Inorganic Chemistry

Effect of Alkali-Metal Ions on the Local Structure and Luminescence for Double Tungstate Compounds $AEu(WO_4)_2$ (A = Li, Na, K)

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S Supporting Information

ABSTRACT: The effect of alkali-metal ions on the local structure and luminescence properties for alkali-metal europium double tungstate compounds $AEu(WO_4)_2$ (A = Li, Na, K) has been investigated by a dual-space structural technique, atomic pair distribution function (PDF) analysis, and the Rietveld method of powder X-ray diffraction. The compounds $AEu(WO_4)_2$ (A = Li, Na) crystallize in the isostructure with the tetragonal space group I41/a(No. 88) and show the same luminescence properties in spite of the different doped alkali metals. However, $KEu(WO_4)_2$ crystallizes in monoclinic symmetry with the space group C2/c (No. 15). Compared with the two other counterparts, $KEu(WO_4)_2$ exhibits a more effective charge-transfer excitation, a larger Stokes shift, and a broader 612 nm emission band. This phenomenon is ascribed to the



lower crystal symmetry in $\text{KEu}(WO_4)_2$, which influences bond distances and the coordination number of Eu^{3+} . Two complementary methods, the Rietveld method and PDF analysis, reveal that both $\text{LiEu}(WO_4)_2$ and $\text{NaEu}(WO_4)_2$ afford the same local surroundings of Eu^{3+} . The local structure determined by the Rietveld and PDF methods well account for the observed luminescent properties.

INTRODUCTION

White light-emitting diodes (W-LEDs) have emerged as the most promising solid-state lighting sources to replace conventional incandescent and fluorescent lamps because of their high reliability, long lifetime, low energy consumption, and environ-mentally friendly characteristics.¹ However, at present the search for red phosphors with high efficiency, excellent chemical stability, and effective absorption in the blue or UV region to improve the color-rendering index (Ra) of W-LEDs is still a challenging research task.^{2,3} Eu³⁺-activated tungstates and molybdates with scheelite-like $(CaWO_4)$ structure have attracted much attention recently as interesting candidates for red-emitting phosphors. These materials have a broad and intense charge-transfer (CT) band in the UV region. The excitation intensity of Eu³⁺ in tungstates and molybdates at around 393 and 464 nm is prominently enhanced compared with that of Eu³⁺ in most hosts. For example, the composition $NaY_{0.5}Eu_{0.5}(WO_4)(MoO_4)$ shows a much higher light output than Y₂O₃S:Eu under 394 nm excitation.⁴ This efficient longwavelength-excited photoluminescence property of scheelitetype materials may find application in the production of red phosphors for LEDs. Remarkably, for alkali-metal-ion-containing luminescence materials, the effect of alkali-metal ions (Li, Na, and K) on the luminescence behavior of Eu³⁺-activated tungstates and molybdates has been widely discussed.⁵ It is found that the alkali-metal ions could not only enhance the luminescence intensity but also improve the color purity of the red phosphor. However, the effects of alkali-metal ions on the

luminescence properties for various host matrixes are often inconsistent. For instance, Shi et al.⁶ reported that under excitation of 395 and 465 nm, in the system of 0.24 concentration of Eu³⁺-activated CaWO₄, the enhanced luminescence was regarded as the result of a charge compensator of alkali-metal ions. In addition, the luminescent intensity varied with Li⁺, Na⁺, and K⁺ ions. With an increase of the alkali-metal ionic radius, the emission intensities gradually decreased. Therefore, the $Ca_{1-2x}Eu_xLi_xWO_4$ (x = 0.24) phosphor exhibits the strongest emission intensity. Li et al.⁷ also found this discrepant influence on the system of CaMoO₄:Tb³⁺, R⁺ (Li⁺, Na⁺ and K⁺), in which Na⁺ ions have an optimal enhancement luminescence, however. It is proposed that the creation of oxygen vacancies due to the radius discrepancy of alkali-metal and Ca²⁺ ions is disadvantageous to the enhancement luminescence. Liu et al.⁸ have investigated the dependence of the red emission intensity on the Eu³⁺ concentration (x) in a series of phosphors under excitation of 393 nm. They reported that for the phosphors $Ca_{1-2x}A_xMoO_4:xEu^{3+}$ (A = K⁺, Na⁺, and Li⁺), before 0.24 Eu³⁺-doped concentrations, the emission intensity increases obviously with various alkali-metal ions. When the doped amount of Eu³⁺ ions is 0.24, K⁺ ions have the best promotion effect. When the amount of dopant Eu³⁺ is increased again, red emission of Eu³⁺ is markedly enhanced by Na⁺ and Li⁺ ions.

