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## Electronic Structure, Bonding, and Properties of $\text{CuP}_2$

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A theoretical study of the electronic structure of  $\text{CuP}_2$  is presented on the basis of molecular orbital and tight-binding band calculations based upon the extended Hückel method. We examined the electronic factors leading to ethane- and diborane-like coordination arrangements of dinuclear compounds and found the diborane-like coordination geometry of the  $d^{10}$  ions in  $\text{CuP}_2$  to be favorable on electronic grounds. The analysis of DOS and COOP curves shows that there are two important contributions to Cu–Cu bonding: delocalized bonding involving the bridging phosphorus atoms in the  $\text{Cu}_2\text{P}_2$  rings and through-space Cu(I)–Cu(I) interactions due to mixing of the occupied  $d_z$  and empty  $s$  and  $p_z$  orbitals. The electronic band structure of  $\text{CuP}_2$  has a substantial energy gap between the valence and conduction bands. The valence band is dispersive along the interlayer direction due to the coupling of the metal  $d$  orbitals through the polyphosphide sublattice.

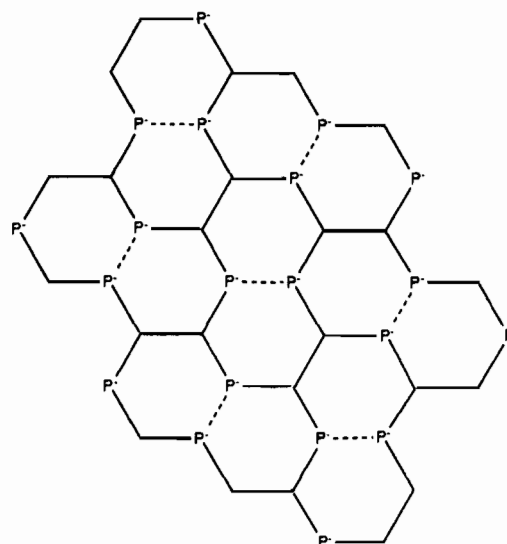
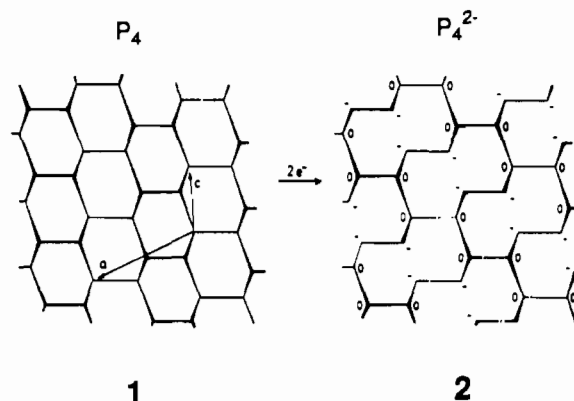
The  $\text{MP}_4$  stoichiometry is probably the most common one for phosphorus-rich transition-metal polyphosphides and includes more than 17 compounds which crystallize in 11 different structural types.<sup>1–4</sup> In these  $\text{MP}_4$  compounds, the phosphorus sublattice is formed by condensation of puckered ten-membered rings, which can be formally described as  $\text{P}_4^{2-}$ , and the transition-metal ion is octahedrally coordinated by the phosphorus atoms. The known structural types differ from one another by (a) the way in which the  $\text{P}_{10}$  rings are condensed, (b) the way in which the coordination octahedra are linked together, and (c) the existence or absence of metal–metal contacts to form either pairs or chains of metal atoms.

One of the structural types of tetraphosphides is the  $\text{CdP}_4$  structure,<sup>5–10</sup> which is found for  $\text{MgP}_4$ ,  $\text{MgAs}_4$ , and the  $\alpha$  form of  $\text{RuP}_4$  and  $\text{OsP}_4$ . The copper and silver diphosphides,  $\text{CuP}_2$  and  $\text{AgP}_2$ , have a related structure.<sup>11,12</sup> These diphosphides present a phosphorus sublattice of the  $\text{CdP}_4$  type, in which the octahedral site is occupied by a pair of metal atoms [Cu–Cu and Ag–Ag distances are 2.476 (1) and 2.816 (1) Å, respectively]. The  $\text{MP}_2$  phosphides ( $M = \text{Cu}, \text{Ag}$ )<sup>13,14</sup> and their mononuclear analogues  $\text{MP}_4$  ( $M = \text{Cd}, \text{Ru}, \text{Os}$ ) have been found to be diamagnetic and semiconducting.<sup>10,15</sup>

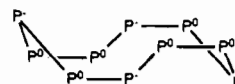
Bonds between  $d^{10}$  ions are found in a number of solid-state compounds,<sup>16</sup> and unlike their molecular analogues, no theoretical analysis of such bonding in three-dimensional structures has been reported so far. A striking structural feature of  $\text{CuP}_2$  and  $\text{AgP}_2$  is the diborane-like geometry of the M–M pairs, not a familiar arrangement in extended structures. All these prompted us to study the electronic band structure of  $\text{CuP}_2$ . In what follows we first describe the general structure of the phosphorus sublattice and how the  $\text{M}_2$  groups are connected to the phosphorus atoms. Then the electronic structures of  $\text{CuP}_2$  and related compounds are studied with the help of molecular orbital and band structure calculations of the extended Hückel type, and their bonding and electrical properties are discussed.

