

Density Functional Theory Analysis of the Interplay between Jahn-Teller Instability, Uniaxial Magnetism, Spin Arrangement, Metal-Metal Interaction, and Spin-Orbit Coupling in Ca_3 CoMO₆ (M = Co, Rh, Ir)

Yuemei Zhang,† Erjun Kan,† Hongjun Xiang,‡ Antoine Villesuzanne,§ and Myung-Hwan Whangbo*,†

† Department of Chemistry, North Carolina State University, Raleigh, North Carolina 27695-8204, United States, [‡]Key Laboratory of Computational Physical Sciences (Ministry of Education) and Department of Physics, Fudan University, Shanghai 200433, P. R. China, and[§]CNRS, Université de Bordeaux, ICMCB, 87 Av. Dr. A. Schweitzer, 33608 Pessac cedex, France

Received November 5, 2010

In the isostructural oxides Ca₃CoMO₆ (M = Co, Rh, Ir), the CoMO₆ chains made up of face-sharing CoO₆ trigonal prisms and MO₆ octahedra are separated by Ca atoms. We analyzed the magnetic and electronic properties of these oxides on the basis of density functional theory calculations including on-site repulsion and spin-orbit coupling, and examined the essential one-electron pictures hidden behind results of these calculations. Our analysis reveals an intimate interplay between Jahn-Teller instability, uniaxial magnetism, spin arrangement, metal-metal interaction, and spin-orbit coupling in governing the magnetic and electronic properties of these oxides. These oxides undergo a Jahn-Teller distortion, but their distortions are weak, so that their trigonal-prism Co^{n+} ($n = 2, 3$) ions still give rise to strong easy-axis anisotropy along the chain direction. As for the d-state split pattern of these ions, the electronic and magnetic properties of Ca_3CoMO_6 (M = Co, Rh, Ir) are consistent with $d_0 < (d_2, d_{-2}) < (d_1, d_{-1})$ but not with $(d_2, d_{-2}) < d_0 < (d_1, d_{-1})$. The trigonal-prism Co³⁺ ion in Ca₃Co₂O₆ has the L = 2 configuration $(d_0)^1(d_2, d_{-2})^3(d_1, d_{-1})^2$ because of the metal-metal interaction between adjacent Co^{3+} ions in each Co₂O₆ chain, which is mediated by their z^2 orbitals, and the spin-orbit coupling of the trigonalprism Co^{3+} ion. The spins in each CoMO₆ chain of Ca₃CoMO₆ prefer the ferromagnetic arrangement for M = Co and Rh but the antiferromagnetic arrangement for M = Ir. The octahedral M⁴⁺ ion of Ca₃CoMO₆ has the $(1a)^1(1e)^4$ configuration for M = Rh but the $(1a)^2(1e)^3$ configuration for M = Ir, which arises from the difference in the spin-orbit coupling of the M⁴⁺ ions and the $Co \cdots M$ metal-metal interactions.

1. Introduction

For a magnetic system with transition-metal ions exhibiting uniaxial (i.e., Ising) magnetism, the ions have an unevenly filled degenerate d-state so that the ΔJ_z value of the lowestlying Kramer's doublet state is greater than $1¹$ However, such a system has Jahn-Teller (T) instability² and the associated JT distortion may lift the d-state degeneracy causing the uniaxial magnetism. Thus, a true uniaxial magnetism is not possible unless a JT distortion is prevented by steric hindrance. 3 Indeed, uniaxial magnetism and JT instability were found to compete in the magnetic oxide $Ca_3CoMnO₆⁴$

which consists of the $CoMnO_6$ chains made up of face-sharing $CoO₆$ trigonal prism (TP) and $MnO₆$ octahedron (OCT) units (Figure 1). In the room-temperature structure of $Ca₃Co \text{MnO}_6$ ⁵ each CoMnO₆ chain has a 3-fold rotational symmetry, C_3 , so that the high-spin Co²⁺ (d⁷) ion at each TP CoO₆ has the d-electron configuration $(d_0)^2(d_2, d_{-2})^3(d_1, d_{-1})^2$, giving rise to both JT instability and uniaxial magnetism. Here we use the local coordinate system in which the z-axis is taken along the $CoMO₆$ chain (i.e., the crystallographic c direction), so that the d_0 orbital is equivalent to the z^2 orbital, the degenerate (d_2, d_{-2}) set to the (x^2-y^2, xy) set, and the degenerate (d_1, d_{-1}) set to the (xz, yz) set (Figure 2a).¹ $Ca₃CoMnO₆$ is regarded to have uniaxial spins,⁶ but first principles density functional theory (DFT) calculations showed⁴ that $Ca₃CoMnO₆$ should undergo a JT distortion removing the C_3 symmetry and hence cannot be truly

^{*}To whom correspondence should be addressed. E-mail: mike whangbo@ ncsu.edu.

⁽¹⁾ Dai, D.; Whangbo, M.-H. *Inorg. Chem.* **2005**, 44, 4407.
(2) (a) Kugel, K. I.; Khomskii, D. I. Sov. Phys. Usp. **1982**, 25, 231. (b) Bersuker, I. B. The Jahn-Teller Effect; Cambridge University Press: 2006.

^{(3) (}a) Reiff, W. M.; LaPointe, A. M.; Witten, E. H. J. Am. Chem. Soc. 2004, 126, 10206. (b) Reiff, W. M.; Schulz, C. E.; Whangbo, M.-H.; Seo, J. I.; Lee, Y. S.; Potratz, G. R.; Spicer, C. W.; Girolami, G. S. J. Am. Chem. Soc. 2009, 131, 404.

⁽⁴⁾ Zhang, Y.; Xiang, H. J.; Whangbo, M.-H. Phys. Rev. B 2009, 79, 054432.

⁽⁵⁾ Zubkov, V. G.; Bazuev, G. V.; Tyutyunnik, A. P.; Berger, I. F. J. Solid State Chem. 2001, 160, 293.

⁽⁶⁾ Choi, Y. J.; Yi, H. T.; Lee, S.; Huang, Q.; Kiryukhin, V.; Cheong, S.-W. Phys. Rev. Lett. 2008, 100, 047601.

Figure 1. (a) Projection view of the crystal structure of $Ca₃CoMO₆$ along the c-direction. (b) Perspective view of an isolated $CoMO₆$ chain. The gray, purple, blue, and red balls represent Ca, Co, M, and O atoms, respectively.

Figure 2. Shapes and relative energies of (a) the d-states of the $CoO₆$ trigonal prism and (b) the t_{2g}-states of the CoO₆ octahedron of Ca₃Co₂O₆ obtained from extended Hückel tight-binding calculations.

uniaxial, although it has strong magnetic anisotropy with the easy axis along the $CoMnO₆$ chain.

The magnetic oxides $Ca_3CoMO_6(M = Co^7 Rh, ^8 Ir^9)$, isostructural with Ca_3CoMnO_6 ⁵ belong to the family of hexagonal perovskites.¹⁰ Due to the face sharing of the TP CoO₆ and OCT MO_6 , the nearest-neighbor (NN) $Co \cdots M$ distance of the CoMO₆ chain is short (i.e., 2.595, 2.682, and 2.706 \AA for $M = Co, Rh, and Ir, respectively$ so that the $Co \cdot \cdot M$ direct metal-metal interaction mediated by their z^2 orbitals can be substantial. (Here the NN Co \cdots Ir distance of 2.706 A is taken from the structure of Ca_3CoIrO_6 optimized by DFT calculations. See below.) The X-ray photoemission study¹¹ of Ca_3CoMO_6 revealed that the Co atoms of the TP CoO_6 exist as Co^{3+} ions for M = Co but as Co^{2+} ions for M = Rh and Ir, and hence, the M atoms of the MO_6 octahedra exist as M^{3+} ions for $M = Co$ but as M^{4+} ions for $M = Rh$ and Ir. The magnetic properties of Ca_3CoMO_6 (M = Co, Rh, Ir) show

(11) Takubo, K.; Mizokawa, T.; Hirata, S.; Son, J.-Y.; Fujimori, A.; Topwal, D.; Sarma, D. D.; Rayaprol, S.; Sampathkumaran, E.-V. Phys. Rev. B 2005, 71, 073406.

