High-Pressure Synthesis and Superconductivity of a New Binary Barium Germanide BaGe₃

Hiroshi Fukuoka,* Yusuke Tomomitsu, and Kei Inumaru

Department of Applied Chemistry, Faculty of Engineering, Hiroshima University, Higashi-Hiroshima 739-8527, Japan

S Supporting Information

ABSTRACT: A new binary barium germanide $BaGe₃$ was prepared by highpressure and high-temperature reactions using a Kawai type multi-anvil press. It crystallizes in a hexagonal unit cell with $a = 6.814(1)$ Å, $c = 5.027(8)$ Å, and $V = 202.2(5)$ Å³ (the space group $P6_3/mmc$, No. 194). The unit cell contains two layers along the c axis composed of Ba atoms and $Ge₃$ triangular units. The triangular units stack along the c axis to form 1D columns in which the adjacent $Ge₃$ units turn to opposite directions. The columns, therefore, can be described as the face-sharing stacking of elongated $Ge₆$ octahedra. Each Ba atom is surrounded by six columns. Ba $Ge₃$ is metallic and shows superconductivity at 4.0 K. The band structure calculations revealed that there are four conduction bands mainly composed of Ge 4p and Ba 5d orbitals. From Fermi surface analysis, we confirmed that three of them have a large contribution of Ge 4pz orbitals in the vicinity of the Fermi level and

show a simple 1D appearance. The remaining one contains Ge 4px, 4py, and Ba 5d contributions and shows a 2D property.

INTRODUCTION

The binary Ba-Ge system has received considerable attention in recent years because of its diversity of structure as well as interesting properties such as thermoelectric and superconducting behaviors. Figure 1 depicts the structural evolution with an increase in Ge content in the Ba-Ge binary system.^{1,2} Binary compounds with Ge/Ba \leq 2 form alloys or Zintl phases. The orthorhombic BaGe₂ containing Ge₄²⁻ anions is a typical example of the latter group and shows semiconducting properties.^{3,4} The orthorhombic phase undergoes a phase transition at 4.0 GPa and 1000 °C to the α -ThSi₂ structure.⁵ This high-pressure phase shows superconductivity with a critical temperature T_c of 4.93 K.⁶

In Ge-rich conditions, two clathrate compounds are produced under ambient pressure. They are $Ba_{24}Ge_{100}$ and Ba_8Ge_{43} having the type III and I clathrate structures, respectively.⁷⁻¹⁴ The host Ge atoms compose 3D covalent networks with large cages where Ba atoms are situated. Recently, a new germanium clathrate compound, BaGe₅, has been reported.¹⁵ It is a semiconducting Zintl phase.

These clathrate compounds and their derivatives prepared by substitution of post-transition elements for some Ge atoms are extensively studied as promising candidates for the application of thermoelectric devices.^{9,16} The superconductivity of clathrate compounds also attracts much attention these days. $Ba_{24}Ge_{100}$ is isotypic with the superconducting silicon analogue $Ba_{24}Si_{100}$ and shows superconductivity at 0.24 K^{17-19} There have been many studies of the physical properties of $Ba_{24}Ge_{100}$.^{20–23}

Thus, many binary compounds are reported in the $Ba-Ge$ system. However, no 1:3 compound has been prepared, although many 1:3 compounds having the famous structure types of

Cu₃Au, BaPb₃, Ni₃Sn, YGe₃, and so forth were discovered in many binary germanide systems. We have examined the reactions of 1:3 mixtures of Ba and Ge by changing reaction pressures from 5 to 13 GPa, and have successfully obtained a new binary barium germanide BaGe₃.

EXPERIMENTAL SECTION

BaGe₃ was prepared by the following two-step reactions. A mixture of Ba (Nakarai Tesque 99%) and Ge (Mitsuwa Pure Chemical 99.999%) with a molar ratio of 1:2 was reacted in an Ar-filled arc furnace to obtain BaGe₂. It was mixed with a Ge powder with a molar ratio BaGe₂/Ge = 1:1 (Ba/Ge = 1:3). The mixture was placed in an h-BN cell. The cell was placed in an MgO octahedral pressure medium and was heated at high pressures using a Kawai-type multi-anvil press.²⁴ We performed the reactions varying temperature (500-1200 °C) and pressure (3-13 GPa).

The products were characterized by X-ray powder diffraction (XRD) measurements with a Bruker AXS D8 Advance diffractometer with Nifiltered $CuK\alpha$ radiation. The crystal structure was analyzed using a single crystal with a size of 0.05 \times 0.10 \times 0.10 mm 3 . The X-ray diffraction data was collected using a Bruker APEX-II CCD diffractometer with graphite-monochromated MoKR radiation. The structure was solved and refined using the Bruker SHELXTL software package.²⁵ Chemical compositions of the products were examined by an electron probe micro-analyzer (EPMA) (JEOL JCMA-733). Magnetic susceptibility measurements were performed with a SQUID magnetometer (Quantum Design MPMS-5) in a 20 Oe field. Temperature dependence of electrical

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Published: June 06, 2011
Received: April 20, 2011
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Figure 1. Binary compounds of the Ba-Ge system with a Ge to Ba ratio ranging from 2 to 6.