### Description of the Structures

Our starting point for a description of the structure of the  $\text{P}_4^{2-}$  sublattice is a  $\text{P}_4$  layer 1 formed by fusing  $\text{P}_6$  rings with boat conformation. Such layers differ slightly from those of black phosphorus,<sup>17,18</sup> in which the  $\text{P}_6$  rings have a chair conformation. Shown in 2 is a  $\text{P}_4^{2-}$  layer that results from the  $\text{P}_4$  layer 1 by adding two electrons thereby breaking one P–P bond per formula unit. This is the  $\text{P}_4^{2-}$  layer found in  $\text{MP}_4$  ( $M = \text{V}, \text{Cr}, \text{Mo}$ ).<sup>19–21</sup> Notice that the disconnected P–P bonds are related by the transition vectors  $a$  and  $2c$ . Isomeric  $\text{P}_4^{2-}$  layers can be generated with a different choice of translation vectors, schematically shown in 3,



as found for  $\text{CdP}_4$ . The  $\text{P}_4^{2-}$  layer 3 consists of fused  $\text{P}_{10}$  rings with a double boat conformation, 4, and has two kinds of phos-



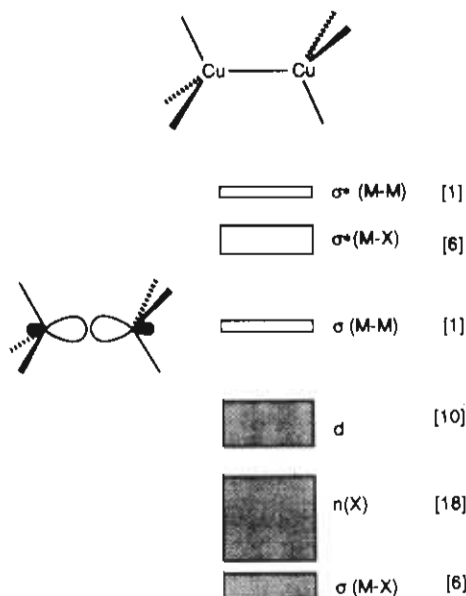
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(1) Jeitschko, W.; Flörke, U.; Möller, M. H.; Rühl, R. *Ann. Chim. Fr.* 1982, 7, 525.

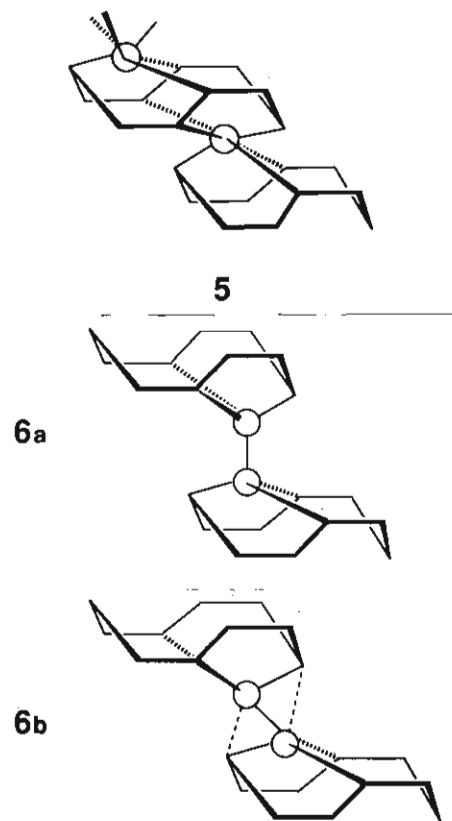


**Figure 1.** Block diagram of the molecular orbitals of  $[\text{Cu}_2\text{Br}_6]^{4-}$  with an ethane-like staggered structure. Shaded blocks corresponded to filled orbitals. The numbers in square brackets indicate the number of orbitals within each block.

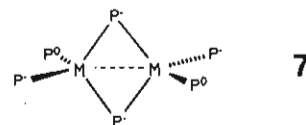
phorus atoms in each  $\text{P}_{10}$  ring: six  $\text{P}^0$  atoms shared by three rings bear one lone pair, whereas four  $\text{P}^-$  atoms shared by two rings bear two lone pairs.

The metal ions in the  $\text{CdP}_4$  structure are sandwiched between the  $\text{P}_4^{2-}$  layers 3. It is clear from 4 that one metal atom can sit at the center of each of the boats, coordinated by one  $\text{P}^0$  and two  $\text{P}^-$  atoms of a  $\text{P}_{10}$  ring in a *fac* arrangement. In order to complete the octahedral coordination of the metal ion, the next phosphorus layer 3 must be shifted as shown in 5, resulting in a monoclinic system.

If we substitute the  $\text{Cd}^{2+}$  ions in the  $\text{CdP}_4$  structure with  $\text{M}_2$  pairs [ $\text{M} = \text{Cu}(\text{I}), \text{Ag}(\text{I})$ ], an  $(\text{M}_2)\text{P}_4$  formula unit results. In principle, the coordination environment of an  $\text{M}_2$  pair can be either ethane-like, 6a, or diborane-like, 6b.  $\text{CuP}_2$  and  $\text{AgP}_2$  are found



to adopt the arrangement 6b. As shown in 7, each metal atom



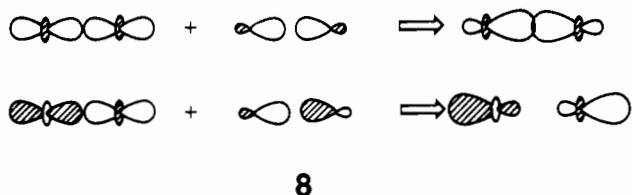
is surrounded by four phosphorus atoms in an approximately tetrahedral fashion, with the two tetrahedra sharing an edge. The bridging atoms are of  $\text{P}^-$  type. The  $\text{M}-\text{M}$  distances are 2.476 and 2.816 Å for  $\text{M} = \text{Cu}$  and  $\text{Ag}$ , respectively, comparable to the corresponding  $\text{Cu}(\text{I})-\text{Cu}(\text{I})$  bonding distances in solid-state<sup>16</sup> or in molecular complexes.<sup>22,23</sup> There are several  $\text{Cu}(\text{I})$  compounds with diborane structures in which the copper atoms are bridged by  $\text{X}$  or  $\text{XR}_2$  groups.<sup>24</sup> Only in  $[\text{Cu}(\text{PMe}_3)_2(\mu\text{-SbR}_2)]_2$  and in the  $\text{CuP}_2$  structure the bridging groups are of the  $\text{XR}_2$  or  $\text{XR}_3$  type.<sup>25</sup> In the latter case, the bridging  $\text{P}^-$  atoms are linked to two other  $\text{P}$  atoms (see 6b) and coordinated to a  $\text{Cu}$  atom as a terminal ligand and can be therefore considered as a  $\text{PR}_3$  group.