Received: June 23, 2011 **Published:** October 26, 2011



Figure 1. Rietveld refinement of X-ray diffraction patterns for (a) $\text{LiEu}(WO_4)_2$, (b) $\text{NaEu}(WO_4)_2$, and (c) $\text{KEu}(WO_4)_2$. The observed counts are indicated by thin crosses in black, and the calculated pattern is indicated by a solid line in red. The difference pattern below is in blue.

When the doped amount of Eu³⁺ is 0.5, Li⁺ ions have the best effect. Actually, with the amount of Eu³⁺ up to 0.5, the phase $A_{0.5}Eu_{0.5}MoO_4$ (A = K⁺, Na⁺, and Li⁺) formed, which is absolutely ascribed to another series of compounds. Recently, Guo et al.⁹ reported that, in the double molybdate phosphors $AEu(MoO_4)_2$, the luminescence intensity of Eu³⁺ at the same temperature decreases in the order of $I_{Li} > I_{Na} > I_K$.

Taking into account the above discussion, to investigate the effect of alkali-metal ions on the emission intensity for alkalimetal-containing phosphors, we should keep the number of variables to a minimum. Specifically, the host structures and the doping concentration of alkali-metal ions and activator ions should be limited to those of comparable materials. Herein, we investigate the effect of alkali-metal ions on the local structure and luminescence properties for alkali-metal europium double tungstate compounds $AEu(WO_4)_2$ (A = Li, Na, K). This series of tungstates can be taken for the product of Eu³⁺ and an alkalimetal ion codoping scheelite-like (CaWO₄) structure with a maximum molar amount of Eu³⁺ and alkali of 0.5, wherein half the alkaline-earth ions are replaced by alkali metal and the other half by europium ions. For the family of $AEu(WO_4)_2$ (A = Li, Na, K), LiEu $(WO_4)_2$ and NaEu $(WO_4)_2$ adopt tetragonal space group I41/a (No. 88), whereas $KEu(WO_4)_2$ crystallize in

monoclinic symmetry with the space group C2/c (No. 15). It is believed that alkali-metal ions not only modify the crystal structure but also distort the metal oxide polyhedron and disturb the sublattice structure around the luminescent center ions. By a dual-space structural technique combining the Rietveld and atomic pair distribution function (PDF) methods, it is possible to observe the effect of changes of the structure parameters on the luminescence brightness related to the site symmetry and the strength of the crystal field. The long-range ordering of a crystalline structure can always be accurately determined by analysis of the Bragg intensities and positions using the Rietveld method. However, local atomic displacements away from the crystallographic sites, if they exist, are reflected in the crystal structure only in terms of the large thermal or Debye-Waller factor, which cannot be easily separated from the lattice vibration. The PDF analysis technique takes all of the components of the diffraction data (Bragg peaks and diffuse scattering) into account and thus reveals both the longer range atomic order and the local deviations from it, yielding the atomic structure in terms of a small set of parameters such as a unit cell and atomic coordinates. In order to gain further insight into the structural features of alkali-metal europium double tungstate compound $AEu(WO_4)_2$ (A = Li, Na, K), both short- and long-range order in these compounds should be considered. We expect that PDF analysis could help in getting a more complete and accurate picture of the effect of alkali-metal ions on the local structure and luminescence properties for alkali-metal europium double tungstate compounds.

EXPERIMENTAL SECTION

Synthesis. The red phosphors $AEu(WO_4)_2$ (A = Li, Na, K) were prepared by the solid-state reaction. The starting materials NaHCO₃, Li₂CO₃, K₂WO₄, WO₃, and Eu₂O₃ were weighted according to the stoichiometric ratio.^{10,11} After these powders were mixed thoroughly using a mortar, the homogeneous mixture was filled into a porcelain crucible and calcined in a muffle furnace for 10 h at a temperature of 750 °C. The products obtained were found to be polycrystalline and pink.

