# Theoretical Ab Initio Study of Neutral and Charged $B_3H_n$ (n = 3-9) Species. Importance of Aromaticity in Determining the Structural Preferences

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The geometries and stabilization energies (SE) of  $B_3H_n$  molecules and ions were computed *ab initio* at MP2-(FULL)/6-31+G\* + ZPE(HF/6-31+G\*). QCISD(T)/6-311+G\*\*//MP2(FULL)/6-31+G\* (QCI) single point energies and MP2(FC)/6-31+G\* analytical frequencies also were calculated for some of these species. The lowest energy isomers of the electron and hydrogen deficient boron hydrides  $B_3H_3$ ,  $B_3H_4^+$ ,  $B_3H_4^-$ ,  $B_3H_5$ , and  $B_3H_6^+$  have the greatest aromatic stabilization. The aromatic SEs of  $B_3H_4^-$ ,  $B_3H_5$ ,  $B_3H_6^+$ ,  $B_3H_3^{-2}$ , and  $B_3H_3L_2$ , estimated from appropriate isodesmic equations, approach the large value of the  $2\pi$ -electron cyclopropenium ion. The relative energies and even the character of  $B_3H_n$  stationary points are influenced strongly by electron correlation. The BB distances vary considerably and depend on the bonding character as well as nonbonded repulsions. The isoelectronic and isostructural analogies between boron and carbon species guide searches for the new boron hydride isomers.

# Introduction

The considerable current interest in three-membered boron rings is documented by numerous experimental<sup>1,2</sup> and theoretical<sup>2r,3-13</sup> papers. The three-boron cyclic systems are implicated in the mechanism of diborane pyrolysis.<sup>1,8e</sup> It is possible that besides  $B_3H_7$  and  $B_3H_9$  other three-membered boron intermediates also may be involved in the reaction of BH<sub>3</sub> with B<sub>2</sub>H<sub>6</sub>. In this regard, note the novel mechanism proposed recently for the formation of H<sub>2</sub>BNH<sub>2</sub> from B<sub>2</sub>H<sub>6</sub> and NH<sub>3</sub>.<sup>13e</sup> B<sub>3</sub>H<sub>4</sub><sup>+</sup> and B<sub>3</sub>H<sub>6</sub><sup>+</sup> cations were reported in electron impact mass-spectrometric studies on B<sub>4</sub>H<sub>8</sub>CO.<sup>2g</sup>

This *ab initio* study of  $B_3H_3$  (1),<sup>3</sup>  $B_3H_4^+$  (2),  $B_3H_4^-$  (3),<sup>3</sup>  $B_3H_5$  (4),<sup>3,4</sup>  $B_3H_6^+$  (5),<sup>4</sup>  $B_3H_6^-$  (6),<sup>3</sup>  $B_3H_7$  (7),<sup>3,5-8</sup>  $B_3H_8^+$  (8),

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 $B_3H_8^-$  (9),<sup>5,9,10</sup>  $B_3H_9$  (10),<sup>4,5,8,11,12</sup>  $B_3H_3^{-2}$  (11),  $B_3H_3Li^-$  (12), and  $B_3H_3Li_2$  (13) summarizes and extends earlier investigations.<sup>3-13</sup> We demonstrate that the global minima of 1-5, as well as the dianion 11 and its lithium complexes 12 and 13, benefit from aromatic (cyclic 3-center- $2\pi$ -electron) delocalization.

Hückel  $\pi$  aromaticity (4*n* + 2 electrons) is recognized to be largest per atom in three-membered rings.<sup>14,15</sup> The stabilization energy (SE) of the  $D_{3h}$  cyclopropenium cation, **14** (as defined by eq 1), is 64.1 kcal/mol.<sup>14c,15</sup> The aromatic (cyclic) stabiliza-

$$\underbrace{\bigoplus_{C_3H_3^+(14)}}_{C_3H_5^+} + \underbrace{\bigoplus_{C_3H_6}}_{C_3H_4} + \underbrace{\bigoplus_{C_3H_5^+}}_{C_3H_5^+}$$
(1)

 $\Delta E = 64.1 \text{ kcal/mol at MP2/6-31+G}^{*} + ZPE(HF/6-31+G^{*})^{14c}$ 

$$\underbrace{\bigcirc}_{C_3H_3^+(14)} + \swarrow_{C_3H_6} \implies \underbrace{\frown}_{C_3H_5^+} + \underbrace{\frown}_{C_3H_4}$$
(2)

 $\Delta E = 35.7 \text{ kcal/mol} \text{ at MP2/6-31+G}^{*} + ZPE(HF/6-31+G^{*})^{14c}$ 

$$\begin{array}{c} H \\ B \\ HC \\ HC \\ BC_{2}H_{3} \end{array} + \begin{array}{c} \bigcirc \\ BH_{3} \\ BC_{2}H_{6}^{-} \end{array} \Longrightarrow \begin{array}{c} H \\ BC_{2}H_{5} \end{array} + \begin{array}{c} H \\ B \\ H \\ BC_{2}H_{4}^{-} \end{array}$$
(3)

 $\Delta E \approx 20.8 \text{ kcal/mol at MP2/6-31+G}^{*} + ZPE(HF/6-31+G^{*})^{14c}$ 



 $\Delta E \approx 17.8 \text{ kcal/mol at MP2/6-31+G}^{*} + ZPE(HF/6-31+G^{*})^{14c}$ 

tion energy (ASE) may be obtained from eq 2, which employs the allyl cation as the reference species.<sup>14c</sup> Similarly defined ASEs (at MP2/6-31+G\* + ZPE(HF/6-31+G\*) of  $C_{2\nu}$  borirene<sup>21-n,13f-i,15</sup> (eq 3) and of the  $C_{2\nu}$  diboriranyl anion<sup>20,2p</sup> (eq 4) are about half of the value for **14**.<sup>14c</sup>

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How does aromaticity influence the structures and energies of three-boron hydrides? In recent *ab initio* studies, Simons and co-workers established that the global minima structures of  $B_3$  (15),<sup>13a</sup>  $B_3H$  (16), and  $B_3H_2$  (17)<sup>13b</sup> contain three-



membered rings with cyclic  $\pi$  electron delocalization. The substitution of H in **16** by Li to give B<sub>3</sub>Li leads to the electrostatically favored pyramidal structure **18**,<sup>13c</sup> which has some 4c-2e bonding<sup>13d</sup> arising from the interaction of the empty s orbital of Li<sup>+</sup> with the 3c-2e  $\pi$  bond of the B<sub>3</sub><sup>-</sup> anion.

The most favorable cyclic structures of  $B_3H_4^{-}$  (3a),<sup>3a</sup>  $B_3H_5$  (4a), and  $B_3H_6^{+}$  (5a)<sup>4</sup> (all isoelectronic with 14) also display



 $\begin{aligned} & 2B_3H_6^+ (\textbf{5a}) + 2C_3H_6 (D_{3h}) \rightarrow 2C_3H_3^+ (\textbf{14}) + 3B_2H_6 \quad \Delta E = \textbf{59 kcal/mol}^4 (\textbf{5}) \\ & B_3H_6^+ (\textbf{5a}) + C_3H_6 (D_{3h}) \rightarrow C_3H_3^+ (\textbf{14}) + B_3H_9 (C_{3v}) \quad \Delta E = \textbf{42 kcal/mol} (\textbf{6}) \end{aligned}$ 

3c-2e aromatic ring  $\pi$  delocalization. The  $C_{3\nu}$  B<sub>3</sub>H<sub>6</sub><sup>+</sup> (**5a**) with three out-of-plane bridged hydrogens was declared to be the "first three-membered nonplanar  $2\pi$  aromatic" species.<sup>4</sup> Indeed, **5a** is 42-45 kcal/mol more stable than the planar  $D_{3h}$  structure **5b**. The "extra stability" relative to **14** was deduced from *nonisodesmic*<sup>16</sup> eqs 5 and 6.<sup>4</sup>

Thus, the literature shows the importance of aromaticity in establishing structures of three-boron hydrides. Our goals in this paper are (1) to estimate ASEs of the three-membered ring aromatic species 3-5, 11, and 13, (2) to study the three-membered ring aromatics (1-5) and the reference  $B_3H_n$  species (6-10) involved in isodesmic equations, and (3) to examine the structure and stability of Li<sup>+</sup> (12) and 2Li<sup>+</sup> (13) complexes of the aromatic dianion 11. The literature data, where available, are compared with our results.