Figure 3. High-spin electron configurations expected for the $\text{Co}^{3+}(\text{d}^6)$ and $\text{Co}^{2+}(\text{d}^7)$ ions at a trigonal prism site when the d-state split pattern is and Co^{2+} (d⁷) ions at a trigonal prism site when the d-state split pattern is given by $d_0 < (d_2, d_{-2}) < (d_1, d_{-1})$ in (a), (b), and (e), and by $(d_2, d_{-2}) < d_0$ \leq (d₁, d₋₁) in (c) and (d).

that the TP Co atoms are present as high-spin ions, the $CoMO₆$ chains have uniaxial spins, and their intrachain spin arrangement is ferromagnetic (FM) for $M = Co^{12-14}$ and Rh,¹⁵ and the same is presumed to be true for $M = Ir$.¹⁶ The electronic and magnetic properties of $Ca_3CoMO_6(M =$ Co, Rh, Ir) have been investigated in a number of DFT studies.^{$17-25$}

It has been well established that the d-states of a transition metal ion at an isolated TP site with C_3 rotational symmetry are split as $d_0 < (d_2, d_{-2}) < (d_1, d_{-1})^2$. This leads to $L = 0$ configuration $(d_0)^2(d_2, d_{-2})^2(d_1, d_{-1})^2$ (Figure 3a) for an isolated TP high-spin Co^{3+} (d⁶) ion, hence predicting the absence of uniaxial magnetism. Thus, it was concluded¹ that the TP Co^{3+} ion of Ca₃Co₂O₆ should have the L = 2 configuration $(d_0)^1(d_2, d_{-2})^3(d_1, d_{-1})^2$ (Figure 3b) due to the interaction between the z^2 orbitals of adjacent TP and

(12) Åasland, S.; Fjellvåg, H.; Hauback, B. Solid State Commun. 1997, 101, 187.

(13) Kageyama, H.; Yoshimura, K.; Kosuge, K.; Azuma, M.; Takano,

M.; Mitamura, H.; Goto, T. *J. Phys. Soc. Jpn.* **1997**, 66, 3996.
(14) Maignan, A.; Michel, C.; Masset, A. C.; Martin, C.; Raveau, B. Eur. Phys. J. B 2000, 15, 657.

(15) (a) Niitaka, S.; Kageyama, H.; Yoshimura, K.; Kosuge, K.; Kawano, S.; Aso, N.; Mitsuda, A.; Mitamura, H.; Goto, T. J. Phys. Soc. Jpn. 2001, 70, 1222. (b) Niitaka, S.; Yoshimura, K.; Kosuge, K.; Nishi, M.; Kakurai, K. Phys. Rev. Lett. 2001, 87, 177202.

(16) Sugiyama, J.; Morris, G. D.; Nozaki, H.; Ikedo, Y.; Russo, P. L.; Stubbs, S. L.; Brewer, J. H.; Ansaldo, E. J.; Martin, C.; Hebert, S.; Maignan, A. Phys. B 2009, 404, 603.

(17) Whangbo, M.-H.; Dai, D.; Koo, H.-J.; Jobic, S. Solid State Commun. 2003, 125, 413.

(18) Vidya, R.; Ravindran, P.; Fjellvåg, H.; Kjekshus, A. Phys. Rev. Lett. 2003, 91, 186404.

(19) Eyert, V.; Laschinger, C.; Kopp, T.; Fresard, R. Chem. Phys. Lett. 2004, 385, 249.

(20) Vidya, R.; Ravindran, P.; Vajeeston, P.; Fjellvåg, H.; Kjekshus, A. Ceram. Int. 2004, 30, 1993.

(21) Wu, H.; Haverkort, M. W.; Hu, Z.; Khomskii, D. I.; Tjeng, L. H. Phys. Rev. Lett. 2005, 95, 186401.

(22) Villesuzanne, A.; Whangbo, M.-H. *Inorg. Chem.* **2005**, 44, 6339.
(23) Stoeffler, D. *Microelectron. Eng.* **2008**, 85, 2451.

(24) Eyert, V.; Schwingenschlögl, U.; Hackenberger, C.; Kopp, T.; Fresard, R.; Eckern, U. J. Solid State Chem. 2007, 36, 156.

(25) Wu, H.; Hu, Z.; Khomskii, D. I.; Tjeng, L. H. Phys. Rev. B 2007, 75, 245118.

(26) (a) Stiefel, E. I.; Eisenberg, R.; Rosenberg, R. C.; Gray, H. B. J. Am. Chem. Soc. 1966, 88, 2956. (b) Schrauzer, G. N.; Mayweg, V. P. J. Am. Chem. Soc. 1966, 68, 3234. (c) Hulliger, F. Struct. Bonding (Berlin, Ger.) 1968, 4, 83. (d) Anzenhofer, K.; van den Berg, J. M.; Cossee, P.; Heile, J. N. J. Phys. Chem. Solids 1970, 31, 1057. (e) Hoffmann, R.; Howell, J. M.; Rossi, A. R. J. Am. Chem. Soc. 1976, 98, 2484.

⁽⁷⁾ Fjellvåg, H.; Gulbrandsen, E.; Åasland, S.; Olsen, A.; Hauback, B. C. J. Solid State Chem. 1996, 124, 190.

⁽⁸⁾ Niitaka, S.; Kageyama, H.; Kato, M.; Yoshimura, K.; Kosuge, K. J. Solid State Chem. 1999, 146, 137.

⁽⁹⁾ Kageyama, H.; Yoshimura, K.; Kosuge, K. J. Solid State Chem. 1998, 140, 14.

^{(10) (}a) Darriet, J.; Subramanian, M. A. J. Mater. Chem. 1995, 5, 543. (b) Perez-Mato, J. M.; Zakhour-Nakhl, M.; Weill, F.; Darriet, J. J. Mater. Chem. 1999, 9, 2795. (c) Stitzer, K. E.; Darriet., J.; Zur Loye, H. -C. Curr. Opin. Solid State Mater. Sci. 2001, 5, 535.

OCT Co^{3+} ions. In the DFT study of Ca₃Co₂O₆ by Wu et al.,²¹ spin-orbit coupling (SOC) interactions were found essential for the occurrence of the $L = 2$ configuration $(d_0)^1$ $(d_2, d_{-2})^3$ $(d_1, d_{-1})^2$; the TP Co³⁺ ion has the $(d_0)^1$ $(d_2, d_{-2})^3$ $(d_{-2})^3$ $(d_1, d_{-1})^2$ configuration if SOC interactions are included, but the $(d_0)^2(d_2, d_{-2})^2(d_1, d_{-1})^2$ configuration otherwise. Nevertheless, they assumed the split pattern of the TP Co^{3+} ion to be $(d_2, d_{-2}) < d_0 < (d_1, d_{-1})$, which leads to the L = 2 configuration $(d_2, d_{-2})^3 (d_0)^1 (d_1, d_{-1})^2$ (Figure 3c) even if the SOC effect is not included. Furthermore, Burnus et al. 27 employed this $L = 2$ configuration for the TP $Co³⁺$ ion to interpret their X-ray absorption and X-ray magnetic dichroism data of Ca₃Co₂O₆, and concluded that the d_0 < $(d_2, d_{-2}) < (d_1, d_{-1})$ pattern is incorrect for the TP Co³⁺ ion. However, the $(d_2, d_{-2}) < d_0 < (d_1, d_{-1})$ split pattern gives rise to serious conceptual difficulties. First, for a transition metal atom surrounded by oxygen ligands, the split pattern of its the d-states is determined by how strong the antibonding interactions between the metal *n*d and O 2p orbitals are.²⁸ The z² orbital of the TP Co³⁺ ion, being aligned along the C_3 axis of the TP $CoO₆$, overlaps least well with the 2p-orbitals of the surrounding O atoms. As a consequence, the d_0 level should be the lowest-lying state of the TP Co d-states (Figure 2a) regardless of whether the TP ion is $Co³⁺$ or Co^{2+} , so that the $(d_2, d_{-2}) < d_0 < (d_1, d_{-1})$ split pattern cannot be correct. Second, the (d_2, d_{-2}) < $d_0 < (d_1, d_{-1})$ split pattern cannot explain the uniaxial magnetism of $Ca₃CoRhO₆$, because it gives rise to the L = 0 configuration $(d_2, d_{-2})^2$. $(d_0)^1(d_1, d_{-1})^2$ for the TP Co²⁺ (d⁷) ion (Figure 3d). In contrast, the $d_0 < (d_2, d_{-2}) < (d_1, d_{-1})$ split pattern gives the L = 2 configuration $(d_0)^2(d_2, d_{-2})^3(d_1, d_{-1})^2$ (Figure 3e), and the latter is consistent with the density functional calculations for Ca_3CoRhO_6 by Wu et al.²⁵ In interpreting their X-ray absorption and X-ray magnetic dichroism data of Ca₃CoRhO₆, Burnus et al.²⁹ used the $d_0 < (d_2, d_{-2}) < (d_1,$ d_{-1}) pattern for the TP Co²⁺ ion and suggested that the d_0 state is nearly degenerate with the (d_2, d_{-2}) states.

