

# A Computational Study of the Nondissociative Mechanisms that Interchange Apical and Equatorial Atoms in Square Pyramidal Molecules

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The lowest energy transition state for the nondissociative apical/equatorial atom exchange mechanism for three square pyramidal AEX<sub>5</sub> molecular species was calculated (CCSD(T)/pVTZ; B3LYP/pVTZ, aug-cc-pV5Z) to have a hemidirected geometry with C<sub>s</sub> symmetry for BrF<sub>5</sub>, IF<sub>5</sub>, and XeF<sub>5</sub><sup>+</sup>. In contrast, holodirected C<sub>2v</sub>-symmetric transition states for this process were located for the AEX<sub>5</sub> square pyramidal molecules ClF<sub>5</sub>, ICl<sub>5</sub>, and IBr<sub>5</sub>. Imaginary frequencies were calculated and examined in a visual/dynamic fashion to gain insight into these fluxional processes. Although both mechanisms exchange one apical for one equatorial atom in each cycle of motion, processes that pass through C<sub>2v</sub> transition states have characteristic features of the well-known Berry pseudorotation and Lever mechanisms while those which pass through transition states of C<sub>s</sub> symmetry have features that are a mixture of Berry, Lever, and turnstile-like character. Two periodic trends are observed: as the atomic number on the central atom increases (same terminal atoms), the barrier for apical/equatorial exchange and the value of the imaginary frequency both decrease. Similarly, as the atomic number of the terminal atoms increase (same central atom), the barrier for apical/equatorial exchange decreases, as does the computed imaginary frequency.

## Introduction

Motions that exchange symmetry nonequivalent atoms within a molecule, referred to as fluxional processes or nondissociative exchange mechanisms, are documented for many chemical species. Two very well-known examples are the axial/equatorial hydrogen exchange in cyclohexane,<sup>1</sup> and the Berry pseudorotation (BPR) that exchanges the axial and equatorial atoms in trigonal bipyramidal molecules such as PF<sub>5</sub>.<sup>2</sup> Similar mechanisms, that interchange symmetry nonequivalent terminal atoms in a nondissociative fashion, have been reported in the literature for several other small molecules: These include the Lever mechanism (observed for ClF<sub>3</sub> and in one high-energy pathway for SF<sub>4</sub>),<sup>3,4</sup> the BPR for disphenoidal molecules, (observed for SF<sub>4</sub>, for X(CH<sub>3</sub>)<sub>4</sub>

where X = S, Se, and Te, and in X(R'N–CR–NR')<sub>2</sub> where X = Si, Ge, Sn, and Pb),<sup>4–6</sup> the turnstile mechanism (experimentally observed in the fluxional processes of several Mo(II) complexes<sup>7</sup> and calculated for the cis/trans isomerization for SF<sub>4</sub>Cl<sub>2</sub><sup>8</sup>) and the Bartell Mechanism observed for apical/equatorial atom exchange in IF<sub>7</sub>.<sup>9</sup> Animations of

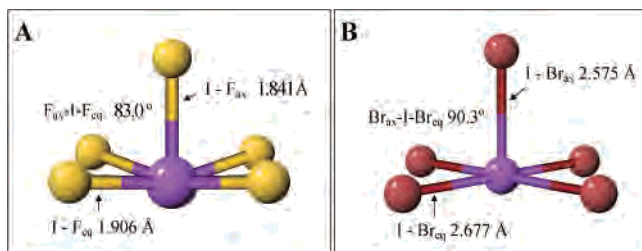
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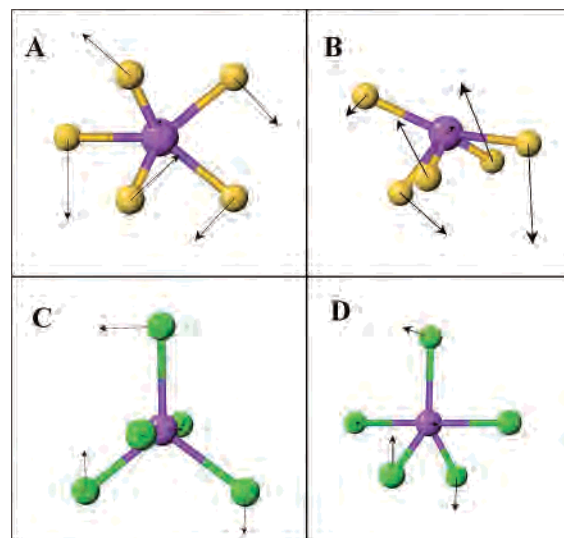
**Figure 1.** Equilibrium geometries for (A) IF<sub>5</sub> (B3LYP/aug-cc-pV5Z-pp) and (B) IBr<sub>5</sub> (B3LYP/pVTZ).

