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Crystal Structure and Local Structure of $Mg_{2-x}Pr_xNi_4$ (x = 0.6 and 1.0) Deuteride Using in Situ Neutron Total Scattering

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ABSTRACT: We studied crystal structure and local structure of $Mg_{2-x}Pr_{x}Ni_{4}$ (x = 0.6 and 1.0) and their deuterides using in situ neutron total scattering and first-principles calculations. The total scattering data were analyzed using Rietveld refinement and pair distribution function analysis (PDF). The crystal structure of Mg2[−]xPrxNi4 before deuterium absorption was C15b in space group $F\overline{4}3m$. No difference between the crystal and local (PDF) structures was observed. The crystal structure of $Mg_{1,0}Pr_{1,0}Ni_4D_{\sim 4}$ was found to be orthorhombic in space group $Pmn2_1$, with three deuterium occupation sites: $PrNi₃$ and two types of bipyramidal Pr_2MgNi_2 that have a plane of symmetry composed of $MgNi_2$. There is no significant difference between the crystal structure and the local structure of Mg_{1.0}Pr_{1.0}Ni₄D_{∼4}. On the other hand,

the average crystal structure of the Mg-rich Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6} was C15b with two deuterium occupation sites: PrNi₃ and MgPrNi₂ suggesting that the deuterium occupation shifts away from the Pr₂MgNi₂ bipyramid. First-principles relaxed structures also showed the shift of the hydrogen occupation site toward the Pr atom of the bipyramid, when induced by Mg substitution for the opposing Pr, resulting in hydrogen occupation in the MgPrNi₂ tetrahedral site. The PDF pattern of Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6} cannot be refined below 7.2 Å in atomic distances using the C15b structure which was obtained from Rietveld refinement but can be done using an orthorhombic structure. It suggests that Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6} was locally distorted to the orthorhombic.

1. INTRODUCTION

Hydrogen storage materials have been extensively investigated for the nickel-hydride battery for many applications, including fuel cell vehicles. Various studies on the Mg-containing alloys such as hexagonal PuNi₃-type compounds (RE, Mg)Ni₃ (RE = rare earth) $^{1-4}$ and a C15b-type Laves phase ${Mg_{1.0}Y_{1.0}Ni_4}^S$ have been done to increase the gravimetric density and to tune the thermody[nami](#page-8-0)c property. Chot[a](#page-8-0)rd et al. found that $Mg_{10}La_{10}Ni_4$ absorbed hydrogen up to ∼1.0 H/M (H/M: ratio of the number of hydrogen and metal atoms) with two distinct plateaus on the pressure composition $(P-C)$ isotherms,⁶ although most of reported Mg_{1.0}RE_{1.0}Ni₄ absorbed only ~0.7 H/M with one plateau.^{7−12} We found that the dependen[ce](#page-8-0) of Mg/RE ratio in Mg2[−]xRExNi4 on the hydrogenation properties and the crystal structu[re](#page-8-0)s [of](#page-8-0) the hydrides. The compounds with $x = 1.0$ had two different hydride phases, an orthorhombic Mg_{2-x}RE_xNi₄H_{∼4} in space group $Pmn2_1$, and a cubic C15b Mg_{2−x}RE_xNi₄H_{∼6} (at high-hydrogen content), while those with $x < 1.0 \, \text{(Mg-rich)}$ had only cubic C15b $Mg_{2-x}RE_xNi_4H_{\sim 3.6}$.^{13–15} In addition, those compounds with $x > 1.0$ transform to amorphous hydrides.¹³

The dependence of the Mg/RE ratio on the crystal structure of hydrides likely originates from the different hydrogen occupation sites induced by the Mg/RE ratio.

Neutron total scattering is a powerful technique to solve crystal structures, especially for hydrogen storage materials because the deuterium occupation sites can be solved by Rietveld analysis of the Bragg peaks. Since the total scattering data includes not only the Bragg scattering but also the diffuse scattering, the total scattering experiment provides the information of both the crystal structure and the local structure. In general, a very large amount of the lattice defects and lattice strain are introduced upon hydrogenation in most hydrogen storage materials because of the large volume expansion.¹⁶⁻²⁶ These may lead the metal lattice to distort or atom positions to deviate from the average position determined by the Ri[etveld](#page-8-0) analysis. The atomic pair distribution function (PDF) is a local structural probing technique, utilizing scattering at large

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momentum transfer (large 2θ scattering angle), that gives the probability of finding atom pairs separated by distance r^{27} The PDF analysis on neutron powder diffraction data reveals these local distortions and deviations, as well as deuterium occ[upa](#page-8-0)tion sites.

