

and  $AB_2Te_4$ . The observation that  $NiCr_2S_4$  and  $NiCr_2Se_4$  are semiconductors, not metals,<sup>13</sup> is another indication that metal-metal bonding is not a prerequisite for the formation of an NiAs-type phase. In addition, the relatively small  $c/a$  and  $c/b$  values found in certain  $AB_2Se_4$  compounds suggest that the occurrence of metallic conductivity may best be treated as a

phenomenological observation rather than a structural determinant.

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## The Crystal Structure of a Hexanuclear Basic Lead(II) Perchlorate Hydrate: $Pb_6O(OH)_6(ClO_4)_4 \cdot H_2O$ <sup>1a</sup>

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The structure of  $Pb_6O(OH)_6(ClO_4)_4 \cdot H_2O$  has been determined by single-crystal X-ray diffraction. The crystals are orthorhombic, space group  $Pbca$ ,  $Z = 8$ ,  $a = 10.814 \pm 0.005 \text{ \AA}$ ,  $b = 16.706 \pm 0.006 \text{ \AA}$ ,  $c = 26.273 \pm 0.008 \text{ \AA}$ ,  $d_x = 4.973 \text{ g/cm}^3$ ,  $d_m = 5.07 \pm 0.03 \text{ g/cm}^3$ . The structure was refined to a conventional  $R$  factor of 5.5%, using 791 intensities which were collected by counter methods. The crystal contains discrete  $Pb_6O(OH)_6^{4+}$  units. Four of the lead atoms are found in a central tetrahedron (distorted) while the remaining two cover two of the tetrahedral faces, thereby forming two exterior tetrahedra. The adjacent Pb-Pb distances average 3.81  $\text{\AA}$  and range from 3.44 to 4.09  $\text{\AA}$ . A unique oxygen atom (oxide) is found at the center of the central lead tetrahedron. The remaining six oxygen atoms, presumably hydroxide, are located over the six external faces of the two exterior lead tetrahedra. These results contradict an earlier conclusion from Raman evidence that the lead atoms are at the corners of an octahedron.

### Introduction

Recently Maroni and Spiro<sup>2</sup> investigated the vibrational spectra of a series of hydroxy- and alkoxy-bridged polyhedra of Bi(III), Pb(II), and Tl(I). The most significant result was the finding of a set of low-frequency Raman bands attributable almost entirely to the motions of the metal atoms. The high intensity of these bands was taken as evidence for some degree of metal-metal bonding and the simplicity of their pattern suggested that they might be useful in structural characterization of polynuclear species.

Of particular interest in the latter connection were the species present in perchlorate solutions of lead(II) containing 1.33 mol of hydroxide per mole of lead. Potentiometric<sup>3</sup> and ultracentrifuge<sup>4</sup> data were consistent with an equilibrium between  $Pb_3(OH)_4^{2+}$  and

$Pb_6(OH)_8^{4+}$ . Crystals of composition  $Pb_3(OH)_4(ClO_4)_2$  were described in 1930 by Willard and Kassner.<sup>5</sup> The Raman spectrum<sup>2b</sup> of these crystals showed three strong low-frequency bands similar to those exhibited<sup>2a</sup> by octahedral  $Bi_6(OH)_{12}^{6+}$ . Since in the concentrated solutions from which the crystals were obtained  $Pb_6(OH)_8^{4+}$  was presumably predominant, it was inferred that these crystals also contained this complex, and its structure was predicted to be octahedral.<sup>2b</sup> The eight hydroxide ions were presumed to lie above the eight trigonal faces of the lead octahedron, giving a structure analogous to that of  $Mo_6Cl_8^{4+}$ .<sup>6</sup> A normal-coordinate analysis<sup>2b</sup> showed that this structure was capable of predicting all of the observed Raman and infrared bands of the crystals.

We report here a determination of the structure of these crystals by X-ray diffraction. The results are consistent with the chemical analysis by Willard and Kassner<sup>5</sup> but indicate that the crystals should be formulated as  $Pb_6O(OH)_6(ClO_4)_4 \cdot H_2O$  and that the

(1) (a) Work done under auspices of the Atomic Energy Commission. Supported in part by Public Health Service Research Grant GM13498 to T. G. S. (b) Princeton University. (c) University of California.

(2) V. A. Maroni and T. G. Spiro, *Inorg. Chem.*: (a) **7**, 183 (1968); (b) **7**, 188 (1968); (c) **7**, 193 (1968).

(3) A. Olin, *Acta Chem. Scand.*, **14**, 126, 814, 1999 (1960); *Scensk Kem. Tidsskr.*, **73**, 482 (1961).

(4) O. E. Esva and J. S. Johnson, *J. Phys. Chem.*, **69**, 959 (1965).

(5) H. H. Willard and J. L. Kassner, *J. Am. Chem. Soc.*, **52**, 2395 (1930).

(6) C. Brosset, *Arkiv Kemi*, **1**, 353 (1949); *Arkiv Kemi, Mineral. Geol.*, **A20**, No. 7 (1945).

Raman prediction of structure is incorrect. Discrete hexanuclear complexes are indeed found, but the lead atoms are arranged at the corners of three face-sharing tetrahedra rather than at the corners of an octahedron. As indicated in the formula, this complex contains six rather than eight hydroxide ions and also one oxide ion, the latter being located at the center of the central tetrahedron of lead atoms.