Ⓜ Animations of the apical/equatorial atom exchange mechanisms for ClF<sub>5</sub>, BrF<sub>5</sub>, IF<sub>5</sub>, ICl<sub>5</sub>, IBr<sub>5</sub>, and XeF<sub>5</sub><sup>+</sup> are available, together with animations for the pure BPR mechanism of apical/equatorial atom exchange for PF<sub>5</sub>, the pure Lever mechanism of apical/equatorial atom exchange for ClF<sub>3</sub> and the pure turnstile mechanism of apical/equatorial atom exchange for SF<sub>4</sub>Cl<sub>2</sub>. Equilibrium geometries (giving bond lengths and bond angles) and transition state structures are included.

the BPR in PF<sub>5</sub>, the Lever Mechanism in ClF<sub>3</sub>, and the turnstile mechanism can be found in ref 8 and/or in our supplemental material [enhanced Web objects 9a, 9b, and 9c, respectively] for comparison to the mechanisms described herein.

Surprisingly, very little quantitative information is available on the apical/equatorial atom exchange in square pyramidal AEX<sub>5</sub> molecules (using VSEPR nomenclature where A represents the central atom, E an electron lone pair, and X the terminal atoms). Representative square pyramidal ground-state structures of IF<sub>5</sub> and IBr<sub>5</sub> are shown in Figure 1. Early variable-temperature <sup>19</sup>F NMR studies on IF<sub>5</sub>, BrF<sub>5</sub>, and ClF<sub>5</sub> showed<sup>10,11</sup> that these three species were stable to apical/equatorial exchange at room temperature, implying barriers for the process of greater than approximately 25 kcal mol<sup>-1</sup>. No terminal atom exchange was observed for BrF<sub>5</sub> at elevated temperatures; however, under the same conditions, IF<sub>5</sub> began to lose F–F coupling and then broaden, characteristic of apical/equatorial atom exchange.<sup>10</sup> Although the exchange was proposed to proceed through an associative/dissociative process (via either bridging fluorines in dimers or by heterolytic dissociation), this early research established that the barrier for any fluxional process in these square pyramidal molecules, regardless of whether they are associative/dissociative or nondissociative, must be significantly larger than the barriers observed for similar small molecules such as PF<sub>5</sub> and IF<sub>7</sub> which are known to be highly fluxional.

We report herein our computational study of the nondissociative mechanisms that interchange apical and equatorial atoms in the square pyramidal AEX<sub>5</sub> molecular species ClF<sub>5</sub>, BrF<sub>5</sub>, IF<sub>5</sub>, ICl<sub>5</sub>, IBr<sub>5</sub>, and XeF<sub>5</sub><sup>+</sup>. We have found that these nondissociative exchange mechanisms proceed through one of two pathways; one that proceeds through a C<sub>s</sub> transition state (for BrF<sub>5</sub>, IF<sub>5</sub>, and XeF<sub>5</sub><sup>+</sup>) which we describe as “hemidirected”, or through a C<sub>2v</sub> transition state (for ClF<sub>5</sub>, ICl<sub>5</sub>, and IBr<sub>5</sub>) which we describe as “holodirected”. We have



**Figure 2.** (A and B) Two orientations of the hemidirected C<sub>s</sub> transition state for BrF<sub>5</sub> shown with the displacement vectors of the calculated imaginary frequency. View B illustrates “the void” of coordinated atoms in the top hemisphere of the structure. (C and D) Two orientations of the holodirected C<sub>2v</sub> transition-state structure for ICl<sub>5</sub> also showing the displacement vectors for the calculated single imaginary frequency. Note that the mode of the imaginary frequency primarily involves the four coplanar (three equatorial Cl’s and the central I) atoms.

borrowed the holodirected and hemidirected descriptors from the literature, where they are used to denote the distribution of ligands around the central metal ion in complexes of, e.g., lead or tin. A holodirected geometry is one “in which the bonds to ligands atoms are distributed throughout the surface of an encompassing globe”.<sup>12</sup> In contrast a hemidirected geometry is one “in which the bonds to ligand atoms are directed throughout only part of an encompassing globe, i.e., there is an identifiable void in the distribution of bonds to the ligands.”<sup>12</sup> Application of these descriptors to our two transition-state geometries seems wholly appropriate, as the C<sub>s</sub> transition state clearly has “a void” on one side (see Figure 2B), and in the C<sub>2v</sub> transition state, the terminal atoms are “distributed throughout” the surface of an encompassing globe (Figure 2C and D).