#### Methods

All geometries were optimized at HF/6-31+G\* and MP2(FULL)/ 6-31+G\* (simply designated HF and MP2 in the following text) using the GAUSSIAN 92 program package.<sup>17</sup> Analytical frequencies were obtained at HF/6-31+G\*. Zero point energies were scaled by 0.89, as recommended.<sup>15d</sup> The energy comparisons are at MP2(FULL)/6-31+G\* + ZPE(HF/6-31+G\*) unless otherwise noted. For a limited number of structures, single point QCISD(T)/6-311+G\*\*//MP2(FULL)/ 6-31+G\* (designated QCI) energy and MP2(FC)/6-31+G\* analytical

<sup>(16)</sup> These estimates are imperfect, as the number of CH and BH bonds as well as the B and C hybridizations differ in the species on both sides of eqs 5 and 6.

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Figure 1. B<sub>3</sub>H<sub>3</sub> structures. The number of imaginary frequencies is given in parentheses.

frequency computations were performed to determine the effect of electron correlation on relative energies and the nature of stationary states. The energies are presented in Table 1, and the geometries, in Figures 1–9. The number of imaginary frequencies (NIMAG) characterizes each stationary point: 0 = minimum; 1 = transition state (TS), etc. The numbering of the boron atoms (when not shown on figures) is from left to right unless indicated specifically. A detailed study of all possible forms and excited states of three-membered boron hydrides is beyond the scope of this paper. We computed some triplets only in cases where lower energies were expected.

The HF/6-31+G\*//MP2/6-31+G\* wave functions are characterized by natural bond orbital (NBO) charges (q), Wiberg bond indices (WBI), and Mulliken bond populations (MBP).<sup>18,19</sup> In particular cases, we have also considered the Mulliken gross populations of  $p\pi$  orbitals (MPP).

### **Results and Discussion**

Different definitions and measures of "aromaticity" based on structures, energies, electron distributions, and magnetic and chemical properties have been suggested and discussed extensively.<sup>20</sup> The qualitative attributes applicable to three-membered

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Figure 2. B<sub>3</sub>H<sub>4</sub><sup>+</sup> structures. The number of imaginary frequencies is given in parentheses.

aromatic species include the following: (1) a delocalized  $3c-2e \pi$  bonding orbital perpendicular to the cyclic plane; (2) equalization of the internal bond lengths to values intermediate between those of corresponding single and double bonds; (3) aromatic stabilization energy (ASE) defined with respect to appropriate reference species.<sup>21</sup> If the ASE energy is substantial, the cyclic isomer with  $3c-2e \pi$  bonding usually is the global minimum. Bond lengths also are influenced by strain and electrostatic interactions, etc. Since the choice of reference species for evaluating of ASEs often is not unambiguous, the electronic structure may provide the best criteria of aromaticity in some cases.<sup>21b</sup>

The different kinds of bridged bonds have been found here. As there is no unique way to display such bonds,<sup>1</sup> we have employed different modes of representation. Mode I gives the



electron count (one line, curved or straight, for two electrons), while mode II displays the coordination number and shows the geometry (bond lengths and bond angles) perspective. Mode III indicates that the bridging is quite unsymmetrical.

**B**<sub>3</sub>H<sub>3</sub> (Figure 1). The "classical" three-membered ring  $D_{3h}$  isomer **1f**  $(1a_1'^2)e'^42a_1'^22e'^43a_1'^23e'^4)$  does not have a favorable electronic structure (there are no  $\pi$  electrons<sup>3b</sup>) and is higher in energy than other alternatives. The strain energy in **1f**, estimated

<sup>(21) (</sup>a) The strain energy and  $\sigma$  aromaticity (see ref 20c) should also be taken into account. (b) The magnetic criteria of aromaticity (see ref 20a-c) will be considered separately for the species studied here.



Figure 3. B<sub>3</sub>H<sub>4</sub><sup>-</sup> structures. The number of imaginary frequencies is given in parentheses.

from eq 7, is higher than the corresponding value in cyclopro-





pane defined from eq 8 (for earlier estimates, see ref 22). All structures chosen in eq 7 are planar and have no  $\pi$  electrons.

The BB distances in **1f** (1.726 Å), in the  $D_{2h}$  structure of  $B_2H_4$  (1.744 Å), and in  $C_{2\nu}$  **4b** (1.742 Å) may be considered as "standard" boron-boron single bond lengths, since they are not influenced by conjugation or by hyperconjugation (compare with BB = 1.652 Å in the  $D_{2d}$  structure of  $B_2H_4$ , which benefits from double hyperconjugation<sup>23</sup>).



of electrons is moved from the  $\sigma$  framework to a  $\pi$  orbital (MPP for 1a: B<sup>1</sup>, -0.74; B<sup>2</sup>, -0.77; B<sup>3</sup>, -0.49. MPP for 1b: B<sup>1</sup> (B<sup>3</sup>), -0.61; B<sup>2</sup>, -0.78. MPP for 1c: B<sup>1</sup> (B<sup>3</sup>), -0.80; B<sup>2</sup>, -0.60). The global minimum 1a has unsymmetric B-H-B bonding without direct bonding overlap between the bridged boron atoms (WBI [MBP] (B<sup>1</sup>B<sup>2</sup>) = 1.321 [-0.811]). The two  $C_{2\nu}$  minima, 1b and 1c, arise from the first-order Jahn-Teller distortions of the  $D_{3h}$  symmetrical structure with two electrons in a degenerate e' orbital lying in the ring plane. Structure 1b has one localized BB and one three-center BBB

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bond, while 1c has two symmetrical  $\sigma$  bonds. There is no  $\sigma$  electron bonding between B<sup>1</sup> and B<sup>3</sup> atoms in 1c (MBP = -0.230). Nevertheless B<sup>1</sup> and B<sup>3</sup> are bound by a  $p_{\pi}-p_{\pi}$  interaction (WBI = 0.626). The B<sup>1</sup>B<sup>3</sup> separation of 1.922 Å is too short to be a nonbonded distance.

The open-chain isomer HB=B-BH<sub>2</sub> (1d) (the lowest energy minimum located in an earlier *ab initio* study<sup>3a</sup>) is substantially higher in energy than structures 1a-c. While the B<sup>1</sup>B<sup>2</sup> (1.554 Å) and the B<sup>2</sup>B<sup>3</sup> (1.586 Å) bond lengths do not differ considerably in 1d, there is no appreciable delocalization of  $\pi$ electrons into the B<sup>3</sup> p<sub> $\pi$ </sub> orbital (MPP = 0.10). The relative energies of 1b-d (with respect to the global minimum 1a) are similar at QCI (1b = 5.3 kcal/mol, 1c = 7.5 kcal/mol, and 1d = 28.8 kcal/mol), as at MP2 (see Figure 1). The other structures, 1e-h, have higher energies and are not minima.

