Contribution from the Laboratoire de Chimie Théorique,<sup>§</sup> Université de Paris-Sud, 91405 Orsay, France, and Department of Chemistry, North Carolina State University, Raleigh, North Carolina 27695-8204

# **Semimetallic versus Semiconducting Properties of MX<sub>2</sub> Layer Compounds Containing d<sup>2</sup> Metal Ions**

Enric Canadell<sup>\*,†</sup> and Myung-Hwan Whangbo<sup>\*,†</sup>

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Electronic structures of CrNb2Se4, P-MoTe,, and **cu-Zr12** were examined by performing tight-binding band calculations. **Our** study suggests that the electronic properties of M'Nb<sub>2</sub>Se<sub>4</sub> (M' = Ti, V, Cr) are more consistent with the oxidation state of +2 for M' rather than that of  $+3$ .  $\alpha$ -ZrI<sub>2</sub> and  $\beta$ -MoTe<sub>2</sub> are semiconducting and semimetallic, respectively, despite their structural similarity and identical d-electron count on the metal  $(i.e., d^2)$ . The structural origin of this difference was also examined.

Many layered compounds contain MX<sub>2</sub> layers made up of MX<sub>6</sub> octahedra.<sup>1</sup> In MX<sub>2</sub> layers containing  $d^2$  metal ions, metal atoms are found to cluster to form zigzag chains.<sup> $2-5$ </sup> It is convenient to regard such an MX<sub>2</sub> layer as made up of  $M_2X_6$  double octahedral chains (1) having zigzag metal-metal bonds (i.e., dashed



lines in 1),<sup>6</sup> since the electronic structure of the MX<sub>2</sub> layer closely resembles that of its constituent  $M_2X_6$  chain.<sup>6</sup> For the  $M_2X_6$  chain **1** with  $X = S$  or Se, the bottom four of its six  $t_{2g}$ -block bands overlap<sup>6,7</sup> and hence become partially filled for  $d^2$  metal ions, so that  $MX_2$  layers with  $d^2$  metal ions are expected to be metals. The present work is concerned with  $d^2$  metal ions, i.e.,  $M'Nb_2Se_4$  ( $M'$ = Ti, V, Cr),<sup>3</sup>  $\beta$ -MoTe<sub>2</sub>,<sup>4</sup> and  $\alpha$ -ZrI<sub>2</sub>.<sup>5</sup> Both M'Nb<sub>2</sub>Se<sub>4</sub><sup>3a</sup> and  $\beta$ -MoTe<sub>2</sub><sup>4e</sup> are metals, as expected, but they exhibit resistivity anomalies at low temperature.<sup>3a,4c,d</sup>  $\alpha$ -ZrI<sub>2</sub> is a semiconductor with activation energy of 0.1 eV,<sup>5</sup> although it is quite similar in structure to the  $MX_2$  layers of  $M'Nb_2Se_4$  and  $\beta-MoTe_2$ . We examine the electronic properties of these systems by performing tight-binding band electronic structure calculations<sup>8</sup> on the basis of the extended Hückel method. $9$  The atomic parameters employed in our study are summarized in Table I.

### **Crystal Structure**

A perspective view of the  $M_2X_6$  double octahedral chain 1 is shown in  $2$ , where each  $MX_6$  octahedron represents a single octahedral chain of **1.** The projection view of **2** along the chain is



given **by 3,** where two chalcogen atoms indicated by a double-



<sup>+</sup> Université de Paris-Sud.<br><sup>‡</sup> North Carolina State University.

<sup>8</sup> The Laboratoire de Chimie Théorique is associated with the CNRS (UA 506) and **is** a member of the ICMO and the lPCM (Orsay, France).