In addition to examining the geometry and symmetry of the transition states in these reactions, we have also examined the motion of the apical/equatorial exchange mechanisms by animating the calculated imaginary frequency of the transition state. Following either the positive or the negative displacement of the imaginary frequency along the potential surface lowers the energy and eventually would lead to either the reactant or the product of the reaction. We can therefore use the output vibrational information from our computation to visually examine the operative exchange mechanism for a molecule under question. We observe distinctly different types of motion based on whether the mechanism proceeds through a hemidirected C<sub>s</sub> transition state or a holodirected C<sub>2v</sub> transition state. Visual/dynamic analysis was crucial to our understanding of these mechanisms and we therefore strongly encourage the reader to go to our supplemental

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**Table 1.** Calculated Energies for Nondissociative Fluxional Apical/Equatorial Atom Exchange in Square Pyramidal AEX<sub>5</sub> Molecules

AEX <sub>5</sub>	calculation method/ basis set	ground-state energy in Hartrees	symmetry	barrier kcal/mol	imaginary frequency in cm <sup>-1</sup>	WEO ref	notes	
ClF <sub>5</sub>	CCSD(T)/pVTZ	-957.62901	C <sub>s</sub>	40.5	—		<i>a</i>	
			C <sub>2v</sub>	33.4	—		<i>b</i>	
	B3LYP/aug-cc-pV5Z	-959.35502	C <sub>s</sub>	40.2	199.4	199.4	Suppl. 3b	<i>c</i>
			C <sub>2v</sub>	36.5	328.5	328.5	Suppl. 3a	
	B3LYP/pVTZ	-959.21305	—	—	—	—		<i>d</i>
			C <sub>2v</sub>	29.1	267	267		<i>ef</i>
KMLYP/pVTZ	-957.84872	C <sub>s</sub>	53.2	251.1	251.1			
		C <sub>2v</sub>	57.3	454.1	454.1			
BrF <sub>5</sub>	CCSD(T)/pVTZ	-3071.01275	C <sub>s</sub>	35.6	—		<i>a</i>	
			C <sub>2v</sub>	36.8	—		<i>b</i>	
	B3LYP/aug-cc-pV5Z	-3073.45244	C <sub>s</sub>	31.9	171.3	171.3		<i>g</i>
			C <sub>2v</sub>	31.9	254.2	254.2	Suppl. 4b	<i>g</i>
	B3LYP/pVTZ	-3073.26470	C <sub>s</sub>	31.9	171.2	171.2	Suppl. 4a	<i>h</i>
			C <sub>2v</sub>	29.3	240.6	240.6		
KMLYP/pVTZ	-3071.26094	C <sub>s</sub>	43.9	214.1	214.1		<i>hf</i>	
		C <sub>2v</sub>	54.3	371.7	371.7			
IF <sub>5</sub>	CCSD(T)/pVTZ	-7416.65020	C <sub>s</sub>	29.3	—		<i>a</i>	
			C <sub>2v</sub>	49.5	—		<i>b</i>	
	B3LYP/aug-cc-pV5Z-pp	-797.17427	C <sub>s</sub>	24.7	139.8	139.8	Suppl. 5a	<i>i</i>
			C <sub>s</sub>	26.7	150.6	150.6		<i>j</i>
	B3LYP/pVTZ	-7419.82665	C <sub>s</sub>	44.8	180.3	180.3	Suppl. 5b	<i>k</i>
			C <sub>2v</sub>	40.9	258.0	258.0	Suppl. 5c	<i>l</i>
KMLYP/pVTZ	-7417.18400	C <sub>s</sub>	32.3	172.5	172.5		<i>f</i>	
		D <sub>3h</sub>	76.7	285.7	285.7		<i>m</i>	
ICl <sub>5</sub>	B3LYP/pVTZ	-9221.58867	C <sub>2v</sub>	11.5	69.3	69.3	Suppl. 6a	<i>e</i>
			D <sub>3h</sub>	11.7	44.2	44.2	Suppl. 6b	<i>k</i>
	KMLYP/pVTZ	-9217.79738	C <sub>s</sub>	29.9	93.4	93.4		<i>f</i>
			C <sub>2v</sub>	28.6	157.4	157.4		<i>f</i>
IBr <sub>5</sub>	B3LYP/pVTZ	-19791.25590	C <sub>2v</sub>	4.9	25.2	25.2	Suppl. 7	<i>h</i>
	KMLYP/pVTZ	-19784.21444	C <sub>2v</sub>	19.1	80.5	80.5	—	<i>h</i>
XeF <sub>5</sub> <sup>+</sup>	B3LYP/cc-pV5Z-pp	-828.17381	C <sub>s</sub>	28.3	154.4	154.4	Suppl. 8	<i>n</i>

<sup>a</sup> CCSD(T) energy at CCSD geometry. No frequencies available. <sup>b</sup> 3- $\zeta$  on F, Cl, coupled cluster singles doubles. <sup>c</sup> Correlation consistent aug-5- $\zeta$  on F, Cl. <sup>d</sup> Geometry collapses to ground state. <sup>e</sup> 3- $\zeta$  on F, Cl. <sup>f</sup> KMLYP method. <sup>g</sup> Correlation consistent aug-5- $\zeta$  on F, Br.  $\Delta G_{298}^\ddagger$  30.5 (C<sub>s</sub>/28.8 (C<sub>2v</sub>) kcal mol<sup>-1</sup>. <sup>h</sup> 3- $\zeta$  on F, Br. <sup>i</sup> Correlation consistent aug-5- $\zeta$  on F, aug-5- $\zeta$ +ECP on I.  $\Delta G_{298}^\ddagger$  23.8 kcal mol<sup>-1</sup>. <sup>j</sup> 3- $\zeta$  on F, I. <sup>k</sup> Transition mode degenerate. <sup>l</sup> Second imaginary mode -75.3 cm<sup>-1</sup>. <sup>m</sup> Third imaginary mode: -110.0 reduces symmetry to C<sub>3v</sub>. <sup>n</sup> Correlation consistent aug-5- $\zeta$  on F, aug-5- $\zeta$ +ECP on Xe.