In this study, we investigated the crystal structure and the local structure of $Mg_{2-x}Pr_{x}Ni_4$ (x = 0.6 and 1.0) and their deuterides using neutron total scattering and first-principles calculations to understand the origin of the different crystal structures of the deuterides and to observe the local distortion upon deuterium absorption. The origin of different deuterium occupation sites and the local distortion will be discussed from the viewpoint of metal coordination changes with varying composition.

2. EXPERIMENTAL PROCEDURES

2.1. Sample Preparation.¹³ The same alloy ingots that were investigated in ref 13 were used. Ingots of Mg, Pr, and Ni, each with purity higher than 99.9%, [wer](#page-8-0)e used as the starting materials. $Mg_{1.0}Pr_{1.0}Ni_4$ and $Mg_{1.4}Pr_{0.6}Ni_4$ were prepared by high-frequency induction melting [us](#page-8-0)ing an alumina crucible and were cast into a water-cooled board mold under a He atmosphere. The as-cast alloys were annealed at 1323 K for 10 h under an Ar atmosphere. The chemical analysis showed that the compositions of the annealed alloys were $Mg_{1.4}Pr_{0.6}Ni_{4.1}$ and $Mg_{1.0}Pr_{1.0}Ni_{4.0}$.

2.2. Neutron Total Scattering Experiment. The annealed alloys were crushed into powders and put into a stainless steel vessel. The vessel was evacuated by rotary pump at 423 K for more than 2 h. Deuterium absorption was carried out at room temperature at 5 MPa, and then deuterium desorption was carried out using a rotary pump at 423 K for more than 2 h. After several cycles of absorption and desorption of deuterium, the samples were taken out of the vessel and crushed into fine powders. These fine powders were loaded into a cylindrical high-pressure sample holder made of vanadium for in situ neutron total scattering. After evacuation for 2 h at 423 K, deuterium gas was introduced into sample holder up to 1 MPa to prepare the deuterides. Time-of-flight (TOF) neutron total scattering experiments were carried out on the NPDF instrument²⁸ at the Lujan Neutron Scattering Center at Los Alamos National Laboratory. Data sets for $Mg_{2-x}Pr_xNi_4$ a[nd](#page-9-0) $Mg_{2-x}Pr_xNi_4D_{\sim y}$ (x = 0.6 and 1.0) were collected for around 4 h at a temperature of 100 K to reduce the thermal vibration.

2.3. Data Processing and Analysis for Neutron Total **Scattering.** The signal from an empty container (a vanadium holder) was subtracted from the raw data, and various other corrections were made.²⁷ The PDF is obtained by a sine Fourier transformation of the powder diffraction data according to eq 1:

$$
G(r) = \frac{2}{\pi} \int_{Q_{\text{min}}}^{Q_{\text{max}}} Q[S(Q) - 1] \sin(Qr) dQ,
$$
\n(1)

where Q is the magnitude of the momentum transfer and $S(Q)$ is the total scattering structure function.²⁷ Because of the unfavorable signal-to-noise ratio at the high-Q regions, $Q[S(Q)-1]$ was truncated at Q_{max} = 35 Å⁻¹ [for](#page-8-0) neutron data before the transformation. Data processing program PDFgetN²⁹ was used for obtaining neutron PDFs. Real space modeling was carried out using the PDFgui program.³⁰ The PDF is simply a bond length [di](#page-9-0)stribution, and therefore the PDF of a given structure can be calculated using the following equation:

$$
G(r) = \frac{1}{r} \sum_{i} \sum_{j} \left[\frac{b_i b_j}{\langle b \rangle^2} \delta(r - r_{ij}) \right] - 4\pi r \rho_0 \tag{2}
$$

where b_i is the scattering power of atom *i* (neutron scattering lengths), **is the average scattering power of the sample,** r_{ij} **is the distance between atoms** *i* **and** *j***, and** ρ_0 **is the number density.³¹ The sums go** over all the atoms in the model crystal. It is worth noting that the intensity of a PDF peak located at r is proportional t[o t](#page-9-0)he number of atom pairs separated by distance r and the scattering powers of the contributing atoms.

Structural refinement in reciprocal space was carried out by Rietveld analysis using the EXPGUI-GSAS program.^{32,33} Four patterns with different d space obtained from the different detectors were analyzed simultaneously.

2.4. Computational Method. First-pri[nciple](#page-9-0)s calculations were performed to understand the effect of substitution of Mg and Pr atoms on the hydrogen occupation site energies using the Vienna *ab initio* simulation package (VASP) package.^{34,35} The generalized gradient approximation (GGA) proposed by Perdew et al.³⁶ was used for the exchange-correlation functional. We us[ed th](#page-9-0)e VASP Pr potential where f-electrons are kept frozen in the core. This is a [st](#page-9-0)andard model for the treatment of localized f electrons. The potentials based upon the treatment of localized f electrons. all-electron projector augmented wave (PAW) method were used.³ The structure relaxations were performed until the maximum force dropped below 0.001 eV/ \AA , with a self-consistent field (SCF) co[nver](#page-9-0)gence criterion of 10^{-7} eV. The plane wave cutoff energy was chosen to be 425 eV. The k-point spacing was chosen to be 0.15 \AA^{-1} . .