*<sup>a</sup>*Contraction coefficients used in the double-{ expansion.

headed arrow are projected as one chalcogen atom. According to this projection view, an  $MX_2$  layer with  $d^2$  metal ions is represented by  $4.6$  It is such  $\overline{MX}_2$  layers that stack to form



three-dimensional lattices in M'Nb<sub>2</sub>Se<sub>4</sub> (M' = Ti, V, Cr),  $\beta$ -MoTe<sub>2</sub>, and  $\alpha$ -ZrI<sub>2</sub>. In M'Nb<sub>2</sub>Se<sub>4</sub>, the M' atoms occupy half the octahedral sites between NbSe<sub>2</sub> layers.

### **Band Electronic Structures**

**A.**  $M'Nb_2Se_4$  ( $M' = Ti$ ,  $V$ ,  $Cr$ ). In understanding the electrical properties of  $M'Nb<sub>2</sub>Se<sub>4</sub>$ , it is crucial to know the oxidation state

- Hulliger, F. **In** *Structural Chemistry* of *Layer-Type Phases;* Levy, F., Ed.; Reidel: Dordrecht, The Netherlands, 1976.
- Kadijk, F.; Huisman, R.; Jellinek, F. Acta Crystallogr. 1968, B24, 1102.<br>(a) Meerschaut, A.; Spiesser, M.; Rouxel, J.; Gorochov, O. J. Solid<br>State Chem. 1980, 31, 31. (b) Meerschaut, A.; Rouxel, J. C. R. Seances  $(3)$ *Acad. Sci., Ser. C* **1977, 277,** 163.
- (a) Brown, B. E. *Acta Crystallogr*. **1986**, 20, 268. (b) Manolikas, C.;<br>van Landuyt, J.; Amelinckx, S. *Phys. Status Solidi A* **1979**, 53, 327.<br>(c) Hughes, H. P.; Friend, R. H. J. *Phys. C* 1978, 11, L103. (d) Clarke, R.; Marseglia, E.; Hughes, H. P. *Philos. Mag. B* **1978,** *38,* 121. (e) Wilson, J. A.; Yoffe, **A.** D. *Ado. Phys.* **1969,** *18,* 193. *(f)* Vellinga, M.
- B.; de Jonge, R.; Haas, C. J. Solid State Chem. 1970, 2, 299.<br>Guthrie, D. H.; Corbett, J. D. J. Solid State Chem. 1981, 37, 256.<br>Canadell, E.; Le Beuze, A.; El Khalifa, M. A.; Chevrel, R.; Whangbo,<br>M.-H. J. Am. Chem. Soc.  $(6)$
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- berg-Helmholz formula was used to calculate the off-diagonal  $H_{ij}$  values: Ammeter, J. H.; Bürgi, H.-B.; Thibeault, J.; Hoffmann, R. *J. Am. Chem. SOC.* **1978,** *100,* 3686.



**Figure 1.** Dispersion relations of the t<sub>2g</sub>-block bands (a, b, and c) of a single NbSe<sub>2</sub> layer, where  $\Gamma = (0, 0)$ ,  $Y = (b^*/2, 0)$ ,  $M = (b^*/2, c^*/2)$ , single NbSe<sub>2</sub> layer, where  $\Gamma = (0, 0)$ ,  $Y = (b^2/2, 0)$ ,  $M = (b^2/2, c^2/2)$ , and  $Z = (0, c^2/2)$ . The Fermi levels  $e_f$  and  $e'_f$  refer to the d<sup>2</sup> and d<sup>2.5</sup> directions refer to the divisory respectively. to the intra- and the interchain directions, respectively.