material to view the three-dimensional animations that we have provided which include interactive content to illustrate the points we will make within this paper.

## Results

**Ground-State Structures.** The computed ground-state structures of ClF<sub>5</sub>, BrF<sub>5</sub>, IF<sub>5</sub>, ICl<sub>5</sub>, IBr<sub>5</sub>, and XeF<sub>5</sub><sup>+</sup> all have square pyramidal geometry with C<sub>4v</sub> symmetry. Computational methods and ground-state energies are listed in Table 1. The computational methods were chosen to match those carried out to locate transition states and are therefore discussed *vide infra*. All species are AEX<sub>5</sub> VSEPR structures with one central atom (A), one electron pair (E), and five terminal atoms: one in an apical position and four others sitting in symmetry-equivalent equatorial positions. The geometry varies only slightly within the series from a nearly perfect square pyramid in IBr<sub>5</sub> (Figure 1B) to a somewhat distorted square pyramidal structure for IF<sub>5</sub> (Figure 1A) with F<sub>axial</sub>—I—F<sub>equatorial</sub> angles of 83.0°. (See Supplement 1 for three-dimensional movable images of the equilibrium geometry computed for each molecular species in this study and for the comparison of computed bond lengths and angles to those reported in the literature for known structures).

**Transition-State Structures.** The fluxional processes for all of the molecules examined in this study have motions that appear to have some mixture of the physical characteristics of the BPR, turnstile, and Lever mechanisms. The molecules that have fluxional processes that pass through transition states with C<sub>s</sub> symmetry (BrF<sub>5</sub>, IF<sub>5</sub>, and XeF<sub>5</sub><sup>+</sup>) exhibit characteristics from all three motions; Berry, turnstile, and Lever. In recognition of this mixed character, we have christened this a “chimeric pseudorotation”.<sup>8</sup> In contrast, ClF<sub>5</sub>, ICl<sub>5</sub>, and IBr<sub>5</sub> pass through transition states of C<sub>2v</sub> symmetry and exhibit only Lever and Berry character, with dominance of the Lever character in transition states that approach D<sub>3h</sub> symmetry (to see animations of the BPR, Lever, and turnstile mechanisms, see Supplement 9a, 9b, and 9c, respectively, or to the animations provided in ref 8).

Transition states were located using the following protocols (see Table 1); (a) using the triple- $\zeta$  basis reported by Sadlej<sup>13</sup> and the B3LYP density functional hybridization. (b) We have previously reported on inter-halogen compounds<sup>14</sup> for which

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a different hybridization of the density functional approach known as KMLYP<sup>15</sup> was suggested as resulting in improved treatment of the electron correlation of such systems with reference to the more complete (but computationally very much slower) coupled cluster (CCSD(T)) approach. (c) We include here several results at the CCSD level (for optimized geometries) and CCSD(T) for single-point energies for comparison. (d) To evaluate behavior toward the basis set limit, calculations at the correlation consistent 5- $\zeta$  level (aug-cc-pV5Z) level are also included.

**Transition States of  $C_s$  Symmetry (Hemidirected).** The nondissociative apical/equatorial atom exchange mechanisms for BrF<sub>5</sub>, IF<sub>5</sub>, and XeF<sub>5</sub><sup>+</sup> proceed through transition states that have  $C_s$  symmetry. Two orientations of the  $C_s$  transition state for BrF<sub>5</sub> are shown in Figure 2A and B.

**BrF<sub>5</sub>.** Each method predicts both  $C_s$  and  $C_{2v}$  symmetric transition states to coexist on the potential surface and to be relatively similar in energy. B3LYP/cc-pV5Z and B3LYP/pVTZ indicate the  $C_{2v}$  transition state to be lower in energy than that of the  $C_s$  transition state, although for the former, it is only by 0.1 kcal/mol. The CCSD(T) and KMLYP calculations both found the  $C_s$  geometry as having the lowest energy, and we assign the fluxional behavior in BrF<sub>5</sub> to proceed through a true transition state of  $C_s$  symmetry. Animation of the single computed imaginary frequency can be viewed in Supplement 4a. Animation of the imaginary frequency calculated for the  $C_{2v}$  stationary point of higher energy can be found in Supplement 4b for comparison.