Three structure models with compositions $Mg_4Pr_4Ni_{16}H_1$, $Mg_5Pr_3Ni_{16}H_1$, and $Mg_3Pr_5Ni_{16}H_1$ were created. (1) The $Mg_4Pr_4Ni_{16}$ structure model with C15b structure was initially created with a hydrogen atom placed at (0.25, 0.25, 0). This is the center of a Pr_2MgNi_2 bipyramidal interstitial site and is on the $MgNi_2$ symmetry plane for the bipyramid. (2) The Pr atom at (0,0,0), an end cap of the bipyramid, was replaced by Mg to create the $Mg_SPr_3Ni_{16}H_1$ structure model, breaking the mirror symmetry of the bipyramid. (3) To create the $Mg_3Pr_5Ni_{16}H_1$ structure model, the Mg atom that is the nearest neighbor of the hydrogen atom was replaced by Pr (the symmetry plane of the bipyramid is now $PrNi₂$). Two types of structure relaxation were carried out. One was fully structure relaxation in which the atomic positions, cell volume, and cell shape were all allowed to change. In the second, to retain the cubic structure, the cell volume only was initially optimized and then the atomic positions were optimized, and these processes were repeated more than three times.

3. RESULTS

3.1. Crystal Structure and Local Structure of $Mg_{1.0}Pr_{1.0}Ni_4$ and $Mg_{1.4}Pr_{0.6}Ni_4$ Alloys. Figure 1a,b shows the results of Rietveld refinement for the neutron diffraction patterns of $Mg_{1,0}Pr_{1,0}Ni_4$ an[d](#page-2-0) $Mg_{1,4}Pr_{0,6}Ni_4$ measured at 100 K. The crystal structure was a C15b with space group $F\overline{4}3m$. The refined lattice constants of $Mg_{1.0}Pr_{1.0}Ni_4$ and $Mg_{1.4}Pr_{0.6}Ni_4$ were 7.0827 and 7.0068 Å, respectively. These agree with our previous XRD results.^{13,15} Table 1 shows the refined atomic positions of $Mg_{1,0}Pr_{1,0}Ni_4$ and $Mg_{1,4}Pr_{0,6}Ni_4$. The obtained atomic displacement [param](#page-8-0)eters, U, were reasonable values.

Figure 1c,d shows the result of l[oc](#page-2-0)al structure analysis for the pair distribution function of $Mg_{1.0}Pr_{1.0}Ni_4$ and $Mg_{1.4}Pr_{0.6}Ni_4$. The stru[ct](#page-2-0)ure models obtained from the Rietveld refinement were used for the local structure analysis as the initial structure model. The simulated $G(r)$ fits the measured data very well. The refined atomic positions of $Mg_{1,0}Pr_{1,0}Ni_4$ and $Mg_{1,4}Pr_{0,6}Ni_4$ using PDF analysis is shown in Table 2. These results indicate that no significant difference between the average structure and the local structure was observed for t[he](#page-2-0) alloys.

3.2. Crystal Structure and Local Structure of Mg_{1.0}Pr_{1.0}Ni₄D_{∼4}. Before the neutron experiment, it was confirmed that the isotope effect on the crystal structure of metal lattice and the hydrogenation properties such as hydrogen content and equilibrium pressure were not observed in $Mg_{1.0}Pr_{1.0}Ni_4$. Figure 2a shows the result of Rietveld refinement for the neutron diffraction pattern of $Mg_{1.0}Pr_{1.0}Ni_4D_{\sim 4}$ measured at 100 K. [Th](#page-3-0)e crystal structure was an orthorhombic structure with space group $Pmn2₁$ that was the same as the crystal structure of $Mg_{1.0}La_{1.0}Ni_4D_{3.7}$ and $Mg_{1.0}Nd_{1.0}Ni_4D_{3.6}$.^{6,8} The lattice constants of $Mg_{1,0}Pr_{1,0}Ni_4D_{\sim 4}$ were $a = 5.0829(1)$ Å, $b = 5.4729$ (1) Å, and $c = 7.3838$ (2) Å. The volu[me](#page-8-0)

Figure 1. Results of Rietveld and PDF analyses of neutron total scattering data measured at 100 K; (a) and (b) Rietveld analyses for $Mg_{1,0}Pr_{1,0}Ni_4$ and $Mg_{1.4}Pr_{0.6}Ni_4$, (c) and (d) PDF analyses for $Mg_{1.0}Pr_{1.0}Ni_4$ and $Mg_{1.4}Pr_{0.6}Ni_4$.