**Figure 2. Hole** (a) and electron Fermi surfaces (b) associated with the **d2** electron counting **(er)** of **Figure** 1. The shaded and unshaded regions of wave vector lead to filled and unfilled band levels respectively.

of M'. The NbSe<sub>2</sub> layers have zigzag metal chains as in  $\beta$ -MoTe<sub>2</sub> and  $\alpha$ -ZrI<sub>2</sub>, so that the electron count on Nb is expected to be d2. This requires the oxidation state of *2+* for M', which seems consistent with the magnetic properties of  $M'Nb<sub>2</sub>Se<sub>4</sub>$ : For example, the effective magnetic moment of  $Cr$  in  $CrNb<sub>2</sub>Se<sub>4</sub>$  is 4.4  $\mu_{\rm B}$ ,<sup>3a</sup> which is quite close to that of Cr<sup>2+</sup> found for CrMo<sub>2</sub>S<sub>4</sub> (i.e.,  $4.6 \pm 0.1 \mu_B$ .<sup>10</sup> Figure 1 shows the dispersion relations calculated for the  $t_{2g}$ -block bands (a, b, and c) of a single NbSe<sub>2</sub> layer taken from the crystal structure of  $CrNb<sub>2</sub>Se<sub>4</sub>$ <sup>3a</sup> As described elsewhere,<sup>7</sup> bands a and c result from the metal-metal bonding and antibonding levels of zigzag metal-metal bonds, respectively, while band b originates from the metal  $x^2 - y^2$  orbitals. The latter describe 1,3-interactions in each zigzag metal chain. Band d overlapping the bottom portion of the  $t_{2g}$ -block bands is the top of the Se pblock bands. The Fermi level *ef* of Figure 1 corresponds to the d2 electron counting. The partially filled bands of Figure 1 lead to a hole and an electron Fermi surface shown in parts a and b of Figure 2, respectively, which show that the NbSe<sub>2</sub> layer is a semimetal. This conclusion is consistent with the results of the Hall coefficient measurements on  $M'Nb<sub>2</sub>Se<sub>4</sub>.<sup>3a</sup>$  The hole pockets of Figure 2 are nested by the vector  $q \approx 0.29b^*$ . Thus, an electronic instability associated with this nesting might be

- (1 1) (a) Alcock, **N.** W.; Kjekshus, **A.** *Aczu Chem. Scund.* **1965,19,79. (b)**  Wildervanck, J. C.; Jellinek, F. *J. Less-Common Mer.* **1971,** *24,* **73.**
- (12) Canadell, E.; Whangbo, M.-H. *Inorg. Chem.* 1987, 26, 3974.<br>(13) Canadell, E.; Mathey, Y.; Whangbo, M.-H. *J. Am. Chem. Soc.* 1988,
- *110,* **104. (14)** Whangbo, M.-H.; Foshee, M. **J.** *Inorg. Chem.* **1981,** *20,* **113.**
- **(15)** Summerville, R. H.; Hoffmann, R. J. *Am. Chem. SOC.* **1976, 98, 7240.**



**Figure 3.** Fermi surface associated with the  $d^{2.5}$  electron counting  $(e_0)$ of Figure 1. The shaded and unshaded regions of wave vectors lead to filled and unfilled band levels, respectively.



Figure 4. Dispersion relations of the  $t_{2g}$ -block bands calculated for (a) a single MoTe<sub>2</sub> layer and (b) the 3D  $\beta$ -MoTe<sub>2</sub> lattice.  $\Gamma = (0, 0), X = (a^*/2, 0)$  and  $Y = (0, b^*/2)$  for the MoTe<sub>2</sub> layer, and  $\Gamma = (0, 0, 0), X = (a$  $r = (a^*/2, 0, 0)$  and  $Y = (0, b^*/2, 0)$  for the 3D  $\beta$ -MoTe<sub>2</sub> lattice. The  $\Gamma \rightarrow X$  and  $\Gamma \rightarrow Y$  directions represent the inter- and the intrachain directions, respectively. The dashed line refers to the Fermi **level.** 

responsible for a weak resistivity upturn of  $CrNb<sub>2</sub>Se<sub>4</sub>$  at  $\sim$  50 K.<sup>3a</sup> However, such a resistivity upturn is absent in  $TiNb<sub>2</sub>Se<sub>4</sub>$  and  $VNb<sub>2</sub>Se<sub>4</sub>.<sup>3a</sup>$  An electronic factor responsible for this observation might be that the hole pockets of  $TiNb<sub>2</sub>Se<sub>4</sub>$  and  $VNb<sub>2</sub>Se<sub>4</sub>$  are not large enough.

