

## New Pathways for Chlorine Dioxide Decomposition in Basic Solution

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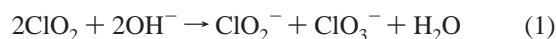
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The product distribution from the decay of chlorine dioxide in basic solution changes as the  $\text{ClO}_2$  concentration decreases. While disproportionation reactions that give equal amounts of  $\text{ClO}_2^-$  and  $\text{ClO}_3^-$  dominate the stoichiometry at millimolar or higher levels of  $\text{ClO}_2$ , the ratio of  $\text{ClO}_2^-$  to  $\text{ClO}_3^-$  formed increases significantly at micromolar  $\text{ClO}_2$  levels. Kinetic evidence shows three concurrent pathways that all exhibit a first-order dependence in  $[\text{OH}^-]$  but have variable order in  $[\text{ClO}_2]$ . Pathway 1 is a disproportionation reaction that is first order in  $[\text{ClO}_2]$ . Pathway 2, a previously unknown reaction, is also first order in  $[\text{ClO}_2]$  but forms  $\text{ClO}_2^-$  as the only chlorine-containing product. Pathway 3 is second order in  $[\text{ClO}_2]$  and generates equal amounts of  $\text{ClO}_2^-$  and  $\text{ClO}_3^-$ . A  $\text{Cl}_2\text{O}_4$  intermediate is proposed for this path. At high concentrations of  $\text{ClO}_2$ , pathway 3 causes the overall  $\text{ClO}_3^-$  yield to approach the overall yield of  $\text{ClO}_2^-$ . Pathway 2 is attributed to  $\text{OH}^-$  attack on an oxygen atom of  $\text{ClO}_2$  that leads to peroxide intermediates and yields  $\text{ClO}_2^-$  and  $\text{O}_2$  as products. This pathway is important at low levels of  $\text{ClO}_2$ .

## Introduction

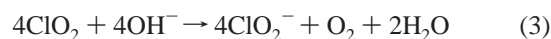
Recent use of chlorine dioxide for the disinfection of anthrax-contaminated premises<sup>1</sup> as well as its growing use in water disinfection,<sup>2</sup> wastewater treatment,<sup>3</sup> pulp bleaching,<sup>4</sup> chemosterilization,<sup>5</sup> and food preservation<sup>6</sup> shows the need for a better understanding of the chemical reactions of this free radical. The rate of decomposition of  $\text{ClO}_2$  in neutral aqueous solutions is quite slow,<sup>7</sup> but its decay is accelerated by base.<sup>8</sup> The disproportionation reaction in eq 1 has been proposed by many investigators.<sup>8–13</sup> Bray<sup>8</sup> proposed a third-order rate expression for this disproportionation (eq 2) with a rate constant of  $15.3 \text{ M}^{-2} \text{ s}^{-1}$  at  $19^\circ\text{C}$ . Halperin and Taube<sup>9</sup> studied the general features of  $\text{ClO}_2$  decay in base with  $^{18}\text{O}$ -labeling techniques at millimolar  $\text{ClO}_2$  levels and concluded that a dimer,  $\text{Cl}_2\text{O}_4$ , forms which subsequently reacts with

$\text{OH}^-$ . Disproportionation rate expressions with both a first-order and a second-order dependence in  $\text{ClO}_2$  concentration have been cited several times.<sup>10–13</sup> However, the rate constants are not in agreement and it is not clear how the kinetic data were fit to the rate expression.



$$-\frac{d[\text{ClO}_2]}{dt} = k[\text{OH}^-][\text{ClO}_2]^2 \quad (2)$$

In this work we show that an integrated rate expression can be used to determine reliable first-order and second-order rate constants for the mixed-order decay of  $\text{ClO}_2$  over a wide concentration range. Furthermore, we show that at low  $\text{ClO}_2$  concentrations the yield of  $\text{ClO}_2^-$  is greater than the yield of  $\text{ClO}_3^-$ . We attribute this behavior to the presence of the decay reaction in eq 3, where  $\text{ClO}_2$  oxidizes the solvent. The mixed-order integrated rate expression and the use of ion chromatographic measurements of  $\text{ClO}_2^-$  and  $\text{ClO}_3^-$  yields permit the identification of three pathways for the decay of  $\text{ClO}_2$ . The reaction orders and product yields are different for the proposed pathways, but all three mechanisms have base-assisted electron-transfer steps.<sup>14</sup>



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## Experimental Section

**Reagents.** All solutions were prepared with doubly deionized, distilled water. Chlorine dioxide was prepared as described elsewhere<sup>14</sup> and was protected from light and stored in a refrigerator. The stock ClO<sub>2</sub> solution was standardized spectrophotometrically at 359 nm ( $\epsilon = 1230 \text{ M}^{-1} \text{ cm}^{-1}$ ).<sup>15</sup> Commercially available NaClO<sub>2</sub> was recrystallized using a previously described procedure,<sup>16</sup> and its purity was determined by ion chromatography. Stock solutions of NaClO<sub>2</sub> were standardized spectrophotometrically at 260 nm ( $\epsilon = 154.0 \text{ M}^{-1} \text{ cm}^{-1}$ ).<sup>15</sup> Ionic strength,  $\mu$ , was adjusted to 1.0 M with recrystallized NaClO<sub>4</sub>.

**pH Measurement.** An Orion model 720A digital pH meter equipped with a Corning combination electrode was used for pH measurements. The electrode was calibrated with previously standardized HClO<sub>4</sub> and NaOH to correct pH to  $p[\text{H}^+]$  when  $pK_w$  is 13.60 (25.0 °C, 1.0 M NaClO<sub>4</sub>).<sup>17</sup>

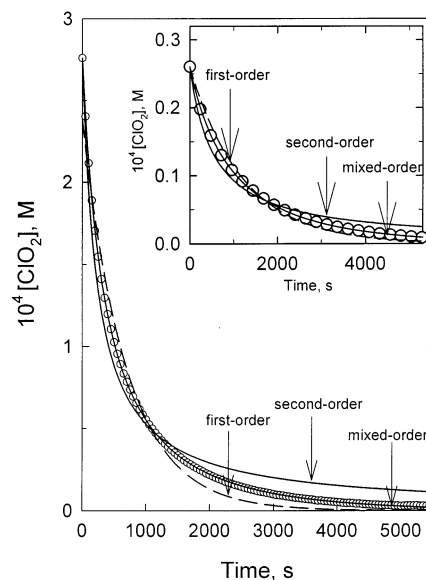
**Kinetics.** Kinetic traces for ClO<sub>2</sub> decay in base were acquired with a Perkin-Elmer Lambda 9 UV-vis-NIR spectrophotometer. The kinetics of the ClO<sub>2</sub> reaction with HO<sub>2</sub><sup>-</sup> were followed by use of an Applied PhotoPhysics SX18 MV stopped-flow spectrophotometer (APPSF, optical path length = 0.962 cm). These reactions were followed by measuring the loss of ClO<sub>2</sub> at 359 nm. SigmaPlot 8.0<sup>18</sup> was used for regression analyses.