Two triplet structures considered,  $D_{3h}$  1j and  $C_{2v}$  1k (see Figure 1), have lower energies than singlet forms 1f and 1d, respectively. Structure 1j (NIMAG = 2) has two unpaired electrons in the  $\sigma$  framework and an electron pair in a  $\pi$  MO. The singlet-triplet energy difference between 1d and 1k (8.2 kcal/mol) is lower than the corresponding HB=BH S-T value (23 kcal/mol; see also ref 23). This decrease in the S-T energy separation is due to more effective delocalization of two  $\pi$ electrons by the  $p_{\pi}$  orbital of the BH<sub>2</sub> group in 1d than corresponding delocalization of one electron in 1k. The double BB bond (1.554 Å) is longer and the single BB bond (1.586 Å) is shorter in 1d than the corresponding separations in 1k (1.527 and 1.651 Å). The decreased number of  $\sigma$  electrons and the cyclic  $\pi$  bonding lead to shorter BB bonds (1.599 Å) in 1j than in 1f (1.726 Å).

 $B_3H_4^+$  (Figure 2). The two lowest energy  $C_{2\nu}$  structures 2a and 2b arise from the protonation of the BB bonds in 1a and in



**1b**, respectively. But **2b** is not a minimum (NIMAG = 2) and collapses to **2a** if the  $C_{2\nu}$  symmetry constraint is removed. Both **2a** and **2b** have cyclic delocalized  $3c-2e \pi$  orbitals (MPP for **2a**: B<sup>1</sup> (B<sup>3</sup>) = 0.55; B<sup>2</sup> = 0.90. MPP for **2b**: B<sup>1</sup> (B<sup>3</sup>) = 0.71; B<sup>2</sup> = 0.58), while the B<sup>1</sup>B<sup>3</sup> bond length in **2a** (1.729 Å) is close to the BB distance in **1f**.

All other open-chain (2c-g) and cyclic (2h-j) structures have higher energies. Single point energy computations on 2a-cand 2e, f at QCI show their energies to be closer to 2a than those at MP2, but the relative order does not change (in kcal/ mol): 2a (0.0), 2b (3.2), 2c (4.7), 2e (14.8), and 2f (15.8). The highest energy structure 2j is employed below in eq 10 as the reference species in the ASE estimate for  $B_3H_4^-$ . There are two localized and one H-bridged BB bonds in 2j and no  $\pi$ electrons.

 $B_3H_4^-$  (Figure 3).  $B_3H_4^-$  is isoelectronic with aromatic  $CB_2H_4^{3a,4,13d,24}$  and has a similar global minimum structure (3a)



with a delocalized  $3c-2e \pi$  bond (MPP: B<sup>1</sup> (B<sup>3</sup>), -0.75; B<sup>2</sup>, 0.50). Another  $C_{2\nu}$  structure (**3b**) with a  $3c-2e \pi$  bond (MPP: B<sup>1</sup> (B<sup>3</sup>), -0.68; B<sup>2</sup>, 0.62) is only 2.8 kcal/mol higher in energy. Both **3a** and **3b** are lower in energy than the open-chain  $D_{2h}$  structure (**3c**), which has a linear  $3c-2e \pi$  bond. The relative QCI energies are as follows: **3a**, 0.0 kcal/mol; **3b**, 2.1 kcal/mol; **3c**, 11.2 kcal/mol.

While the SE in 3a, estimated from eq 9 (44.5 kcal/mol), is smaller than the SE of 14 (64.1 kcal/mol, eq 1), the ASE



estimates for **3a** (eq 10, 38.7 kcal/mol) and for **14** (eq 2, 35.7 kcal/mol) are similar. Because the reference structures in eqs 9 and 10 are so different from their counterparts in eqs 1 and

kcal/mol) are similar. Because the reference structures in eqs9 and 10 are so different from their counterparts in eqs 1 and2, such comparisons are only qualitative.

Remarkably, the  $C_{3\nu}$  structure **3d** is also a minimum, although its energy is quite high. It can be regarded as a 4c-2e  $\pi$ 



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4j, C<sub>2v</sub> (2): 65.3 kcal/mol

4k, D3h (2): 76.2 kcal/mol

Figure 4. B<sub>3</sub>H<sub>5</sub> structures. The number of imaginary frequencies is given in parentheses.

complex (nonplanar  $2\pi$  aromatic) of the aromatic dianion  $B_3H_3^{2-}$  (11), which is isoelectronic with  $14.^{13d,25a}$  Four other computed structures (3e-h) have higher energies. The  $C_{2\nu}$  form (3g), with a tetrahedral boron atom, was not a minimum; the same is true for the isoelectronic and isostructural CB<sub>2</sub>H<sub>4</sub>.<sup>13d,24</sup>

The triplet  $D_{2d}$  minimum, **3i** (see Figure 3), is considerably less stable at MP2 (42.6 kcal/mol) than the global minimum **3a**.

**B<sub>3</sub>H<sub>5</sub>** (Figure 4). The lowest energy minima 4a,d,e have already been examined by *ab initio* methods.<sup>3a,4</sup> Our data agree well with those of Jemmis et al.<sup>4</sup> at MP2/6-31G\*. Structures 4b (localized  $\sigma$  bonds and no  $\pi$  electrons) and 4c (H and BH<sub>2</sub> bridges and  $\pi$  bond between B<sup>1</sup> and B<sup>3</sup>) were employed as the reference species in eqs 7 and 9, respectively. Structure 4d arises from the rotation of the bridging BH<sub>2</sub> group in 4c to the ring plane, which leads to the cyclic delocalization of the  $\pi$ electrons into the B<sup>2</sup> p $\pi$  orbital. The B<sup>1</sup>B<sup>2</sup> and B<sup>2</sup>B<sup>3</sup> (1.639 Å) bonds are shorter and the B<sup>1</sup>B<sup>3</sup> (1.527 Å) bond is longer in 4d compared to 4c (B<sup>1</sup>B<sup>3</sup> = B<sup>2</sup>B<sup>3</sup> = 1.863 Å and B<sup>1</sup>B<sup>3</sup> = 1.466 Å). The cyclic C<sub>2v</sub> structures 4a,d, with  $\pi$  electron delocalization (MPP for 4a: B<sup>1</sup> (B<sup>3</sup>) = 0.59; B<sup>2</sup> = 0.82. MPP for 4d: B<sup>1</sup> (B<sup>3</sup>) = 0.76; B<sup>2</sup> = 0.48), have very similar energies: 4a is