The above discussion is based upon the assumption of  $d^2$  electron counting for Nb. If the M' atoms of  $M'Nb<sub>2</sub>Se<sub>4</sub>$  have the oxidation state  $+3$ , as suggested by Meerschaut et al.,<sup>3a</sup> the electron count on Nb becomes  $d^{2.5}$ . This raises the Fermi level to  $e_f$  in Figure 1, thereby making band b, half-filled. Consequently, the resulting Fermi surface, shown in Figure 3, is one-dimensional in nature, and is nested by a vector  $q = 0.5b^* + 0.5c^*$ . One may rationalize the resistivity upturn of CrNb<sub>2</sub>Se<sub>4</sub>, which occurs at 50 K,<sup>3a</sup> as a consequence of an electronic instability associated with this nesting. According to this reasoning,  $TiNb<sub>2</sub>Se<sub>4</sub>$  and  $VNb<sub>2</sub>Se<sub>4</sub>$  are expected to exhibit a similar resistivity anomaly as in  $CrNb<sub>2</sub>Se<sub>4</sub>$ , in disagreement with experiment.<sup>3a</sup> Slight differences in the  $Nb<sub>2</sub>Se<sub>4</sub>$ layer structures of M'Nb<sub>2</sub>Se<sub>4</sub> induced by the different M' atoms would have stronger effects on their electronic properties when their Fermi surfaces are given by Figure **2** rather than by Figure 3. Thus, the available resistivity data on  $TiNb<sub>2</sub>Se<sub>4</sub>$  and  $VNb<sub>2</sub>Se<sub>4</sub>$ are more consistent with the semimetallic band picture based upon a d<sup>2</sup> electron counting on Nb.

**B.**  $\beta$ -MoTe<sub>2</sub>. Due to displacive movement between MoTe<sub>2</sub> layers,  $\beta$ -MoTe<sub>2</sub> shows a resistivity anomaly at about 250 K.<sup>4b- $\bar{e}$ </sup> This suggests that the nature of the partially filled bands of  $\beta$ -MoTe<sub>2</sub> is affected by a slight change in MoTe<sub>2</sub> layers. Figure 4a shows the dispersion relations calculated for the  $t_{2a}$ -block bands of a single MoTe<sub>2</sub> layer. In general, the t<sub>2g</sub>-block bands, a, b, and c of the MoTe<sub>2</sub> layer are similar to the corresponding ones of the NbSe<sub>2</sub> layer (Figure 1). At  $\Gamma$ , the top of band  $a_2$  is close in energy to the bottom of band  $b_2$  in the MoTe<sub>2</sub> layer while this is not the case in the NbSe<sub>2</sub> layer. This is caused by the fact that the top of the Te p-block bands lies considerably higher in energy than case in the NbSe<sub>2</sub> layer. This is caused by the fact that the top<br>of the Te p-block bands lies considerably higher in energy than<br>that of the Se p-block bands. Along  $\Gamma \rightarrow Y$  of Figure 4a, bands<br>and a base of d have the s  $a_2$  and d have the same symmetry so that they mix. Band  $a_2$  has more metal d-orbital character near *Y* but more Te p-orbital character near  $\Gamma$ .

**<sup>(</sup>IO)** Chevrel, R.; Sergent, M.; Meury, J. **L.;** Quan, D. T.; Colin, *Y. J. Solid Stare Chem.* **1974.** *IO,* **260.** 



**Figure 5.** Dispersion relations of the  $t_{2g}$ -block bands calculated for a rigure 5. Dispersion relations of the  $t_{2g}$ -block bands calculated for a single Zrl<sub>2</sub> layer, where  $\Gamma = (0, 0), X = (a^*/2, 0), M = (a^*/2, b^*/2)$ <br>and  $Y = (0, b^*/2)$ . The  $\Gamma \rightarrow X$  and  $\Gamma \rightarrow Y$  directions represent the interand the intrachain directions, respectively. The dashed line refers to the Fermi level.