**Product Analysis.** A Dionex DX-500 chromatograph was used to measure yields of ClO<sub>2</sub><sup>-</sup> and ClO<sub>3</sub><sup>-</sup> by a method similar to EPA 300.1.<sup>19</sup> Samples were injected via an autosampler (AS 40) through a 25  $\mu\text{L}$  injection loop onto quaternary amine anion-exchange guard (AG9 HC) and separation (AS9 HC) columns. Analytes were eluted with 9 mM Na<sub>2</sub>CO<sub>3</sub> at a flow rate of 1.0 mL/min. Gas-assisted suppressed-conductivity detection (ED 40), with an ASRS-Ultra suppressor in the self-regenerating mode and a current of 100 mA, was used to detect the analytes. Residual ClO<sub>2</sub> was purged with Ar prior to injection onto the column. Ionic strength was not adjusted in the stoichiometric analyses. The use of polypropylene as opposed to glass containers<sup>12</sup> and alternative preparation methods of ClO<sub>2</sub> synthesis<sup>20</sup> did not affect the product distribution.

**Computation.** Calculations were performed using the GAUSSIAN 98 program<sup>21</sup> to determine plausible structures for the reaction intermediates. Equilibrium geometries were optimized using the Becke three-parameter hybrid functional combined with the Lee, Yang, and Parr correlation (B3LYP) density functional theory method. Initial geometry optimizations were done at the B3LYP level of theory using the 6-311G(d) basis set. The calculations with the large 6-311++G(3df,3pd) basis set were also performed and included. All equilibrium geometries were fully optimized to better than 0.001 Å for bond distances and 0.1° for bond angles. All energies were corrected for zero-point energies as determined from harmonic vibrational frequency calculations.

## Results and Discussion

**Kinetics.** The decay of ClO<sub>2</sub> in basic solution (with excess [OH<sup>-</sup>]) does not fit the second-order dependence in [ClO<sub>2</sub>] that is given in eq 2, nor does it fit a simple first-order dependence in [ClO<sub>2</sub>]. As shown in Figure 1, the decay fits



**Figure 1.** Kinetic trace and regression results for the decomposition of ClO<sub>2</sub> in basic solution. Conditions: 0.37 mM ClO<sub>2</sub>; 0.40 M NaOH; 25.0–(2) °C;  $\mu = 1.0 \text{ M}$ . Circles are the experimental data. The mixed-order dependence in [ClO<sub>2</sub>] regression line is based on eq 5. Insert shows the decomposition of ClO<sub>2</sub> at 25  $\mu\text{M}$  levels, with all other conditions as above (circles). The mixed-order fit is obtained using eq 5.  $k_{a,\text{obsd}} = 6.19(3) \times 10^{-4} \text{ s}^{-1}$ , and  $k_{b,\text{obsd}} = 8.28(3) \text{ M}^{-1} \text{ s}^{-1}$ .

a mixed-order (combination of first-order and second-order) dependence in [ClO<sub>2</sub>] as given in eq 4. This is the case over a wide range of ClO<sub>2</sub> concentrations (see insert of Figure 1). An integrated rate expression (eq 5) gives excellent fits for all the kinetic data, where [ClO<sub>2</sub>]<sub>0</sub> is the initial concentration of ClO<sub>2</sub> and [ClO<sub>2</sub>]<sub>t</sub> is the concentration of ClO<sub>2</sub> at any time during the course of the reaction.

$$-\frac{d[\text{ClO}_2]}{dt} = k_{a,\text{obsd}}[\text{ClO}_2] + k_{b,\text{obsd}}[\text{ClO}_2]^2 \quad (4)$$

$$[\text{ClO}_2]_t = \frac{k_{a,\text{obsd}}[\text{ClO}_2]_0 e^{-k_{a,\text{obsd}}t}}{k_{a,\text{obsd}} + k_{b,\text{obsd}}([\text{ClO}_2]_0 - [\text{ClO}_2]_0 e^{-k_{a,\text{obsd}}t})} \quad (5)$$

This expression permits resolution of  $k_{a,\text{obsd}}$  and  $k_{b,\text{obsd}}$  values as the OH<sup>-</sup> concentration varies from 0.05 to 0.45 M (Figure 2) and shows that there is a first-order dependence in [OH<sup>-</sup>] for both  $k_{a,\text{obsd}}$  and  $k_{b,\text{obsd}}$  (eq 6). The resolved values are  $k_a = 1.38(8) \times 10^{-3} \text{ M}^{-1} \text{ s}^{-1}$  and  $k_b = 21.8(4) \text{ M}^{-2} \text{ s}^{-1}$  at 25.0 °C,  $\mu = 1.0 \text{ M}$ . The  $k_a$  value is a factor of 2.3 smaller and the  $k_b$  value is 1.3 larger than the corresponding values of Granstrom and Lee.<sup>10</sup> However, our stoichiometric studies show that  $k_a$  represents two first-order pathways rather than one. The data show, as will be detailed later, that ClO<sub>2</sub> decomposition proceeds by three concurrent pathways.

$$-\frac{d[\text{ClO}_2]}{dt} = k_a[\text{OH}^-][\text{ClO}_2] + k_b[\text{OH}^-][\text{ClO}_2]^2 \quad (6)$$

**Stoichiometry.** Ion chromatography shows that ClO<sub>2</sub><sup>-</sup> and ClO<sub>3</sub><sup>-</sup> are the only chlorine-containing products formed from the decomposition of ClO<sub>2</sub> in basic solution. However, the ratio of ClO<sub>2</sub><sup>-</sup> to ClO<sub>3</sub><sup>-</sup> is not 1:1 as required for the disproportionation reaction (eq 1) and reported by several