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Table 1. Total Energies (in au) and Zero Point Energies (in kcal/mol) of  $B_3H_n$  and Related Species

molecule	no. (PG)	HF/6-31+G*//6-31+G*	MP2(fu)/6-31+G*//MP2(full)/6-31+G*a	ZPE (NIMAG) <sup>b</sup>
$B_3H_3$	$1a(C_s)$	-75.65095	-75.92043 (-75.99361)	23.2 (0)
	<b>1b</b> $(C_{2\nu})$	-75.64855	-75.90701 (-75.98278)	21.5 (0)
	<b>1c</b> $(C_{2\nu})$	-75.64904	-75.90170 (-75.97939)	21.6 (0)
	<b>1d</b> $(C_{2\nu})$	-75.64065	-75.86026	21.1 (0)
	$1e(C_{2\nu})$	-75.50054	-75.82153	19.4 (2)
	$\frac{1}{1} \frac{D_{3h}}{D_{3h}}$	-75.59733	-75.81057	20.3(2) 22.1(1)
	$1g(C_{2\nu})$ 1b(C <sub>2</sub> )	-75.53102	-75.79942	22.1(1) 21.8(1)
	$\mathbf{1i}(C_{2\nu})$	-75 47369	-75,77750	21.0(1) 21.0(3)
	$11(D_{34})^{c}$	-75.64759	-75.87651	22.0 (2) [20.2 (2)]
	$\frac{1}{1k} (C_{2y})^c$	-75.67327	-75.87311	22.0 (0)
$B_{3}H_{4}^{+}$	<b>2a</b> $(C_{2\nu})$	-75.96408	-76.22031 (-76.29735)	29.1 (0)
	<b>2b</b> $(C_{2\nu})$	-75.96110	-76.21206 (-76.29058)	27.9 (2) [26.3 (3)]
	<b>2c</b> $(C_{2v})$	-75.98556	-76.20388 (-76.28858)	27.5 (0)
	<b>2d</b> $(C_{2\nu})$	-75.94895	-76.18950	28.8 (1)
	$2e(C_s)$		-76.18820	27.9(0) 27.7(0)
	$2n(D_{2d})$ $2g(D_{2d})$	-75 98976	-76.18321	27.7(0)
	$2h(C_{2\nu})$	-75.95785	-76.17003	27.2 (1)
	$2i(C_{2v})$	-75.95029	-76.15570	27.5 (2)
	<b>2j</b> $(C_{2\nu})$	-75.94389	-76.14787	26.4 (2)
$\mathbf{B}_{3}\mathbf{H}_{4}^{-}$	<b>3a</b> $(C_{2\nu})$	-76.30113	-76.58819 (-76.67796)	28.9 (0)
	<b>3b</b> $(C_{2\nu})$	-76.29788	-76.58287 (-76.67383)	28.4 (0)
	$3c(D_{2h})$	-76.30336	~76.55869 (-76.65783)	27.4 (0)
	$3d(C_{3\nu})$	- /6.25626	-76.53309	24.8 (0)
	$3e(C_{2\nu})$	-76.22327	-76 51073	27.2(1)
	$3q(C_{2n})$	-76.23229	-76.49386	25.0 (2)
	$3h(C_{2\nu})$	-76.17939	-76.45597	26.6 (0)
	<b>3i</b> $(D_{2d})^c$	-76.29792	-76.51752	27.0 (0)
$B_3H_5$	<b>4a</b> $(C_{2\nu})$	-76.86764	-77.15293 (-77.24644)	36.4 (0)
	<b>4b</b> $(C_{2\nu})$	-76.84567	-77.06562	33.5 (2)
	<b>4c</b> $(C_{2\nu})$	76.78743	-77.05915	34.8 (2)
	4d $(C_{2\nu})$	-76.86979	-77.15140 (-77.24569)	36.0 (0)
	$4e(C_{2v})$		-77 10021	35.8 (0)
	$4r(C_{2v})$	-76.82550	~77.09391	36.1 (1)
	<b>4h</b> $(C_{2\nu})$	-76.80453	-77.06890	35.6 (3)
	<b>4i</b> $(C_{2\nu})$	-76.80374	-77.06239	31.7 (1)
	<b>4j</b> $(C_{2\nu})$	76.78211	-77.04261	32.0 (2)
	<b>4k</b> $(D_{3h})$	-76.75321	-77.03099	33.3 (2)
$B_{3}H_{6}^{+}$	<b>5a</b> $(C_{3\nu})$	-77.19371	-77.46114	44.7 (0) 42.0 (1)
	$SD(D_{3h})$	-77.19534	-77.44066	43.0 (1)
	$5C(C_{2v})$	-77 18871	-77 43642	43.4 (0)
	$5e(C_{3})$	-77.17713	-77.42906	42.7 (1)
	<b>5f</b> $(C_s)$	-77.17022	-77.41435	41.7 (1)
	<b>5g</b> $(C_{2\nu})$	-77.16890	-77.41344	41.6 (1)
	<b>5h</b> $(C_{2\nu})$	-77.17515	-77.40920	42.2 (0)
	$5i(C_s)$	-77.16142	-77.39916	41.2 (1)
	5j ( $C_{2\nu}$ )	-77.13362	- / /.38280	41.0(2) 30.1(3)
<b>В.Ц.</b> -	$5\mathbf{K}(D_{3h})$	-77.47375	-77 75846	39.1 (3)
D3116	<b>6h</b> $(C_{2\nu})$	-77.42320	-77.72522	40.9 (0)
	<b>6c</b> $(C_1)$	-77.47909	-77.76711	39.8 (0)
	<b>6d</b> $(D_{3d})$	-77.47550	-77.75002	37.5 (0)
	<b>6e</b> $(C_{2\nu})$	-77.46591	-77.73980	37.9 (0)
	$\mathbf{6f}\left(C_{s}\right)$	-77.46361	-77.73861	37.5 (1)
	$\mathbf{og}(C_{2\nu})$	- 77.45859	- / /. / 3840	38.5 (1)
	<b>6i</b> $(C_{2\nu})$	-77,43565	-77.73425	40.2 (0)
	<b>6i</b> $(C_{2\nu})$	-77.46010	-77.72528	38.8 (2)
	<b>6k</b> $(C_{2\nu})$	-77.42865	-77.71894	41.2 (0)
	<b>61</b> $(D_{3h})$	-77.39876	-77.69742	40.7 (2)
$B_3H_7$	<b>7a</b> $(C_{2\nu})$	-78.03119	-78.30321	48.5 (2)
	7b $(C_{2\nu})$	-77.99930	- /8.28913	40.7 (3)
	$7c(C_{2\nu})$	-78.03422	-78 31884	49.5 (2)
	$7\mathbf{e}(C_s)$	-78.04901	-78.33388	50.1 (0)
	$7f(C_{2n})$	-78.05125	-78.32637	49.6 (0)
	$7 \mathbf{g}(C_s)$	-78.05119	-78.31724	49.4 (0)
	$7h(C_s)$	-77.98289	-78.26416	47.5 (1)

Table 1 (	Continued)
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molecule	no. (PG)	HF/6-31+G*//6-31+G*	MP2(fu)/6-31+G*//MP2(full)/6-31+G*a	ZPE (NIMAG) <sup>b</sup>
$B_{3}H_{8}^{+}$	<b>8a</b> ( $C_{2v}$ )	-78.29852	-78.55263	50.5 (2)
	$\mathbf{8b}(C_s)$	-78.30012	-78.57945	52.1 (1)
	8c $(D_{2d})$	-78.35062	-78.61987	57.7 (0)
	<b>8d</b> $(C_{2\nu})$	-78.33445	-78.61282	58.1 (0)
	$\mathbf{8e}(C_s)$	-78.32649	-78.58875	55.5 (1)
	8f ( $C_{2\nu}$ )	-78.31619	-78.55880	53.2 (2)
	8g $(C_{2\nu})$	-78.30845	-78.54956	52.0 (2)
$B_{3}H_{8}^{-}$	<b>9a</b> $(C_{2v})$	-78.66539	-78.98121 (-79.1243)	43.4 (1) [53.4 (0)]
	<b>9b</b> $(C_s)$	-78.66638	-78.97815 (-79.12068)	54.2 (0) [53.0 (1)]
	$9c(C_s)$	-78.64485	-78.94451	53.0 (0)
$B_3H_9$	<b>10a</b> $(D_{3h})$	-79.18196	79.47914	62.0 (3) [61.4 (3)]
	<b>10b</b> $(C_{3\nu})$	-79.18471	-79.48849	63.5 (0)
	$10c(C_2)$	-79.18004	-79.48207	62.5 (1) [61.7 (0)]
$B_3H_3^{2-}$	11 $(D_{3h})$	-75.51083	-75.80995	21.4 (0)
$B_{3}H_{5}^{2-}$	$(C_{2\nu})$	-76.71714	-77.00324	31.8 (0)
$B_3H_3Li^-$	12a $(C_{2v})$	-83.14662	-83.44967	22.4 (0)
	<b>12b</b> $(C_{3v})$	-83.13853	-83.44494	22.7 (0)
$B_3H_3Li_2$	13a $(C_{2\nu})$	-90.63788	-90.94594	24.6 (0)
	<b>13b</b> $(D_{3h})$	-90.60960	-90.91733	23.5 (2)
$B_3H_5Li_2$	$(C_{2\nu})$	91.80815	-92.12102	35.6 (1)

