

occurred with the chromium compounds. It may be that the thermal instability in all cases is due to anisotropic contractions of the lattice.

The spectrum of  $W_2Cl_9^{3-}$  has been previously discussed.<sup>10</sup> The first observed absorption, which appears at  $13,200\text{ cm}^{-1}$  ( $\epsilon$  50), would not correspond to a reasonable estimate of the wave numbers of the same absorption in the unknown  $WCl_6^{3-}$ . For this reason, it was believed that the absorptions are the result of transitions between d orbitals which are delocalized between the two metal atoms.

**Possible Chemical Significance.**—A comparison of the properties of  $Cr_2Cl_9^{3-}$  and  $W_2Cl_9^{3-}$  reveals three distinct differences: structural, magnetic, and spectroscopic. It is not difficult to believe that these differences occur because of electron localization in the former and electron delocalization in the latter. The effect of these properties on the chemical reactivity of each ion is a subject which is currently receiving our attention. However, several points related to this subject can be discussed. In salts of  $Cr_2Cl_9^{3-}$ , the energy associated with the intraionic coupling of spins is not chemically significant, and it is not expected that the long-range spin coupling alone will prevent the degradation of the dinuclear ion into mononuclear units during the course of a chemical reaction. On the other hand, bonding between the adjacent metal atoms in  $W_2Cl_9^{3-}$  could reasonably be expected to deter, if not prevent, the conversion to mononuclear complexes of trivalent tungsten. The products of the reactions of  $Cr_2Cl_9^{3-}$  and  $W_2Cl_9^{3-}$  with pyridine are in full accord with this reasoning. When  $K_3Cr_2Cl_9$  is allowed to react with hot pyridine, mononuclear  $CrCl_3(py)_3$  is obtained. However, in the corresponding reaction with  $K_3W_2Cl_9$ , it was shown<sup>10</sup> that at least one-

third of the product was diamagnetic  $W_2Cl_6(py)_4$ , in which it was presumed that adjacent octahedra were joined by two chlorine bridges. The three-dimensional X-ray study of Jackson and Streib<sup>21</sup> confirmed this hypothesis and showed that the metal-metal internuclear distance had increased to only 2.6 Å. Thus, the product retains a considerable amount of interaction between the metal atoms in their adjacent octahedra. It may be that kinetic factors alone are responsible for the different products. However, the special nature of  $W_2Cl_9^{3-}$  can be further exemplified. The remarkable stability of this ion toward degradation was recently demonstrated<sup>22</sup> in the mass spectrum of  $K_3W_2Cl_9$ , wherein  $W_2Cl_6^+$  and  $W_2Cl_5^+$  were observed. Although mass spectroscopic data for  $Cr_2Cl_9^{3-}$  are not available, similar ions were not found in the mass spectrum of  $MoCl_3$ . Furthermore, it is noteworthy that the only reported reactions of  $W_2Cl_9^{3-}$  which lead to mononuclear compounds are those involving oxidation or the loss of some of the electrons which are thought to be extensively involved in metal-metal bonding. Thus, the reaction of this ion with the cyanide ligand<sup>23</sup> leads to  $W(CN)_8^{4-}$ , while the pyrolysis of  $(NH_4)_3W_2Cl_9$  with 8-hydroxyquinoline yields<sup>24</sup> the eight-coordinate tetrakis derivative of W(IV).

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## Solubility of Silver Chloride and Bromide and the Formation of Silver Halide Complexes in Molten Ammonium Nitrate Dihydrate

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The solubilities of silver chloride and bromide as a function of the corresponding ammonium halide concentration were determined in molten  $NH_4NO_3 \cdot 2H_2O$ , at 55, 70, and 85°. Solubility measurements were made using a radioactive-tracer technique with  $^{110}Ag$ . The solubility product  $K_{sp}$  and the consecutive stability constants of the complexes  $AgX$ ,  $AgX_2^-$ , and  $AgX_3^-$  ( $X^- = Cl^-, Br^-$ ) were computed. The results are discussed in terms of a quasi-lattice model of molten salts.