Figure 4b shows the  $t_{2g}$ -block bands calculated for the threedimensional (3D)  $\beta$ -MoTe<sub>2</sub> lattice. With respect to the case of a single MoTe, layer, all the band levels are doubled in  $\beta$ -MoTe, since it has two MoTe<sub>2</sub> layers per unit cell. Figure 4b shows that this band doubling does not lead to nearly degenerate bands but to substantially split ones. Namely, the t<sub>2g</sub>-block bands of  $\beta$ -MoTe<sub>2</sub> reflect appreciable interlayer Te-Te interactions. This is possible since the  $t_{2g}$ -block bands have large Te p-orbital character and since MoTe<sub>2</sub> layers interact via short Te-Te contacts (e.g., 3.86) and 3.91 **A)** smaller than the van der Waals radii sum of 4.20 **A.** With d2 metal ions, the Fermi level cuts the bands arising from the t<sub>2g</sub>-block bands  $a_2$  and  $b_1$ . It is clear from Figure 4b that this will lead to hole and electron Fermi surfaces, and hence  $\beta$ -MoTe<sub>2</sub> is a semimetal. Since a displacive movement of MoTe, layers will modify the interlayer Te-Te contact distances, the band splittings of Figure 4b will also change so that the resulting hole and electron Fermi surfaces will be slightly different. Consequently, the electrical resistivity of  $\beta$ -MoTe<sub>2</sub> should be affected by a displacive movement of MoTe<sub>2</sub> layers.

**C.**  $\alpha$ -**ZrI**<sub>2</sub>. Figure 5 shows the t<sub>2g</sub>-block bands of a single ZrI<sub>2</sub> layer. In contrast to the case of  $NbSe_2$  and  $MoTe_2$  layers, the bottom two of the  $t_{2g}$ -block bands are separated from the rest, thereby leading to a band gap. The top of the iodine p-block bands lies below the t<sub>2g</sub>-block bands, and hence are not shown in Figure 5. As in  $\beta$ -MoTe<sub>2</sub>,  $\alpha$ -ZrI<sub>2</sub> has two ZrI<sub>2</sub> layers per unit cell.<sup>5</sup> Our band calculations on the 3D  $\alpha$ -ZrI<sub>2</sub> lattice show that each band of Figure 5 splits into two, thereby reducing the band gap. It is clear from Figures I, 4a, and *5* that the presence of a band gap in  $\alpha$ -ZrI<sub>2</sub> is caused by the fact that band  $a_2$  lies below band b<sub>1</sub>. We now examine why this happens for  $\alpha$ -ZrI<sub>2</sub> but not for  $M'Nb<sub>2</sub>Se<sub>4</sub>$  and  $\beta$ -MoTe<sub>2</sub>. Shown in 5-7 are various bond angles



associated with three adjacent  $MX_6$  octahedra found in the NbSe<sub>2</sub>,

MoTe<sub>2</sub> and ZrI<sub>2</sub> layers, respectively. Clearly, the  $MX_6$  octahedra of M'Nb<sub>2</sub>Se<sub>4</sub>,  $\beta$ -MoTe<sub>2</sub>, and  $\alpha$ -ZrI<sub>2</sub> are remarkably similar in shape. This distortion of  $MX<sub>6</sub>$  octahedra could not have induced the difference in their electronic structures.