**IF<sub>5</sub>.** Only a transition state of  $C_s$  geometry with a single imaginary frequency could be located for IF<sub>5</sub> at any of the computational methods. The form of this mode when animated (Supplement 5a) shows what we term chimeric behavior. Stationary points with  $D_{3h}$  symmetry and  $C_{2v}$  symmetry were also located; the former stationary point has a degenerate (E) imaginary mode; animation of each mode (Supplement 5b) illustrates that one has a combined Lever and Berry character, while the other mixes Berry character with a stretching motion. The stationary point of lower  $C_{2v}$  also yields two imaginary frequencies, but these are no longer degenerate. The larger of these shows both Lever and Berry character and the smaller shows a “wag” nature that does not result in the exchange of apical and equatorial atoms but if followed reduces the symmetry further to  $C_s$  (see Supplement 5c for visualization of these imaginary frequencies).

**XeF<sub>5</sub><sup>+</sup>.** A transition state of  $C_s$  symmetry with a single imaginary frequency was the only one that could be located. Examination of the animation of the imaginary frequency (Supplement 8) confirms that the mode is chimeric in nature.

**Transition States of  $C_{2v}$  Symmetry (Holodirected).** The nondissociative apical/equatorial atom exchange mechanisms for ClF<sub>5</sub>, ICl<sub>5</sub>, and IBr<sub>5</sub> proceed through transition states that have  $C_{2v}$  rather than  $C_s$  symmetry. Two orientations of the

$C_{2v}$  transition state for ICl<sub>5</sub> are shown in Figure 2C and D. Other symmetries ( $C_s$  and  $D_{3h}$ ) were also explored.

**ClF<sub>5</sub>.** Although a transition state of  $C_s$  symmetry can be located using the KLMYP hybrid, which is lower in energy than that found for  $C_{2v}$  symmetry, the CCSD(T) and B3LYP calculations both invert this energy ordering, predicting  $C_{2v}$  to be the true transition state with the appropriate single imaginary frequency and displacement coordinates. On the basis that the CCSD(T) method is likely to give the most reliable result, we conclude that the apical/equatorial exchange mechanism for ClF<sub>5</sub> proceeds through a  $C_{2v}$ -symmetric transition state. Examination of the animated imaginary frequency for this transition state (Supplement 3a) allows one to recognize the Berry-like and Lever-like character. Unlike the apical/exchange mechanisms that proceed through a  $C_s$  transition state, no twisting (turnstile) motion is observed. The four atoms contained within the plane involved in the Lever motion show no out-of-plane deformation, as is illustrated (in the analogous ICl<sub>5</sub> case) by the vectors in Figure 2C and D, and can be observed in a visual/dynamic fashion in Supplement 3a. We have found this absence of out-of-plane deformation to be a signature of mechanisms proceeding through  $C_{2v}$  transition states in apical/equatorial exchange for the square planar AEX<sub>5</sub> molecules in our study. The imaginary mode calculated for the  $C_s$  stationary point was also animated and is presented in Supplement 3b for comparison.

**ICl<sub>5</sub>.** B3LYP and KLMYP DFT calculations enable location of a true transition state of  $C_{2v}$  symmetry for ICl<sub>5</sub> with a single imaginary frequency. Only the KMLYP procedure enables a second transition state of  $C_s$  symmetry (of higher energy) to be located. This system is too large for a CCSD(T) calculation to be performed, but extrapolating from the previous CCSD(T) results suggest that KMLYP overemphasizes the stability of the  $C_s$  structure. Animation of the displacement vectors for the imaginary frequency for the  $C_{2v}$  transition state (Supplement 6a) illustrates that the mode, like that observed for ClF<sub>5</sub>, has no out-of-plane deformation for the atoms involved in the Lever motion. Unlike in ClF<sub>5</sub>, however, the mode is predominantly Lever in character and only exhibits a small amount of Berry-like character. The stationary point of  $D_{3h}$  symmetry for ICl<sub>5</sub> has also been calculated, and the degenerate imaginary frequencies have been animated (Supplement 6b). Analogous to the  $D_{3h}$  stationary point found for IF<sub>5</sub>, this stationary point has a degenerate mode: one is of primary Lever character, and the other mode is of Berry-like character, mixed with a stretching motion.

**IBr<sub>5</sub>.** B3LYP and KLMYP calculations for IBr<sub>5</sub> both allow only location of a transition state with  $C_{2v}$  symmetry, with a lower barrier than that observed for ICl<sub>5</sub>. Animation of the single imaginary frequency found in the calculation (Supplement 7) illustrates that the mode has no out-of-plane deformation for the atoms involved in the Lever motion. This mode is even more dominantly Lever in character than that observed for ICl<sub>5</sub> and exhibits an almost undetectable degree of Berry-like character. Attempts to locate a stationary point

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(15) Kang, J. K.; Musgrave, C. B. *J. Chem. Phys.* **2001**, *115*, 11040–51. Senosiain, H. J. P.; Musgrave, C. B.; Golden, D. M. *Faraday Discuss.* **2001**, *119*, 173–89.

of  $C_s$  symmetry result in collapse of the geometry to a ground-state structure/energy.