### Introduction

The solubility of silver chloride<sup>1-5</sup> and bromide<sup>2,4,6-8</sup> in water at various halide ion concentrations has been

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extensively studied. From solubility data it was concluded that soluble silver complexes of the type  $AgX_n^{-(n-1)}$  were formed ( $X^-$  denotes the halide ion,  $n = 1-4$ ) and in some cases the stability constants of the complexes were calculated. The association of silver(I) ions with halide ions was also studied at high

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temperature in anhydrous ionic molten salts,<sup>9-15</sup> mostly by emf measurements at low halide concentration. Formally, the formation of silver halide complexes proceeds along the same path in water and ionic melt and the same species were identified in both media. However, one would expect a different mechanism in the coordination of ligands. In a dilute aqueous solution the silver cation is surrounded by polar water molecules, while in a molten salt it is incorporated in the ionic quasi-lattice and surrounded by the anions of the solvent salt. Indeed, a difference is revealed by comparing the consecutive stability constants of the species  $\text{AgX}$  and  $\text{AgX}_2^-$ . Thus, the ratio  $K_1/K_2$  differs appreciably in the two media, which indicates different statistics of ligand coordination.

The equilibrium constants of some metal complexes in ionic melts are often in good agreement with a quasi-lattice model for reciprocal salt systems.<sup>16,17</sup> This model was also applied to complexes in aqueous melts,<sup>18-20</sup> and recently the theory was extended to molten salt systems containing variable amounts of water.<sup>21</sup>

The present work investigates the formation of silver chloride and bromide complexes in molten  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$  by the solubility method. The solvent  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$ , which is liquid above  $35^\circ$ , is intermediate between concentrated aqueous electrolyte solutions and anhydrous molten salts (it is nearly a 28 *m* solution of ammonium nitrate). So far no data on silver complexes in aqueous melts or concentrated electrolyte solutions have been available and, in general, little information on metal complexes in such media can be found. The purpose of the present paper is to provide some new information about chemical reactions in this type of solvent.

### Experimental Section

The solvent  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$  was prepared from dry, reagent grade ammonium nitrate and distilled water. Inactive silver nitrate was mixed with radioactive  $^{110}\text{AgNO}_3$  (specific activity about 12 mCi/g) and dissolved in molten  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$ , thus obtaining melts of initial silver concentration  $10^{-4}$ – $10^{-3}$  *M* and of known specific activity.

Active melt samples (0.1–0.2 g) were weighed in tared vials. The sample was dissolved in 3 ml of 6 *M* aqueous ammonia and then counted in a well-type  $\gamma$ -scintillation counter. From these data and a standard silver sample counted under the same

conditions, the molal concentration of silver in the melt was determined.

The experimental procedure consisted of equilibrating known amounts of  $\text{AgNO}_3$ ,  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$ , and  $\text{NH}_4\text{Cl}$  (or  $\text{NH}_4\text{Br}$ ) in 50-ml stoppered glass tubes in a thermostat for at least 1 week. In all cases the aged, well-formed precipitate was visible on the bottom of the tube. With preheated disposable glass pipets, samples of the clear supernatant were withdrawn, placed in counting vials, weighed, and counted as described above. The solubility of silver halide was calculated from the counting data, the sample weight, and the activity of a standard silver sample. The equilibrium concentration of halide was obtained from the initial ammonium halide concentration and the initial and equilibrium concentration of silver, assuming the precipitate is pure  $\text{AgX}$ .

Solubility determinations of silver chloride and bromide were made at three temperatures in dependence on the halide concentration of the melt. The experimental data are presented in Figures 1 and 2 as solubility *S* vs. halide concentration  $m_x$ .<sup>22</sup>

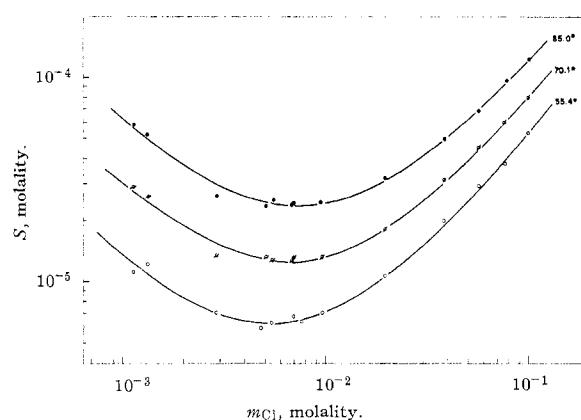


Figure 1.—The dependence of silver chloride solubility (*S*) in  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$  on ammonium chloride concentration ( $m_{\text{Cl}}$ ). The curves were calculated from eq 6 with the constants given in Table I.