X-ray Diffraction Data Collection. X-ray diffraction patterns were collected on a Bragg–Brentano diffractometer (Rigaku D/Max-2000) with monochromatic Cu K α radiation ($\lambda = 1.5418$ Å) of a graphite curve monochromator. The X-ray diffraction data for structure determination and refinement were collected from $2\theta = 9$ to 130°, with a step length of 0.02 (2θ) and counting times of 40 s/ step. The Rietveld refinement software used is *GSAS*.¹⁷

PDF Data Acquisition. The experimental PDF, $G \exp(r)$, is the direct sine Fourier transformation of the normalized scattering intensity S(Q). S(Q) is obtained from the total scattering I(Q) by experimental background subtraction, polarization correction, Compton scattering correction, and the atomic form factor of the material under investigation.¹² Here, sample and empty sample data were collected by a powder X-ray diffraction experiment from $2\theta = 5$ to 105° , with a step length of 0.01 (2θ) and counting times of 10 s/step, $Q_{\text{max}} = 13.4 \text{ Å}^{-1}$. We used Mo K α ($\lambda = 0.717$ 07 Å; in-house Rigaku D/Max-2000) with a sealed X-ray tube source and a scintillation detector. The PDFs were generated using the program *PDFgetX2*.¹³ *PDFgui*, a real-space nonlinear least-squares regression refinement program, was used to fit the structural model to all experimental PDFs.¹⁴

Optical Measurements. The excitation and emission spectra were measured at room temperature by a Varain Cary-Eclipse 500 spectrofluorometer with a 60 W xenon lamp as the excitation source.

RESULTS AND DISCUSSION

Phase Characterization and X-ray Structure Analysis. The structures of the compositions were successfully refined by the *GSAS* suite.¹⁷ The refined instrument and structure parameters were cell parameters, background, sample displacement, asymmetry by divergence,¹⁸ spherical harmonics, etc. While $KEu(WO_4)_2$ has the lower symmetry C2/c (No. 15), $NaEu(WO_4)_2$ (JCPDF 04-002-3849) and $LiEu(WO_4)_2$ (JCPDF 04-008-0354) crystallize in a scheelite structure with the space group of I41/a (No. 88). Parts a-c of Figure 1 show the measured and calculated XRD patterns and the difference between them for LiEu(WO₄)₂, NaEu(WO₄)₂, and KEu- $(WO_4)_2$, respectively. The crystal structure of $KEu(WO_4)_2$ presented here is different from that of the previous study. The structure was refined using the atomic parameters from $KY(WO_4)_2$.¹⁶ From Figure 1, it can be seen that all diffraction peaks match well and no traces of the additional peaks from other impurities were observed. The ionic radii of Li, Na, and K in eight coordination (CN8) are 1.06, 1.32, and 1.38 Å, respectively.^{19–21} The smaller ionic radius of Li (CN8) directly results in the lattice contraction of $LiEu(WO_4)_2$. The formula unit volume of $KEu(WO_4)_2$ is 161.46, larger than those of both $LiEu(WO_4)_2$ (76.61) and $NaEu(WO_4)_2$ (78.87). This phenomenon is ascribed to the lower crystal symmetry of $KEu(WO_4)_2$. The crystallographic refinement data for these

compounds are summarized in Table 1 (also see the Supporting Information, Tables S1–S3).

Table	1.	Crystal	llograph	ic D)ata	of	LiEu(WO_4) ₂ ,
NaEu(V	VO ₄)	2, and K	Œu(WO ₄) ₂ at 1	Room	Ter	nperat	ure	