The electronegativity difference between M and X can affect the extent of orbital mixing between the two atoms. To examine how strongly our results are influenced by this factor, we calculated the band structure of the NbSe<sub>2</sub> layer using the  $H_{ii}$  (valence shell ionization potential) values of Zr and I and that of the ZrI<sub>2</sub> layer using the  $H_{ii}$  values of Nb and Se. These calculations still show that bands  $a_2$  and  $b_1$  are overlapping in the NbSe<sub>2</sub>, but are separated in the  $ZrI_2$  layer. Thus the difference in the  $H_{ii}$  values of M and **X** is not responsible for why the electronic structure  $\alpha$ -ZrI<sub>2</sub> differs from that of M'Nb<sub>2</sub>Se<sub>4</sub> or  $\beta$ -MoTe<sub>2</sub>. anic Chemistry, Vol. 29, No. 7, 1990<br>
MoTe<sub>2</sub> and ZrI<sub>2</sub> layers, respectively. Clearly, the MX<sub>6</sub> octahe<br>
of M'Nb<sub>2</sub>Se<sub>4</sub>,  $\beta$ -MOTe<sub>2</sub> and  $\alpha$ -ZrI<sub>2</sub> are remarkably similar<br>
of M'Nb<sub>2</sub>Se<sub>4</sub>,  $\beta$ -MOTe<sub>2</sub> and  $\alpha$ -ZrI<sub>2</sub>

It is noted that Figures 1, 4a, and 5 that, along the chain direction, bands  $a_2$  and  $b_1$  have different symmetries and hence overlap when band  $a_2$  is raised high enough in energy, thereby leading to a metallic situation for  $d^2$  metal systems. Bands  $a_2$  and d have the same symmetry, so that band  $a_2$  lies high in energy when the p-block band of  $X$  lies high in energy. To have bands  $a_2$  and  $b_1$  overlapping, therefore, the p-block band of X should be high in energy. The latter requires strong antibonding in intralayer  $X \cdots X$  contacts. The relevant  $X \cdots X$  distances in the NbSe<sub>2</sub>, MoTe<sub>2</sub>, and ZrI<sub>2</sub> layers are summarized in 8-10, re-



spectively. Clearly, the  $X \cdots X$  contact distances are much longer in the ZrI, layer than in the NbSe, or MoTe, layer, which is a direct consequence of the fact that the Zr-I bonds are much longer than the Nb-Se and Mo-Te bonds. In addition, iodine has more contracted orbitals than does tellurium. Consequently, the top of the iodine p-block bands lies considerably lower in energy compared with that of the tellurium or selenium p-block bands. This explains why bands  $a_2$  and  $b_1$  overlap in the NbSe<sub>2</sub> and MoTe<sub>2</sub> layers but not in the  $ZrI<sub>2</sub>$  layer.

## **Concluding Remarks**

 $\beta$ -MoTe<sub>2</sub> and  $\alpha$ -ZrI<sub>2</sub> are structurally similar in that they all contain  $M\bar{X}_2$  layers of  $d^2$  metal ions. Nevertheless,  $\beta$ -MoTe<sub>2</sub> is a semimetal while  $\alpha$ -ZrI<sub>2</sub> is a semiconductor. This difference originates from the fact that, in contrast to the case of  $\beta$ -MoTe<sub>2</sub>, the top of the p-block bands of X lies below the bottom of the metal t<sub>2g</sub>-block bands in  $\alpha$ -ZrI<sub>2</sub> due to the long intralayer I<sup>...</sup>I contact distances. Our calculations on  $\beta$ -MoTe<sub>2</sub> show that the partially filled t<sub>2s</sub>-block bands of  $\beta$ -MoTe<sub>2</sub> contain a sizable contribution from tellurium p-orbitals, so the hole and electron Fermi surfaces resulting from them are expected to be affected by a slight change in the interlayer Te-Te contact distances.