The above discussion raises several important questions: (a) It is necessary to determine whether or not the spins of the $CoIrO₆$ chains in $Ca₃CoIrO₆$ have the FM arrangement as found in $Ca_3Co_2O_6$ and Ca_3CoRhO_6 . (b) In all three oxides $Ca_3CoMO_6(M = Co, Rh, Ir)$, the TP $Co^{n+}(n = 2 \text{ or } 3)$ ions possess the $L = 2$ electron configuration. Thus, $Ca₃CoMO₆$ $(M = Co, Rh, Ir)$ should be susceptible to JT instability as found for Ca_3CoMnO_6 .⁴ It is important to examine how strong their JT distortions can be. (c) Concerning the d-state split pattern of a transition-metal ion at a TP site, it is controversial whether the $d_0 \leq (d_2, d_{-2}) \leq (d_1, d_{-1})$ or $(d_2,$ d_{-2}) < d_0 < (d₁, d₋₁) pattern is correct. It is desirable to determine if the split pattern depends on the charge of the TP Co^{n+} (n = 2, 3) ion as reported in the studies of Burnus et al.^{27,29} and/or whether the d₀ state is nearly degenerate with the (d_2, d_{-2}) states as suggested by Burnus et al.²⁹ (d) In $Ca_3CoMO_6(M) = Rh, Ir)$, the OCT M^{4+} ions might exhibit SOC effects because of their open-shell electron configuration

 $(t_{2g})^5$. It is interesting to examine if the SOC effects of these ions affect the electronic and magnetic structures of $Ca₃Co MO₆$. In the present work, we investigate these questions on the basis of DFT calculations for Ca_3CoMnO_6 (M = Co, Rh, Ir). Results of our study are presented in what follows.

2. Calculations

To optimize the crystal structures of $Ca_3CoMO_6(M = Co,$ Rh, Ir) in the presence and absence of C_3 rotational symmetry, we employed the projector augmented wave (PAW) method encoded in the Vienna ab initio simulation package $(VASP)^{30}$ with the local spin density approximation (LSDA). To properly describe the electron correlation associated with the d-states of transition metal atoms, the LSDA plus on-site repulsion U (LSDA+U) method was adopted.³¹ In addition, SOC effects³² were considered by performing LSDA+U+ SOC calculations with the spins oriented parallel and perpendicular to the $CoMO₆$ chain direction (hereafter the $||c$ - and Lc-spin orientations, respectively). The convergence threshold for our LSDA+U+SOC calculations was set to 10^{-5} eV in energy and 10^{-2} eV/Å in force with the plane-wave cutoff energy of 400 eV and a set of $3 \times 3 \times 3$ k-points for the irreducible Brillouin zone. For $Ca₃CoIrO₆$, only the cell parameters have been reported.33 Therefore, we determined the atomic positions of Ca_3CoIrO_6 by optimizing the crystal structure on the basis of $LSDA+U+SOC$ calculations. This optimization leads to two kinds of structures for each Ca₃- $CoMO₆$ (M = Co, Rh, Ir), namely, one with high orbital moment (μ_L) and the other with low μ_L , on the TP Co^{n+} (n = 2, 3) ions. As found for Ca_3CoMnO_6 ⁴ the CoMO₆ chains of $Ca₃CoMO₆$ have the C₃-rotational symmetry in the high- μ_L structure, but do not in the low- μ _L structure. The geometry optimization with $LSDA+U+SOC$ calculations is carried out with no symmetry constraint, so it is generally difficult to have the calculations converge to the high- μ_L structure.

In discussing the spin and orbital moments of the TP and OCT ions of Ca_3CoMO_6 (M = Co, Rh, Ir) as well as their density of states (DOS), we have carried out $LSDA+U+SOC$ calculations for the experimental and the optimized structures of $Ca_3Co_2O_6$ and Ca_3CoRhO_6 and for the optimized structure of $Ca₃CoIrO₆$ by using the full-potential linearized augmented plane wave (FPLAPW) method 34 encoded in the WIEN2k package, $35 \times 5 \times 5$ k-points for the irreducible Brillouin zone, the threshold of 10^{-5} Ry for the energy convergence, the cutoff energy parameters of $RK_{\text{max}} = 7$ and $G_{\text{max}} = 12$, and the energy threshold of -9.0 Ry for the separation of the core and valence states.

For the effective on-site repulsion $U_{\text{eff}} = U - J$ (where J is the Stoner intra-atomic parameter) needed for the geometry optimization with the LSDA+U+SOC (VASP) calculations,

⁽²⁷⁾ Burnus, T.; Hu, Z.; Haverkort, M. W.; Cezar, J. C.; Flahaut, D.; Hardy, V.; Maignan, A.; Brookes, N. B.; Tanaka, A.; Hsieh, H. H.; Lin,

H.-J.; Chen, C. T.; Tjeng, L. H. *Phys. Rev. B* 2006, 74, 245111.
(28) Albright, T. A; Burdett, J. K.; Whangbo, M.-H. *Orbital Interactions* in Chemistry; Wiley: New York, 1985.

⁽²⁹⁾ Burnus, T.; Hu, Z.; Wu, H.; Cezar, J. C.; Niitaka, S.; Takagi, H.; Chang, C. F.; Brookes, N. B.; Lin, H.-J.; Jang, L. Y.; Tanaka, A.; Liang, K. S.; Chen, C. T.; Tjeng, L. H. Phys. Rev. B 2008, 77, 205111.

^{(30) (}a) Kresse, G.; Hafner, J. Phys. Rev. B 1993, 47, 558. (b) Kresse, G.; Furthmüller, J. Comput. Mater. Sci. 1996, 6, 15. (c) Kresse, G.; Furthmüller, J. Phys. Rev. B 1996, 54, 11169.

⁽³¹⁾ Dudarev, S. L.; Botton, G. A.; Savrasov, S. Y.; Humphreys, C. J.; Sutton, A. P. Phys. Rev. B 1998, 57, 1505.

⁽³²⁾ Kunes, J.; Novak, P.; Divis, M.; Oppeneer, P. M. Phys. Rev. B 2001, 63, 205111.

⁽³³⁾ Kageyama, H.; Yoshimura, K.; Kosuge, K. J. Solid State Chem. 1998, 140, 14.

⁽³⁴⁾ Singh, D. J. Plane waves, Pseudopotentials and the LAPW Method; Kluwer Academic: Boston, 1994.