	$LiEu(WO_4)_2$	$NaEu(WO_4)_2$	$KEu(WO_4)_2$
structure	tetragonal	tetragonal	monoclinic
space group	I41/a (No. 88)	I41/a (No. 88)	C2/c (No. 15)
a (Å)	5.2115(3)	5.25997(3)	10.7043(2)
b (Å)	5.2115(3)	5.25997(3)	10.4730(2)
c (Å)	11.2823(4)	11.4030(1)	7.6082(2)
α (deg)	90.00	90.00	90.00
β (deg)	90.00	90.00	130.78(1)
γ (deg)	90.00	90.00	90.00
Ζ	4	4	4
volume of the unit cell $(Å^3)$	306.43(4)	315.49(1)	645.87(3)
<i>R</i> _p (%)	6.65	6.70	9.74
R _{wp} (%)	9.22	10.3	13.7
$R_{\rm F}$ (%)	4.23	3.56	4.34

In these structures, LiEu(WO₄)₂ and NaEu(WO₄)₂ are isostructures, which crystallize in the tetragonal space group I41/a (No. 88). The Eu³⁺ ions are in the distorted EuO₈ octahedral coordination with S₄ symmetry. Compound KEu-(WO₄)₂ crystallizes in monoclinic symmetry with the space group C2/c (No. 15), in which Eu³⁺ ions are in the EuO₆ polyhedron with C₂ symmetry. The local surroundings of Eu³⁺ ions of these three compounds are presented in Figure 2. The



Figure 2. Surroundings of the luminescent center (Eu³⁺ in light blue and O²⁻ in red) of (a) LiEu(WO₄)₂, (b) NaEu(WO₄)₂, and (c) KEu(WO₄)₂.

selected bond distances and coordination numbers of LiEu- $(WO_4)_2$, NaEu $(WO_4)_2$, and KEu $(WO_4)_2$ are listed in Table 2. The Eu-O bond distances in LiEu $(WO_4)_2$ and NaEu $(WO_4)_2$ are longer than that in KEu $(WO_4)_2$, while the Eu-O bond distance in NaEu $(WO_4)_2$ is longer than that in LiEu $(WO_4)_2$.

As mentioned above, the average structures have been determined by the Rietveld method. However, the local distortion information reflected in the crystal structure only in terms of the large thermal or Debye–Waller factor, which

Table 2. Selected Bond Distances of $LiEu(WO_4)_2$, $NaEu(WO_4)_2$, and $KEu(WO_4)_2$

	(a) Selected Bond Distances of LiEu(WO ₄) ₂						
bond type		CN			bond distance (Å)		
LilEu-O1		4			2.4465(2)		
LilEu-O2		4			2.4532(2)		
W-O		4			1.7602(3)		
(b) Selected Bond Distances of NaEu(WO ₄) ₂							
bond type	2	CN			bond distance (Å)		
NalEu-O	1	4			2.4543(2)		
NalEu-O2	2	4			2.4876(2)		
W–O		4			1.7866(1)		
(c) Selected Bond Distances of $KEu(WO_4)_2$							
bond type	CN	bond distance (Å)	bond type	CN	bond distance (Å)		
W-01	1	1.7974(2)	Eu-O1	2	2.2779(2)		
W-02	1	1.9963(2)	Eu-O2	2	2.3187(2)		
W-02	1	2.1046(1)	Eu-O3	2	2.3285(2)		
W-03	1	1.8343(3)	K-01	2	2.9588(1)		
W-04	1	1.7814(3)	K-04	2	2.7752(2)		
W-04	1	2.3576(3)	К-О4	2	2.8476(2)		

can not be easily separated from the lattice vibration. The local surrounding information of the Eu^{3+} ions is expected to be obtained by PDF analysis. Fourier transform shows that what PDF physically represents is a real-space map of the atomic positions within a solid. It allows the direct analysis of real space, rather than reciprocal space, which is conceptually easier to visualize. From Figure 3, the W–O and Eu–O bond



Figure 3. Experimental PDFs of LiEu(WO₄)₂ (blue), NaEu(WO₄)₂ (red), and KEu(WO₄)₂ (black).