**Basis Set and Correlation Effects.** In general, the triple- and the 5- $\zeta$  (aug-cc-pV5Z) basis sets are fairly congruent, the largest deviation being the predicted barrier for  $\text{ClF}_5$  and associated imaginary mode frequency. More difference is observed between the B3LYP and KMLYP density functional hybrids; the former favoring  $C_{2v}$  symmetry, the latter  $C_s$ . Adjudication using the CCSD(T) procedure for  $\text{BrF}_5$  suggests the most realistic estimate of the balance between the two symmetries is closer to that predicted by the B3LYP than the KMLYP method; use of the latter should probably be deprecated for such systems. The barrier heights predicted by B3LYP and CCSD(T) agree very well, and again, KMLYP appears to significantly overestimate their values. No accurately measured experimental values are available for comparison.

## Discussion

Computationally, we have located a transition state that links two ground-state structures via a nondissociative apical/equatorial atom exchange process for all of the  $\text{AEX}_5$  molecular species examined in this study. In all cases, the nondissociative process exchanges one apical atom for one equatorial atom in a single concerted motion. This one-for-one exchange can be easily visualized in our supplemental materials, where we have provided animations to view the exchange mechanisms. Although each cycle exchanges only two atoms, several cycles of motion can completely scramble the apical and equatorial atoms. In contrast, the BPR mechanism, (observed in trigonal bipyramidal molecules of which  $\text{PF}_5$  is the quintessential example and disphenoidal (seesaw) molecules of which  $\text{SF}_4$  is an example) and the Bartell Mechanism (observed for  $\text{IF}_7$ ) concertedly exchange two apical atoms for two equatorial atoms.<sup>2,16</sup> Animations of the BPR and Bartell Mechanism can be found in Supplement 9 or elsewhere for comparison.<sup>8</sup> Again, several cycles of BPR or several cycles of exchange through a Bartell mechanism will completely scramble the apical/equatorial atoms in a molecule. Interestingly, although all of the  $\text{AEX}_5$  molecular species proceed via exchange of one apical atom for one equatorial atom and begin from, and end in, a square pyramidal ground-state structure, two types of pathways are observed; one that passes through a transition state of  $C_{2v}$  symmetry that may be described as a holodirected structure and one that passes through a transition state of  $C_s$  symmetry that may be described as a hemidirected structure.

Why some species ( $\text{IF}_5$ ,  $\text{BrF}_5$ , and  $\text{XeF}_5^+$ ) pass through a  $C_s$  hemidirected transition state, and others ( $\text{ClF}_5$ ,  $\text{ICl}_5$ , and  $\text{IBr}_5$ ) pass through a  $C_{2v}$  holodirected transition state is not altogether clear to us, however. Interestingly, all the molecular species that “appropriate” the least amount of room for the lone pair on the central atom in the ground state (i.e., the bonding pairs and lone pair have similar space requirements) have  $C_{2v}$  holodirected transition states. In contrast, all of the molecular species that “appropriate” the most room

for the lone pair on the central atom in the ground state have transition states of  $C_s$  hemidirected geometry. Thus, although all the molecular species we have examined in this study have hemidirected ground-state structures (to accommodate the lone pair of electrons on the central atom), those which are “more hemidirected” pass through hemidirected  $C_s$  transition states.

The mechanisms for apical/equatorial exchange (operative for  $\text{IF}_5$ ,  $\text{BrF}_5$ , and  $\text{XeF}_5^+$ ) that proceed through a  $C_s$  transition state are all “chimeric” in nature. This chimeric mode has features that can be recognized visually that are Berry-like, Lever-like, and turnstile-like motions. Interactive animations of apical/equatorial atom exchange that proceed through pure Berry (for  $\text{PF}_5$ ), pure Lever (for  $\text{ClF}_3$ ), and pure turnstile (for  $\text{SF}_4\text{Cl}_2$ ) mechanisms have been included in the supplemental material (Supplements 9a, 9b, and 9c, respectively) for comparison. Symmetry analysis of the vibrational modes available to  $\text{AEX}_5$  species with  $C_s$  symmetry indicates that there are seven  $A'$  symmetric modes and five  $A''$  asymmetric modes. All  $A'$  modes are symmetrically allowed to mix with other  $A'$  modes, and all  $A''$  modes are allowed to mix with other  $A''$  modes. It is not surprising, therefore, that the imaginary frequency of the  $C_s$  transition state (which has  $A''$  symmetry: antisymmetric with respect to the plane of symmetry) has highly mixed character.