Figure 2. X-ray powder diffraction patterns of two samples prepared at 1200 °C under different pressures. Asterisk and star marks show the diffraction peaks of Type I clathrate compound and $BaGe₂$ (highpressure phase), respectively. Open circles show diffractions of the new compound.

resistivity was observed with the van der Pauw method using dc from room temperature to 2 K.

The band structure calculation was performed using the WIEN2k package with a full-potential augmented plane-wave $+$ local orbitals $(APW+I_o)$ code.^{26,27} Some parameters used were as follows: Muffin-Tin radius (RMT), 4.0 for Ba and 2.46 for Ge; Gmax, 12; RMT \times kmax, 7; number of k points, 10 000. Electron localization functional (ELF) and chemical bond analysis using Crystal orbital Hamilton population (COHP) techniques were calculated and analyzed using a tight-binding linear muffin-tin orbital-atomic sphere approximation with TB-LMTO-ASA software.²⁸

RESULTS AND DISCUSSION

The reaction at 5 GPa and 1200 °C yielded Ba_8Ge_{43} and BaGe₂ with the α -ThSi₂ structure as shown in part a of Figure 2. Several peaks marked with open circles seemed to be attributed to a new phase. The new phase became a main product by the reaction at 10 GPa and 1200 °C. The XRD pattern shown in part b of Figure 2 could not be identified as any binary $Ba-Ge$ compound.

We, therefore, performed single-crystal X-ray analysis and found that the phase crystallizes in a hexagonal unit cell with $a =$ 6.814(1) Å, $c = 5.027(8)$ Å, and $V = 202.2(5)$ Å³. The composition determined by the structure analysis was $BaGe₃$, which is

Table 1. Crystallographic Data and Details on the Structure Determination of BaGe₃

formula	BaGe3
fw	355.25
space group	$P6_3/mmc$ (No. 194)
$a/\text{\AA}$	6.814(1)
c /Å	5.027(8)
V/\AA^3	202.2(5)
Z	$\mathfrak{2}$
cryst size (mm)	$0.05 \times 0.1 \times 0.1$
diffractometer	Bruker APEX-II CCD
radiation (graphite monochromated)	МοΚα
μ (Mo K α)/mm ⁻¹	31.261
2θ limit	53.88
No. of observed unique reflections	105
No. of variables	8
R1, wR2	0.0156, 0.0328
goodness of fit, S	1.239
largest diff. peak and hole	$0.833/-0.525$

identical to the composition BaGe_{2.99} determined by the EPMA method. An EPMA image of $BaGe₃$ is shown in Figure S1 of the Supporting Information. The crystallographic data and atomic and thermal displacement parameters of $BaGe₃$ are listed in Tables 1 and 2.

The structure of BaGe₃ presented in Figure 3 is isotypic with the BaSn₃ structure.²⁹ It has a layer structure and each layer is composed of both Ba and Ge atoms. The arrangement of atoms in the layer is similar to that in a closest packing structure but not ideal. The Ge site is slightly away from the ideal position. This displacement forms $Ge₃$ triangular units with a $Ge-Ge$ distance of 2.613(4) Å in the layers. The direction of apexes of the triangular units in adjacent layers is opposite. The triangular units, therefore, make elongated $Ge₆$ octahedra by sharing their faces and form $1D$ columns as shown in Figure 3. The $Ge-Ge$ distance between the adjacent triangular units is 2.932(3) Å, which is quite longer than that of an intra-unit. Ba atoms are located around the columns. The physical properties of BaGe3 possibly reflect this 1D nature of the structure.

Figure 4 shows the temperature dependence of the resistivity of BaGe₃. The resistivity decreases with decreasing temperature showing that $BaGe₃$ is metallic. Furthermore, the zero resistivity was observed below 4.0 K suggesting that $BaGe₃$ is a superconductor

Figure 3. Crystal structure of BaGe₃ projected along the c axis (left) and on the $a-b$ plane (right). Orange and green spheres show Ba and Ge atoms, respectively.

Figure 4. Temperature dependence of the electrical resistivity of BaGe₃.

Figure 5. Temperature dependence of magnetic susceptibility of BaGe₃.

with the critical temperature (T_c) of 4.0 K. The magnetic susceptibility of $BaGe₃$ is presented in Figure 5. The Meissner effect was observed at 4.0 K and the superconducting volume fraction of the zero-field cooling sample at 2 K is calculated to be 146%. Owing to the demagnetization effect, the volume fraction is over 100%. From these observations, we confirmed that $BaGe₃$ is a new superconductor with a T_c of 4.0 K.