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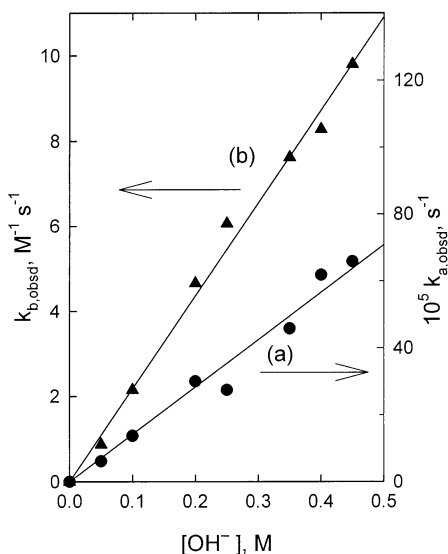
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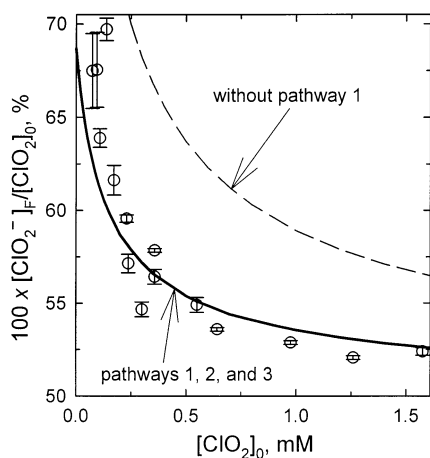
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**Figure 2.** Dependence of the observed rate constants on  $[\text{OH}^-]$ : (a)  $k_{a,\text{obsd}}$ ; (b)  $k_{b,\text{obsd}}$ . Conditions: 0.37 mM  $\text{ClO}_2$ ; 0.05–0.45 M NaOH; 25.0(2) °C;  $\mu = 1.0$  M.  $k_a = 1.38(8) \times 10^{-3} \text{ M}^{-1} \text{ s}^{-1}$ , and  $k_b = 21.8(4) \text{ M}^{-2} \text{ s}^{-1}$ .

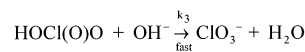
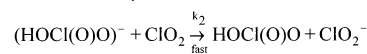
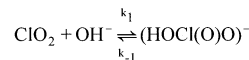


**Figure 3.** Effect of increasing  $[\text{ClO}_2]_0$  on the  $[\text{ClO}_2^-]_{\text{F}}/[\text{ClO}_2]_0$  ratio due to  $\text{ClO}_2$  decomposition in basic solution (circles). Conditions: 0.05–1.58 mM  $\text{ClO}_2$ ; 0.20 M NaOH. Predicted  $[\text{ClO}_2^-]_{\text{F}}/[\text{ClO}_2]_0$  is based on the relative contribution from pathways 1 and 2 following eq 15 (solid line).  $\alpha = 0.60(3)$ , and  $\beta = 0.40(2)$ . The dashed line is the predicted  $[\text{ClO}_2^-]_{\text{F}}/[\text{ClO}_2]_0$  ratio if only pathways 2 and 3 existed (eq 6, where  $k_a$  corresponds to pathway 2 only and  $k_b$  corresponds to pathway 3). The subscript F in  $[\text{ClO}_2^-]_{\text{F}}$  refers to the final levels of chlorite formed upon the completion of the  $\text{ClO}_2$  decay reaction.

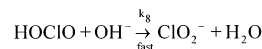
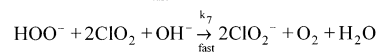
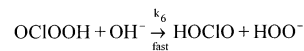
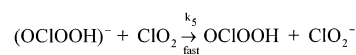
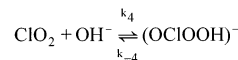
authors.<sup>8,10,12</sup> As shown in Figure 3, the percent yield of  $\text{ClO}_2^-$  becomes greater than that of  $\text{ClO}_3^-$  as the concentration of  $\text{ClO}_2$  decreases. At 74  $\mu\text{M}$   $\text{ClO}_2$ , the  $\text{ClO}_2^-$  yield is 67.5% of the chlorine-containing products while the  $\text{ClO}_3^-$  yield is only 32.5%. As will be shown, there is a need to introduce three pathways to account for all products formed. It is clear that something must be oxidized to balance the excess reduction to  $\text{ClO}_2^-$ , and oxidation of water is the only possibility. Therefore, we propose the formation of  $\text{O}_2$  (eq 3), a reaction that is thermodynamically very favorable in basic solution. The oxidation of water would proceed via peroxide intermediates, and it is known that  $\text{HO}_2^-$  reacts rapidly with  $\text{ClO}_2$  to form  $\text{O}_2$  and  $\text{ClO}_2^-$ .<sup>22</sup> To eliminate other possible pathways, we also tested to see if any  $\text{OCl}^-$  is

### Scheme 1. Proposed Mechanism for the Decomposition of Chlorine Dioxide in Basic Solution

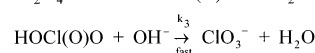
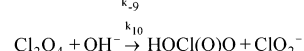
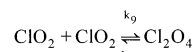
*Pathway 1.* First-order in  $[\text{ClO}_2]$ ; products:  $[\text{ClO}_2^-] = [\text{ClO}_3^-]$ .



*Pathway 2.* First-order in  $[\text{ClO}_2]$ ; products:  $\text{ClO}_2^-$  and  $\text{O}_2$ .



*Pathway 3.* Second-order in  $[\text{ClO}_2]$ ; products:  $[\text{ClO}_2^-] = [\text{ClO}_3^-]$ .

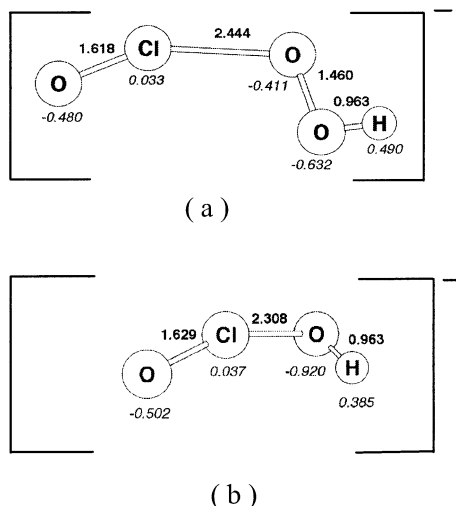


formed during  $\text{ClO}_2$  decomposition. A flow-through apparatus allowed a continuous stream of  $\text{ClO}_2(\text{g})$  to bubble slowly through a flask containing 0.20 M NaOH. This procedure allowed the  $\text{ClO}_2$  that decomposed to be replenished and maintained a  $\text{ClO}_2$  concentration of 0.10(2) mM in solution. Spectrophotometric analysis at two wavelengths (molar absorptivities ( $\text{M}^{-1} \text{ cm}^{-1}$ ) at 260 nm are  $\epsilon_{\text{OCl}^-} = 87.9$  and  $\epsilon_{\text{ClO}_2^-} = 154$ , and at 295 nm  $\epsilon_{\text{OCl}^-} = 356$  and  $\epsilon_{\text{ClO}_2^-} = 125$ ) was used to determine whether  $\text{OCl}^-$  was present. No  $\text{OCl}^-$  could be detected ( $< 1 \mu\text{M}$ ) under conditions where 0.57(1) mM  $\text{ClO}_2^-$  formed. Ion chromatographic results for these conditions show that 0.560(4) mM  $\text{ClO}_2^-$  and 0.436(5) mM  $\text{ClO}_3^-$  formed. The values obtained by the ion chromatographic method are more precise than those determined using spectrophotometry and are in agreement within the error.