expansion was 15.6%, which is consistent with those for $M_{g_{1.0}Pr_{1.0}Ni_4H_{\sim4}}$ (15.4%),¹⁵ Mg_{1.0}La_{1.0}Ni₄D_{3.7} (14.5%),⁶ and $Mg_{10}Nd_{10}Ni_4D_{3.6}$ (14.6%).⁸ The obtained atomic coordination is shown in Table 3a, and [the](#page-8-0)se values were consistent wi[th](#page-8-0) the values reported for Mg_{1.0}Nd_{1.0}Ni₄D_{∼3.6}⁸ and Mg_{1.0}La_{1.0}Ni₄D_{∼3.7}⁶ an[d](#page-3-0) the optimized atomic coordination for $Mg_{1.0}RE_{1.0}Ni_4H_4$ using ab initio calculations.¹⁴ Th[e](#page-8-0)re were three deuteriu[m](#page-8-0) occupation sites. Two of them were the $Pr₂MgNi₂$ triangular

bipyramid (4b, 2a), and the other was the PrNi₃ tetrahedron (2a). The occupancy of these sites was refined, but the obtained values were close to 1 and the R_{wp} value did not change. Therefore, they were fixed at the value of 1. The number of deuterium atoms in the structure model used for the refinement was similar to the experimental value evaluated from the P−C isotherm. In addition the shortest distance between two deuterium atoms was 2.502 Å, which is larger than Westlake's

Figure 2. Result of Rietveld (a) and PDF analyses (b) for Mg_{1.0}Pr_{1.0}Ni₄D_{∼4} measured at 100 K.

empirical criteria of 2.1 \AA ³⁹ It indicates that the repulsive interactions are unlikely to interrupt the deuterium occupation. Therefore, a full occupation [str](#page-9-0)ucture model is reasonable.

Figure 2b shows the fitting result of the PDF of $Mg_{1,0}Pr_{1,0}Ni_4D_{\sim 4}$ for local structure analysis. The structure model obtained from the Rietveld refinement was used as an initial model. The occupancy of deuterium sites was refined, but the obtained values were close to and slightly above 1. Therefore, deuterium occupancy was also fixed at a value of 1. The refined atomic positions from a PDF analysis are shown in Table 3b. The result of the local structure analysis is in good agreement with the Rietveld analysis. No significant difference between the average structure and the local structure was observed in Mg_{1.0}Pr_{1.0}Ni₄D_{∼4}.

3.3. Crystal Structure and Local Structure of Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6}. Before the neutron experiment, it was confirmed that the isotope effect on the crystal structure of metal lattice and the hydrogenation properties were not observed in $Mg_{1.4}Pr_{0.6}Ni_4$. Figure 3a shows the result of Rietveld refinement for the neutron diffraction pattern of Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6}. The crystal structure was a C[15](#page-4-0)b with space group F43m, which is the same as the alloy phase. The lattice constant of $Mg_{1.4}Pr_{0.6}Ni_4D_{~0.3.6}$ was *a* = 7.3409 (1) Å. The volume expansion was 15.0%, which is close to that for $Mg_{1.4}Pr_{0.6}Ni_4H_{~2.6} (13.4%)$ $Mg_{1.4}Sm_{0.6}Ni_4H_{\sim3.6}$ (15.1%), and $Mg_{1.4}Gd_{0.6}Ni_4H_{\sim3.6}$ (14.1%).^{14,15}

The expansion was also close to that for $Mg_{1,0}Pr_{1,0}Ni_4D_{\sim 4}$ even though the crystal structures were different. The obtained atomic coordinates are shown in Table 4. There were two deuterium occupation sites, $PrNi₃$ tetrahedron (16e) and $PrMgNi₂$ tetrahedron (48h) as shown in Figure [3](#page-4-0)b. The deuterium occupation sites were different from those in Mg_{1.0}Pr_{1.0}Ni₄D_{∼4}. The deuterium atom in the PrMgNi₂ tetr[ah](#page-4-0)edron was located near the MgNi₂ plane, but not in the plane. It suggests that the deuterium occupation site shifted from the center of the Pr_2MgNi_2 triangular bipyramid (24g) toward the center of the $PrMgNi₂ tetrahedron.$ The occupancy of deuterium at these sites was small, as shown in Table 4, in accordance with the larger multiplicity of the Wyckoff position. The number of deuterium atoms in the refined structure [m](#page-4-0)odel was 14.24, close to that evaluated from P−C isotherms (14.4). The obtained atomic displacement parameters U were relatively larger than usual values which were obtained in $Mg_{2-x}Pr_xNi_4$ and $Mg_{1,0}Pr_{1,0}Ni_4D_{\sim 4}$. Another structure model in which the deuterium atoms occupy the high-symmetry center of Pr_2MgNi2 triangular bipyramid $(24g)$ instead of PrMgNi₂ tetrahedron $(48h)$ was also applied. The number of deuterium atoms in the unit cell did not change, but the atomic displacement parameter of this deuterium site became larger and R_{wp} value became worse. Since almost half of Pr atoms were replaced by Mg atoms in Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6}, many

Figure 3. (a, b) Result of Rietveld analysis for Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6} measured at 100 K.