For further studies about the electronic properties of BaGe₃, we have performed the density of state (DOS) calculations. The

Figure 6. The density of state (DOS) of BaGe₃ obtained from $APW+$ lo calculations (the Wien2k code). The Fermi level is set as zero. (a) Total DOS diagram. The black, green, and red plots are the total, Getotal, and Ba-total DOSs, respectively. (b) Ge-partial DOS. The black, red, green, and blue lines show the total, 4s, 4p, and 4d contributions, respectively. (c) Ba-partial DOS. The black, red, green and blue lines show the contributions of the total, 5s, 5p, and 5d contributions, respectively.

results are shown in Figure 6. The total DOS diagram proves the metallic property of BaGe₃. The deep-lying bands below -5 eV are mainly composed of Ge 4s orbitals. The conduction bands are mainly composed of Ge 4p orbitals but a measurable contribution of Ba orbitals is also observed. The states in the vicinity of Fermi level (E_F) are mainly composed of Ge 4p and Ba 5d orbitals. It is noteworthy that the contribution of the Ge 4pz

Figure 7. COHP and ICOHP diagrams of $BaGe₃$ for the $Ge-Ge$ bond with a distance of 2.613 Å in the $Ge₃$ triangular unit.

orbital is observed to the conduction bands but large contributions of Ge 4px and 4py are also observed in the vicinity of E_F . This suggests that the two-dimensionally spread orbitals made of Ba 5d and Ge 4p orbitals are also important for the conductivity of BaGe₃ as well as the bands made of 1D Ge₃ columns. The detailed structure of conduction bands is discussed below using Fermi surface diagrams.

The COHP and ICOHP diagrams for the $Ge-Ge$ bond with 2.613 Å in the $Ge₃$ triangular unit are helpful to understand the detailed electronic structure of the unit. They are shown in Figure 7. The -ICOHP values at the Fermi level is 2.1 eV/bond, clearly suggesting the presence of a strong Ge-Ge covalent bond.

A -ICOHP value of 0.78 eV/bond was obtained for the 2.932 Å Ge $-Ge$ bond corresponding to the contact between two adjacent triangular units. This value also shows a fairly strong covalent interaction of $Ge₃$ triangles along the c axis, and supports the 1D column model of $BaGe₃$ from the point of view of electronic structure.

Figure 8 shows the electron localization functions for the $z = \frac{1}{4}$ plane of BaGe₃ projected along the *c* axis. Ba atoms and Ge3 triangular units reside on the plane. At each corner of the triangular units, a crescent-shaped area with high ELF values (η = 0.7) is observed. This corresponds to a lone pair of electrons. Other elevations of ELF values (η = 0.6) are observed around the middle points between Ge atoms. They presumably show the covalent electrons of the Ge-Ge bonds. This is in good agreement with the results of the COHP analysis.

LaGe₃, SrSn₃, and BaSn₃ also contain Ge₃ or Sn₃ triangular units.²⁹⁻³¹ All of them are composed of layers including one part of guest atoms and three parts of tetrel atoms but the stacking manner of the layers is different. The layer sequence is $ABAB \cdots$ or h in BaGe₃ and BaSn₃, whereas it is ABABCBCAC \cdots or hhc and ABABCACABCBC \cdots or hhcc in LaGe₃ and SrSn₃, respectively. Therefore, Ge_3 or Sn_3 units are one-dimensionally stacked in the former compounds but not in $LaGe₃$ and $SrSn₃$. Nonetheless, the ELF diagram of $BaGe₃$ is very similar to those of $LaGe₃$ and SrSn₃ as well as that of BaSn₃. The similarity shows the electronic structures of $Ge₃$ or $Sn₃$ triangular units in these compounds are quite similar to each other.

It is noteworthy to consider the schematic molecular orbitals (Figure 9) of Sn_3^2 proposed by Fässler et al.^{29,31} They estimated the orbitals using cyclo-propanyl cations $(C_3R_3^+)$ because it is

Figure 8. Electron localization function (ELF) diagram of $BaGe₃$ for the plane parallel to the $a-b$ plane on which Ge₃ triangle units and Ba atoms are situated. Red and green colors show the low and high ELF areas, respectively.

Figure 9. Schematic molecular orbitals of Sn_3^2 triangular unit proposed by Fässler et al. The highest occupied orbital for BaGe₃ is orbital 7. An arrow with dashed line shows the case of LaGe3.

isoelectronic with Sn_3^2 . The Ge_3 unit probably has a similar electronic structure to that of Sn_3^{2} . The lowest orbital (1) is a bonding one composed of three Sn 5s orbitals. The second lowest ones (2, 3) are 5s antibonding orbitals. These are well corresponding to the COHP diagram for $BaGe₃$ in Figure 7. The bands between -14 to -8 eV in the COHP diagram have negative COHP values, whereas positive values are seen from -8 to -6 eV. The former would be assigned to bonding bands of Ge 4s orbitals and the latter to antibonding ones.