<sup>a</sup> Values in parentheses are at QCISDT/6-311+G\*\*//MP2(FULL)/6-31+G\*. <sup>b</sup> Not scaled; at HF/6-31+G\* [MP2(FC)/6-31+G\*]. <sup>c</sup> In the triplet state.

more stable at MP2 (see Table 1). Both 4a and 4d may be regarded as protonated forms of the lowest energy  $C_{2\nu}$  B<sub>3</sub>H<sub>4</sub>-structures 3a,b, respectively.



The "classical" open structure 4e is the global minimum at HF (in agreement with earlier *ab initio* findings<sup>3a</sup>) but less stable than 4a at MP2. The QCI energies, relative to 4a, are 0.3 kcal/mol (4d) and 17.4 kcal/mol (4e). Structure 4e arises from the rotation of two BH<sub>2</sub> groups in 4b leading to the planar  $C_{2\nu}$  structure. The shorter BB distances in 4e (1.646 Å) than in 4b (1.752 Å) are due to hyperconjugation between the BH bonds and the empty p orbitals of neighboring B atoms. A similar variation is found in the BB bond lengths of the planar  $D_{2h}$  (1.744 Å) and the rotated  $D_{2d}$  (1.653 Å) B<sub>2</sub>H<sub>4</sub> structures.<sup>23</sup> The 30 kcal/mol 4b  $\rightarrow$  4e energy difference is about twice the  $D_{2d}$   $\rightarrow D_{2h}$  rotation value in B<sub>2</sub>H<sub>4</sub> (13 kcal/mol).

Our highest energy minimum 4f, with its doubly H-bridged bond (a protonated form of 3h), has not been considered previously. The strongly negative  $B^1B^3$  MBP (-0.552) indicates the absence of direct bonding. All other structures we examined, 4g-k, have higher energies and are not minima.

The  $C_{2\nu}$  planar 4g is 16 kcal/mol lower in energy than the isostructural 4i. This energy difference can be attributed to the delocalization of  $\pi$  electrons to B<sup>1</sup> p<sub> $\pi$ </sub> orbital in planar 4g. Structure 4h (no  $\pi$  electrons) is the analog of 3g with an additional B-H-B bridged bond. The relative energies of 3g and 4h are similar to those of global minima, 3a and 4a, respectively. Isomer 4j originates from a different distribution of two  $\sigma$  electron pairs bonding three boron atoms than in 4e.



There are two localized BB bonds in 4e and one localized and

We have considered the high energy  $D_{3h}$  structure **4k** because of its potential three-dimensional aromaticity:<sup>4,26</sup> **4k** is the doubly protonated form of the aromatic dianion, **11**. However, **4k** is not a minimum and has a high energy.

4k

Isodesmic eq 11 gives an estimate of the SE of 4a, which is similar to the SE of the cyclopropenium cation, 14 (eq 1).<sup>27</sup> All species in eq 11 are isoelectronic with their corresponding counterparts in eq 1.



(26) (a) Krogh-Jespersen, K.; Schleyer, P. v. R.; Pople, J. A.; Cremer, D. J. Am. Chem. Soc. 1978, 100, 4301. (b) Chandrasekhar, J.; Schleyer, P. v. R.; Krogh-Jespersen, K. J. Comput. Chem. 1981, 2, 356.



**Figure 5.**  $B_3H_6^+$  structures. The number of imaginary frequencies is given in parentheses.

While **6b** is not the lowest energy  $B_3H_6^-$  minimum and **7b** is not a minimum at all (NIMAG = 3), we believe that these reference structures are the most appropriate for the comparative SE estimation of **14** with **4a**. This assumption is based on an isoelectronic and isostructural analogy between corresponding structures in eq 1 and eq 11. The bonding patern is similar in the carbon and boron counterparts in eqs 1 and 11, respectively, while two localized bonds in the three-membered carbon cycles are replaced by 3c-2e H-bridged bonds in the boron rings. Thus, differences between counterparts in eqs 1 and 11 are counterbalanced in the left and right sides of the equations, and aromatic

stabilization is emphasized. Similar approach was been employed, for example, in a comparative analysis of cyclic strain energies.<sup>15d</sup>

 $B_3H_6^+$  (Figure 5). We have examined many  $B_3H_6^+$  isomers (5a-k) and have estimated the isodesmic SEs in 5a,b in order to compare the aromatic stabilization of  $B_3H_6^+$  with  $C_3H_3^+$ . The 42 kcal/mol stabilization with respect to the planar  $D_{3h}$  structure 5b results (as suggested in ref 4) from electron delocalization, as well as from the hydrogen atoms. The bridging and the terminal hydrogens are out of the ring plane by 0.678 and 0.385 Å, respectively, and BB bond distances are elongated by 0.03 Å in 5a compared to those in  $D_{3h}$  5b.

The higher energy 5c,d minima also have three bridged bonds. The bridging  $BH_2$  group in 5c is replaced by a bridging hydrogen in 5d. The latter structure is an analog of the

<sup>(27)</sup> Our later 64.1 kcal/mol SE estimate of C<sub>3</sub>H<sub>3</sub><sup>+</sup> at MP2/6-31+G<sup>\*</sup> + ZPE is closer to the earlier 69.5 kcal/mol value from ref 15a than to 78 kcal/mol value from ref 14b.



propargyl cation,  $H_2C-CCH^+$ , with a triply H-bridged BB arrangement instead of the triple CC bond. The energy difference between the cyclopropenium ion, 14, and the propargyl cation (25-34 kcal/mol<sup>24,27</sup>) is about twice as large as between 5a and 5d (14.4 kcal/mol). Both 5c and 5d can also be related to the triply H-bridged  $B_2H_5^+ D_{3h}$  structure 19, studied earlier by *ab initio* methods.<sup>28</sup>

The transition structure  $C_{2\nu}$  5e is similar to 5c but with the BH<sub>2</sub> group rotated. Both transition structures  $C_s$  5f and  $C_{2\nu}$  5g



optimize to the global minimum 5a, if the symmetry constraints are eliminated. In  $C_{2v}$  5h, the bond lengths of  $B^1B^2$  (WBI = 0.700; MBP = 0.306) doubly H-bridged and  $B^2B^3$  (WBI = 1.006; MBP = 0.248) localized single BB bonds are equal despite the difference in their bonding character. Nevertheless, WBIs (0.700 and 1.006) and MBPs (0.306 and 0.248) are also similar for  $B^1B^2$  and  $B^2B^3$  bonds. Like 5c,d, the 5h minimum and the 5f transition structure are related through the exchange of a bridging hydrogen (e.g., in 5h) with a bridging BH<sub>2</sub> group (in 5f). The greater stability of 5c, relative to 5d (2.8 kcal/ mol), as well as of 5f, relative to 5h (5.3 kcal/mol), reflects the better electron and charge delocalization in cyclic rather than open structures.

