edges on the polyhedron, here shown idealized, are drawn bold.

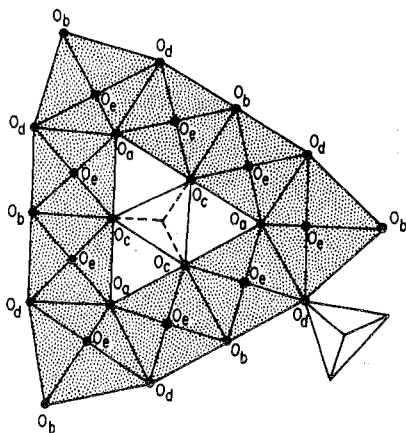


Figure 7. Labeling of the oxygens O_a through O_e about the idealized octahedral nonameric ring.

Table V also lists two compounds, betpakdalite and melkovite, which we suspect are derivative structures of the mitridatite structure type. Their morphological characters and reported structure cell parameters²³ reveal a close relationship to mitridatite. The authors proposed $\text{CaFe}^{\text{III}}_2(\text{H}_2\text{O})_{14}[\text{As}_2\text{Mo}_5\text{O}_{24}]$ for betpakdalite; we suggest it be isomorphically rearranged into a mitridatite formula, that is $\text{Ca}(\text{H}_2\text{O})_5[\square_3(\text{Mo}^{\text{VI}}_3\text{Fe}^{\text{III}})\text{O}_6(\text{FeO}_4)(\text{AsO}_4)_2(\text{OH})_{12}]\cdot 3\text{H}_2\text{O}$. Here, the three Fe(a) atoms in mitridatite are voided ($=\square$) and the

$\text{P(c)}\text{O}_4$ tetrahedra are voided, the free octahedral apices above and below bonded to $(\text{OH})^-$ groups only. Note that local electrostatic neutrality is well-preserved in this model, with $\Delta p_{\text{O}_a}, \Delta p_{\text{O}_b} \sim 0.00$, $\Delta p_{\text{O}_c} \sim +0.75$, $\Delta p_{\text{O}_d} \sim +0.25$, and $\Delta p_{\text{O}_e} \sim 0.00$. The structure, in effect, is a linkage of central girdles of the Keggin molecule by tetrahedra; the girdle and central tetrahedron have average composition $[\text{Fe}^{\text{III}}_9\text{O}_6(\text{PO}_4)_9]\cdot 3\text{H}_2\text{O}$.

Acknowledgment. It is a pleasure to thank the National Science Foundation whose support through Grant GA-40543 awarded to P.B.M. and a Materials Research Laboratory grant awarded to The University of Chicago made possible the collection of samples and the completion of the structure investigation.

Registry No. Mitridatite, $\text{Ca}_6(\text{H}_2\text{O})_6[\text{Fe}^{\text{III}}_9\text{O}_6(\text{PO}_4)_9]\cdot 3\text{H}_2\text{O}$, 61966-51-6.

Supplementary Material Available: Listing of structure factor amplitudes (46 pages). Ordering information can be found on any current masthead page.

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