Low concentrations of  $\text{ClO}_2$  favor  $\text{ClO}_2^-$  as a product compared to nearly equimolar levels of  $\text{ClO}_2^-$  and  $\text{ClO}_3^-$  formed at high  $\text{ClO}_2$  concentrations. This suggests that the second-order pathway, which is preferred at higher concentrations, is responsible for the products in eq 1. However, the second-order pathway is not sufficient to account for all the chlorate formed. This indicates the presence of two pathways with a first-order dependence in  $\text{ClO}_2$ , one produces equal amounts of  $\text{ClO}_2^-$  and  $\text{ClO}_3^-$  and the other forms  $\text{ClO}_2^-$  and  $\text{O}_2$ . The product distribution is not affected by changes of  $\text{OH}^-$  concentration because all pathways have first-order dependence in  $[\text{OH}^-]$ .

**Mechanism.** Scheme 1 shows the proposed mechanism with three concurrent pathways needed to account for the kinetic and stoichiometric results. Pathway 1 generates a species where  $\text{OH}^-$  adducts to the Cl atom of  $\text{ClO}_2$  to form an  $(\text{HOCl}(\text{O})\text{O})^-$  intermediate. This is similar to adducts proposed for  $\text{ClO}_2$  reactions with  $\text{HO}_2^-$ ,<sup>23</sup>  $\text{I}^-$ ,<sup>24</sup> and  $\text{S}_2\text{O}_3^{2-}$ .<sup>25</sup>

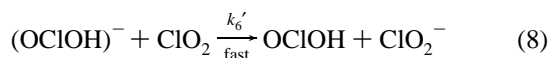
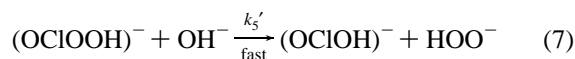
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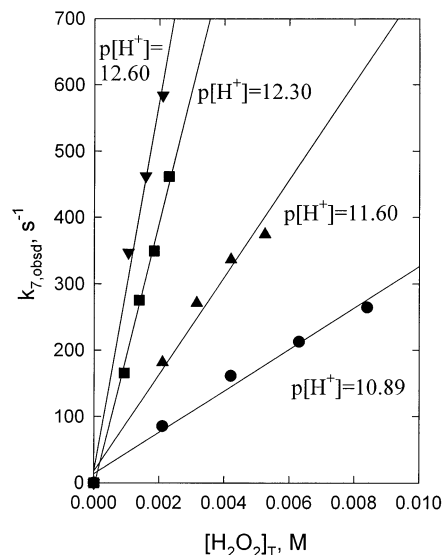
**Figure 4.** Equilibrium geometries (bond distances in Å) and atomic charges for the steady-state species (a)  $(\text{OCIOOH})^-$  and (b)  $(\text{OCIOH})^-$ . The numbers are reported for the B3LYP/6-311++G(3df,3pd) level of theory.

An ab initio calculation for the  $(\text{HOCl}(\text{O})\text{O})^-$  adduct<sup>14</sup> shows a weak, but significant, interaction between Cl and the OH group. The subsequent electron-transfer step ( $k_2$ ) is very rapid and generates  $\text{ClO}_2^-$  and  $\text{HOClO}_2$  (which reacts rapidly with  $\text{OH}^-$  ( $k_3$ ) to give  $\text{ClO}_3^-$ ). Hence, the reaction is first order in  $[\text{ClO}_2]$  and  $[\text{OH}^-]$  and forms equimolar  $\text{ClO}_2^-$  and  $\text{ClO}_3^-$ . The reactions in the  $k_1$  and  $k_2$  steps can be considered as an example of base-assisted electron transfer.<sup>14</sup>

In pathway 2 we propose  $\text{OH}^-$  forms an adduct to one of the oxygen atoms of  $\text{ClO}_2$  to give  $(\text{OCIOOH})^-$  ( $k_4$ ) as a reactive intermediate. An ab initio calculation of this species (Figure 4a) indicates a favorable intermediate where an OCl segment with a net charge of  $-0.447$  is weakly bound to an OOH segment with net charge of  $-0.553$ . This adduct can undergo rapid electron transfer with a second  $\text{ClO}_2$  ( $k_5$ ) to give  $\text{ClO}_2^-$  and  $\text{OCIOOH}$ . The latter species reacts favorably with  $\text{OH}^-$  to generate  $\text{HOClO}$  and  $\text{HOO}^-$  ( $k_6$ ). The reaction between  $\text{HOO}^-$  and  $\text{ClO}_2$  is known to give  $\text{ClO}_2^-$  and  $\text{O}_2$ , where  $k_7$  represents a series of rapid steps.<sup>22</sup> The stoichiometry for the overall reaction in pathway 2 is given in eq 3, where no  $\text{ClO}_3^-$  is formed. The reactions in the  $k_4$  and  $k_5$  steps can be considered as another example of a base-assisted electron-transfer process. Alternative steps for the reaction of  $(\text{OCIOOH})^-$  that lead to the same products are given in eqs 7 and 8. Ab initio calculations show that  $(\text{OCIOH})^-$  is a possible intermediate (Figure 4b).