⁽³⁵⁾ Blaha, P.; Schwarz, K.; Madsen, G. K. H.; Kvasnicka, D.; Luitz, J. $WIEN2K$, An Augmented Plane Wave $+$ Local Orbitals Program for Calculating Crystal Properties; Techn. Universität: Wien, Austria, 2001.

we used $U_{\text{eff}} = 4 \text{ eV}$ on Co for Ca₃Co₂O₆, $U_{\text{eff}} = 4 \text{ eV}$ on Co, and $U_{\text{eff}} = 2$ eV for Rh and Ir for Ca₃CoMO₆ (M = Rh, Ir). (We note that, for $LSDA+U$ and $LSDA+U+SOC$ calculations, only the difference $U - J = U_{\text{eff}}$ matters for the calculations.) These parameters are quite similar to those employed by Wu et al. in their DFT studies of $Ca_3Co_2O_6^{21}$ and $\text{Ca}_3\text{CoRhO}_6$.²⁵ We also employed these parameters for our LSDA+U+SOC (WIEN2k) calculations on $Ca₃CoMO₆$ (M = Co, Rh, Ir) to find that the use of $U_{\text{eff}} = 4$ and 2 eV on Co and M, respectively, does not lead to magnetic insulating states for Ca_3CoMO_6 (M = Rh, Ir) but the use of $U_{\text{eff}}= 4$ eV on both Co and M does. Hereafter, the U_{eff} values on Co, Rh, and Ir will be designated as $U_{\text{eff}}(\text{Co})$, $U_{\text{eff}}(\text{Rh})$, and $U_{\text{eff}}(\text{Ir})$, respectively.

Possible ordered spin arrangements for each $CoMO₆$ chain of Ca_3CoMO_6 (M = Co, Rh, Ir) include the FM (i.e., $\uparrow\uparrow\uparrow\uparrow$), antiferromagnetic (AFM) (i.e., \mathbb{W}), and \mathbb{W} arrangements. It should be noted that the AFM state represents a ferrimagnetic arrangement in each $CoMO₆$ chain because the magnetic moments of the Co and M sites are different (see below). In our calculations, the spin arrangement between adjacent $CoMO₆$ chains is assumed to be FM.

3. Magnetic Ground States of $Ca_3CoM_6(M = Co, Rh, Ir)$

Our WIEN2k calculations show that, for $Ca_3Co_2O_6$, a magnetic insulating state can be obtained at the $LSDA+U$ and $LSDA+U+SOC$ levels of calculations, but the $LSDA+$ $U+SOC$ level of calculations are necessary to obtain the L = 2 configuration $(d_0)^1(d_2, d_{-2})^3(d_1, d_{-1})^2$ for the TP Co³⁺ ion, as found by Wu et al.²¹ For both $Ca₃CoRhO₆$ and $Ca₃CoIrO₆$, a magnetic insulating state is obtained only at the $LSDA+U+SOC$ level of calculations. Our $LSDA+U+SOC$ calculations reveal that only the FM state is stable for the experimental structure of $Ca₃Co₂O₆$, while both the FM and $\mathsf{M}\mathsf{W}$ states are stable for the experimental structure of Ca₃-CoRhO₆. The FM state is more stable than the MW state by 308 meV per formula unit (FU) from calculations with $U_{\text{eff}}(\text{Co}) = 4 \text{ eV}$ and $U_{\text{eff}}(\text{Rh}) = 2 \text{ eV}$, and by 422 meV/ FU from calculations with $U_{\text{eff}}(Co) = U_{\text{eff}}(Rh) = 4 \text{ eV}$. For the optimized structure of $Ca₃CoIrO₆$ with $C₃$ symmetry, only the AFM state is stable as long as $U_{\text{eff}}(\text{Co}) \ge U_{\text{eff}}(\text{Ir})$ in LSDA+U+SOC calculations. When $U_{\text{eff}}(\text{Co}) \leq U_{\text{eff}}(\text{Ir}),$ $LSDA+U+SOC$ calculations lead to a stable FM state, but the FM state is less stable than the AFM state (e.g., by 39 meV/FU with $U_{\text{eff}}(\text{Co}) = 3.5 \text{ eV}$ and $U_{\text{eff}}(\text{Ir}) = 4.0 \text{ eV}$.

4. Jahn-Teller Distortion and Magnetic Anisotropy

To see whether $Ca_3CoMO_6(M = Co, Rh, and Ir)$ undergoes a JT distortion, all the structures of Ca_3CoMO_6 (M = Co, Rh, and Ir) were optimized by performing $LSDA+$ $U+SOC$ (VASP) calculations with the $||c\text{-spin orientation}||$ for their FM states. In the geometry optimizations, the cell parameters were fixed at the experimental values, but the atom positions were allowed to relax with and without the C_3 rotational symmetry for each $CoMO₆$ chain. The atom positions of the optimized structures of $Ca₃CoMO₆$ (M = Co , Rh, Ir) are summarized in Tables $S1-S3$ of the Supporting Information.

The relative energies of the experimental and optimized structures of Ca_3CoMO_6 (M = Co, Rh, Ir) obtained by $LSDA+U+SOC$ (VASP) calculations are summarized in Table 1, and the spin and orbital moments (μ _S and μ _L,

Table 1. Relative Energies ΔE (meV/FU) of the Experimental and Optimized Structures of Ca₃CoMO₆ (M = Co, Rh, Ir) Obtained from the LSDA+U+SOC Calculations Using the PAW Method of the VASP with $U_{\text{eff}} = 4 \text{ eV}$ for Co and U_{eff} = 2 eV for M = Rh and Ir^a

| geometry used | $Ca_3Co_2O_6$ | Ca_3CoRhO_6 | Ca_3CoIrO_6 |
|------------------------------|---------------|---------------|---------------|
| experimental with C_3 axis | 94.3 | 65.7 | |
| optimized with C_3 axis | 65.5 | 35.2 | 139.8 |
| optimized with no C_3 axis | 0.0 | 0.0 | 0.0 |

^aFor each Ca₃CoMO₆ (M = Co, Rh, Ir), the optimization was carried out for the FM state.

Table 2. Spin and Orbital Moments (μ_s and μ_l , Respectively) of the TP and OCT $Co³⁺$ Ions in the FM State of Ca₃Co₂O₆ Obtained from the LSDA+U+SOC (WIEN2k)^a Calculations with $U_{\text{eff}}(\text{Co}) = 4 \text{ eV}^{b,c}$

| | $Co3+ (TP)$ | | $Co3+ (OCT)$ | |
|--|-------------|------|---|------|
| geometry used | | | $\mu_{\rm S}(\mu_{\rm B})$ $\mu_{\rm L}(\mu_{\rm B})$ $\mu_{\rm S}(\mu_{\rm B})$ $\mu_{\rm L}(\mu_{\rm B})$ | |
| experimental with C_3 axis optimized with C_3 axis ^a optimized with no C_3 axis | 2.94 | 1.58 | 0.08 2.94/2.94 1.48/1.48 0.16/0.16 0.05/0.05 2.92/2.89 0.31/0.45 0.02/0.02 0.03/0.02 | 0.18 |

 a Our LSDA+U+SOC (WIEN2k) optimization converges to the structure with no C_3 -rotational symmetry. The numbers listed are obtained from our $LSDA+U+SOC$ (VASP) optimization. b The orbital</sup> and spin moments have the same direction when they have the same sign, and the opposite directions otherwise. ^c There are two slightly different TP Co atoms as well as two slightly different OCT Co atoms in the optimized structures with or without C_3 symmetry.

Table 3. Spin and Orbital Moments (μ_S and μ_L , Respectively) of the TP Co²⁺ and OCT Rh^{4+} Ions in the FM State of Ca_3CoRhO_6 Obtained from the LSDA+U+SOC (WIEN2k) Calculations with $U_{\text{eff}}(\text{Co}) = U_{\text{eff}}(\text{Rh}) = 4 \text{ eV}^{a,b}$

| | | Co^{2+} (TP) | | $Rh^{4+} (OCT)$ | |
|---|------|---|--|---|--|
| geometry | | | μ _S $(\mu$ _B $)$ μ _L $(\mu$ _B $)$ μ _S $(\mu$ _B $)$ | μ _L (μ _B) | |
| experimental with C_3 axis optimized with C_3 axis optimized with no C_3 axis 2.64/2.64 0.50/0.50 0.31/0.31 | 2.71 | 1.76 $2.69/2.69$ 1.76/1.76 0.59/0.59 | 0.49 | 0.01 0.01/0.01 0.01/0.01 | |

^aThe orbital and spin moments have the same direction when they have the same sign, and the opposite directions otherwise. b There are</sup> two slightly different TP Co atoms as well as two slightly different OCT Co atoms in the optimized structures with or without C_3 symmetry.