The bands ranging -4 eV to E_F have negative COHP values, bonding character. They correspond to the four occupied orbitals $(4 - 7)$ in Figure 9. They can be assigned to a π -bonding orbital and three lone pairs of the $Ge₃$ unit. The highest occupied orbital (HOMO) of $BaGe₃$ is orbital 7, which has a bonding character. In LaGe $_3$, however, one more electron should be accommodated in the $Ge₃$ unit because one La atom donates three electrons. The additional electrons occupy π^* orbitals (8, 9). This should weaken the covalency of the Ge-Ge bond in the $Ge₃$ unit. In fact, the Ge-Ge distance is 2.634 Å for LaGe₃, which is longer than that for BaGe₃ (2.613 Å).³⁰ Thus, the consideration about the electronic structure of the $Ge₃$ unit is possible from the

Figure 10. Band structure (k-dispersion) of $BaGe₃$ and its schematic Brillouin zone with the reciprocal repetition axes. Blue, green, yellow, and red bands correspond to the Fermi surfaces of bands 51, 52, 53, and 54 in Figure 12, respectively.

Figure 11. Contributions of the (a) Ge px, (b) Ge py, (c) Ge pz, and (d) Ba d orbitals are shown in a fat band presentation.

discussion based on this simple model. Of course, because theoretical calculations should be required for detailed research for the electronic structure, we calculated the band structure of BaGe₃ using Wien2k and TB-LMTO-ASA programs.

The band structure of BaGe3 along the highly symmetrical paths is shown in Figure 10. Three bands (51, 52, and 53; latter two are degenerated) cross the $E_{\rm F}$ along the path from Γ to A,

 (a)

 (c)

Figure 12. Fermi surfaces of BaGe₃ calculated with Wien2k and XCrys- $Den³²$ software; (a) band 51, (b) band 52, (c) band 53, and (d) band 54.

corresponding the direction of the c axis in the real space. According to the fat band analysis, these bands are mainly contributed by Ge 4pz orbitals in the vicinity of E_F as shown in part c of Figure 11. The Fermi surfaces of these bands are presented in parts a, b, and c of Figure 12. The surfaces show a typical 1D character. These bands, therefore, reflect the column structure of $Ge₃$ triangular units. Another band (54) crosses the E_F along the Γ to K and K to M. The Fermi surface of the band 54 (part d of Figure 12) shows an electron-like surface. This band is mainly composed of Ge 4px, 4py, and Ba 5d orbitals as shown in parts a, b, and d of Figure 11, respectively. Because of the combination of Ge and Ba orbitals, BaGe3 acquires the conduction path spreading in the $a-b$ plane.

If the electronic structure of $BaGe₃$ were highly 1D, the crystal structure would have a superstructure along the c axis due to a presence of charge density wave (CDW). The 2D interactions between Ba and Ge would prevent the CDW and help the occurrence of superconductivity of BaGe3.

CONCLUSIONS

We prepared a new binary trigermanide $BaGe₃$ by highpressure and high-temperature reactions. It crystallizes in the BaSn₃ structure ($P6_3/mmc$) containing Ge₃ triangular units. The units stack along the c axis and form 1D $[Ge_3]_{\infty}$ columns. The COHP and ELF calculations revealed the electronic structure of the $Ge₃$ triangular unit. Each Ge atom has a lone pair and a strong covalent bond is observed between the Ge atoms. BaGe3 shows a superconducting transition at 4.0 K. There are four conduction bands; three have 1D character and are mainly contributed by Ge $4pz$ orbitals in the vicinity of E_F ; the remaining one shows an electron-like Fermi surface contributed by Ge 4px, 4py, and Ba 5d orbitals.

ASSOCIATED CONTENT

b Supporting Information. EPMA image of BaGe₃, and the crystallographic information file (CIF). This material is available free of charge via the Internet at http://pubs.acs.org.

NO AUTHOR INFORMATION

Corresponding Author

*Phone: $+81-824-24-7742$. Fax: $+81-824-24-5494$. E-mail: hfukuoka@hiroshima-u.ac.jp.

ACKNOWLEDGMENT

We are grateful to Mr. Yasuhiro Shibata of Hiroshima University for his help with the EPMA measurements. This work was supported by a Grant-in-Aid for Scientific Research from the Ministry of Education, Science, and Culture of Japan, Grant No. 16037212, 16750174, 18750182, 18027010, and 20550178.

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