The other  $B_3H_6^+$  structures we considered (5i-k) are higher in energy and are not minima. Structure 5j is a protonated form of 4j and also has two imaginary frequencies. The  $D_{3k}$  structure 5k, with a single 3c-2e symmetric  $\sigma$  bond between the three boron atoms, has very high energy. Planar 5b has the same  $D_{3h}$  symmetry as the aromatic cyclopropenium ion, 14. We suggest the isodesmic eq 12 for



the estimation of the SE in 5b. As in eq [1, all reference structures in eq 12 are isoelectronic with the corresponding structures in eq 1. The SE of 5b, despite its higher symmetry, is smaller than that of 4a. The BB bond lengths are longer in 5b than in 4a, due to the greater repulsion of nonbonded hydrogens in 5b.

The SEs of the  $D_{3h}$  symmetric 14 (eq 1) and 5b (eq 12) are similar and are quite large. Nevertheless, the energy of nonplanar  $C_{3\nu}$  5a is 42 kcal/mol *lower* than 5b. Is this due to increase of aromaticity in 5a? In an attempt to elucidate this question, we have estimated the SE of 5a from isodesmic eq 13. The structures in eq 13 ( $C_{3\nu}$  5a and  $C_s$  7d, 8b, and 10b) have lower symmetry than the corresponding structures in eq 12 ( $D_{3h}$  5b and  $C_{2\nu}$  7c, 8a, and 10a) as the bridging hydrogens are out of the boron ring plane.



The species in eq 13 are more stable than the corresponding forms in eq 12 by 41.9 kcal/mol (5a vs 5b), 4.6 kcal/mol (10a vs 10b), 66.7 kcal/mol (7d vs 7c), and 15.4 kcal/mol (8b vs 8c). The sum of these energy differences due to symmetry reduction are higher for the reference species in the right side of eq 13. As a consequence, the SE of 5a (24.6 kcal/mol, deduced from eq 13) is less than the SE of 5b (59.9 kcal/mol, eq 12) despite the lower energy of 5a than 5b. This demonstrates how strongly the choice of reference species can influence SEs. While the bridging hydrogens are located more or less symmetrically in all species employed in eq 12, as well as in 5a and in 10b in eq 13, it is not true for 7d and 8b. The unsymmetrical H-bridging in B<sup>1</sup>-H-B<sup>2</sup> and B<sup>2</sup>-H-B<sup>3</sup> bonds of 7d and 8b complicates the comparison of the SEs estimated from eqs 12 and 13 (despite their formal correspondence), as hydrogen-hydrogen repulsion may not be properly counterbalanced in the left and right sides of eq 13. Nevertheless, we

<sup>(28) (</sup>a) Rastogi, R.; Ray, N. K. Int. J. Quantum Chem. 1977, 11, 435. (b) McKee, M. L.; Lipscomb, W. N. Inorg. Chem. 1985, 24, 762. (c) Curtiss, L. A.; Pople, J. A. J. Chem. Phys. 1988, 89, 4875. (d) Olah, G. A.; Aniszfeld, R.; Surya Prakash, G. K.; Williams, R. E.; Lammertsma, K.; Guner, O. F. J. Am. Chem. Soc. 1988, 110, 7885. (e) Sana, M.; Leroy, G.; Henriet C. H. J. Mol. Struct. THEOCHEM 1989, 187, 233. (f) Curtiss, L. A.; Pople, J. A. J. Chem. Phys. 1989, 91, 4189.



Figure 6.  $B_3H_6^-$  structures. The number of imaginary frequencies is given in parentheses.

doubt that lower energy of nonplanar **5a** with respect to planar **5b** is due to an increase of aromaticity. Delocalization of this MO from the boron  $p_{\pi}$  orbitals to the bridging hydrogens (allowed by  $C_{3\nu}$  symmetry of the nonplanar **5a**) is not a convincing explanation; the same is true for the MO energy splitting.<sup>4</sup> The structure **7d** (eq 13), which does not involve aromaticity, is 67 kcal/mol lower in energy than **7c** (eq 12). We suggest that the cyclic delocalized  $\pi$  MO in **5b**, symmetrical with regard to the ring plane, corresponds to the cyclic 3c-2e bond in **5a** which also binds three borons and that the BHB three-center bonding is more favorable in **5a** than in **5b**. The central symmetric B-B-B bridge in **5a** can be depicted by ring line, similar to the cyclic  $\pi$  bond in **5b**.

 $B_3H_6^-$  (Figure 6). The singly (6a) and doubly H-bridged (6b) minimum energy structures (both  $C_{2\nu}$ ) were employed as the reference species in eqs 9 and 11, respectively. The singly bridged 6a is only 5.4 kcal/mol higher in energy than the global

 $B_3H_6^-$  minimum **6c** ( $C_1$ ), while the doubly bridged isomer is 27.2 kcal/mol less stable than **6c**. Two localized BB bonds and one H-bridged bond comprise the three-membered ring in **6a**:  $B^1$  and  $B^3$  share the negative charge ( $q(B^1) = q(B^3) = -0.476$ ;  $q(B^2) = 0.186$ ).

The asymmetric H-bridged open-chain structure **6c** is the global minimum both at HF and MP2. The negative charge in **6c** is substantially delocalized:  $q(B^1) = -0.206$ ,  $q(B^2) = -0.331$ , and  $q(B^3) = -0.158$ . Some bonding exists between B<sup>1</sup> and B<sup>3</sup> (WBI = 0.326, MBP = 0.071) in spite of the long B<sup>1</sup>B<sup>3</sup> separation (2.169 Å). The B<sup>1</sup>-H-B<sup>2</sup> bridged bond (WBI = 0.944; MBP = -0.107) has no direct bonding between the boron atoms, but the B<sup>2</sup>B<sup>3</sup> bond in **6c** (WBI = 1.304; MBP = 0.372) has partial double bond character. This is apparent from the short bond length, as well as from the population analysis. The two resonance contributors depict the bonding in **6c**.



Two open-chain minimum energy structures with localized single bonds ( $D_{3d}$  6d and  $C_{2\nu}$  6e) have alternating charges. The central boron atom in 6d is positively charged ( $q(B^2) = 1.087$ ), whereas the terminal borons have negative charges ( $q(B^1) =$  $q(B^3) = -0.965$ ). In 6e B<sup>2</sup> is negatively charged ( $q(B^2) =$ -0.892;  $q(B^1) = q(B^3) = 0.283$ ). The small BBB bond angle (88.1°) and positive bond population between B<sup>1</sup> and B<sup>3</sup> atoms (WBI = 0.169; MBP = 0.091) indicates hyperconjugation between the  $\sigma^{BB}$  bonds and the empty p orbitals of B<sup>1</sup> and B<sup>3</sup>.



The bonding is similar in transition structures 6f-h: all three have a bridging BH<sub>2</sub> group. If the  $C_{2\nu}$  symmetry constraint of 6g is reduced to  $C_s$ , the lower energy 6f results upon further optimization. Both 6e and 16h both result from first-order Jahn-Teller distortions of the  $D_{3h}$  symmetrical structure with two  $\sigma$  electron pairs in the three-boron plane.