#### Cu-Cu Bonding in a Model $\text{Cu}_2\text{X}_6$ Molecule

The weak metal-metal bonding present in nonbridged dinuclear complexes of  $d^{10}$  ions has been theoretically analyzed previously.<sup>23,26-30</sup> Such bonds are due to second-order mixing of the occupied  $d_{z^2}$  and the empty  $s$  and  $p_z$  orbitals, which results in a hybridization of the  $\sigma$  combination of  $d_{z^2}$  toward, and of their  $\sigma^*$  combination away from, the interior of the metal-metal region, as depicted in 8. However, the metal atoms in  $\text{CuP}_2$  and  $\text{AgP}_2$  are bridged by phosphorus atoms, and it has been recently shown<sup>24</sup> that in dinuclear  $\text{Cu}(\text{I})$  compounds with bridging ligands the  $\text{Cu}-\text{Cu}$  interaction is a delocalized one as in diborane, with only

- (2) Hulliger, R. *Struct. Bonding* **1968**, 83.
- (3) Schnering, H.-G. v.; Hönle, W. *Chem. Rev.* **1988**, 88, 243.
- (4) Evain, M.; Brec, R.; Fiechter, S.; Tributsch, H. *J. Solid State Chem.* **1987**, 71, 40.
- (5) Krebs, H.; Müller, K.-H.; Zürn, G. *Z. Anorg. Allg. Chem.* **1956**, 15, 285.
- (6) Schnering, H. G. v.; Menge, G. *Z. Anorg. Allg. Chem.* **1976**, 422, 219.
- (7) Gibinski, T.; Cisowaska, E.; Zdanowicz, W.; Henkie, Z.; Wojakowski, A. *Krist. Tech.* **1974**, 9, 161.
- (8) Maslout, A. E.; Zanne, M.; Jeannot, F.; Gleitzer, C. *J. Solid State Chem.* **1975**, 14, 85.
- (9) Gerardin, R.; Aubry, J.; Courtois, A.; Protas, J. *Acta Crystallogr., Sect. B: Struct. Crystallogr. Cryst. Chem.* **1977**, B33, 2091.
- (10) Flörke, U.; Jeitschko, W. *J. Less-Common Met.* **1982**, 86, 247.
- (11) Olofsson, O. *Acta Chem. Scand.* **1965**, 19, 229.
- (12) Möller, M. H.; Jeitschko, W. *Z. Anorg. Allg. Chem.* **1982**, 491, 225.
- (13) Odile, J. P.; Soled, S.; Castro, C., A.; Wold, A. *Inorg. Chem.* **1978**, 17, 283.
- (14) (a) Ugai, Y. A.; Pshestanchik, V. R.; Anokhin, V. Z.; Gukov, O. Y. *Izv. Akad. Nauk. SSSR, Neorg. Mater.* **1974**, 10, 405. (b) Juza, R.; Bär, K. *Z. Anorg. Allg. Chem.* **1956**, 283, 230. (c) Goryunova, N. A.; Orlov, V. M.; Sokolova, V. I.; Shpenkov, G. P.; Tsvetkova, E. V. *Phys. Status Solidi* **1968**, 25, 513. (d) Haraldsen, H. *Z. Anorg. Allg. Chem.* **1939**, 240, 337.
- (15) Zdanowicz, W.; Wojakowski, A. *Phys. Status Solidi* **1966**, 16, K129.
- (16) Jansen, M. *Angew. Chem., Int. Ed. Engl.* **1987**, 26, 1098.
- (17) Brown, A.; Rundqvist, S. *Acta Crystallogr.* **1965**, 19, 684.
- (18) Burdett, J. K.; McLarnan, T. *J. Chem. Phys.* **1981**, 75, 5764.
- (19) Jeitschko, W.; Flörke, M.; Scholz, M. *J. Solid State Chem.* **1984**, 52, 320.
- (20) Jeitschko, W.; Donohue, P. C. *Acta Crystallogr., Sect. B: Struct. Crystallogr. Cryst. Chem.* **1972**, B28, 1893.
- (21) Alvarez, S.; Fontcuberta, J.; Whangbo, M.-H. *Inorg. Chem.* **1988**, 27, 2702.

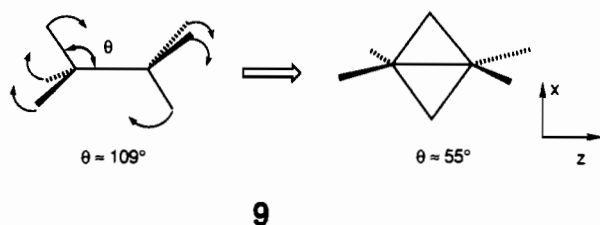
- (22) Camus, A.; Marisch, N.; Nardin, G.; Randaccio, L. *Inorg. Chim. Acta* **1977**, 23, 131.
- (23) Mehrotra, P. K.; Hoffmann, R. *Inorg. Chem.* **1978**, 17, 2187.
- (24) Alemany, P.; Alvarez, S. To be submitted for publication.
- (25) Cowley, A. H.; Jones, R. A.; Nunn, C. M.; Westmoreland, D. L. *Angew. Chem., Int. Ed. Engl.* **1989**, 28, 1019.
- (26) Jiang, Y.; Alvarez, S.; Hoffmann, R. *Inorg. Chem.* **1985**, 24, 749.
- (27) Komiya, S.; Albright, T. A.; Hoffmann, R.; Kochi, J. K. *J. Am. Chem. Soc.* **1977**, 99, 8440.
- (28) Dedieu, A.; Hoffmann, R. *J. Am. Chem. Soc.* **1978**, 100, 2074.
- (29) Mingos, D. M. P. *Proc. R. Soc. London, Ser. A* **1982**, A308, 75.
- (30) Evans, D. G.; Mingos, D. M. P. *J. Organomet. Chem.* **1982**, 232, 171.