distances of these compounds are directly observed, showing that both LiEu(WO₄)₂ and NaEu(WO₄)₂ have the some bond distance distribution and coordination number. The bondlength distribution of LiEu(WO₄)₂ is generally shorter than the one of NaEu(WO₄)₂, which suggests a lattice contraction phenomenon. For KEu(WO₄)₂ with lower crystal symmetry, the W–O bond distance is longer, but the Eu–O bond distance is shorter than the ones of both LiEu(WO₄)₂ and NaEu-(WO₄)₂, which can be understood by bond-valence theory.^{22–24} The result of PDF calculation is in good agreement with that of the Rietveld refinement method and gives more precise information about the bond distance distribution and coordination number. Most importantly, it performs more directly than the Rietveld refinement method. The fit was also carried out by the program *PDFgui* (see the Supporting Information, Table S4 and Figures S4–S6). The agreement factor R_{wp} is larger in PDF analysis compared to that in the Rietveld method, which is ascribed to a noise in G(r), the termination ripples, derived from the finite Q_{max} (13.4 Å⁻¹). Good agreement around 30% is also reported. ^{12,25,26}

Luminescence Properties. Figure 4 presents excitation spectra monitored at 614 nm of $LiEu(WO_4)_2$ and NaEu-



Figure 4. Excitation spectrum for the 615 nm emission of the phosphors $\text{LiEu}(WO_4)_2$ (black), $\text{NaEu}(WO_4)_2$ (red), and $\text{KEu}(WO_4)_2$ (blue) sintered at 750 °C for 10 h. The dotted box represents the CT bands of these compounds.

 $(WO_4)_2$ phosphors and at 615 nm of $KEu(WO_4)_2$ phosphor for ${}^5D_0-{}^7F_2\,$ emission of Eu^{3+} ions. The excitation spectrum consists of a broad band and some sharp lines. The broad excitation band centered at 270 nm is attributed to the CT transition from oxygen to tungstate and europium. This transition is sensitive to the coordination environment of the Eu³⁺ ions, and the intensity is strongly influenced by the crystalfield environment of the Eu³⁺ ions. In the range from 325 to 550 nm, the characteristic intraconfigurational 4f-4f transition of Eu³⁺ of sharp $^7F_0 \rightarrow {}^5L_6$ transition for 394 nm, $^7F_0 \rightarrow {}^5D_2$ transition for 464 nm, and $^7F_0 \rightarrow {}^5D_1$ transition for 535 nm can be observed.⁴ According to the excitation spectrum, it is evident that the LiEu $(WO_4)_2$, NaEu $(WO_4)_2$, and KEu $(WO_4)_2$ phosphors can be excited efficiently by near-ultraviolet (about 396 nm) or blue (about 464 nm) light.^{4,10} In Figure 4, the vital difference is only at the 270 nm CT band of oxygen to tungsten $(W^{6+}-O^{2-})$ and europium $(Eu^{3+}-O^{2-})$.²⁷ This process has been known as "host-sensitized" energy transfer. The dotted box shows that the intensity of CT excitation of $KEu(WO_4)_2$ is more effective than that of both $LiEu(WO_4)_2$ and NaEu- $(WO_4)_2$. The energy transfer from the absorbing group to the rare-earth ion was ascribed by Dexter to an exchange mechanism.²⁸ Furthermore, the superexchange between paramagnetic ions depends on the angle in paramagnetic ion-oxygen ion-paramagnetic ion.^{29,30} This interaction is usually strong if the angle is 180° (using σ bonding) and considerably weaker for 90° (using π bonding). A similar discussion has been invoked by Van Uitert et al. to explain the concentration quenching of luminescence of Eu3+.31 For alkali-metal europium double tungstate compounds, the maximum bond angle of W–O–Eu for LiEu(WO₄)₂ and NaEu(WO₄)₂ is about 143° , while for $KEu(WO_4)_2$, the maximum W–O–Eu angle is about 176°. This means more efficient energy transfer from the host

matrix to the luminescent center for $\text{KEu}(\text{WO}_4)_2$ than for both $\text{LiEu}(\text{WO}_4)_2$ and $\text{NaEu}(\text{WO}_4)_2$. From Figure 4, the excitation spectra of an intraconfigurational 4f-4f transition remained unchanged for all alkali-metal europium double tungstate compounds because of the well-shielded 4f intershell, avoiding the disturbance from the surroundings (see Table 2 and Figure 3).