The  $C_{2\nu}$  minimum **6i** is another cyclopropene analog with doubly H-bridged ring B<sup>1</sup>B<sup>3</sup> bond. This structure is 6.2 kcal/



mol more stable than 6b. The bridging in planar  $C_{2\nu}$  6j is similar to that in 6e. However, the empty p orbitals of the terminal boron atoms in 6j are perpendicular to the three-boron plane (hyperconjugation with BH instead of BB bonds) and the B<sup>1</sup>B<sup>2</sup>B<sup>3</sup> bond angle is widened (121.4°). Our highest energy minimum, 6k, is an analog of allene with doubly H-bridged bond. While allene is 20-22 kcal/mol more stable than cyclopropene,<sup>25g,29</sup> cyclic 6i is 9.6 kcal/mol more stable than the open-chain 6k. The  $D_{3h}$  ring of 6l is constructed from one  $\sigma$  and one  $\pi$  3c-2e bond.

**B<sub>3</sub>H<sub>7</sub>** (Figure 7). **B**<sub>3</sub>H<sub>7</sub> isomers have been studied *ab initio* many times.<sup>3,5-8</sup> None of the four reference structures 7a-d employed in the isodesmic eqs 9 and 11–13 are minima. The  $C_s$  global minimum, 7e, with two bridged hydrogens, arises from the optimization of 7b, when the  $C_{2\nu}$  symmetry constraint is removed.<sup>5,6</sup>



While 7d (with the H's bridges out of the ring plane) was considered in eq 13 as an analog of the triply in-plane H-bridged 7c, the bonding and energy of 7d is closer to those of singly H-bridged 7a. Despite the long B<sup>2</sup>H<sup>b</sup> distance in 7d (1.719 Å), bonding between each of the two bridging hydrogens and B<sup>2</sup> is indicated by WBI(B<sup>2</sup>H<sup>b</sup>) = 0.167 (compare with WBI(B<sup>2</sup>H<sup>b</sup>) = 0.429 in 7b). The B<sup>1</sup>B<sup>3</sup> separation in 7d (1.613 Å) is closer to that in 7c (1.595 Å) than in 7a (1.703 Å). However, the WBI in 7d (0.903) approaches the 7a value (0.780) closer than that of 7c (1.458). The shorter B<sup>1</sup>B<sup>2</sup> and B<sup>2</sup>B<sup>3</sup> bond lengths in 7d (1.787 Å), compared to the corresponding bond distances in 7a (1.905 Å) and in 7c (1.922 Å), are a consequence of the diminished H<sup>b...H<sup>i</sup></sup> repulsion in 7d.

The electronic structure of 7e has been analyzed recently<sup>8g</sup> in terms of Bader's theory of atoms in molecule (AIM).<sup>30</sup> No



bond lines and critical points were found between the bridging hydrogens and the two equivalent borons, B<sup>1</sup> and B<sup>3</sup>. AIM analysis also shows no bonding between B<sup>1</sup> and B<sup>3</sup>. Instead, direct B<sup>1</sup>B<sup>2</sup> and B<sup>2</sup>B<sup>3</sup> bonding was demonstrated (7e'). The electron densities at the critical points ( $\rho$ ) on B<sup>2</sup>H<sup>1</sup> and on B<sup>2</sup>H<sup>b</sup> are 0.189 and 0.145, respectively. Our population analysis agrees qualitatively but does not exclude bridging B<sup>1</sup>H<sup>b</sup>B<sup>2</sup> and B<sup>2</sup>H<sup>b</sup>B<sup>3</sup> (WBI = 0.393; MBP = 0.081) and cyclic bonding B<sup>1</sup>B<sup>3</sup> (WBI = 0.381; MBP = 0.061). B<sup>2</sup>H<sup>1</sup> (WBI = 0.973; MBP = 0.445) and B<sup>2</sup>H<sup>b</sup> (WBI = 0.555; MBP = 0.215) bond populations differ more that their  $\rho$  values.<sup>8g</sup> We believe that 7e provides the more satisfactory qualitative presentation of the bonding in B<sub>3</sub>H<sub>7</sub> global structure.

The two energy minima, 7f,g, are related to diborane 20 since bridging (7f) or terminal (7g) hydrogens are substituted by a



 $BH_2$  group. In agreement with an earlier study,<sup>6</sup> 7f is the most

<sup>(29)</sup> Yoshmine, M.; Pacansky, J.; Honjou, N. J. Am. Chem. Soc. 1989, 111, 4198.

<sup>(30)</sup> Bader, R. F. W. Atoms in Molecules: A Quantum Theory; Clarendon Press: Oxford, U.K., 1990.



Figure 7. B<sub>3</sub>H<sub>7</sub> structures. The number of imaginary frequencies is given in parentheses.

stable structure at HF, but electron correlations favors 7e. Perpendicular (90°) rotation of the  $B^2H_2$  group in 7f out of ring plane leads to the higher energy structure 7a.

The highest energy  $B_3H_7$  isomer (7h) is the structural analog of the 1-methylvinyl cation 21. Another rotamer 7h' collapses



to 7g (an analog of  $H_2C=CH-CH_2^+$  (22)) upon optimization. This contrasts with the conversion of the nonplanar allyl cation (22) into 21.<sup>31</sup> The B<sup>1</sup>B<sup>2</sup> bond in 7h is unusually short (1.587 Å), is strongly polar ( $q(B^1) = -0.793$ ;  $q(B^1H_3) = -0.696$ ), and has partial double bonding character (WBI = 1.189).

 $B_3H_8^+$  (Figure 8). Neither  $B_3H_8^+$  structure 8a nor 8b employed in eqs 12 and 13 is a minima. These two structures are related to 7b and 7e with an additional H-bridged bond between  $B^1$  and  $B^3$  in 8a and 8b. The two minima, 8c,d, can

be regarded as H-bridged analogs of allene and cyclopropene, respectively. The BB separation in doubly H-bridged cyclic 8d ( $B^1B^3 = 1.625$  Å) is shorter than in the open-chain 8c ( $B^1B^2$ 



=  $B^2B^3 = 1.717$  Å). The double bond in cyclopropene (1.296 Å) is also shorter than the cumulated C=C bonds in allene (1.308 Å).<sup>32</sup> The BB bond population indices are similar for doubly bridged bonds in 8c (WBI = 0.650; MBP = 0.171) and 8d (WBI = 0.791; MBP = 0.174).

Open-chain  $B_3H_8^+$  isomers with three  $BH_2$  groups held together by H-bridges also might be expected. However, none of our three structures with this bonding pattern, 8e-g, were minima. Reduction of symmetry in 8f or 8g gave 8d directly ( $C_2$  rotation of the terminal  $BH_2$  groups) or the  $C_3$  structure 8e. A similar situation was encounted in the open-chain H-bridged  $H_2B-H-BH_2^+$  cation.<sup>28</sup>

 $B_3H_8^-$  (Figure 9). The  $C_{2\nu}$  structure 9a, employed in eq 11 as an analog of cyclopropane (eq 1), is the lowest energy

<sup>(31)</sup> Foresman, J. B.; Wong, M. W.; Wiberg, K. B.; Frisch, M. J. J. Am. Chem. Soc. 1993, 115, 2220-2226.

<sup>(32)</sup> Calloman, J. H.; Hirota, E.; Iijima, T.; Kuchitsu, K.; Lafferty, W. J. Landoldt-Börnstein. Structural Data of Free Polyatomic Molecules; Springer Verlag: Berlin, 1987; Vol. 15, Suppl. V.II/7.