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a small contribution from the  $s + p_z + d_{z^2}$  mixing. On the other hand, it would be interesting to see how the electronic band structure of such compounds correlates with the molecular orbital description of analogous isolated molecules. Therefore, we study first the local electronic structure and bonding of  $\text{Cu}_2\text{X}_6$  models, and then look at the band structure of  $\text{CuP}_2$ .

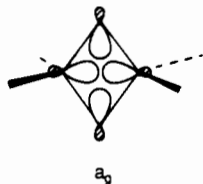
Let us consider a hypothetical  $[\text{Cu}_2\text{Br}_6]^{4-}$  ion in ethane-like (staggered,  $D_{3d}$  point group) and diborane-like (7,  $D_{2h}$  point group) structures and their interconversion via the geometrical rearrangement 9. The molecular orbitals of the staggered compound



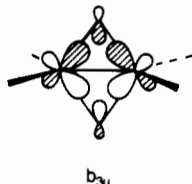
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can be described from those of two pyramidal  $\text{CuX}_3$  fragments, as schematically presented in Figure 1. The lowest occupied orbitals are those of  $\sigma_{\text{Cu-X}}$  character. Then come the "lone-pair" orbitals of the X atoms. At higher energy one finds the combinations of the Cu d orbitals; since they are all occupied for Cu(I), no contribution to Cu-Cu bonding results unless second-order effects are considered (see refs 23 and 26-30 for a detailed discussion on this subject). The lowest empty orbital of each  $\text{CuX}_3$  fragment is a high-energy  $sp^3$  hybrid, and the LUMO of  $[\text{Cu}_2\text{Br}_6]^{4-}$  is therefore the bonding combination of such hybrids. With  $\sigma_{\text{Cu-Cu}}$  empty, the Cu-Cu overlap population is 0.089, comparable to that found for a  $d^{10}$ - $d^{10}$  dinuclear compound (0.091) with a similar bond length (2.451 Å).<sup>31</sup>

Upon rearrangement of the ligands as in 9, the LUMO is strongly destabilized, as the ligands moving toward bridging positions overlap with two instead of one copper atom (Figure 2, top). Since this orbital is metal-ligand antibonding, its bonding counterpart is stabilized. Therefore, for a Cu(I) compound, with the electron count shown in Figure 1, the diborane-like structure is expected to be more stable (Figure 2, bottom), in agreement with the local structure experimentally found for  $\text{CuP}_2$  and  $\text{AgP}_2$ . Hence, the diborane-like coordination geometry of the  $d^{10}$  ions in  $\text{CuP}_2$  is electronically favored. In fact,  $\text{M}_2\text{X}_2$  diamonds of  $d^{10}$  metal ions are not uncommon, showing a wide range of M-M distances.<sup>24</sup> In  $d^{10}$  complexes with diborane-like structure, the delocalized bonding<sup>24,32</sup> is associated with the two occupied molecular orbitals  $a_g$  and  $b_{3u}$  shown in 10 and 11.

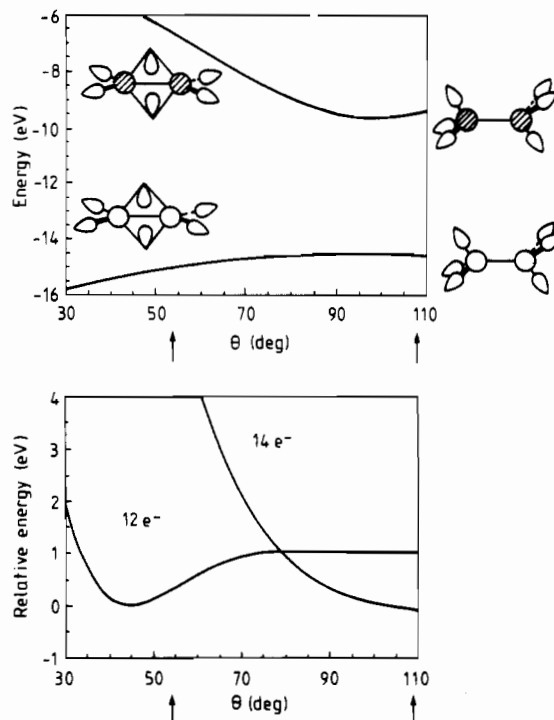


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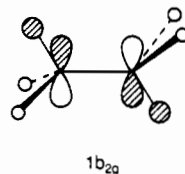
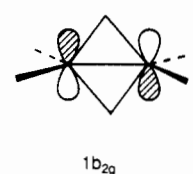
If one more electron per metal atom is added, as in Cu(0) or Zn(I), the LUMO becomes occupied. A true metal-metal bond is formed (Zn-Zn overlap population for  $\text{ZnBr}_6^{4-}$  jumps to 0.40), and the ethane structure is expected to be more stable (Figure



**Figure 2.** Top: Simplified Walsh diagram showing the energy variation of the HOMO and LUMO of  $[\text{Cu}_2\text{Br}_6]^{4-}$  during the diborane ( $D_{2h}$ )  $\rightarrow$  ethane ( $D_{3d}$ ) distortion. Contributions from the p orbitals of Cu are omitted in the representation of the MO's for simplicity. Bottom: Energy variation for  $[\text{Cu}_2\text{Br}_6]^{4-}$  (12 electrons) and the hypothetical 14-electron species isoelectronic with  $[\text{Zn}_2\text{Br}_6]^{4-}$  for the same transformation. The arrow at  $110^\circ$  indicates the ethane-like structure, and the one at  $54^\circ$  the diborane-like structure.

2). This structure is found<sup>33</sup> in the isoelectronic anion  $\text{Sn}_2\text{P}_6^{12-}$  present in  $\text{Ba}_6\text{Sn}_2\text{P}_6$ . It has also been reported for the monoclinic black form of  $\text{ZnP}_2$ , in which half of the Zn atoms are Zn(I)-Zn(I) pairs in  $\text{Zn}_2\text{P}_6$  units with the staggered ethane structure.<sup>34</sup> Although Fleet and Mowles<sup>35</sup> have reexamined the structure of  $\text{ZnP}_2$  and found it to be isostructural with  $\text{ZnAs}_2$ , the possibility of Zn(I)-Zn(I) bonds is theoretically sound.