Figure 5 shows the emission spectra of $LiEu(WO_4)_2$ and $NaEu(WO_4)_2$ at 396 nm and $KEu(WO_4)_2$ at 395 nm light



Figure 5. Emission spectra of LiEu(WO₄)₂ (black), NaEu(WO₄)₂ (red), and KEu(WO₄)₂ (blue). Left Inset: difference of LiEu(WO₄)₂ and NaEu(WO₄)₂. Right inset: difference of LiEu(WO₄)₂, NaEu-(WO₄)₂, and KEu(WO₄)₂.

Table 3. ${}^{5}D_{0}-{}^{7}F_{2}$ Relative Intensities of LiEu(WO₄)₂, NaEu(WO₄)₂, and KEu(WO₄)₂

phosphor	excitation wavelength (nm)	emission wavelength (nm)	⁵ D ₀ - ⁷ F ₂ relative intensity		
$LiEu(WO_4)_2$	396	614	1.04		
$NaEu(WO_4)_2$	396	614	1.04		
$KEu(WO_4)_2$	395	615	1.00 ^{<i>a</i>}		
^{<i>a</i>} The intensity of KEu(WO ₄) ₂ is regarded as 1.00.					

excitation. Table 3 gives a comparison between the emission intensities of LiEu $(WO_4)_2$ and NaEu $(WO_4)_2$ under excitation of 396 nm and of $KEu(WO_4)_2$ at 395 nm. The spectra essentially consists of several sharp lines with wavelengths ranging from 580 to 710 nm, which are associated with the ${}^{5}D_{0}$ \rightarrow ⁷F₁ (J = 1-4) transitions from the excited-state levels of Eu^{3+} to the ground state. The major emissions of LiEu(WO₄)₂ and NaEu(WO₄)₂ were found at about 614 nm and that of $\text{KEu}(\text{WO}_4)_2$ was found at 615 nm (⁵D₀ \rightarrow ⁷F₂), which correspond to red emission of the hypersensitivity transition for trivalent europium. In addition, three weak emission lines at 590 nm (${}^{5}D_{0} \rightarrow {}^{7}F_{1}$), 654 nm (${}^{5}D_{0} \rightarrow {}^{7}F_{3}$), and 702 nm (${}^{5}D_{0}$ \rightarrow ⁷F₄) can also be observed. From Figure 5, the emission spectra of $KEu(WO_4)_2$ appears broader than the ones of both $LiEu(WO_4)_2$ and $NaEu(WO_4)_2$. Blasse²⁷ pointed out that when excited, the lattice vibration results in a deviation of the metalligand distance (R) from that of the ground state (R_0) . For $KEu(WO_4)_2$, the presence of K⁺ ions with a larger radius affords softer surroundings around the luminescence center, which results in a larger deviation ($\triangle R$), thus producing a larger Stokes shift and a broader optical bands. In addition, the lower crystal symmetry of $KEu(WO_4)_2$ may also contribute to the large Stokes shift and broader optical bands of $KEu(WO_4)_2$.

On the other hand, the same Eu–O bond distances of $\text{LiEu}(WO_4)_2$ and $\text{NaEu}(WO_4)_2$ (see Figures 3 and 5) lead to well-overlapping peaks of the emission spectra.

CONCLUSION

The present study investigates the luminescent properties of LiEu(WO₄)₂, NaEu(WO₄)₂, and KEu(WO₄)₂ by Rietveld and PDF analysis. Both LiEu(WO₄)₂ and NaEu(WO₄)₂ have the same luminescent properties, in which the identical local surroundings of Eu³⁺ ions are revealed by PDF analysis. For KEu(WO₄)₂, the more effective CT excitation, the larger Stokes shift, and the broader optical bands than those of both LiEu(WO₄)₂ and NaEu(WO₄)₂ are observed, which is in good agreement with the crystal structures discussed. The results obtained by the PDF experimental method are also confirmed by bond-valence theory. The dual-space technique combining Rietveld and PDF analysis offers a powerful tool to revealing correlation of the luminescence properties with the local environment of the emission center through study of the local and average structures of the host matrix.

ASSOCIATED CONTENT

Supporting Information

Rietveld and PDF refinement results. This material is available free of charge via the Internet at http://pubs.acs.org.

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ACKNOWLEDGMENTS

We are grateful to Professor Lv Guanglie at Zhejiang University and Gao Zhongmin at Ji Lin University for providing the beneficial discussion on this paper.

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