Pathway 3 is second-order in  $\text{ClO}_2$  and proceeds via a  $\text{Cl}_2\text{O}_4$  intermediate that is in rapid preequilibrium with two  $\text{ClO}_2$  molecules ( $k_9/k_{-9}$ ). This intermediate was proposed by Halperin and Taube<sup>9</sup> and is similar to the proposed  $\text{BrO}_2^-$

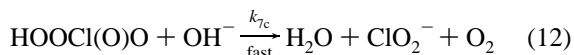
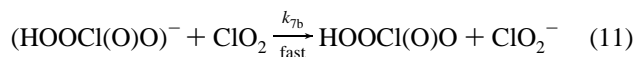


**Figure 5.** Effect of increasing  $[\text{H}_2\text{O}_2]_{\text{T}}$  on the rate of the  $\text{ClO}_2/\text{HO}_2^-$  reaction in the  $\text{p}[\text{H}^+]$  range 10.89 to 12.60. The reaction was followed at 359 nm, 25.0 °C,  $\mu = 1.0$  M, and 0.050 mM  $\text{ClO}_2$ .  $k_{7a} = 1.6(3) \times 10^5 \text{ M}^{-1} \text{ s}^{-1}$ .

$\text{ClO}_2$ <sup>14</sup> and  $\text{Br}_2\text{O}_4$ <sup>26</sup> intermediates. Ab initio calculations have been reported previously<sup>16</sup> for  $\text{Cl}_2\text{O}_4$ . The reaction of  $\text{Cl}_2\text{O}_4$  with  $\text{OH}^-$  in step  $k_{10}$  is another example of base-assisted electron transfer, in this case between two weakly associated  $\text{ClO}_2$  molecules.

**Hydrogen Peroxide Reaction with  $\text{ClO}_2$ .** Hoigné<sup>22</sup> assigned a rate constant of  $1.3(2) \times 10^5 \text{ M}^{-1} \text{ s}^{-1}$  for the reaction between  $\text{HOO}^-$  and  $\text{ClO}_2$  in the pH range 5–11 (temperature and other conditions were not specified). We measured the rate by stopped-flow methods from  $\text{p}[\text{H}^+] = 9.4$  to 12.6 by observing the loss of  $\text{ClO}_2$  under pseudo-first-order conditions where  $[\text{H}_2\text{O}_2]_{\text{T}} \gg [\text{ClO}_2]$ . Figure 5 shows the dependence of  $k_{7,\text{obsd}} (=k_{7a}[\text{HO}_2^-])$  on  $[\text{H}_2\text{O}_2]_{\text{T}}$  at several  $\text{p}[\text{H}^+]$  values. The rate expression is given in eq 9, where  $[\text{H}_2\text{O}_2]_{\text{T}} = [\text{H}_2\text{O}_2] + [\text{HOO}^-]$  and  $k_{7a}$  is the rate-determining step for the reaction sequence given in eqs 10–12. Our value of  $1.6(3) \times 10^5 \text{ M}^{-1} \text{ s}^{-1}$  for  $k_{7a}$ , at 25.0 °C and 1.0 M ionic strength, where  $K_{\text{a}}^{\text{H}_2\text{O}_2}$  is  $10^{-12.13} \text{ M}$ ,<sup>27</sup> is in good agreement with Hoigné's value. The reaction is independent of carbonate and phosphate (up to 80 mM) buffer concentrations. The  $k_{7a}$  rate constant for the  $\text{HOO}^-$  reaction is 9 orders of magnitude greater than the  $k_4$  rate constant in pathway 2 and therefore does not affect the reaction rate between  $\text{ClO}_2$  and  $\text{OH}^-$ .

$$\frac{-d[\text{ClO}_2]}{dt} = \left( \frac{2k_{7a}K_{\text{a}}^{\text{H}_2\text{O}_2}}{K_{\text{a}}^{\text{H}_2\text{O}_2} + [\text{H}^+]} \right) [\text{H}_2\text{O}_2]_{\text{T}}[\text{ClO}_2] \quad (9)$$



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**Table 1.** Summary of Rate Constants and Activation Parameters for the Decomposition of ClO<sub>2</sub> in Basic Solution

basic nucleophile	rate const <sup>a</sup>	$\Delta H^\ddagger$ , kJ mol <sup>-1</sup>	$\Delta S^\ddagger$ , J mol <sup>-1</sup> K <sup>-1</sup>
OH <sup>-</sup>	$k_a = 1.38(8) \times 10^{-3} \text{ M}^{-1} \text{ s}^{-1}$	60(2)	-101(6)
	$k_b = 21.8(4) \text{ M}^{-2} \text{ s}^{-1}$	32(2)	-119(7)
	$k_1 = 4.1(1) \times 10^{-4} \text{ M}^{-1} \text{ s}^{-1}$		
	$k_4 = 1.4(1) \times 10^{-4} \text{ M}^{-1} \text{ s}^{-1}$		
CO <sub>3</sub> <sup>2-</sup>	$(k_9/k_{-9})k_{10} = 10.9(2) \text{ M}^{-2} \text{ s}^{-1}$		
	$k_a^{\text{CO}_3} = 8.6(4) \times 10^{-4} \text{ M}^{-1} \text{ s}^{-1}$		
PO <sub>4</sub> <sup>3-</sup>	$k_b^{\text{CO}_3} = 6.7(2) \text{ M}^{-2} \text{ s}^{-1}$		
	$k_a^{\text{PO}_4} = 2.8(6) \times 10^{-5} \text{ M}^{-1} \text{ s}^{-1}$		
	$k_b^{\text{PO}_4} = 24(2) \text{ M}^{-2} \text{ s}^{-1}$		

<sup>a</sup> Conditions: 25.0 °C;  $\mu = 1.0 \text{ M NaClO}_4$ ;  $\lambda = 359 \text{ nm}$ .

**Detailed Rate Expressions and Resolved Rate Constants.** As the mechanism in Scheme 1 indicates, two ClO<sub>2</sub> radicals are consumed in pathways 1 and 3 while four are consumed in pathway 2. The rate expression in eq 13

$$\frac{-d[\text{ClO}_2]}{dt} = 2[\text{OH}^-][\text{ClO}_2] \left( \frac{k_1 k_2 [\text{ClO}_2]}{k_{-1} + k_2 [\text{ClO}_2]} + \frac{2k_4 k_5 [\text{ClO}_2]}{k_{-4} + k_5 [\text{ClO}_2]} + \frac{k_9 k_{10} [\text{ClO}_2]}{k_{-9} + k_{10} [\text{OH}^-]} \right) \quad (13)$$

$$\frac{-d[\text{ClO}_2]}{dt} = 2(k_1 + 2k_4)[\text{OH}^-][\text{ClO}_2] + \frac{2k_9 k_{10}}{k_{-9}} [\text{OH}^-][\text{ClO}_2]^2 \quad (14)$$