Provided that the ligands are two-electron donors and the filled d orbitals are disregarded, the number of valence electrons in  $[\text{Cu}_2\text{X}_6]^{4-}$  and  $[\text{Zn}_2\text{X}_6]^{4-}$  (12 and 14, respectively) are the same as in  $\text{B}_2\text{H}_6$  and  $\text{C}_2\text{H}_6$ . Thus, it is not surprising to find that the geometry preference is similar in both pairs of compounds. A detailed discussion of the orbital control of the diborane-ethane transformation can be found in the literature.<sup>36,37</sup> Comparison of these works with our discussion shows that the geometry preference is the same in both cases, but the orbital explanation is somewhat different. In  $\text{A}_2\text{H}_6$  (A = C, B) the geometrical preference can be ascribed to the  $1b_{2g}$  orbital, since it is A-H bonding and occupied in ethane but A-H nonbonding and empty in diborane (12). Namely, an additional bonding orbital is created

1b<sub>2g</sub>1b<sub>2g</sub>

12

(33) Eisenmann, B.; Jordan, H.; Schäfer, H. *Z. Naturforsch. B: Anorg. Chem. Org. Chem.* **1983**, *38*, 404.

(34) Hegyi, I. J.; Laebner, E. E.; Poor, E. W.; White, J. G. *J. Phys. Chem. Solids* **1963**, *24*, 333.

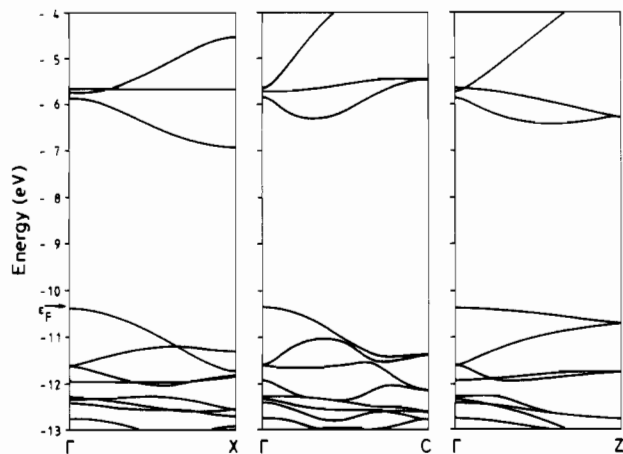
(35) Fleet, M. E.; Mowles, T. A. *Acta Crystallogr.* **1984**, *C40*, 1778.

(36) Gimarc, B. M. *Molecular Structure and Bonding*; Academic Press: New York, 1979.

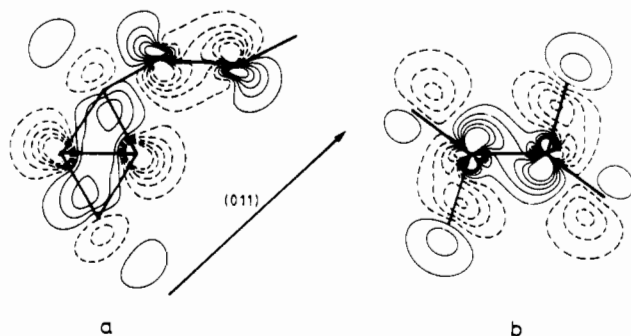
(37) Hoffmann, R.; Williams, J. E., Jr. *Helv. Chim. Acta* **1972**, *55*, 67.

(31) Brown, I. D.; Dunitz, J. D. *Acta Crystallogr.* **1961**, *14*, 480.

(32) Summerville, R. H.; Hoffmann, R. *J. Am. Chem. Soc.* **1976**, *98*, 7240.



**Figure 3.** Dispersion relationships for  $\text{CuP}_2$  along the most relevant symmetry lines of the Brillouin zone (13).

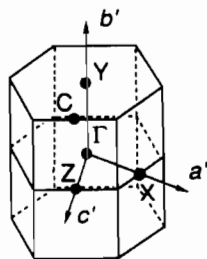


**Figure 4.** Contour diagrams for the highest occupied band at the  $\Gamma$  point: (a) projection showing the connection of the relevant fragment orbital of a  $\text{Cu}_2\text{P}_6$  unit in the (011) direction; (b) projection showing the connectivity along the  $a$  (interlayer) direction.

in ethane to make room for the two extra electrons. In the  $\text{M}_2\text{X}_6$  compounds, however, the  $1b_{2g}$  orbital is mostly localized on the X atoms due to electronegativity reasons, thus remaining occupied for both structures. The geometrical preference is related to the conversion of localized M-X interactions into a stronger, delocalized  $\text{M}_2\text{X}_2$  interaction (Figure 2, top).

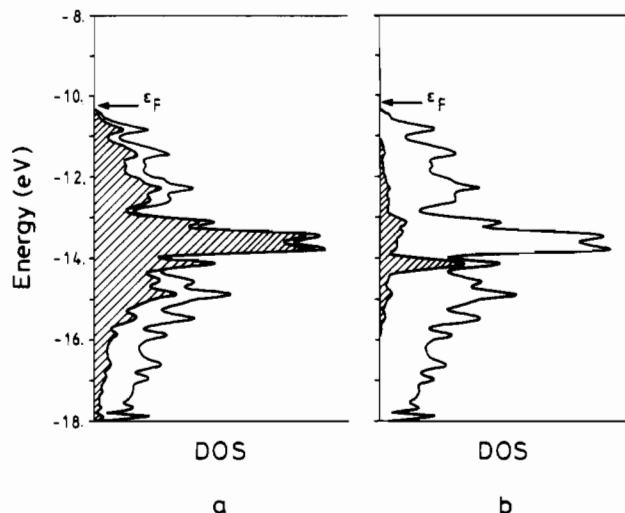
#### Electronic Band Structure of $\text{CuP}_2$