Table 4. Spin and Orbital Moments (μ_S and μ_L , Respectively) of the TP Co²⁺ and OCT Ir⁴⁺ Ions in the AFM State of Ca₃CoIrO₆ Obtained from the Ions in the AFM State of Ca_3CoIrO_6 Obtained from the LSDA+U+SOC (WIEN2k) Calculations with $U_{\text{eff}}(\text{Co}) = U_{\text{eff}}(\text{Ir}) = 4 \text{ eV}^{a,b}$

| | Co^{2+} (TP) | | $Ir^{4+} (OCT)$ | |
|---|---|--|---|---|
| geometry used | $\mu_{\rm S}(\mu_{\rm B})$ $\mu_{\rm L}(\mu_{\rm B})$ | | μ _S (μ _B) | μ _L (μ _B) |
| optimized with C_3 axis optimized with no C_3 axis 2.62/2.62 0.57/0.72 $-0.44/-0.44$ $-0.54/-0.54$ | | | $2.62/2.62$ 1.77/1.77 $-0.43/-0.43$ $-0.51/-0.51$ | |

 a ^aThe orbital and spin moments have the same direction when they have the same sign, and the opposite directions otherwise. b There are</sup> two slightly different TP Co atoms as well as two slightly different OCT Co atoms in the optimized structures with or without C_3 symmetry.

respectively) of the TP and OCT transition-metal ions of $Ca₃CoMO₆$ (M = Co, Rh, Ir) obtained by the LSDA+ $U+SOC$ (WIEN2k) calculations are shown in Tables 2-4. For the optimized structure with C_3 rotational symmetry, the orbital moment on the TP Coⁿ⁺ ion is large (i.e., $\mu_L = 1.48$, 1.68, and 1.69 μ _B for M = Co, Rh, and Ir, respectively). However, for the optimized structure without C_3 symmetry, the orbital moment on the TP Coⁿ⁺ ion is smaller (i.e., μ_L = 0.47, 0.60, and 0.30 μ_B for M = Co, Rh, and Ir, respectively). (The spin and orbital moments of the OCT sites will be discussed in section 6.) For each Ca_3CoMO_6 (M = Co, Rh

Figure 4. Displacements of the atoms associated with the Jahn-Teller distortions in the magnetic ground state of (a) $Ca₃Co₂O₆$, (b) $Ca₃CoRhO₆$, and (c) $Ca₃CoIrO₆$ with respect to their positions of the experimental structures for $Ca_3Co_2O_6$ and Ca_3CoRhO_6 and with respect to their positions of the optimized structure with C_3 symmetry for Ca₃CoIrO₆. The largest atom displacement is 0.044 Å in $Ca_3Co_2O_6$, 0.064 Å in $Ca₃CoRhO₆$, and 0.051 Å in Ca₃CoIrO₆. In each panel, the left side shows a perspective view of the atom displacements in the $CoMO₆$ chain, and the right side the projection view (along the chain direction) of the atom displacements in the $CoO₆$ trigonal prisms and $MO₆$ octahedra.

or Ir), the optimized structure without C_3 symmetry is more stable than that with C_3 symmetry (i.e., $\Delta E = 65.5, 35.2,$ and 139.8 meV/FU for $M = Co$, Rh, and Ir, respectively). This shows that the structural change of $Ca_3CoMO_6(M=Co, Rh)$ or Ir), from the structure with C_3 symmetry to that without C_3 symmetry, is a JT distortion. Figure 4 shows the atom displacements involved in the JT distortions of $Ca₃CoMO₆$ $(M = Co, Rh, Ir)$, with respect to the experimental structure for $M = Co$ and Rh, and with respect to the optimized structure with C₃-rotational symmetry for $M = Ir$. In Ca₃- $Co₂O₆$ with TP Co³⁺ ions, the largest displacement (0.064 A) is found for one of the O atoms with a smaller displacement for the TP Co atom (i.e., 0.027 Å). In $Ca₃CoRhO₆$ and $Ca₃CoIrO₆$ with TP Co²⁺ ions, however, the TP Co atom shows the largest displacement (i.e., 0.064 and 0.051 A, respectively). A probable cause for this difference is discussed in section 7.

An important consequence of the JT distortion is that the orbital moments of the TP Co^{n+} ions are reduced by the JT distortion but the JT distortions are not strong enough to completely quench the orbital angular moment of $Coⁿ⁺$ (Tables 2–4). As found for Ca_3CoMnO_6 ,⁴ therefore, the oxides $Ca_3CoMO_6 (M=Co, Rh, Ir)$ cannot possess a genuine uniaxial magnetism. We investigate the preference of their spin orientation by performing $LSDA+U+SOC$ (WIEN2k) calculations for the JT-distorted $Ca₃Co₂O₆$, $Ca₃CoRhO₆$, and $Ca₃CoIrO₆$ with $||c-$ and $\perp c$ -spin orientations. Our calculations show that the \bot c-spin orientation is less stable than the ||c-spin orientation by 33, 26, and 27 meV/FU for $Ca₃Co₂O₆$, $Ca₃CoRhO₆$, and $Ca₃CoIrO₆$, respectively, which represent very strong easy-axis anisotropy. This renders the observed anisotropic magnetic character to $Ca_3Co_2O_6$, Ca_3 - $CoRhO₆$, and $Ca₃CoIrO₆$.

5. One-Electron Picture in $DFT+U$ Description: Analysis of the Electronic Structure of $Ca₃Co₂O₆$

In general, it is not straightforward to decipher a oneelectron picture hidden behind the results of DFT calculations especially when the latter include effects of spin-polarization/ on-site repulsion.³⁶ To estimate the energy separation Δ_1 between d_0 and (d₂, d₋₂) as well as the energy separation Δ_2 between (d_2, d_{-2}) and (d_1, d_{-1}) (see Figure 2a) of the TP Co³⁺ ion in $Ca_3Co_2O_6$, one may perform one-electron tight-binding calculations for an isolated TP $CoO₆$. The $CoO₆$ TP found in $Ca₃Co₂O₆$ differs slightly from the ideal $Co₆TP$ in that the two O₃ triangular faces are not eclipsed but are rotated away from each other around the C_3 axis by the angle $\phi = 14.25^{\circ}$. Our extended Hückel tight-binding calculations $37,38$ for the CoO₆ TP show that $\Delta_1 = 0.20$ eV and $\Delta_2 = 0.65$ eV for the CoO₆ TP with $\phi = 0^{\circ}$, while $\Delta_1 = 0.13$ eV and $\Delta_2 = 0.74$ eV for the CoO₆ TP with $\phi = 14.25^{\circ}$. (The atomic parameters used for these calculations are summarized in Table S4 of the Supporting Information.) Thus, $\Delta_1 (0.13 - 0.20 \text{ eV})$ is greater than the typical SOC energy expected for 3d transition metal oxides (i.e., less than 0.05 eV^{39} by a factor of 3-4 and is smaller than Δ_2 only by a factor of 3-6. Consequently, the correct d-state split pattern for the TP Co^{n+} ions of Ca_3Co- MO₆ should be $d_0 < (d_2, d_{-2}) < (d_1, d_{-1})$ with $\Delta_1 = 0.13$ -0.20 eV and $\Delta_2 = 0.65 - 0.74$ eV. In the following, we examine how this split pattern is manifested in the $LSDA+U$ and LSDA+U+SOC calculations for $Ca_3Co_2O_6$.