accounts for these stoichiometric factors and is derived on the basis of the assumption that (HOClO<sub>2</sub>)<sup>-</sup>, (OClOOH)<sup>-</sup>, and Cl<sub>2</sub>O<sub>4</sub> are each steady-state intermediates. If  $k_{-1} \ll k_2$ ,  $k_{-4} \ll k_5$ , and  $k_{-9} \gg k_{10}$ , the rate expression is simplified to eq 14 that agrees with our experimental observations. The agreement between the experimental data and the fit down to micromolar levels of ClO<sub>2</sub> (Figure 1, insert) suggests that values for  $k_2/k_{-1}$  and  $k_5/k_{-4}$  are larger than  $10^6 \text{ M}^{-1}$ . As seen from eqs 6 and 14, the first-order rate constant ( $k_a$ ) obtained from kinetic data equals  $2(k_1 + 2k_4)$  and the second-order rate constant ( $k_b$ ) equals  $2k_9 k_{10}/k_{-9}$ . Yields of ClO<sub>2</sub><sup>-</sup> and ClO<sub>3</sub><sup>-</sup> as a function of [ClO<sub>2</sub>] are needed to resolve the  $k_1$  and  $k_4$  values. A total of 15 sets of reactions with [ClO<sub>2</sub>]<sub>0</sub> varying from 0.074 to 1.58 mM in 0.20 M [OH<sup>-</sup>] were analyzed for ClO<sub>2</sub><sup>-</sup> and ClO<sub>3</sub><sup>-</sup> after 99.9% completion. Figure 3 shows the percent [ClO<sub>2</sub><sup>-</sup>]<sub>F</sub>/[ClO<sub>2</sub>]<sub>0</sub> as a function of the initial ClO<sub>2</sub> concentration. To resolve  $k_1$  and  $k_4$  values, kinetic traces were generated on the basis of eq 6 for the conditions in Figure 3. These traces were divided into 20 s intervals, and the amounts of ClO<sub>2</sub><sup>-</sup> and ClO<sub>3</sub><sup>-</sup> formed at the midpoint of each interval were calculated by successive approximation for 3000 data points. The summation of ClO<sub>2</sub><sup>-</sup> formed at each time interval to give [ClO<sub>2</sub><sup>-</sup>]<sub>F</sub> is expressed by eq 15, where  $\alpha$  and  $\beta$  are the relative contributions of pathways 1 and 2, respectively,  $m$  is the interval number, and  $n$  is the total number of intervals. Similarly, the [ClO<sub>3</sub><sup>-</sup>]<sub>F</sub> is given by eq 16, which needs only the  $\alpha$  value. The value of 0.5 in these equations corresponds to the disproportionation reactions

(pathways 1 and 3), where half of the ClO<sub>2</sub> lost forms ClO<sub>2</sub><sup>-</sup> and half forms ClO<sub>3</sub><sup>-</sup>. The regression analysis gives  $\alpha = 0.60(3)$  and  $\beta = 0.40(2)$ . The solid line in Figure 3 shows the fit of the experimental data to eq 15 (after multiplying by 100/[ClO<sub>2</sub>]<sub>0</sub>) and corresponds to  $k_1 = 4.1(4) \times 10^{-4} \text{ M}^{-1} \text{ s}^{-1}$  and  $k_4 = 1.4(1) \times 10^{-4} \text{ M}^{-1} \text{ s}^{-1}$  (Table 1). The dashed line shows that pathways 2 and 3 alone are not sufficient to account for the observed [ClO<sub>2</sub><sup>-</sup>]<sub>F</sub>/[ClO<sub>2</sub>]<sub>0</sub> ratio (eq 6, where  $k_a$  corresponds to pathway 2 only and  $k_b$  corresponds to pathway 3).

$$[\text{ClO}_2^-]_F = \sum_{m=1}^n \left( \frac{0.5(\alpha k_a + k_b([\text{ClO}_2]_{20m} + [\text{ClO}_2]_{20m-20})/2) + \beta k_a}{k_a + k_b([\text{ClO}_2]_{20m} + [\text{ClO}_2]_{20m-20})/2} \right) \times ([\text{ClO}_2]_{20m-20} - [\text{ClO}_2]_{20m}) \quad (15)$$

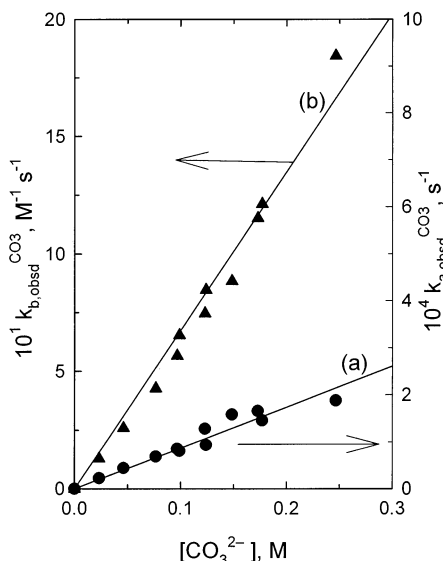
$$[\text{ClO}_3^-]_F = \sum_{m=1}^n \left( \frac{0.5(\alpha k_a + k_b([\text{ClO}_2]_{20m} + [\text{ClO}_2]_{20m-20})/2)}{k_a + k_b([\text{ClO}_2]_{20m} + [\text{ClO}_2]_{20m-20})/2} \right) \times ([\text{ClO}_2]_{20m-20} - [\text{ClO}_2]_{20m}) \quad (16)$$

**Temperature Dependence.** The decomposition reactions of 0.10 mM ClO<sub>2</sub> in 0.20 M NaOH at  $\mu = 1.0 \text{ M}$  were measured from 0.0 to 25.0 °C to resolve activation parameters for the composite rate constants,  $k_a$  and  $k_b$  (eq 6). The  $\Delta H^\ddagger$  values, 60(2) kJ mol<sup>-1</sup> for  $k_a$  and 32(2) kJ mol<sup>-1</sup> for  $k_b$ , are in substantial agreement with previous values.<sup>10</sup> The  $\Delta S^\ddagger$  values are -101(6) J mol<sup>-1</sup> K<sup>-1</sup> for  $k_a$  and -119(7) J mol<sup>-1</sup> K<sup>-1</sup> for  $k_b$ . The large negative  $\Delta S^\ddagger$  values for  $k_a$  ( $=2k_1 + 4k_4$ ) and for  $k_b$  ( $=2k_9 k_{10}/k_{-9}$ ) are consistent with the need to bring together several species in these composite rate constants. Eyring plots are given in Figure S3 (Supporting Information).