Figure 8.  $B_3H_8^+$  structures. The number of imaginary frequencies is given in parentheses.

minimum at MP2; transition structure **9b** is 1.5 kcal/mol higher in energy (1.2 kcal/mol at QCI; for earlier *ab initio* studies of  $B_3H_8^-$ , see refs 5, 9, and 10). In contrast, **9b** is a minimum at HF, but **9b** is a TS (see Table 1). The negative charge in **9a** is



delocalized over the boron atoms  $(q(\mathbf{B}^1) = q(\mathbf{B}^3) = -0.389, q(\mathbf{B}^2) = -0.172)$ . The  $\mathbf{B}^2\mathbf{H}_3$  group in **9b** bridges  $\mathbf{B}^1$  and  $\mathbf{B}^3$  atoms. The negative charge is distributed equally between the  $\mathbf{B}\mathbf{H}_3$  group  $(q(\mathbf{B}^2) = -0.500; q(\mathbf{B}^2\mathbf{H}_3) = -0.550)$  and the remainder of the anion.

Isomer 9c, related to 7g with H<sup>-</sup> attached to the terminal BH<sub>2</sub> group, is 22.7 kcal/mol less stable than 9a. The negative charge in 9c is concentrated on the terminal B<sup>1</sup>H<sub>3</sub> group ( $q(B^1) = -0.603$ ;  $q(B^1H_3) = -0.906$ ).

**B<sub>3</sub>H<sub>9</sub>** (Figure 9). (For earlier *ab initio* studies of B<sub>3</sub>H<sub>9</sub>, see refs 5, 8, 11, and 12). The B<sub>3</sub>H<sub>9</sub>  $D_{3h}$  form 10a was used in eq



12 and the  $C_{3\nu}$  form 10b was used in eq 13 as the best isostructural analogs of cyclopropane (eq 1). Triborane 10b is less stable than diborane (2B<sub>3</sub>H<sub>9</sub>  $\rightarrow$  3B<sub>2</sub>H<sub>6</sub>;  $\Delta E = 24.5$  kcal/



Figure 9. B<sub>3</sub>H<sub>8</sub><sup>-</sup> and B<sub>3</sub>H<sub>9</sub> structures. The number of imaginary frequencies is given in parentheses.

mol; see also refs 8d and 12). The energies of **10a** and **10b** differ by only 4.6 kcal/mol despite of the substantial differences in geometry. The nature of the bonding in **10b**, discussed<sup>8f</sup> recently in terms of AIM theory,<sup>30</sup> is characterized by six terminal BH bonds and three BHB bridged bonds without direct bonding interaction of BB atoms.

We have also considered the  $C_2$  structure 10c, which has recently been discussed in relation with the heavier analogs, Al<sub>3</sub>H<sub>9</sub> and Ga<sub>3</sub>H<sub>9</sub>, as well as in diborane pyrolysis.<sup>12</sup> The 3.7 kcal/mol energy difference between 10b and 10c agrees with the CCSD/DZP value of 3.5 kcal/mol reported in ref 12. We also find 10c to be a minimum but only when correlation is included<sup>12,33</sup> (see Table 1). The  $C_2$  structure 10c has a fivecoordinated  $B^2$  atom in the center of a distorted trigonal bipyramid. The bond angles at  $B^2$  with the axial and the equatorial bridging hydrogens are 160.8° (H<sup>2</sup>B<sup>2</sup>H<sup>4</sup>) and 122.2°  $(H^1B^2H^3)$ , respectively (see Figure 9). As expected for a bipyramidal structure, the axial  $B^2H^2$  and  $B^2H^4$  bond distances are longer (1.468 Å) than equatorial  $B^2H^1$  and  $B^2H^3$  separations (1.348 Å). The five-coordinated boron atom is negatively charged  $(q(\mathbf{B}^1) = -0.173)$ , while the other two borons possess a substantial positive charge  $(q(\mathbf{B}^1) = q(\mathbf{B}^3) = 0.614)$ .

 $B_3H_3^{2-}$ ,  $B_3H_3Li^-$ , and  $B_3H_3Li_2$ . The  $D_{3h}$  dianion 11 is the most direct boron analog of the isoelectronic aromatic cyclo-

propenium ion, 14. The remarkable similarity between ASEs of  $D_{3h} C_3 H_3^+$  and of 11 is evident from eqs 2 and 14.



Lithium has a substantially lower ionization potential (5.4 eV) than hydrogen  $(13.6 \text{ eV})^{34}$  and is expected to be a suitable counterion for 11. Comparison of the ASEs given by eqs 2, 14, and 15 shows that two Li<sup>+</sup> bridges effectively stabilize the aromatic dianion 11.

<sup>(34)</sup> CRC Handbook of Chemistry and Physics, 73rd ed.; Lide, D. R., Ed.; CRC Press: Boca Raton, FL, 1993.



The replacement of the bridging hydrogens in **3a**,d and **4a**,l by lithiums diminishes the relative energy between planar (**12a**)



and **13a**) and nonplanar (**12b** and **13b**) structures substantially. The  $C_{2\nu}$  planar structure **12a** is only 3.3 kcal/mol more stable than  $C_{3\nu}$  **12b**. Both **12a** and **12b** are minima. The 13 kcal/ mol preference of the  $C_{3\nu}$  pyramidal B<sub>3</sub>Li **18** over the planar  $C_{2\nu}$  **23** isomer, noted by Hernandez and Simons,<sup>13a</sup> agrees with our 15 kcal/mol estimation.

These lithium-containing aromatic structures are complexes of  $Li^+$  cations, as the charge on lithiums is nearly one.<sup>13c,35</sup> Relative to the BB distance in **11** (1.624 Å), the BB bonds are

shorter in the planar  $Li^+$  complexes (12a and 13a) but longer in the nonplanar structures (12b and 13b).

#### Conclusions

Our results show that aromaticity (cyclic  $3c-2e \pi$  delocalization) is important in the structural chemistry of threemembered boron cycles. While it is difficult to define aromaticity uniquely,<sup>20,21</sup> a combined study of energies, structures, and electron distribution help to clarify the nature of bonding in cyclic boron hydrides.

The cyclic aromatic  $B_3H_3$  (1a),  $B_3H_4^+$  (2a),  $B_3H_4^-$  (3a),  $B_3H_5$  (4a), and  $B_3H_6^+$  (5a) structures are the global minima for each composition. The isodesmic stabilization energies of 3a, 4a, *planar* 5b, 11, and 13a approach the substantial value of the cyclopropenium ion. However, we suggest that 42 kcal/mol higher stability of the *nonplanar* 5a is not a consequence of an "extra" aromaticity but rather of the more favorable hydrogen placements in 5a compared to those in 5b. Lithium countercations can stabilize the aromatic anions 3a and 11 and their cyclic electron delocalization.

Electron correlation contributes importantly to the relative stability of the three-boron hydride isomers and favors cyclic delocalized structures. While **5a** is the global minimum both at HF and MP2, open-chain isomers  $C_{2\nu}$  HBBBH<sub>2</sub> (1k, triplet),  $C_{2\nu}$  H<sub>2</sub>B(BH)<sub>2</sub><sup>+</sup> (2c),  $D_{2h}$  H<sub>2</sub>BBBH<sub>2</sub><sup>-</sup> (3c), and  $C_{2\nu}$  HB(BH<sub>2</sub>)<sub>2</sub> (4e) are more stable than aromatic cycles at HF. The BB and BH separations in bridged bonds vary considerably depending on the bond character and non-bonding interactions.

Isoelectronic and isostructural analogies between boron and carbon species guide the search for new ionic and neutral boron hydrides.

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<sup>(35)</sup> NBO charges on Li at HF/6-31+G\* are 0.932 (12a), 0.766 (12b), 0.966 (13a), and 0.953 (13b).