As reported by Wu et al.,²¹ our study for $Ca_3Co_2O_6$ shows that the TP Co³⁺ ion has the L = 2 configuration $(d_0)^1(d_2)$, $(d_{-2})^3(d_1, d_{-1})^2$ in the LSDA+U+SOC calculations but the L = 0 configuration $(d_0)^2(d_2, d_{-2})^2(d_1, d_{-1})^2$ in the LSDA+U calculations. This can be seen from the projected DOS plots presented in Figure 5. To understand the switching of the $L = 0$ configuration to the $L = 2$ configuration by the action of SOC, it is necessary to consider three effects, that is, the spin arrangement between adjacent TP and OCT $Co³⁺ ions, ^{1,40}$ the direct metal-metal interaction between them, and the SOC on the TP $Co³⁺$ ion.^{21,40} It is convenient to discuss these factors by considering an isolated dimer made up of adjacent TP $CoO₆$ and OCT $CoO₆$, as pointed out elsewhere.⁴⁰

We first consider the interaction between the z^2 orbitals of adjacent $Co³⁺$ ions. In a one-electron tight-binding description, the high-spin $\text{Co}^{3+}\text{ (d}^6)$ ion of an isolated TP CoO_6 has the $(d_0)^2(d_2, d_2)^2(d_1, d_1)^2$ configuration while the low-spin Co^{3+} (d⁶) ion of an isolated OCT CoO₆ has the (t_2, g) ⁶ configuration. The OCT CoO₆ in Ca₃Co₂O₆ has C_3 symmetry, so the t_{2g} level is split into the 1a and 1e set as depicted in Figure 2b. The z^2 orbital of the TP Co^{3+} ion can interact directly with the 1a orbital (i.e., the z^2 orbital) of the OCT $Co³⁺$ ion through the shared triangular face due to the very short NN Co \cdots Co distance (2.595 Å). In describing such an interaction at the spin-polarized $DFT+U$ level, it should be noted that one-electron energy levels given by tight-binding calculations are split into the up-spin and down-spin levels by the spin-polarization/on-site repulsion, as illustrated in Figure 6. Thus, the L = 0 configuration $(d_0)^2(d_2, d_{-2})^2(d_1,$ $(d_{-1})^2$ of the TP Co³⁺ ion means that the LUMO of the TP CoO_6 is given by the (d_2, d_{-2}) level. Therefore, if one of the four electrons present in the two z^2 orbitals of adjacent TP

⁽³⁶⁾ Whangbo, M.-H.; Koo, H.-J.; Villesuzanne, A.; Pouchard, M. Inorg. Chem. 2002, 41, 1920.

⁽³⁷⁾ Hoffmann, R. J. Chem. Phys. 1963, 39, 1397.

⁽³⁸⁾ Our calculations were carried out by employing the SAMOA (Structure and Molecular Orbital Analyzer) program package (this program can be downloaded free of charge from the website, http://chvamw.chem. ncsu.edu/).

⁽³⁹⁾ Mapps, F. E.; Machin, D. J. Magnetism and Transition Metal Complexes; Chapman and Hall: London, 1973.

⁽⁴⁰⁾ Dai, D.; Xiang, H. J.; Whangbo, M.-H. J. Comput. Chem. 2008, 29, 2187.

Figure 5. Projected DOS plots for the z^2 , $(x^2-y^2 + xy)$ and $(xz + yz)$ states of the TP and OCT Co³⁺ jons in the FM state of Ca₂Co₂O₆ obtained states of the TP and OCT Co^{3+} ions in the FM state of $\text{Ca}_3\text{Co}_2\text{O}_6$ obtained from the LSDA+U and LSDA+U+SOC calculations by using the FPLAPW method of the WIEN2k package, the experimental structure of $Ca_3Co_2O_6$, and $U_{eff}(Co) = 4$ eV.

Figure 6. Schematic representations of the high-spin electron configuration of the trigonal prism $\text{Co}^{3+}\text{ (d}^6\text{) in (a)}$ the one-electron picture and (b) the spin-polarized $\overline{DFT+U}$ level of description.

and OCT Co³⁺ ions is transferred to the (d_2, d_{-2}) ^{\downarrow} level of the TP $Co³⁺$ ion, the resulting electron configuration of the TP Co^{3+} ion would be close to $(d_0)^1(d_2, d_{-2})^3(d_1, d_{-1})^2$. The spins

Figure 7. DFT+U level description of the orbital interactions between the z^2 orbitals of adjacent TP and OCT Co³⁺ ions in Ca₃Co₂O₆ that lead to the σ and σ^* orbitals when the spins of the two Co³⁺ sites have (a) a ferromagnetic and (b) an antiferromagnetic arrangement.

Figure 8. Effect of the SOC at the TP Co³⁺ ion on the occupancy of the σ^* l level of a dimer unit consisting of two adjacent TP and OCT Co³⁺ ions $\sigma^* \bar{l}$ level of a dimer unit consisting of two adjacent TP and OCT Co³⁺ ions
in Ca₃Co₂O₆ for cases when the d-state split pattern of the TP Co³⁺ ion is given by (a) $d_0 < (d_2, d_{-2}) < (d_1, d_{-1})$ and (b) $(d_2, d_{-2}) < d_0 < (d_1, d_{-1})$.

of the TP and OCT $Co³⁺$ ions are assumed to have the FM arrangement in Figure 7a, where the z^2 and z^2 levels of the OCT Co³⁺ ion are split less than those of the TP Co³⁺ ion OCT $Co³⁺$ ion are split less than those of the TP $Co³⁺$ ion because, to a first approximation, the OCT site has a low-spin $Co³⁺$ ion whereas the TP site has a high-spin $Co³⁺$ ion. Since both TP and OCT sites have Co^{3+} ions, the midpoint between their z^2 and z^2 levels should be nearly the same. The highest
occupied level resulting from the z^2 orbitals of the two Co^{3+} occupied level resulting from the z^2 orbitals of the two Co^{3+} ions is the σ^* level, in which the weight of the TP z^2 orbital is
larger than the OCT z^2 orbital because the former lies higher larger than the OCT z^2 orbital because the former lies higher
in energy than the latter. In the DET+LL level of description in energy than the latter. In the $DFT+U$ level of description, the occupied σ^* level lies below the empty (d_2, d_2) level of the TP $Co³⁺$ ion. The effect of the SOC interaction at the TP $Co³⁺$ ion site is depicted in Figure 8a, where the SOC splits the unoccupied degenerate level $(d_2, d_{-2})\neq 0$ into the $d_2\downarrow$ below-d₋₂^{\downarrow} pattern since $\lambda < 0$ for Co^{3+} (d^{6}). When the unoccupied delevel is lowered below the occupied $\sigma^* \downarrow$ level unoccupied d_2 level is lowered below the occupied σ^* level, an electron transfer occurs from the σ^* level to the d₂ ℓ level. Since the $\sigma^* \downarrow$ level has a greater weight on the TP $z^2 \downarrow$ orbital, this charge transfer effectively amounts to the configuration this charge transfer effectively amounts to the configuration switch of the TP Co³⁺ from the L = 0 configuration $(d_0)^2$ (d_2) , $(d_{-2})^2(d_1, d_{-1})^2$ to the L = 2 configuration $(d_0)^1(d_2, d_{-2})^3(d_1, d_2)$ $(d_{-1})^2$. This is why the TP Co³⁺ ion has the $(d_0)^2(d_2, d_{-2})^2(d_1,$ d_{-1})² configuration at the DFT+U level, but has the $(d_0)^1(d_2)$ $(d_{-2})^3(d_1, d_{-1})^2$ configuration at the DFT+U+SOC level. This explanation is based on the d-state split pattern of $d_0 < (d_2, d_{-2}) < (d_1, d_{-1})$ for the TP Co³⁺ ion. If the TP Co^{3+} ion were to have the $(d_2, d_2) < d_0 < (d_1, d_1)$ split pattern (Figure 8b), the TP Co^{3+} ion would have the d_2 , $\left(\frac{d}{d_1}\right)^3\left(\frac{d_0}{d_1}\right)^1\left(\frac{d_1}{d_1}\right)^2$ configuration in both DFT+U and $DFT+U+SOC$ levels of descriptions because the σ^*V level remains unoccupied regardless of whether or not the singly occupied (d_2, d_2) level is split by the effect of SOC.