Table 4. Refined Atomic Coordination of Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6}; (a) Rietveld Analysis and (b) PDF Analysis to 7.2 Å (c) PDF Analysis from 7.2 to 40 Å

(a) $Mg_{1.4}Pr_{0.6}Ni_4D_{3.6}$: space group <i>F-43m, a</i> = 7.3409 (1) Å, R_w = 4.39%						
atom	Wyckoff position	$\boldsymbol{\mathcal{X}}$	\mathcal{Y}	\boldsymbol{z}	U/\AA^2	occupancy
Pr	4a	0	0	$\bf{0}$	0.029(1)	0.6
Mg	4a	0	Ω	$\mathbf{0}$	0.16(1)	0.4
Mg	4c	0.25	0.25	0.25	0.085(2)	1
Ni	16e	0.6231(1)	0.6231(1)	0.6231(1)	0.0256(2)	1
D	16e	0.8493(2)	0.8493(2)	0.8493(2)	0.018(1)	0.290(6)
D	48h	0.7363(5)	0.7363(5)	0.9979(3)	0.0196(7)	0.200(2)
(b) $Mg_{1.4}Pr_{0.6}Ni_4D_{\sim 3.6}$: space group Pmn21, $a = 5.104$ (8) Å, $b = 5.33$ (1) Å, $c = 7.35$ (1) Å, $R_w = 12.6\%$						
atom	Wyckoff position	\mathcal{X}	\mathcal{Y}	\boldsymbol{z}	U/\AA^2	occupancy
Pr	2a	$\mathbf{0}$	0.347(5)	0.018(4)	0.003(3)	0.6
Mg	2a	$=Pr$	$=Pr$	$=Pr$	$=Pr$	0.4
$_{\rm Mg}$	2a	Ω	0.695(7)	0.256(5)	0.013(5)	1
Ni	2a	0	0.507(2)	0.593(1)	0.003(1)	1
Ni	2a	Ω	0.028(4)	0.648(3)	0.016(3)	
Ni	4 _b	0.751(2)	0.233(2)	0.378(2)	0.0068(9)	
D	4 _b	0.763(3)	0.508(2)	0.755(2)	0.009(1)	
D	2a	Ω	0.716(5)	0.502(3)	0.008(3)	
D	2a		0.933(2)	0.864(2)	0.007(2)	
(c) Mg _{1.4} Pr _{0.6} Ni ₄ D _{~3.6} : space group $F\overline{4}3m$, $a = 7.3484$ (4) Å, $R_w = 13.1\%$						
atom	Wyckoff position	$\boldsymbol{\mathcal{X}}$	\mathcal{Y}	\boldsymbol{z}	U/\AA^2	occupancy
Pr	4a	$\boldsymbol{0}$	$\mathbf{0}$	$\mathbf 0$	0.038(6)	0.6
Mg	4a	$\mathbf{0}$	$\mathbf{0}$	$\mathbf{0}$	$=Pr$	0.4
Mg	4c	0.25	0.25	0.25	0.10(1)	$\mathbf{1}$
Ni	16e	0.6237(8)	0.6237(8)	0.6237(8)	0.0234(5)	1
D	16e	0.848(1)	0.848(1)	0.848(1)	0.022(4)	0.2898
D	48h	0.75(1)	0.75(1)	0.992(1)	0.024(1)	0.1999

Pr₂MgNi₂ bipyramids become PrMg₂Ni₂, which is asymmetric to the MgNi₂ plane. The refinements indicate that it is favorable to shift the deuterium position in this asymmetric $PrMg_2Ni_2$ to either the PrMgNi₂ tetrahedron or Mg₂Ni₂ tetrahedron. Therefore, the structure model where deuterium atoms occupy the 48h site is more reasonable than that for the 24g site.