**Buffer Effects.** Basic carbonate and phosphate buffers accelerate the rate of ClO<sub>2</sub> decay, and the corresponding rate expressions are given in eq 17, where B = CO<sub>3</sub><sup>2-</sup> or PO<sub>4</sub><sup>3-</sup>.

$$\frac{-d[\text{ClO}_2]}{dt} = k_a^{\text{B}}[\text{B}][\text{ClO}_2] + k_b^{\text{B}}[\text{B}][\text{ClO}_2]^2 \quad (17)$$

We found no contribution from HCO<sub>3</sub><sup>-</sup> or HPO<sub>4</sub><sup>-</sup> to the rate of ClO<sub>2</sub> decay. Figure 6 shows the significant contribution of CO<sub>3</sub><sup>2-</sup> to both the first-order path ( $k_a^{\text{CO}_3} = 8.6(4) \times 10^{-4} \text{ M}^{-1} \text{ s}^{-1}$ ) and the second-order path ( $k_b^{\text{CO}_3} = 6.7(2) \text{ M}^{-2} \text{ s}^{-1}$ ), where  $k_{a,\text{obsd}}^{\text{B}} = k_a^{\text{B}}[\text{B}]$  and  $k_{b,\text{obsd}}^{\text{B}} = k_b^{\text{B}}[\text{B}]$ . By contrast, previous evaluation<sup>10</sup> gave  $k_a^{\text{CO}_3} = 7 \times 10^{-14} \text{ M}^{-1} \text{ s}^{-1}$  (a value too low to be measured) and  $k_b^{\text{CO}_3} = 2.45 \text{ M}^{-2} \text{ s}^{-1}$ . The rate constants for PO<sub>4</sub><sup>3-</sup> (Figure S4) are  $k_a^{\text{PO}_4} = 2.8(6) \times 10^{-5} \text{ M}^{-1} \text{ s}^{-1}$  and  $k_b^{\text{PO}_4} = 24(2) \text{ M}^{-2} \text{ s}^{-1}$ . In these studies, contributions from the OH<sup>-</sup> path were also observed with [OH<sup>-</sup>] = 6.3 × 10<sup>-3</sup> M and were taken into account. Product studies in both buffers (Table 2) show that the percent of ClO<sub>2</sub><sup>-</sup> formed increases as the concentration of ClO<sub>2</sub> decreases. This suggests that pathways analogous to pathway 2 also occur with carbonate and phosphate forming adducts



**Figure 6.** Dependence of (a)  $k_{a,obsd}^{CO_3}$  and (b)  $k_{b,obsd}^{CO_3}$  on  $[CO_3^{2-}]$  for  $ClO_2$  decomposition in basic solution. Conditions: 0.2 mM  $ClO_2$ ; 20–250 mM  $CO_3^{2-}$ ;  $p[H^+] = 9.4$ – $10.3$ ; 25.0 °C;  $\mu = 1.0$  M.  $k_a^{CO_3} = 8.6(4) \times 10^{-4} M^{-1} s^{-1}$ , and  $k_b^{CO_3} = 6.7(2) M^{-2} s^{-1}$ .

**Table 2.** Products of  $ClO_2$  Decomposition in the Presence of (a) Carbonate and (b) Phosphate Buffer

$[ClO_2]_0, \mu M$	$[ClO_2^-]_F, \mu M$	$[ClO_3^-]_F, \mu M$	$100[ClO_2^-]_F/[ClO_2]_0, \%$
(a) Decomposition of $ClO_2$ in Carbonate Buffer <sup>a-c</sup>			
43.0(6)	26.4(3)	16.6(5)	61(1)
69.6(6)	39.6(3)	30.0(5)	56.9(7)
83.0(4)	47.2(2)	35.8(4)	56.9(4)
124.2(7)	68.8(2)	55.4(7)	55.4(4)
167.4(3)	90.4(3)	77.00(8)	54.0(2)
217(1)	115.4(2)	101(1)	53.2(3)
256.4(5)	138.4(3)	118.0(4)	54.0(2)
(b) Decomposition of $ClO_2$ in Phosphate Buffer <sup>b-d</sup>			
50.6(7)	32.6(1)	18.0(6)	64.4(9)
76.4(9)	46.2(2)	30.2(8)	60.5(7)
90.0(6)	57.8(2)	32.2(5)	64.2(4)
131.8(7)	75.6(5)	56.2(5)	57.4(5)
164(1)	91(2)	72.6(6)	56(1)
210(1)	119.0(7)	91.4(8)	56.6(4)
248(1)	135.0(6)	113.4(9)	54.3(4)

<sup>a</sup>  $[CO_3]_T = 0.10$  M;  $p[H^+] = 10.2(1)$ ;  $pK_a(HCO_3^-) = 9.48$ ; 25.0 °C. <sup>b</sup> The error represents the standard deviation of at least three runs for each sample analyzed. <sup>c</sup> The subscript F in  $[ClO_2^-]_F$  and  $[ClO_3^-]_F$  refers to the final levels of chlorite and chlorate formed upon the completion of the  $ClO_2$  decay reaction. <sup>d</sup>  $[PO_4]_T = 0.10$  M;  $p[H^+] = 11.8(1)$ ;  $pK_a(HPO_4^{2-}) = 11.08$ ; 25.0 °C.

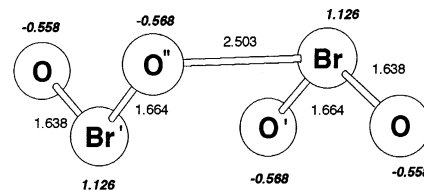
with  $ClO_2$  (i.e.  $(OCIOOCO_2)^{2-}$  and  $(OCIOOPO_3)^{3-}$  species). The ratios of  $k_a/k_b$  rate constants for these bases are  $1.28 \times 10^{-4}$  M for  $CO_3^{2-}$ ,  $6.33 \times 10^{-5}$  M for  $OH^-$ , and  $1.1 \times 10^{-6}$  M for  $PO_4^{3-}$ . Thus, the first-order pathways are more favorable for  $CO_3^{2-}$  than for  $OH^-$  and are less favorable for  $PO_4^{3-}$ .