Figure 9. Orbital interactions between the z^2 orbitals of adjacent TP Co^{2+} and OCT M^{4+} ions in Ca -CoMO_{ϵ}(M = Rh Ir) that lead to the σ **Figure 9.** Orbital interactions between the z^2 orbitals of adjacent TP Co^{2+} and OCT M^{4+} ions in Ca_3CoMO_6 ($M = Rh$, Ir) that lead to the σk and $\sigma^* k$ orbitals when the spins of the two ion sites have (a) an and σ^* orbitals when the spins of the two ion sites have (a) an FM and (b) an AFM arrangement. The midpoint between the z^2 and z^2 orbitals is higher in energy for the M^{4+} ($M = Rh, Ir$) ion than that for the Co^{2 because the Rh 4d and Ir 5d orbital is more diffuse, and lies higher in energy, than the Co 3d orbital. The σ^* orbital lies higher in energy in the FM than in the AFM spin arrangement.

6. Electronic Structures of Ca_3CoMO_6 (M = Rh, Ir)

The reason why Ca_3CoMO_6 (M = Rh, Ir) has Co^{2+} and M^{4+} ions in the TP and OCT sites is that the Co 3d orbital lies lower in energy, and is more contracted, than the Rh 4d and Ir 5d orbitals. Thus, the essential features of the direct metalmetal interaction between the TP Co^{2+} and OCT Rh⁴⁺ ions, which give rise to the configuration $(z^2)^2(x^2-y^2, xy)^3(xz, yz)^2$ for the TP Co²⁺ ion and the configuration $(1a)^{1}(1e)^{4}$ for the OCT Rh^{4+} ion, can be understood in terms of the orbital interaction diagram shown in Figure 9a. Here the two adjacent ions have the FM arrangement, and the midpoint between the z^2 and z^2 orbitals is placed higher in energy for the $M^{4+} (M = Rh \text{ Ir})$ ion than that for the Co^{2+} ion, because the M^{4+} (M = Rh, Ir) ion than that for the Co^{2+} ion, because the Rh 4d and Ir 5d orbital is more diffuse, and lies higher in energy, than the Co 3d orbital.^{38,41} The σ^* level (i.e., the highest-lying level arising from the interactions between the $z²$ orbitals of adjacent Co^{2+} and M^{4+} site) has a larger weight on the OCT M^{4+} ion so that the absence of an electron in the σ^* level amounts to the $(1a)^{1}(1e)^{4}$ configuration for the OCT M^{4+} ion.

The low-spin OCT M^{4+} (d⁵) ion of Ca₃CoMO₆ (M = Rh, Ir) has the open-shell configuration, $(t_{2g})^5$, and the Rh and Ir atoms are a heavier element than Co. Therefore, the local electronic structure of M^{4+} (d⁵) ion can be more strongly affected by the SOC compared with that of the OCT Co³⁺ (d⁶) ion in Ca₃Co₂O₆. In principle, the $(t_{2g})^5$ configuration can be approximated by either $(1a)^{1}(1e)^{4}$ or $(1a)^{2}(1e)^{3}$ (see Figure 2b). The angular momentum behavior of the 1a (i.e., z^2) orbital is described by d_0 , and those of the 1e orbitals by linear combinations of $d_{\pm 1}$ and $d_{\pm 2}$, namely, by $(2/3)^{1/2}$ - $(x^{2}-y^{2})$ - $(1/3)^{1/2}yz$ and $(2/3)^{1/2}xy$ - $(1/3)^{1/2}xz^{42}$ Thus, the orbital moment μ _L of the OCT M^{4+} (d⁵) ion would be negligible if its electron configuration is close to $(1a)^{1}(1e)^{4}$. However, this would not be the case if the electron configuration is close to $(1a)^2(1e)^3$. As discussed below, it depends on the spin arrangement between adjacent Co^{2+} and M^{4+} ions, the direct metal-metal interaction between them, and the SOC of the M^{4+} ion whether the local electronic structure of the OCT M^{4+} (d⁵) ion is close to $(1a)^{1}(1e)^{4}$ or to $(1a)^{2}(1e)^{3}$.

Figure 10. Projected DOS plots for the z^2 , $(x^2-y^2 + xy)$ and $(xz + yz)$ states of the TP Co²⁺ and OCT Rh⁴⁺ ions in the FM state of Ca₃CoRhO₆ obtained from the $LSDA+U+SOC$ calculations by using the FPLAPW method of the WIEN2k package, the experimental structure of $Ca₃CoR$ hO_6 , and $U_{\text{eff}} = 4$ eV on both Co and Rh.

As shown by the projected DOS plots for the FM state of $Ca₃CoRhO₆$ in Figure 10, the LSDA+U+SOC (WIEN2k) calculations with $U_{\text{eff}}(C_0) = U_{\text{eff}}(Rh) = 4 \text{ eV}$ predict Ca_3CoR hO_6 to be a magnetic insulator, whereas our LSDA+U calculations with $U_{\text{eff}}(\text{Co})=U_{\text{eff}}(\text{Rh})=4 \text{ eV}$ predict Ca₃CoR hO_6 to be a metal (see Figure S1 of the Supporting Information). (The LSDA+ U and LSDA+U+SOC calculations with $U_{\text{eff}}(Co) = 4$ eV and $U_{\text{eff}}(Rh) = 2$ eV both predict $Ca₃CoRhO₆$ to be a metal. see Figure S2 of the Supporting Information). The projected DOS plots from the $LSDA+$ U+SOC calculations show that the local electronic structure of the TP Co²⁺ ion is given by $(z^2)^2(x^2-y^2, xy)^3(xz, yz)^2$ and that of the OCT Rh^{4+} ion by $(1a)^{1}(1e)^{4}$. This explains the uniaxial magnetism of Ca_3CoRhO_6 brought about by the $L = 2$ configuration of the TP Co²⁺ ion and why the orbital moment μ_L of the OCT Rh⁴⁺ ion is nearly zero (see Table 3) in the $LSDA+U+SOC$ calculations.

The above discussion for the FM state of $Ca₃CoRhO₆$, which accounts for the configuration $(z^2)^2(x^2-y^2, xy)^3(xz,$ yz)² for the TP Co²⁺ ion and the configuration $(1a)^{1}(1e)^{4}$ for the OCT Rh^{4+} ion, is also applicable to the FM state of $Ca₃CoIrO₆$. The AFM spin arrangement (i.e., the ferrimagnetic state) of $Ca₃CoIrO₆$ has a slightly different picture for the local electronic structure of the OCT Ir^{4+} ion. The projected DOS plots for the AFM state are presented in Figure 11, where the OCT Ir^{4+} ion is not described by $(1a)^{1}(1e)^{4}$ but by $(1a)^{2}(1e)^{3}$. (The LSDA+ U and LSDA+ U+SOC calculations with $U_{eff}(Co) = 4$ eV and $U_{eff}(Ir) = 2$ eV both predict Ca_3CoIrO_6 to be a metal. See Figure S3 of the Supporting Information.) As a consequence, the orbital moment μ _L of the OCT Ir⁴⁺ ion is large (Table 4). This observation is explained by noting from Figure 9 that the σ^* level of the dimer made up of adjacent TP $Co²⁺$ and OCT $Ir⁴⁺$ ions would lie lower in energy in the AFM than in the FM spin arrangement, because the energy gap between the z^2 orbitals of the two ions is greater for the AFM arrange-
ment. The 1el level of the OCT Ir⁴⁺ ion is split by SOC and ment. The 1eV level of the OCT Ir^{4+} ion is split by SOC, and the OCT Ir⁴⁺ ion adopts the $(1a)^2(1e)^3$ configuration when the upper one of the split 1eV level becomes higher in energy

⁽⁴¹⁾ Clementi, E.; Roetti, C. Atomic Data Nuclear Data Tables 1974, 14, 177.

^{(42) (}a) Albright, T. A.; Hofmann, P.; Hoffmann, R. J. Am. Chem. Soc. 1977, 99, 7546. (b) Orgel, L. E. An Introduction to Transition Metal Chemistry; Wiley: New York, 1969; p 174.