Figure 4 shows the result of local structure analysis for the pair distribution function of Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6}. The structure models [ob](#page-5-0)tained from the Rietveld refinement (C15b structure) were used for the local structure analysis. When analysis was performed in the r range from 7.2 Å to 40 Å, the refinement agreements are rather good with R_{wp} values less than 13.1%. The atomic coordination was consistent with that obtained from Rietveld refinement as shown in Table 4. However, when the refinement region was expanded to $1 \text{ Å} \leq r$ \leq 40 Å, the simulated $G(r)$ curve using this structure model did not fit well in the r range from 1 Å to 4 Å as shown in Figure 4a. This suggests that the local structure of this hydride was different from the average structure in C15b, especially below [7.](#page-5-0)2 Å in atomic distances. The first peak of the measured $G(r)$ curve was around 1.64 Å but that of the simulated $G(r)$ one was around 1.56 Å. The first peak of the $G(r)$ curve mainly corresponds to the Ni−D bonding. It suggests that the Ni and/or D positions have deviated from the average position.

Figure 4. Result of PDF analysis for $Mg_{1.4}Pr_{0.6}Ni_4D_{~3.6}$ measured at 100 K. (a) C15b structure model, (b) orthorhombic structure model, and (c) orthorhombic + C15b structure model.

Below 7.2 Å in atomic distances, we applied the structure model with an orthorhombic structure with Pmn2₁, which is the same as the crystal structure of Mg_{1.0}Pr_{1.0}Ni₄D_{∼4} instead of a C15b structure. By changing the structure model, the bond length between Ni-D increased to 1.63 Å, which is close to the position of the first peak for the measured $G(r)$ curve, 1.64 Å. As shown in Figure 4b, this structure model worked well below 7.2 Å, and the fitting was dramatically improved. However, the difference between the simulated $G(r)$ curve and measured data became larger with the increase of r above 7.2 Å in atomic distances. These data suggest that Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6} was distorted orthorhombic *Pmn*2₁ in local structure, although the average structure is still C15b. The domain size showing the orthorhombic structure was around 7.2 Å in atomic distances, which was close to the lattice constant of a C15b Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6} as shown in Figure 4c. This means that the structure within each domain with 7.2 Å in size was orthorhombic and these domains randomly distributed to keep the crystal structure the C15b structure in average.

3.4. Effect of the Mr/Pr Ratio on the Hydrogen Occupation Site. In order to investigate the effect of the Mg/Pr ratio on the hydrogen occupation site, structure relaxations for $Mg_4Pr_4Ni_{16}H_1$, $Mg_5Pr_3Ni_{16}H_1$, and $Mg_3Pr_5Ni_{16}H_1$ were carried out using first-principles calculations. The optimized lattice constants and atomic coordination of $MgPr_2Ni_2$ triangular bipyramid that was obtained by the volume optimization and the atomic optimization independently are shown in Table 5. Since the lattice constants of each alloy phase were 7.126693 Å f[or](#page-6-0) $Mg_4Pr_4Ni_{16}$, 7.058227 Å for $Mg_5Pr_3Ni_{16}$, and 7.186915 Å for $Mg_3Pr_5Ni_{16}$, respectively, the volume expansions were around 1%. In $Mg_4Pr_4Ni_{16}H_1$, the Pr_2MgNi_2 triangular bipyramid site was found to retain the symmetry of the Mg-Ni-Ni plane; the hydrogen atom remained on the Mg-Ni-Ni plane of Pr_2MgNi_2

triangular bipyramid suggesting that the hydrogen atom was on the 24g site as shown in Figure 5a. The distance between Pr and H atoms was 2.492 Å. When the Mg atom in Pr₂MgNi₂ triangular bipyramid was r[ep](#page-6-0)laced by a Pr atom as shown in Figure 5b, the hydrogen atom still sit on the Mg-Ni-Ni plane of Pr_2MgNi_2 triangular bipyramid, but the hydrogen atom shift[ed](#page-6-0) away from the substituted Pr atom because the Pr atom (1.83 Å) is larger than the Mg atom (1.6 Å). This triangular bipyramid is still symmetrical about the Mg-Ni-Ni plane. The distance between Pr and H atoms was 2.595 Å. On the other hand, when one of Pr atoms in Pr_2MgNi_2 was replaced by Mg as shown in Figure 5c, the triangular bipyramid became asymmetric about the Mg-Ni-Ni plane and then the hydrogen atom did not sit [on](#page-6-0) the Mg-Ni-Ni plane. The distances for H-Pr and H-substituted Mg were 2.414 Å and 2.543 Å, respectively. These results indicated that the hydrogen occupation site was influenced by the substitution of Mg into Pr and hydrogen atoms prefer to occupy the PrMgNi₂ tetrahedron rather than the Mg_2Ni_2 tetrahedron. A similar result was obtained when full structure relaxation was carried out even though the shape of unit cell was slightly distorted from a cubic.

4. DISCUSSION

4.1. Deuterium Coordination in Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6} in Average and Local. As described above, $Mg_{1.4}Pr_{0.6}Ni_4D_{~0.3.6}$ showed a distortion from cubic to orthorhombic in the local order. We will discuss the deuterium coordination in Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6} and then the difference between the average and local structures.