Tight-binding electronic band structure calculations of the extended Hückel type were carried out on  $\text{CuP}_2$  using the geometry of the experimental structure (see Appendix for computational details). Dispersion relations along several symmetry lines of the Brillouin zone 13 (BZ) are shown in Figure 3. All bands lying



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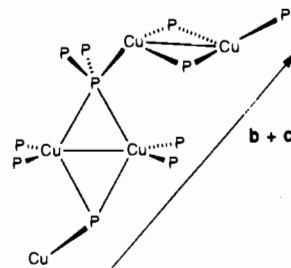
below  $-10$  eV are filled, and the empty ones are separated by an indirect band gap of  $\sim 3.5$  eV. The valence band has its highest energy at the  $\Gamma$  point and goes down in all directions of the BZ. This band is dispersive not only along  $\Gamma\text{Z}$  and  $\Gamma\text{C}$ , which correspond to the interactions within a layer in the real structure, but also along the  $\Gamma\text{X}$  line of the BZ, corresponding to the interlayer direction  $a$  in real space. The dispersive nature of this band would lead to a good conductivity of holes<sup>38</sup> created through any of three



**Figure 5.** Calculated density of states for  $\text{CuP}_2$ . The shaded areas correspond to (a) the total contribution of the Cu atomic orbitals and (b) the contribution of the  $d_{z^2}$  orbitals of one of the two  $\text{Cu}_2$  pairs in the unit cell.

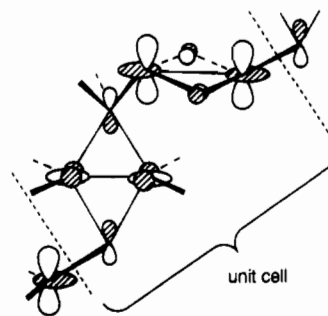
mechanisms: thermal activation, radiative activation, or partial oxidation. While p-type semiconductivity<sup>13</sup> has been observed for  $\text{CuP}_2$ , photoconductivity or partial oxidation have not been reported so far.

To understand the dispersive nature of the highest occupied band, one must analyze its orbital composition. In Figure 3 the highest occupied crystal orbital occurs at the  $\Gamma$  point of the BZ. Within each layer ( $bc$  plane), the  $\text{Cu}_2\text{P}_6$  units are connected as shown in 14. One of the bridging P atoms of a  $\text{Cu}_2\text{P}_2$  diamond



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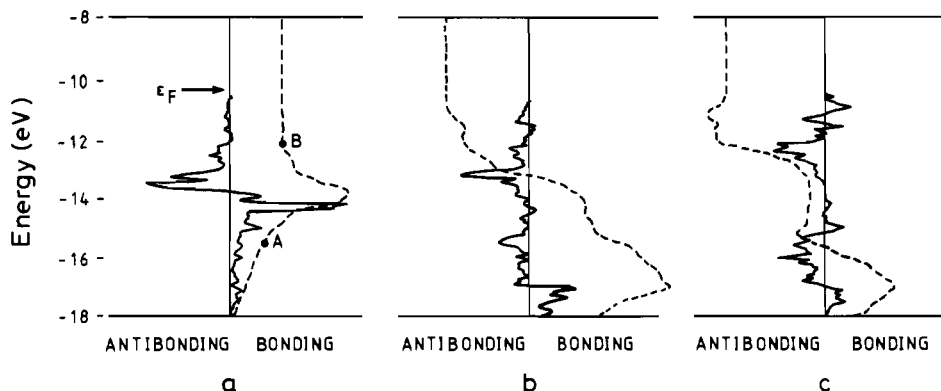
is also coordinated as a terminal ligand to a copper atom of the next diamond in the (011) direction, the planes of both diamonds being approximately perpendicular to each other. Hence, each P<sup>-</sup> atom, linked to two phosphorus atoms, is used as a terminal ligand to one copper atom, formally contributing one electron pair to the bonding in the diborane-like  $\text{Cu}_2\text{P}_2$  unit. The relevant fragment orbital of a  $\text{Cu}_2\text{P}_6$  unit, formally a nonbonding orbital, is shown in Figure 4a as a contour diagram. The uppermost filled band is built up from the antibonding combination of such fragment orbitals (Figure 4a) from the two diamonds in the unit cell, as schematically shown in 15. At the  $\Gamma$  point, the combi-



15

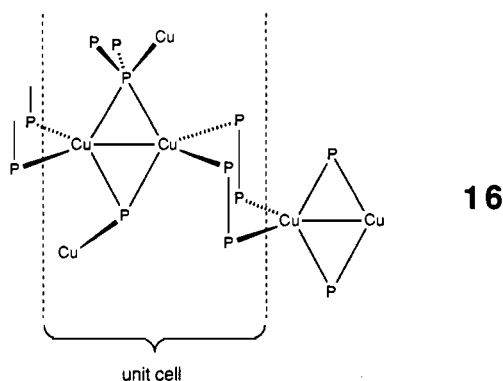
nation of nearest-neighbor orbitals 15 has Cu-P antibonding

(38) Cox, P. A. *The Electronic Structure and Chemistry of Solids*; Oxford University Press: Oxford, England, 1987; p 97.

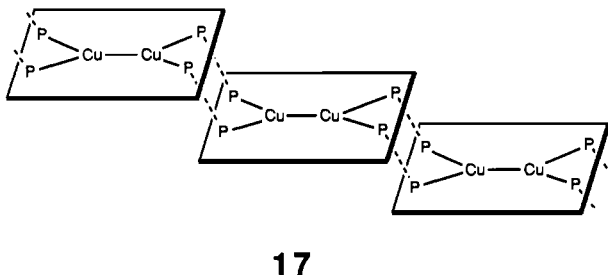


**Figure 6.** COOP curves for the interaction between Cu atoms (a), Cu s orbitals (b), and bridging phosphorus  $p_x$  orbitals (c). The integrated COOPs are represented by the dashed lines, the full scale corresponding to the values 0.22, 0.02, and 0.02 for curves a, b, and c, respectively. Points A and B in (a) indicate the integrated Cu–Cu overlap population before and after filling the  $d_{z^2}$  band, respectively.