Figure 11. Projected DOS plots for the z^2 , $(x^2-y^2 + xy)$ and $(xz + yz)$
states of the TP Co²⁺ and OCT Ir⁴⁺ ions in the AEM state of Ca₂CoIrO states of the TP Co^{2+} and OCT Ir⁴⁺ ions in the AFM state of Ca₃CoIrO₆ obtained from the $LSDA+U+SOC$ calculations by using the FPLAPW method of the WIEN2k package, the experimental structure of Ca₃-CoIrO₆, and $U_{\text{eff}}(\text{Co}) = U_{\text{eff}}(\text{Ir}) = 4 \text{ eV}$.

Figure 12. SOC effects on the 1eV level of the OCT M^{4+} ion and on the occupancy of the σ^* level of a dimer made up of two adjacent TP Co² and OCT M^{4+} ions in Ca₃CoMO₆ (M = Rh, Ir): (a) Ca₃CoRhO₆ and (b) Ca₃CoIrO₆.

than the σ^* level (Figure 12). Since the Ir⁴⁺ ion has a stronger SOC than does the Rh^{4+} ion, the split of the 1eV level is larger in Ca₃CoIrO₆ than in Ca₃CoRhO₆. In addition, the Co \cdots Ir metal-metal interaction is weaker than the $Co \cdots Rh$ metalmetal interaction because the NN $Co \cdot \cdot \cdot$ Ir distance is longer than the NN $Co \cdots Rh$ distance. This makes the 1eV level lying lower in $Ca₃CoIrO₆$ than in $Ca₃CoRhO₆$. Consequently, the OCT Rh⁴⁺ ion has the $(1a)^{1}(1e)^{4}$ configuration, but the OCT Ir⁴⁺ ion the $(1a)^2(1e)^3$ configuration.

7. Discussion

For the SOC effect to induce electron transfer from the σ^* V level to the d₂V level in Ca₃Co₂O₆ (Figure 7a), the σ^* V level should lie high in energy because the split between the d_2 and d_{-2} levels by SOC is not large for a 3d transition metal ion. Important factors raising the σ^* level are the direct metal-metal interaction and the FM spin arrangement between adjacent $Co³⁺$ ions. Compared with the AFM arrangement (Figure 7b), the FM arrangement has a smaller energy difference between the z^2 orbitals of the TP
and OCT Co³⁺ jons, which leads to a stronger interaction and OCT Co^{3+} ions, which leads to a stronger interaction between them hence raising the σ^* level higher. Another important factor is that the TP and OCT sites both have Co^{3+} ions with similarly contracted z^2 orbitals so that

the overlap between them is good hence raising the σ^* level.

In the LSDA+U+SOC calculations, both the σ and σ^* levels are both occupied. In contrast, the $\sigma\ell$ level is filled but the σ^* V level is not. Consequently, the Co \cdots Co metal-metal interaction in $Ca₃Co₂O₆$ is overall bonding. This accounts for why the displacement of the TP Co^{3+} ion is not large in the JT distorted structure of $Ca_3Co_2O_6$. This reasoning suggests that the Co \cdots M metal-metal interaction in Ca₃CoMO₆ (M = Rh, Ir) should be weak because the TP $Co²⁺$ ion has a large displacement in the JT distorted structure. The NN $Co \cdots Rh$ and $Co \cdot \cdot \cdot$ Ir distances of Ca₃CoRhO₆ and Ca₃CoIrO₆, respectively, are short (i.e., 2.682 and 2.706 Å, respectively) but are longer than the NN Co \cdots Co distance (2.595 Å) of $Ca₃Co₂O₆$. Furthermore, the Co 3d and Rh 4d orbitals are different in orbital contractedness, and even more so are the Co 3d and Ir 5d orbitals. Consequently, the direct metalmetal interaction between Co^{2+} and M^{4+} ions in Ca₃CoMO₆ (M = Rh, Ir) would be weaker than that between Co^{3+} ions in $Ca_3Co_2O_6$. This accounts for why the displacement of the TP Co^{2+} ion is large in the JT distorted structures of $Ca₃CoMO₆$ (M = Rh, Ir).

The differences in the z^2 orbital occupations of the TP and OCT ions in Ca_3CoMO_6 (M = Co, Rh, Ir) are important to note. From the viewpoint of two adjacent TP and OCT ions, the highest-lying level resulting from their two z^2 orbitals is the σ^* V level, which decreases in energy with lengthening the NN $Co \cdots M$ distance and with increasing the difference in the contractedness of the Co and M z^2 orbitals. Thus, it is understandable that the two z^2 orbitals of adjacent TP and OCT ions have four electrons in Ca₃CoIrO₆ (i.e., the σ^*) level is occupied) but three electrons in $Ca₃Co₂O₆$ and $Ca₃CoRhO₆$ (i.e., the σ^*) level is unoccupied). The latter is equivalent to a singly occupied z^2 orbital at the TP Co³⁺ ion in Ca₃Co₂O₆, but that at the OCT Rh^{4+} ion in Ca₃CoRhO₆, due to the unequal weights of the TP and OCT z^2 orbitals in the σ^* level (Figure 7 vs Figure 9). A higher-lying σ^* level and a lowerlying σ level are obtained when adjacent TP and OCT ions have an FM spin arrangement than an AFM spin arrangement. Thus, the FM arrangement is energetically more favorable when the σ^* level is unoccupied as found for $Ca₃Co₂O₆$ and $Ca₃CoRhO₆$, but an AFM arrangement is energetically more favorable when the σ^* level is occupied as found for $Ca₃CoIrO₆$.

8. Concluding Remarks

In summary, the JT instability, uniaxial magnetism, spin arrangement, metal-metal interaction, and spin-orbit coupling are intimately interrelated in $Ca₃CoMO₆$ (M = Co, Rh, Ir). The adjacent spins in each $CoMO₆$ chain of $Ca₃CoMO₆$ $(M = Co, Rh, Ir)$ prefer the FM arrangement for $M = Co$ and Rh but the AFM arrangement for $M = Ir$. The magnetism of $Ca_3CoMO₆$ (M = Co, Rh, Ir) cannot be genuinely uniaxial because it undergoes a weak JT distortion. Nevertheless, the orbital moments of the TP $Coⁿ⁺$ ions, though strongly reduced by the distortion, are still substantial enough to produce strong easy-axis anisotropy along the chain direction. The d-state split pattern of the TP Co^{n+} (n = 2, 3) ions that is consistent with the electronic and magnetic properties of Ca₃CoMO₆ (M = Co, Rh, Ir) is not $(d_2, d_{-2}) < d_0 < (d_1,$ (d_{-1}) but $d_0 \leq (d_2, d_{-2}) \leq (d_1, d_{-1})$. The $L = 2$ configuration $(d_0)^1(d_2, d_{-2})^3(d_1, d_{-1})^2$ of the TP Co³⁺ ion in Ca₃Co₂O₆ is a

combined consequence of the FM spin arrangement between adjacent TP and OCT Co^{3+} ions, the direct metal-metal interaction between them mediated by their z^2 orbials, and the SOC of the TP $Co³⁺$ ion. In contrast to the case of $Ca_3Co_2O_6$, the TP and OCT ions of Ca_3CoMO_6 (M = Rh, Ir) have different oxidation states ($+2$ and $+4$, respectively), because the Co 3d orbital lies lower in energy, and is more contracted, than the Rh 4d and Ir 5d orbitals. The OCT M^{4+} ion has the $(1a)^{1}(1e)^{4}$ configuration for M = Rh but the $(1a)^2(1e)^3$ configuration for M = Ir. This difference reflects a combined consequence of the spin arrangement between adjacent TP Co^{2+} and

OCT M^{4+} ions, the direct metal-metal interaction between them mediated by their z^2 orbitals, and the SOC of the TP M^{4+} ions.

Acknowledgment. The work at North Carolina State University was supported by the Office of Basic Energy Sciences, Division of Materials Sciences, U.S. Department of Energy, under Grant DE-FG02-86ER45259.

Supporting Information Available: Additonal tables and figures. This material is available free of charge via the Internet at http://pubs.acs.org.