The deuterium occupation sites in Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6} were $PrNi₃$ tetrahedron (16e) and $PrMgNi₂$ tetrahedron (48h) in the average structure. To simplify the model, the deuterium occupation site is assumed to be the 24g site at (0.75, 0.75, 0.9979),

Table 5. Atomic Coordination of $Mg_{2-x}Pr_xNi_{16}H_1$; (a) $Mg_4Pr_4Ni_{16}H_1$, (b) $Mg_3Pr_5Ni_{16}H_1$, and (c) $Mg_5Pr_3Ni_{16}H_1$

Figure 5. Shift of hydrogen occupation site by changing of the ratio of Mg/Pr using theoretical calculation; (a) $Mg_4Pr_4Ni_{16}H_1$, (b) $Mg_3Pr_5Ni_{16}H_1$, and (c) $Mg_5Pr_3Ni_{16}H_1$.

on the symmetry plane of the bipyramid, which is between two 48h sites (0.7363, 0.7363, 0.9979), because these sites are close. Figure 6 shows deuterium distributions in a C15b structure. The large yellow and red balls show deuterium atoms at 16e and 24g sites, respectively, which are separated by more than 2.1 Å in atomic distances from certain deuterium atoms at 16e sites.

Figure 6. Atomic coordination of Mg_{1.4}Pr_{0.6}Ni₄H_{∼3.6}. Blue line indicates the shorter bond length between two deuterium atoms than 2.1 Å.

Small balls show deuterium atoms at 16e and 24g sites, respectively, which have a distance of less than 2.1 Å. There are four independent tetrahedrons built by deuterium at 16e sites in the unit cell. The distance of nearest-neighbor deuterium atoms at 16e sites is 2.06 Å, which is shown by the blue bar in Figure 6. This is slightly shorter than Westlake's empirical criteria.³⁹ Therefore, more than two deuterium atoms are unlikely to occupy the same tetrahedron simultaneously becaus[e o](#page-9-0)f the repulsive D−D interaction. The maximum deuterium occupancy at a 16e site should be close to 0.25 from the viewpoint of geometry and Westlake's empirical criteria.³⁹ In fact, the refined deuterium occupancy was close to 0.25. Since the distance of the nearest neighboring deuterium at 2[4](#page-9-0)g site is 2.57 Å, the repulsive interactions are unlikely to play a role. However, the distance of the first and second nearest neighboring deuterium between the 16e and 24g sites is 1.50 Å and 2.75 Å, respectively, suggesting the nearest 24g sites to the occupied 16e site cannot be occupied. Taking the Westlake empirical criteria into consideration, if four deuterium atoms would occupy the 16e site, only half of the 24g site can be occupied by deuterium, suggesting that the occupancy is less than 0.5 at the 24g site. This means that the occupancy at the 48h site is less than 0.25. In fact, the refined value was 0.20. Therefore, our experimental results indicate that deuterium

atoms are maximally occupied at both 16e and 24g sites in keeping with Westlake empirical criteria.

Here, we would like to discuss the difference between the average and local structures. As described above, $Mg_{1.4}Pr_{0.6}Ni_4D_{\sim3.6}$ showed the C15b structure in average. To simplify the model, the deuterium occupation site is assumed to be the 24g site again. Figure 7a,b shows the atomic coordination for the average structure of Mg_{1.4}Pr_{0.6}Ni₄H_{∼3.6}. In these figures, deuterium atoms which were less than 2.1 Å in atomic distances from certain deuterium atoms at 16e sites were removed. One Pr atom has possible bonding with four deuterium atoms inside a PrNi₃ tetrahedron (16e site) and with 12 deuterium atoms inside a $Pr₂MgNi₂$ triangular bipyramid (24g site). Taking the occupancy from our present refinement and the Westlake empirical criteria into consideration, one Pr atom has interaction with one deuterium atom inside of the PrNi₃ tetrahedron and with six deuterium atoms inside the $Pr₂MgNi₂$ triangular bipyramid as shown in Figure 7a,b. On the other hand, Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6} was locally distorted to make an orthorhombic hydride. In the orthorhombic structure, the deuterium atoms are located in two types of $Pr₂MgNi₂$ triangular bipyramid and $PrNi₃$ tetrahedron.^{6,8} One Pr atom in the orthorhombic structure interacts with two deuterium atoms inside of the Pr₂MgNi₂ triangular bipyra[mid](#page-8-0) (2a site) and with four deuterium atoms inside different $Pr₂MgNi₂$ triangular bipyramid (4b site) and with one deuterium atom inside a $PrNi₃$ tetrahedron (2*a* site) as shown in Figure 7c,d. When Figure 7a and Figure 7c or Figure 7b and Figure 7d are compared, the coordination of deuterium atoms obtained from the average and local structures was consistent with each other, although the metal atoms slightly deviated. This also suggests that the larger atomic displacement parameters for metal atoms obtained via Rietveld refinement come from the deviation of the metal atoms.