### Results

The solubility *S* of silver halide can be defined by

$$S = m_0 + m_1 + m_2 + m_3 + \dots \quad (1)$$

where  $m_i$  is the molal concentration of a soluble silver species while the indices 0, 1, 2, 3, ... refer to the species  $\text{Ag}^+$ ,  $\text{AgX}$ ,  $\text{AgX}_2^-$ ,  $\text{AgX}_3^{2-}$ , respectively. Under the experimental conditions (excess of halide over silver) the formation of polynuclear silver complexes is improbable. The solubility product  $K_{\text{sp}}$  and the consecutive formation constants ( $K_i$ ) of silver halide complexes are defined in terms of thermodynamic activities ( $a_i = m_i \gamma_i$ ) of the indicated species

$$K_{\text{sp}} = m_0 m_x \gamma_0 \gamma_x \quad (2)$$

$$K_1 = m_1 \gamma_1 / m_0 m_x \gamma_0 \gamma_x \quad (3)$$

$$K_2 = m_2 \gamma_2 / m_1 m_x \gamma_1 \gamma_x \quad (4)$$

$$K_3 = m_3 \gamma_3 / m_2 m_x \gamma_2 \gamma_x \quad (5)$$

Here,  $\gamma_i$  is the activity coefficient of the species *i*, and  $m_x$  is the molal concentration of ammonium halide.

(22) Experimental data have been deposited as Document No. 10009 with the ADI Auxiliary Publications Project, Photoduplication Service, Library of Congress, Washington, D. C. 20540. A copy may be secured by citing the document number and by remitting \$1.25 for photoprints, or \$1.25 for 35-mm microfilm. Advance payment is required. Make checks or money orders payable to: Chief, Photoduplication Service, Library of Congress.

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TABLE I  
 THE EQUILIBRIUM CONSTANTS

Ligand	Temp, °C	$K_{sp}$		$K_1$		$K_2$		$K_3$		(DS) <sub>s</sub> , %	$K_1/K_2$
		$m^a$	$x^b$	$m^a$	$x^b$	$m^a$	$x^b$	$m^a$	$x^b$		
Cl <sup>-</sup>	55.4	$1.00 \times 10^{-8}$	$1.35 \times 10^{-10}$	253	2180	141	1215	4.86	41.7	±5.1	1.8
	70.1	$2.44 \times 10^{-8}$	$3.29 \times 10^{-10}$	216	1860	108	930	3.80	32.4	±4.8	2.0
	85.0	$4.90 \times 10^{-8}$	$6.60 \times 10^{-10}$	205	1760	89.3	769	2.96	25.5	±5.8	2.3
Br <sup>-</sup>	55.7	$4.86 \times 10^{-11}$	$6.55 \times 10^{-13}$	5450	$4.69 \times 10^4$	693	5970	20.8	179	±4.9	7.9
	70.0	$7.74 \times 10^{-11}$	$1.04 \times 10^{-12}$	5280	$4.55 \times 10^4$	754	6490	15.1	130	±3.1	7.0
	85.0	$2.15 \times 10^{-10}$	$2.90 \times 10^{-12}$	4440	$3.85 \times 10^4$	510	4390	7.4	64	±3.4	8.7

<sup>a</sup> Molal scale. <sup>b</sup> Mole fraction scale (based on  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$  as one component).

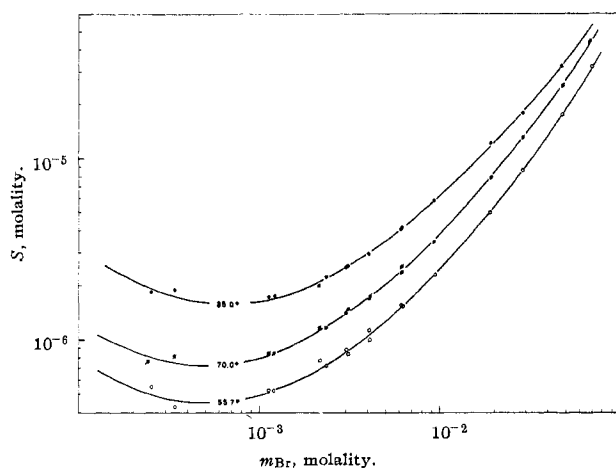


Figure 2.—The dependence of silver bromide solubility ( $S$ ) in  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$  on ammonium bromide concentration ( $m_{\text{Br}}$ ). The curves were calculated from eq 6 with the constants given in Table I.