**Comparison of the Reactions of  $ClO_2/ClO_2$ ,  $ClO_2/BrO_2$ , and  $BrO_2/BrO_2$  in Base.** The decomposition kinetics of  $ClO_2$  require basic nucleophiles ( $CO_3^{2-}$ ,  $PO_4^{3-}$ , and  $OH^-$ ) for both the first-order and the second-order pathways, whereas a much broader group of nucleophiles (that include  $Cl^-$ ,  $Br^-$ ,  $ClO_2^-$ ,  $SO_4^{2-}$ ,  $CH_3COO^-$ , and  $HPO_4^{2-}$  as well as  $CO_3^{2-}$ ,  $PO_4^{3-}$ , and  $OH^-$ ) assists the electron-transfer reactions between  $ClO_2$  and  $BrO_2$ .<sup>14</sup> Both the  $ClO_2/ClO_2$  and  $ClO_2/BrO_2$  reactions consume base and become much more

**Table 3.** Comparison of the Rate Constants for  $Cl_2O_4$ ,  $ClO_2BrO_2$ , and  $Br_2O_4$  Reactions with  $OH^-$

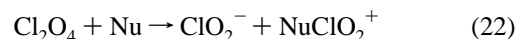
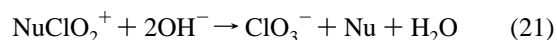
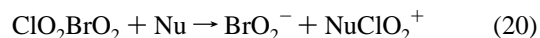
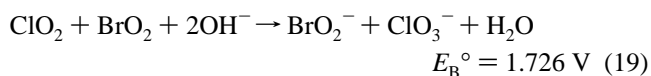
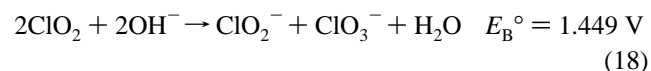
reacn	$K_9 k_{10}, M^{-2} s^{-1} a$
$2ClO_2 + OH^- \rightarrow ClO_2^- + HOClO_2$	10.9 <sup>b</sup>
$ClO_2 + BrO_2 + OH^- \rightarrow BrO_2^- + HOClO_2$	$1.25 \times 10^8$ <sup>c</sup>
$2BrO_2 + OH^- \rightarrow BrO_2^- + HOBrO_2$	$1.3 \times 10^{13}$ <sup>d,e</sup>

<sup>a</sup>  $K_9 = k_9/k_{-9}$ . <sup>b</sup> This work. <sup>c</sup> Reference 14. <sup>d</sup> Reference 26. <sup>e</sup> Reference 28.



**Figure 7.** Equilibrium geometries (bond distances in Å) and atomic charges (italics) for  $OBrOBr(O)O$ . The numbers are reported for the B3LYP/6-311++G(3df,3pd) level of theory.

favorable thermodynamically as the hydroxide ion concentration increases as shown by the redox potentials in eqs 18 and 19. The reactions of nucleophiles (Nu) with  $ClO_2/BrO_2$  have been proposed<sup>14</sup> to first generate  $NuClO_2^+$  and  $BrO_2^-$  (eq 20). These  $NuClO_2^+$  species then react with  $OH^-$  to give  $ClO_3^-$  and release Nu (eq 21). A similar process for  $Cl_2O_4$  would correspond to eq 22, which would be followed by a step analogous to eq 21. However, the reaction in eq 22 is thermodynamically less favorable than that in eq 20 because the reduction potential for  $BrO_2/BrO_2^-$  is favored over that of  $ClO_2/ClO_2^-$  by 0.28 V. The intermediate  $NuClO_2^+$  in eq 22 appears to be more difficult to form unless Nu is a strong base.



Third-order rate constants ( $M^{-2} s^{-1}$ ) for reactions of the halogen dioxides with  $OH^-$  (Table 3) increase by 12 orders of magnitude for the following sequence:  $ClO_2 + ClO_2$ ;<sup>16</sup>  $ClO_2 + BrO_2$ ;<sup>14</sup>  $BrO_2 + BrO_2$ .<sup>26,28,29</sup> Much of this enormous change in reactivity can be attributed to the relative stabilities of  $Cl_2O_4$ ,<sup>16</sup>  $ClO_2BrO_2$ ,<sup>14</sup> and  $Br_2O_4$  (Figure 7, Table S6), where the association constants of the halogen dioxide increase by a factor of  $3 \times 10^5$  from  $Cl_2O_4$  to  $Br_2O_4$  on the basis of our ab initio calculations. The relative rate of  $OH^-$  reaction with the halogen dioxide dimers increases greatly from  $Cl_2O_4$  to  $Br_2O_4$ .

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**Deviation from Marcus Theory.** An alternative possibility for pathway 1 is a direct electron transfer between  $\text{ClO}_2$  and  $\text{OH}^-$  to form  $\text{ClO}_2^-$  and  $\text{OH}$ . A subsequent reaction of  $\text{OH}$  and  $\text{ClO}_2$  would give  $\text{HClO}_3$ . Table S3 gives rate constants determined for the reaction of  $\text{ClO}_2$  with  $\text{OH}^-$  and  $\text{HO}_2^-$  ( $k_{\text{meas}}$ ) as well as the electron-transfer reactions of  $\text{ClO}_2$  with  $\text{NO}_2^-$ ,<sup>30</sup>  $\text{N}_3^-$ ,<sup>31</sup>  $\text{SO}_3^{2-}$ ,<sup>32</sup> and  $\text{SCN}^-$ <sup>33</sup> on the basis of Marcus theory.<sup>34</sup> Self-exchange rate constants<sup>35</sup> and redox potentials<sup>36</sup> have been compiled by Stanbury. The measured rate constant for the  $\text{ClO}_2/\text{OH}^-$  reaction ( $k_{\text{meas}} = k_1$ ) is  $2 \times 10^4$  times larger than expected by Marcus theory. Previous studies have discussed inner-sphere mechanisms, orbital overlap of reactants, and solvent nonadditivity as factors

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responsible for the large deviation from the traditional Marcus theory in the case of small molecules.<sup>31</sup> We propose that the large deviation from the Marcus theory is an indication that the measured rate constants represent adduct formation reactions rather than actual electron-transfer processes. The mechanism proposed in Scheme 1 shows that the adduct in  $k_1$  has to form first for the electron transfer in  $k_2$  to take place. Pathways 2 and 3 also involve adduct formation followed by electron transfer. In the case of  $\text{HOO}^-$ , a similar mechanism is shown in eqs 10 and 11 and is in agreement with the proposed mechanism by Ni and Wang.<sup>23</sup> Recent work in the Margerum group<sup>14</sup> has shown that when  $\text{ClO}_2$  reacts with  $\text{BrO}_2$ , an adduct formation with a nucleophile is needed first to allow an electron-transfer process to occur.

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**Supporting Information Available:** Tables and figures with supplemental kinetic and product data, the derivation of eq 5, and the detailed method for use of eqs 15 and 16. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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