The mechanisms for apical/equatorial exchange that pass through  $C_{2v}$  transition states have “LeverBerry” character, character that is both Lever-like and Berry-like. We reiterate that, unlike apical/exchange that proceeds through a  $C_s$  transition state, no twisting (turnstile) motion is observed. The four atoms contained within the plane involved in the Lever motion show no out-of-plane deformation (see the vectors in Figure 2C and D and a visual/dynamic treatment in Supplements 4b, 6a, 7). This absence of out-of-plane deformation seems to be a signature of the exchange mechanisms proceeding through a  $C_{2v}$  transition state. In the  $\text{ICl}_5$  and  $\text{IBr}_5$  molecules with larger terminal atoms and longer bonds, the Lever character dominates in the vibrational mode of the imaginary frequency. A symmetry analysis for the vibrational modes for an  $\text{AEX}_5$  species of  $C_{2v}$  symmetry yields 12 modes ( $5A_1$ ,  $A_2$ ,  $3B_1$ , and  $3B_2$ ) and examination of the “LeverBerry” mode allows one to identify it as having  $B_1$  symmetry. Interestingly, when  $C_{2v}$  symmetry is imposed on  $\text{IF}_5$  (which has a  $C_s$  transition state), two imaginary frequencies are found: one of  $B_1$  symmetry and “LeverBerry” in character and a second of  $B_2$  symmetry. Animation of these modes for the stationary point of  $C_{2v}$  symmetry can be found in the supplemental material (Supplement 5c).

Two periodic trends can be seen within our computational data. Within a series with the same terminal atoms ( $\text{ClF}_5$ ,  $\text{BrF}_5$ , and  $\text{IF}_5$ ), as the atomic number on the central atom increases, the barrier for axial/equatorial exchange decreases (and the calculated energy of the imaginary frequency decreases as well). Therefore, when we compare the computed barriers for the same computational method (B3LYP/cc-pV5Z), the barrier for apical/equatorial atom exchange decreases across the series  $\text{ClF}_5$  (36.5 kcal/mol) >  $\text{BrF}_5$  (31.9 kcal/mol) >  $\text{IF}_5$  (24.7 kcal/mol). This is consistent through-

(16) Whitesides, G. M.; Mitchell, H. G. *J. Am. Chem. Soc.* **1969**, *91*, 5384.

out the different computational methods: (KMLYP/pVTZ),  $\text{ClF}_5$  (53.2 kcal/mol) >  $\text{BrF}_5$  (43.9 kcal/mol) >  $\text{IF}_5$  (32.3 kcal/mol); (CCSD(T)/pVTZ),  $\text{ClF}_5$  (40.5 kcal/mol) >  $\text{BrF}_5$  (35.6 kcal/mol) >  $\text{IF}_5$  (29.3 kcal/mol). The same periodic trend was observed in two different computational studies examining apical/equatorial atom exchange in disphenoidal  $\text{X}(\text{CH}_3)_4$  molecules where the barrier decreased across the series from S to Te,  $\text{S}(\text{CH}_3)_4 > \text{Se}(\text{CH}_3)_4 > \text{Te}(\text{CH}_3)_4$ , consistent with experimental observations.<sup>5</sup> This periodic trend was also reported in a computational study of the fluxional character in bis amidinate complexes  $(\text{X}(\text{R}'\text{N}-\text{CR}-\text{NR}')_2)$  of silicon, germanium, tin, and lead where the barrier for apical/equatorial atom exchange decreases across the series  $\text{Si} > \text{Ge} > \text{Sn} > \text{Pb}$ .<sup>6</sup>

Finally, if we compare the barriers within a series of  $\text{AEX}_5$  molecules with the same central atom, as the atomic number of the terminal atoms increases, the barrier for apical/equatorial exchange decreases, as does the computed imaginary frequency. The barrier and imaginary frequencies decrease across the series (B3LYP/pVTZ calculation),  $\text{IF}_5$  (26.7 kcal/mol and  $151i \text{ cm}^{-1}$ ) >  $\text{ICl}_5$  (11.5 kcal/mol and  $69.3i \text{ cm}^{-1}$ ) >  $\text{IBr}_5$  (4.9 kcal/mol and  $25.2i \text{ cm}^{-1}$ ). Within this series, the mechanism with the highest barrier proceeds through a hemidirected transition state of  $C_s$  symmetry, and those with a lower barrier proceed through a holodirected transition state of  $C_{2v}$  symmetry.

### Computational Procedures

All calculations were performed using Gaussian 03.<sup>17</sup> Basis sets were either internal or incorporated as a general basis;<sup>18</sup> the only use of an effective core potential was the correlation-consistent cc-pV5Z-pp basis for iodine.<sup>18</sup> Symmetry was utilized throughout. Transition states were computed from an initially calculated Hessian, and resulting stationary points checked for the appropriate characteristics based on the number of computed negative roots in the Hessian matrix. Transition states at the CCSD level were located using an initial Hessian computed at the B3LYP level, and the CCSD(T) energy calculated at the resulting optimized CCSD geometry.