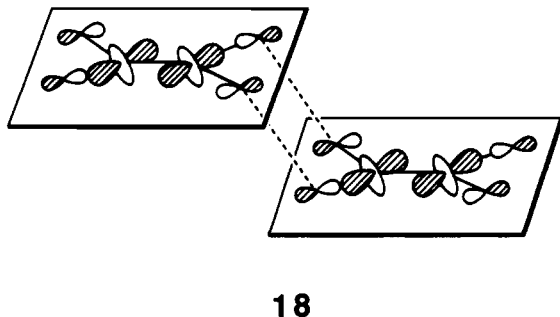
character, so that the band orbital at  $\Gamma$  is high in energy. As the phase is changed on going from  $\Gamma$  to C, the intercell antibonding character is gradually changed to bonding and the band levels become more stable. Similarly, the Cu<sub>2</sub>P<sub>2</sub> diamonds are connected along the  $a$  direction (interlayer direction) as shown in 16 or, more



schematically, in 17, where the phosphorus atoms of the diamond



have been omitted for clarity. The fragment orbital (Figure 4b) is repeated in-phase along  $a$ , as in 18, clearly bearing phospho-



rus–phosphorus  $\pi$ -antibonding character. The dispersion of the valence band along the interlayer direction is due to through-bond coupling of the metal d orbitals (formally one of the nonbonding orbitals of the e set in a tetrahedral ligand field of phosphorus atoms). Important participation of the phosphorus atoms in the

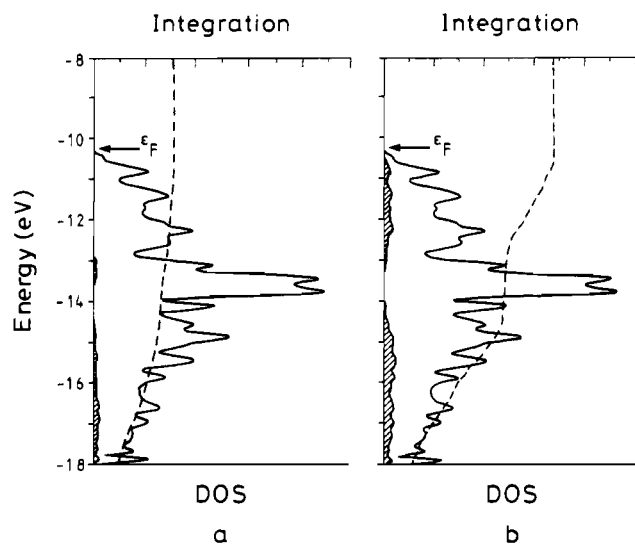
highest occupied levels has already been proposed, on the basis of X-ray emission spectra.<sup>39–42</sup>

The calculated density of states (DOS) is presented in Figure 5, together with the total contribution of the Cu atomic orbitals (shaded area in Figure 5a) and that of  $d_{z^2}$  of one of the Cu<sub>2</sub> pairs in the unit cell (shaded area in Figure 5b). In the DOS, a large gap ( $\sim 3.5$  eV) exists, in qualitative agreement with the semiconducting nature of CuP<sub>2</sub> and AgP<sub>2</sub>. According to the projection of the Cu levels in the DOS plot (Figure 5a), the levels below the Fermi level ( $\epsilon_F$ ) are mostly centered in the copper atoms, although significant contributions from phosphorus atoms exist near  $\epsilon_F$ , in agreement with both X-ray emission and photoelectron spectra.<sup>39–42</sup> Also the levels above  $\epsilon_F$  (not shown in Figure 5) are mainly copper-centered.

The COOP curve (COOP stands for crystal orbital overlap population<sup>43–45</sup>) for the Cu–Cu bond (Figure 6a) shows both bonding and antibonding contributions below the Fermi level, in the region of the d orbitals, but the integrated Cu–Cu overlap population remains positive. Thus there is some Cu–Cu bonding, and the calculated overlap population (0.085) is quite similar to that found for unsupported dinuclear complexes with clearly established  $d^{10}$ – $d^{10}$  interaction<sup>23,26–30</sup> (0.091 for the triazenido compound discussed above<sup>31</sup>). To examine if the same bonding scheme (8) applies to CuP<sub>2</sub>, we repeated the band calculations excluding the copper d orbitals. The calculated Cu–Cu overlap population turns out to be roughly reduced to half (0.048), which indicates that both the delocalized diborane-like interaction and the  $s + p_z + d_{z^2}$  mixing contribute to the Cu–Cu bonding. This result is consistent with the recent finding that in Cu<sub>2</sub>X<sub>2</sub> diamonds the importance of the  $d^{10}$ – $d^{10}$  bonding increases with decreasing Cu–Cu distances across the ring.<sup>24</sup> Since the coexistence of both types of bonding interaction in the solid state has not been studied previously, it is interesting to go through a more detailed analysis of the DOS and COOP curves.

Let us try first to identify the mixing of s,  $p_z$ , and  $d_{z^2}$  orbitals characteristic of unsupported bonding in dinuclear compounds of  $d^{10}$  ions. The contribution of the  $d_{z^2}$  orbitals to the band levels is seen in Figure 5 to be spread between  $-16$  and  $-11$  eV, with the major components at ca.  $-14$  and  $-13$  eV. These levels are built up from  $\sigma$ , Cu–Cu bonding (up to  $\sim -13.8$  eV), or  $\sigma^*$  orbitals,