4.2. Local Distortion in Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6}. Here we would like to discuss why the local distortion appears in Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6}. A well-known example of a compound exhibiting a difference between its average structure and local structure is LaMnO_3 at elevated temperature.⁴⁰ LaMnO₃ shows a phase transformation at around 750 K during heating from an orthorhombic structure with space group [P](#page-9-0)bnm to a cubiclike structure with space group $\overline{Pbnm}^{40,41}$ From the average structure model, LaMnO₃ has three different Mn−O bond lengths below 750 K and only one bo[nd le](#page-9-0)ngth above 750 K. However, PDF analysis clearly showed three different Mn−O

Figure 7. Comparison of atomic coordination between average and local structures of Mg_{1.4}Pr_{0.6}Ni₄H_{~3.6}; (a) average structure from (1¹⁰), (b) average structure from (110), (c) local structure from (100), and (d) local structure from (010).

bond lengths locally in a cubic-like structure as well as the orthorhombic structure. This suggests that the structural characteristic (varying Mn−O bond lengths) in the low temperature phase remains in the local order at high temperature, where the average structure is different. Therefore, one possibility for the local distortion in Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6} is that the orthorhombic structure would be more stable than the C15b structure at low temperature. If it is true, C15b Mg_{1.4}Pr_{0.6}Ni₄D_{∼3.6} would transform to the orthorhombic structure below 100 K. This possibility is supported by the theoretical calculation for $Mg_{1.0}Ce_{1.0}Ni_4$ and $Mg_{1.0}Y_{1.0}Ni_4$ showing that the orthorhombic hydride is more stable than the C15b hydride.^{12,42} At present, however, there is no experimental evidence for the phase transformation between the orthorhombic and the [C1](#page-9-0)5 structure. Another possibility comes from the composition of $Mg_{2-x}Pr_{x}Ni_{4}$. The deuterium occupation sites were known to be AB_3 and A_2B_2 sites in C15 structure, while those were $PrNi₃$ and $Pr₂MgNi₂$ sites in Mg_{1.0}Pr_{1.0}Ni₄D_{∼4} and those were PrNi₃ and PrMgNi₂ sites in Mg_{1.4}Pr_{0.6}Ni₄D_{~3.6}. By Mg substitution into Pr, the deuterium atoms in Pr_2MgNi_2 shifted from on the symmetry plane of MgNi₂ to off the plane, e.g., toward the center of the PrMgNi₂ tetrahedron. If the amount of Mg substitution is small, only a small fraction of deuterium atoms would shift the symmetry plane. By increasing the fraction of Mg, the number of deuterium atoms which shift toward the center of the PrMgNi₂ tetrahedron would increase. Consequently, a cubic structure would be stabilized in Mg-rich Mg_{2−x}Pr_xNi₄ with an increase of Mg content, as seen in hydrides with a C15 structure, while an orthorhombic structure should remain in the local order with a decrease of Mg content. Therefore, our present data suggest that such a local distortion should not be observed in more Mg-rich Mg_{2−x}Pr_xNi₄. In contrast, Mg_{2−x}Pr_xNi₄ with $0.6 < x < 1.0$ should show the local orthorhombic distortion until a higher r region.

5. CONCLUSIONS

We investigated the crystal structure and the local structure of Mg_{2−x}Pr_xNi₄ deuterides using neutron total scattering and firstprinciples calculations to understand the origins of different crystal structures of these deuterides and to observe the local distortion upon deuterium absorption.

Our results highlight several interesting features of these compounds. The crystal structure and the deuterium occupation sites changed with the Mg/Pr ratio in Mg_{2-x}Pr_xNi₄D_y: Mr_{1.0}Pr_{1.0}Ni₄ forms the orthorhombic deuteride with three occupation sites (two types of Pr_2MgNi_2 triangular bipyramid and $PrNi_3$ tetrahedron), and $Mg_{1.4}Pr_{0.6}Ni_4$ forms the C15b deuteride with two occupation sites $(PrNi₃ tetrahedron and PrMgNi₂)$ tetrahedron). The preferential crystal structure and deuterium occupation sites were determined by whether the Pr_2MgNi_2 triangular bipyramid is symmetric or asymmetric to the $MgNi₂$ plane depending on the Mg/Pr ratio. The asymmetric shape of the triangular bipyramid, for Mg-rich compounds results in the deuterium shifting off the Mg-Ni-Ni symmetry plane and serves to stabilize the cubic C15b structure on average. However, the orthorhombic structure survives locally in $Mg_{1.4}Pr_{0.6}Ni_4D_{\sim 3.6}$.

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Notes

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