 $M'Nb<sub>2</sub>Se<sub>4</sub>$  ( $M' = Ti$ , V, Cr) phases are structurally similar to  $\beta$ -MoTe<sub>2</sub> and  $\alpha$ -ZrI<sub>2</sub>. Our calculations show that if the oxidation state of  $\mathbf{M}'$  is +2  $\mathbf{M}'\mathbf{Nb}_2\mathbf{Se}_4$  phases are two-dimensional semimetals with small hole and electron pockets. If the oxidation state of M' is  $+3$ , M'Nb<sub>2</sub>Se<sub>4</sub> phases are calculated to be one-dimensional metals. Therefore, it would be interesting to measure the resistivity anisotropy as well as the possible superlattice modulation of these compounds. comments.

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# **Comparison of the Electronic Structures of Layered Transition-Metal Trichalcogenides**  TaSe<sub>3</sub>, TaS<sub>3</sub>, and NbSe<sub>3</sub>

E. Canadell,<sup>\*,†</sup> I. E.-I. Rachidi,<sup>†</sup> J. P. Pouget,\*,<sup>‡</sup> P. Gressier,§ A. Meerschaut,§ J. Rouxel,\*,§ D. Jung, M. Evain,<sup> $\parallel$ </sup> and M.-H. Whangbo\*, $\parallel$ 

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The electronic structures of the three layered transition-metal trichalcogenides NbSe<sub>3</sub>, TaS<sub>3</sub>, and TaSe<sub>3</sub> were examined by performing tight-binding band electronic structure calculations. The Fermi surfaces of these materials were also calculated to analyze their metallic and/or charge density wave properties. In these trichalcogenides  $MX_1$  ( $M = Nb$ , Ta;  $X = S$ , Se) made up of prismatic **MX3** chains, the broken **X-X** bonds of their equilateral-like **MX,** chains and the short intra- and interlayer **X-X**  contacts are found to be crucial for the semimetallic properties of TaSe, and for the charge density wave phenomena **of** NbSe3 and TaS<sub>3</sub>. For the electronic parameters of the charge density waves in NbSe<sub>3</sub> and TaS<sub>3</sub>, a quantitative agreement is obtained between the experimental observations and the present band electronic structure calculations.

Layered transition-metal trichalcogenides  $MX_3$  (M = Nb, Ta;  $X = S$ , Se) contain layers made up of trigonal-prismatic chains.<sup>1</sup> These  $MX_3$  prismatic chains are classified as isosceles- or equilateral-like depending upon whether the oxidation state of the  $X_3$ triangle forming the base of the  $MX_6$  prism is  $(X^2 + X_2^2)$  or **3X2-,** respectively? For simplicity, isosceles- and equilateral-like prismatic chains may be referred to as I- and E-prismatic chains, respectively. Thus NbSe, and monoclinic TaS, each have four I- and two E-prismatic  $MX_3$  chains per unit cell, while TaSe<sub>3</sub> has two **I-** and two E-prismatic chains per unit cell. Consequently, it is expected that NbSe, and TaS, each have two d electrons per unit cell but TaSe<sub>3</sub> has none. In agreement with this simple electron counting, both NbSe, and TaS, are metals at room temperature. When the temperature is lowered, both undergo two different charge density wave (CDW) transitions. At the end of these two transitions,  $Ta\ddot{S}_3$  becomes a semiconductor but  $NbSe_3$ remains metallic.' The above electron counting on TaSe, suggests that TaSe, would be a semiconductor, but it is a semimetal'. Although a number of band electronic structure studies on  $NbSe<sub>3</sub><sup>3</sup>$ and  $T a S e_1^4$  have been reported, there has been no systematic study concerning how NbSe, and TaS, differ in their electronic structures and why TaSe, is semimetallic from the viewpoint of their crystal structures. In addition, Fermi surfaces have not been reported for  $TaS_3$  and  $TaSe_3$ . Therefore, we carry out tightbinding band electronic structure calculations<sup>5</sup> on NbSe<sub>3</sub>, TaS<sub>3</sub>, and  $TaSe<sub>3</sub>$  within the framework of the extended Hückel method<sup>6</sup> and discuss similarities and differences in their electronic structures. The atomic parameters employed in our study are summarized in Table I.