For the activity coefficients, as usual, the infinite dilution in the solvent  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$  is chosen as a reference state; *i.e.*, these coefficients approach unity at low concentration of all solutes.

The activity coefficients in  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$  are not known and no theoretical limiting law, such as that of Debye-Hückel for dilute aqueous solutions, can be used. However, emf measurements of  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$  solutions containing 1:2 and 1:1 solute salts<sup>19</sup> proved that in this solvent solutes follow Henry's law up to a mole ratio (solute/ $\text{NH}_4\text{NO}_3$ ) of  $6 \times 10^{-3}$ . This limit corresponds to a molal concentration of 0.05. Comparable ranges of ideal solute behavior were observed in anhydrous melts,<sup>17</sup> and in aqueous solutions the activity coefficients are also fairly constant up to this solute concentration if the ionic strength is kept constant with a large excess of a suitable electrolyte. All solubility measurements in the present work were made at a halide concentration below 0.1  $m$ . Moreover, only one point on the bromide solubility curve (Figure 2) and two points on the chloride solubility curve (Figure 1) were above 0.056  $m$  halide concentration. Therefore, it seems reasonable to assume that the activity coefficients in eq 2-5 are constant and, according to the reference state chosen, equal to unity. In this case eq 1-5 give

$$S = K_{sp}m_x^{-1}(1 + K_1m_x + K_1K_2m_x^2 + K_1K_2K_3m_x^3) \quad (6)$$

The experimental results,  $S$  vs.  $m_x$ , were interpreted according to eq 6 in a digital computer by a modified

nonlinear least-squares program.<sup>23</sup> A relative-deviation least-squares treatment was applied so that deviations at low concentration of halide have the same statistical weight as those at high concentration. Values for  $K_{sp}$ ,  $K_1$ ,  $K_2$ , and  $K_3$  and the standard deviation of the solubility,  $(\text{SD})_s$ , were obtained. The results are summarized in Table I. Equation 6 was tested with and without the cubic term in  $m_x$ . However, even in the case of chloride, when  $K_3$  values are low, the fit is significantly better with the cubic term, although the numerical values for  $K_1$  and  $K_2$  only slightly change if this term is omitted. Hence, it is concluded that the  $\text{AgX}_3^{2-}$  species is not very important in the  $m_x$  range of 0.01-0.1, but it cannot be neglected.

As seen from Table I,  $K_{sp}$  increases with temperature, and an opposite trend is valid for the consecutive stability constants. The only apparent exception is the  $K_2$  value for  $\text{AgBr}_2^-$  at 70°, although it seems more probable that the value at 55° is too low.

### Discussion

The ratios  $K_1/K_2$  in Table I provide valuable information on the statistics of ligand coordination. This ratio is actually the equilibrium constant for the disproportionation reaction:  $2\text{AgX} = \text{Ag}^+ + \text{AgX}_2^-$ , which is independent of the concentration scale used. Thus, the  $K_1/K_2$  ratio can be readily compared for various media. In the case of silver chloride complexes,  $K_1/K_2$  in Table I is between 1.8 and 2.3, while for dilute aqueous solutions values of 24<sup>1</sup> and 11<sup>3</sup> are reported. In anhydrous ionic melts, irrespective of the temperature, this ratio is about 2.5,<sup>11,12</sup> which is close to the value obtained in the present work at 70 and 85°. For silver bromide complexes, the  $K_1/K_2$  ratio is rather high in dilute aqueous solutions, *i.e.*, 26 according to Berne and Leden<sup>6</sup> or even 50 according to Lieser.<sup>4</sup> In anhydrous molten salts values between 2 and 4 are reported,<sup>11,15</sup> while according to Table I this ratio is higher in  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$  but still much lower than in dilute aqueous solutions.