- (39) Nefedov, V. I.; Salyn, Y. V.; Domashevskaya, E. P.; Ugai, Y. A.; Terekhov, V. A. *J. Electron Spectrosc. Rel. Phenom.* **1975**, *6*, 231.
- (40) Domashevskaya, E. P.; Terekhov, V. A.; Marshakova, L. N.; Ugai, Y. A. *Izv. Akad. Nauk. SSSR, Ser. Fiz.* **1974**, *38*, 567.
- (41) Domashevskaya, E. P.; Nefedov, V. I.; Salyn, Y. V.; Sergushin, N. P.; Terekhov, V. A.; Marshakova, L. N.; Ugai, Y. A. *Izv. Akad. Nauk. SSSR, Ser. Fiz.* **1976**, *40*, 389.
- (42) Domashevskaya, E. P.; Terekhov, V. A.; Ugai, Y. A.; Nefedov, V. I.; Sergushin, N. P.; Dolenko, G. N. *Fiz. Tverd. Tela (Leningrad)* **1977**, *19*, 3610.
- (43) Hughbanks, T.; Hoffmann, R. *J. Am. Chem. Soc.* **1983**, *105*, 3528.
- (44) Wijeyasekera, S. D.; Hoffmann, R. *Organometallics* **1984**, *3*, 949.
- (45) Hoffmann, R. *Solids and Surfaces: A Chemist's View of Bonding in Extended Structures*; VCH Publishers: New York, 1988.



**Figure 7.** Calculated density of states for  $\text{CuP}_2$ . The shaded areas correspond (a) to the contribution of the s orbitals of Cu and (b) to the contribution of the  $p_y$  orbitals of the bridging phosphorus atoms. The integrated density of states for both projections is represented as a dashed line, the full scale corresponding to 100%.

**Table I.** Atomic Parameters for Extended Hückel Calculations<sup>a</sup>

atom	orbital	$H_{ii}$	$\zeta_{i1} (c_1)$	$\zeta_{i2} (c_2)$	ref
Cu	4s	-11.4	2.20		50
	4p	-6.06	2.20		
	3d	-14.0	5.95 (0.5933)	2.30 (0.5744)	
P	3s	-18.6	1.75		32
	3p	-14.0	1.30		
Br	4s	-22.07	2.588		51
	4p	-13.10	2.131		

<sup>a</sup>  $H_{ii}$ 's are the orbital ionization energies,  $\zeta_{ij}$ 's the Slater exponents, and  $c_j$ 's the coefficients in the double- $\zeta$  expansion of the d orbitals.

as seen in the COOP curve (Figure 6a). What is important to notice is that the Cu–Cu overlap population shows a net increase after filling both the  $\sigma$  and  $\sigma^*$  levels (cf. points A and B in Figure 6a). In other words, there is more Cu–Cu bonding character in the  $\sigma$ -band levels than antibonding character in the  $\sigma^*$  ones, a result which can be only explained by taking into account the  $s + p_z + d_{z^2}$  mixing typical of  $d^{10}$ – $d^{10}$  bonding interactions.

The delocalized bonding orbitals of the  $\text{M}_2\text{X}_2$  diamond (**10**, **11**) are found in the band levels below  $-16$  eV. One finds DOS contributions from the phosphorus  $p_y$  and the copper s and  $p_z$

orbitals but little d contributions in this energy region (Figure 7). According to the corresponding COOP curves (Figure 6b,c), these levels are Cu–Cu and Cu-bridging P bonding, while the lowest ones (below  $-17$  eV) are slightly P–P bonding and the upper ones (between  $-14$  and  $-17$  eV) are P–P antibonding, as expected for **10** and **11**, respectively. In fact, the wave function at the center of the Brillouin zone ( $\Gamma$  point) with an energy of  $-18.09$  eV is formed by the combinations of  $a_g$  orbitals (**10**), and those at  $-15.72$  and  $-15.49$  eV at the same point are built up from  $b_{3u}$  orbitals (**11**).

In summary, both molecular orbital and band structure calculations indicate that the bonding in the  $\text{M}_2\text{X}_2$  diamonds of  $\text{CuP}_2$  and  $\text{AgP}_2$  presents the features of delocalized bonding typical of diborane as well as the  $d^{10}$ – $d^{10}$  interactions characteristic of unsupported dinuclear Au(I) and Cu(I) complexes. The electrical properties of such compounds are predicted to be isotropic and are related to M–M nonbonding d orbitals coupled through  $\text{P}_2$  bridges.

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#### Appendix: Computational Details

The qualitative theoretical discussions in this paper are based on molecular orbital<sup>46</sup> and tight-binding band calculations<sup>47,48</sup> of the extended Hückel type with modified Wolfsberg–Helmholz formula,<sup>49</sup> using the atomic parameters shown in Table I. MO calculations were carried out on the model compound  $[\text{Cu}_2\text{Br}_6]^{4-}$ , using the following bond distances: Cu–Br =  $2.30$  Å; Cu–Cu =  $2.48$  Å; Br–Cu–Br angles =  $109^\circ$ . Average properties of  $\text{CuP}_2$  were calculated using a set of 48  $k$  points chosen according to the geometrical method of Ramírez and Böhm.<sup>52</sup>

**Registry No.**  $\text{CuP}_2$ , 12019-11-3.

- (46) Hoffmann, R. *J. Chem. Phys.* **1963**, *39*, 1397. Hoffmann, R.; Lipscomb, W. N. *J. Chem. Phys.* **1962**, *36*, 2179, 2872, 3489.  
 (47) Whangbo, M.-H.; Hoffmann, R. *J. Am. Chem. Soc.* **1978**, *100*, 6093.  
 (48) Whangbo, M.-H.; Hoffmann, R.; Woodward, R. B. *Proc. R. Soc. London, Ser. A* **1979**, *366*, 23.  
 (49) Ammeter, J. H.; Bürgi, H.-B.; Thibeault, J. C.; Hoffmann, R. *J. Am. Chem. Soc.* **1978**, *100*, 3686.  
 (50) Hay, P. J.; Thibeault, J. C.; Hoffmann, R. *J. Am. Chem. Soc.* **1975**, *97*, 4884.  
 (51) Alvarez, S.; Mota, F.; Novoa, J. *J. Am. Chem. Soc.* **1987**, *109*, 6586.  
 (52) Ramírez, R.; Böhm, M. C. *Int. J. Quantum Chem.* **1988**, *34*, 571. Ramírez, R.; Böhm, M. C. *Int. J. Quantum Chem.* **1986**, *30*, 391.