Animations (found in our enhanced Web objects) of the exchange mechanisms were created using the molecular 3D visualizer Jmol<sup>19</sup>

(17) Frisch, M. J.; Trucks, G. W.; Schlegel, H. B.; Scuseria, G. E.; Robb, M. A.; Cheeseman, J. R.; Montgomery, J. A., Jr.; Vreven, T.; Kudin, K. N.; Burant, J. C.; Millam, J. M.; Iyengar, S. S.; Tomasi, J.; Barone, V.; Mennucci, B.; Cossi, M.; Scalmani, G.; Rega, N.; Petersson, G. A.; Nakatsuji, H.; Hada, M.; Ehara, M.; Toyota, K.; Fukuda, R.; Hasegawa, J.; Ishida, M.; Nakajima, T.; Honda, Y.; Kitao, O.; Nakai, H.; Klene, M.; Li, X.; Knox, J. E.; Hratchian, H. P.; Cross, J. B.; Bakken, V.; Adamo, C.; Jaramillo, J.; Gomperts, R.; Stratmann, R. E.; Yazyev, O.; Austin, A. J.; Cammi, R.; Pomelli, C.; Ochterski, J. W.; Ayala, P. Y.; Morokuma, K.; Voth, G. A.; Salvador, P.; Dannenberg, J. J.; Zakrzewski, V. G.; Dapprich, S.; Daniels, A. D.; Strain, M. C.; Farkas, O.; Malick, D. K.; Rabuck, A. D.; Raghavachari, K.; Foresman, J. B.; Ortiz, J. V.; Cui, Q.; Baboul, A. G.; Clifford, S.; Cioslowski, J.; Stefanov, B. B.; Liu, G.; Liashenko, A.; Piskorz, P.; Komaromi, I.; Martin, R. L.; Fox, D. J.; Keith, T.; Al-Laham, M. A.; Peng, C. Y.; Nanayakkara, A.; Challacombe, M.; Gill, P. M. W.; Johnson, B.; Chen, W.; Wong, M. W.; Gonzalez, C.; Pople, J. A. *Gaussian 03*, revision C.01; Gaussian, Inc.: Wallingford, CT, 2004.

and using Gaussview<sup>20</sup> or Chem 3D<sup>21</sup> as supporting programs to generate alternative orientations for the molecular species from Gaussian log or output files.

### Conclusions

In our computational study on nondissociative mechanisms that interchange apical and equatorial atoms in square pyramidal  $\text{AEX}_5$  molecules, we have found two pathways for terminal atom exchange: one which proceeds through a transition state of  $C_s$  symmetry and a second which proceeds through a transition state of  $C_{2v}$  symmetry. The  $C_s$  transition states located for  $\text{BrF}_5$ ,  $\text{IF}_5$ , and  $\text{XeF}_5^+$  have hemidirected geometries in which the terminal atoms are distributed in such a fashion as to create a coordination void in one hemisphere. In contrast, the  $C_{2v}$  transition states located for  $\text{ClF}_5$ ,  $\text{ICl}_5$ , and  $\text{IBr}_5$  have terminal atoms that are spatially more equally distributed about the central atom in what is referred to as a holodirected geometry. The molecular motions of the apical/equatorial exchange mechanisms also differ on the basis of whether they proceed through a transition state of  $C_s$  symmetry or a transition state of  $C_{2v}$  symmetry. Animation of the imaginary frequencies computed for the transition states allowed us to examine the mechanistic motions in a visual/dynamic fashion. In both pathways, one apical atom is exchanged for one equatorial atom in each cycle of motion. The mechanisms for apical/equatorial atom exchange in those species which pass through transition states of  $C_s$  symmetry have chimeric character with Berry-like, Lever-like, and turnstile-like features. In contrast, the mechanisms that proceed through  $C_{2v}$  transition states are also chimeric in nature but lack twisting (turnstile) character. The ground-state structures for all of the molecular species examined in this study ( $\text{ClF}_5$ ,  $\text{BrF}_5$ ,  $\text{IF}_5$ ,  $\text{ICl}_5$ ,  $\text{IBr}_5$ , and  $\text{XeF}_5^+$ ) have square pyramidal geometry with  $C_{4v}$  symmetry.

The calculated barrier for apical/equatorial exchange decreases as the atomic number of the central atom increases (within a series with the same terminal atom):  $\text{ClF}_5 > \text{BrF}_5 > \text{IF}_5$ . Similarly, The calculated barrier for apical/equatorial exchange decreases as the atomic number of the terminal atoms increase (within a series with the same central atom):  $\text{ClF}_5 > \text{ICl}_5 > \text{IBr}_5$ .

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(19) See <http://jmol.sourceforge.net/>

(20) *Gaussview*, Version 3.0; Gaussian: (see reference for Gaussian).

(21) *CS Chem3D Ultra*, Version 7.0.0; CambridgeSoft: Cambridge, MA, 2001.