Qualitatively, this survey of data indicates that  $\text{AgX}_2^-$  should be a linear species in dilute aqueous solutions. (Only one possible site in the coordination sphere of Ag is available to the second ligand; thus  $K_2$  is low compared with  $K_1$ ). In anhydrous ionic melts the lattice structure probably provides a greater chance for the second ligand to replace any of the available nitrate ions around  $\text{Ag}^+$ , so that  $\text{AgX}_2^-$  is not necessarily a linear grouping. Consequently,  $K_1/$

(23) I. J. Gal and M. Jęftović, to be submitted for publication.

$K_2$  is lower, approaching eventually the statistical ratio of Bjerrum<sup>24</sup> and Adams<sup>25</sup> if the two bonds are of equal strength. In a solvent like  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$  the formation of silver halide complexes is apparently similar to a coordination mechanism valid for anhydrous melts, especially in the case of silver chloride.

A more quantitative test is provided by the quasi-lattice model of Blander.<sup>16</sup> According to this model developed for reciprocal molten salt systems, the stability constants (on a mole fraction scale) can be expressed as

$$K_1 = Z(\beta_1 - 1) \quad (7)$$

$$K_2 = [(Z - 1)/2]\{\beta_2 - 1 + [(\beta_2 - \beta_1)/(\beta_1 - 1)]\} \quad (8)$$

Here,  $Z$  is the coordination number of cations in the "lattice," usually 4–6, and

$$\beta_1 = \exp(-\Delta A_1/RT) \quad (9)$$

$$\beta_2 = \exp(-\Delta A_2/RT) \quad (10)$$

where  $\Delta A_1$  and  $\Delta A_2$  are the Helmholtz free energies of the first and second metal–ligand bond, respectively. Equation 8 is based on the assumption that the second ligand has available  $Z - 1$  sites around the central cation. If only a linear grouping can be formed,  $K_2$  is lower and eq 8 should be replaced by<sup>16</sup>

$$K_2' = 1/2\{\beta_2 - Z + [(\beta_2 - 1)/(\beta_1 - 1)]\} \quad (11)$$

Taking the values for  $K_1$  and  $K_2$  from Table I and  $Z = 6$ , the free energies of the bonds were calculated assuming eq 7–11 valid in the  $\text{NH}_4\text{NO}_3 \cdot 2\text{H}_2\text{O}$  melt. Thus for  $\Delta A_2$  two values are obtained: from eq 8 (nonlinear grouping) and from eq 11 (linear grouping). The results are listed in Table II.

As seen from this table, when chloride ion is the

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TABLE II  
THE BOND FREE ENERGIES

Ligand	Temp, °K	– $\Delta A_1$ , kcal	– $\Delta A_2$ , kcal	
			Nonlinear (eq 8)	linear (eq 11)
Cl <sup>–</sup>	328.5	3.87	4.04	4.91
	343.2	3.94	4.03	5.02
	358.1	4.05	4.07	5.19
Br <sup>–</sup>	328.8	5.87	5.09	7.01
	343.1	6.10	5.36	7.40
	358.1	6.24	5.32	7.38

ligand, the free energies  $\Delta A_1$  and  $\Delta A_2$  (nonlinear) are within a few per cent independent of the temperature and nearly equal. This is in agreement with the results obtained in molten salts,<sup>9–12,17</sup> although the free energies are higher in anhydrous melts. The linear model seems to be less suitable. (As seen from Table II, for chloride,  $\Delta A_2$  (linear) increases with the temperature.)

In the case of bromide ligands  $\Delta A_1$  is larger than  $\Delta A_2$  (nonlinear) and depends strongly on temperature. This differs from the behavior in anhydrous  $\text{KNO}_3$ <sup>15</sup> where the temperature dependence of  $K_1$  is correctly predicted by eq 8.

Recently, Braunstein extended the quasi-lattice model to reciprocal molten salt systems containing water.<sup>21</sup> His theoretical expression for  $K_1$  has two  $\Delta A_1$  terms because a ligand can replace either water or a salt anion from the coordination sphere of the cation. Unfortunately, this interesting model cannot be tested at this time because the stability constants in anhydrous melt and in melts of different water content are required. An extension of the present investigation in this direction is under way.

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