#### **Crystal Structures and Short X.-X Contacts**

In the layered trichalcogenide ZrTe<sub>3</sub>, composed exclusively of I-prismatic chains, short intra- and interlayer Te-Te are found to play a crucial role for its semimetallic property and resistivity anomaly.<sup>7</sup> By analogy, one might expect short  $X \cdots X$  contacts of  $MX_3$  ( $M = Nb$ , Ta;  $X = S$ , Se) to be also important in de-

<b>Table I.</b> Exponents and Parameters Used in the Calculations							
atom	orbital	$H_{ii}$ , eV	ţ,	$\zeta_2$	$c_1^a$	$c_2^{\,a}$	
Nb	5s	$-10.10$	1.90				
	5p	$-6.86$	1.85				
	4d	$-12.10$	4.08	1.64	0.6401	0.5516	
Ta	6s	$-10.10$	2.28				
	6p	$-6.86$	2.24				
	5d	$-12.10$	4.76	1.94	0.6597	0.5589	
S	3s	$-20.00$	1.817				
	3p	$-13.30$	1.817				
<b>Se</b>	4s	$-20.50$	2.44				
	4p	$-13.20$	2.07				

 $^a$  Contraction coefficients used in the double- $\zeta$  expansion.

**Table II.** Short  $X-X$  and  $X \cdots X$  Distances  $(A)$  in NbSe<sub>3</sub>, TaS<sub>3</sub>, and TaSe, Shown in **1** and **2** 

dist	NbSe <sub>1</sub>	TaS <sub>3</sub>	TaSe,
A	2.37	2.07	2.58
A'	2.50	2.11	
B	2.73	2.80	2.66
C	2.92	2.84	2.90
	3.30	3.26	3.49
E	2.92	2.92	

termining the electronic properties of  $MX_3$ . The projection view along the chain direction (i.e., the b-axis direction) of  $NbSe<sub>3</sub><sup>8</sup>$  and

- (2) Whangbo, M.-H. **In** *Crystal Chemistry and Properties of Materials with Quasi-One-Dimensional Structures;* Rouxel, J., **Ed.;** Reidel: Dordrecth, The Netherlands, 1986; p 27.
- (3) (a) Shima, N. J. Phys. Soc. Jpn. 1982, 51, 11; 1983, 52, 578. (b)<br>Bullett, D. W. J. Phys. C: Solid State Phys. 1982, 15, 3069. (c)<br>Whangbo, M.-H.; Gressier, P. Inorg. Chem. 1984, 23, 1305.
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- (4) Bullett, D. W. J. Phys. C: Solid State Phys. 1979, 12, 277.<br>(5) Whangbo, M.-H.; Hoffmann, R. J. Am. Chem. Soc. 1978, 100, 6093.<br>(6) Hoffmann, R. J. Chem. Phys. 1963, 39, 1397. A modified Wolfs-<br>berg-Helmholz formula w *Am. Chem. Soc.* 1978, *100,* 3686.

<sup>&</sup>lt;sup>+</sup> Laboratoire de Chimie Théorique, Université de Paris-Sud.<br><sup>‡</sup> Laboratoire de Physique des Solides, Université de Paris-Sud.

<sup>&</sup>lt;sup>8</sup> Université de Nantes.

<sup>&</sup>lt;sup>1</sup> North Carolina State University.

<sup>(1)</sup> Reviews: (a) Meerschaut, **A.;** Rouxel, J. **In** *Crystal Chemistry and Properties of Materials with Quasi-One-Dimensional Structures;*  Rouxel, J., Ed.; Reidel: Dordrecht, The Netherlands, 1986; p **205.** (b) Monceau, P. **In** *Electronic Properties of Inorganic Quasi-One-Dimensional Compounds;* Monceau, P., Ed.; Reidel: Dordrecht, The Netherlands, 1985; Part **11,** p 139.