### Experimental Section

Crystals of composition  $\text{Pb}_6(\text{OH})_4(\text{ClO}_4)_2$  were prepared by the method of Willard and Kassner.<sup>8</sup> Various crystals were examined in preliminary experiments by the Weissenberg (with Cu  $K\alpha$  radiation) and counter techniques (Mo  $K\alpha$  radiation,  $\lambda$  0.71069 Å). Two sets of intensity data were used in the analysis. The first was obtained with a crystal of irregular shape. For the final measurements, a crystal was ground and etched with water to a sphere of diameter 0.13 mm and glued to a glass fiber. The  $c$  axis was aligned coincident with the  $\phi$  axis of our instrument. The cell dimensions and diffraction intensities were measured at a temperature of ca. 23° using a manually operated General Electric XRD-5 goniostat equipped with a scintillation counter and pulse-height discriminator. The Mo X-ray tube was operated at 45 kV and 20 mA. Each reflection was measured for 10 sec with the stationary-crystal, stationary-counter technique. The background was measured near each reflection. The maximum intensity was 8785 counts in 10 sec for the 002 reflection. The minimum background was 55 counts in 10 sec at  $2\theta = 35^\circ$ . Some difficulty was encountered with overlapping reflections, and we made some adjustments as best as we could to correct for this effect. Defects in this adjustment may be one of the limiting sources of error in the data. Measurements were made for 1111 independent reflections, including all but a few within the limit  $2\theta < 35^\circ$ . Of these, 320 were recorded and were discarded. The remaining 791 reflections were used in the final analysis.

The linear absorption coefficient of the material is estimated as 419  $\text{cm}^{-1}$  (Mo  $K\alpha$ ), and  $\mu R = 2.83$ . The intensities were corrected for absorption on the basis of the tabulation for spherical crystals in the "International Tables."<sup>7</sup> The variance of each intensity was estimated to be

$$\sigma^2(I) = I + 2B + (pI)^2 + q$$

where  $I$  is the net counts,  $B$  is the background,  $p$  is the fraction of  $I$  which is included to represent nonstatistical errors (0.10 in this case), and  $q$  is a constant (30 in this case) which represents additional error in the background. Structure factors were derived from the intensities with the usual corrections for Lorentz and polarization effects. Standard deviations of structure factors were taken as

$$\sigma(F_o) = F_o - (kI - k\sigma(I))^{1/2}, kI = F_o^2$$

No intensity was used which was less than its standard deviation, and therefore the term under the square root is always positive. In the final least-squares refinement, observations were weighted as  $w = [\sigma(F)]^{-2}$ .

Calculations were made with a CDC-6600 computer. The data were adjusted to an absolute scale and expressed as normalized structure magnitudes  $|E|$  using an unpublished program written by H. S. Maddox and M. L. Maddox. We used our own unpublished programs for data processing, Fourier series, full-matrix least squares, and interatomic distances. The function minimized in the method of least squares is  $\sum w(\Delta F)^2 / \sum w |F_o|^2$ ,

(7) W. L. Bond in "International Tables for X-Ray Crystallography," Vol. II, J. S. Kasper and K. Lonsdale, Ed., The Kynoch Press, Birmingham, England, 1959, p 302.

where  $\Delta F$  is the difference between the magnitudes of the observed and calculated structure factors  $F_o$  and  $F_c$ .

Atomic scattering factors and anomalous dispersion corrections for  $\text{Pb}^{2+}$  and neutral Cl and O were taken from the compilations of Cromer and Waber.<sup>8</sup> The real and imaginary dispersion corrections are respectively  $-3.79$  and  $10.18$  for Pb and  $0.15$  and  $0.19$  for Cl.

The isotropic temperature factor is defined as  $\exp(-B\lambda^{-2} \sin^2 \theta)$ , where  $B$  is the thermal parameter. The anisotropic temperature factor is  $\exp(-\frac{1}{4}\sum \sum B_{ij} b_i b_j h_i h_j)$ , for all values of  $i$  and  $j$  from 1 to 3;  $b_i$  is the  $i$ th reciprocal axis length,  $h_i$  is a Miller index, and  $B_{ij}$  is a thermal parameter.

In this paper we designate the conventional  $R$  factor as  $R = \sum |\Delta F| / \sum |F_o|$  and the weighted  $R$  factor as  $R_2 = (\sum w(\Delta F)^2 / \sum w(F_o)^2)^{1/2}$ .

### Results

**Unit Cell and Space Group.**—The crystals are orthorhombic, and the systematic absences ( $0kl$ ,  $k = 2n + 1$ ;  $h0l$ ,  $l = 2n + 1$ ; and  $hk0$ ,  $h = 2n + 1$ ) indicate space group  $\text{Pbca}$ , with eightfold general positions:  $\pm(x, y, z; \frac{1}{2} + x, \frac{1}{2} - y, -z; -x, \frac{1}{2} + y, \frac{1}{2} - z; \frac{1}{2} - x, -y, \frac{1}{2} + z)$ . The cell dimensions are  $a = 10.814 \pm 0.005$ ,  $b = 16.706 \pm 0.006$ , and  $c = 26.273 \pm 0.008$  Å ( $23^\circ$ ). For eight formula units of  $\text{Pb}_6\text{O}(\text{OH})_6(\text{ClO}_4)_4 \cdot \text{H}_2\text{O}$  per cell the calculated density is  $4.973 \text{ g/cm}^3$ . The density measured with pycnometer and carbon tetrachloride at  $24^\circ$  is  $5.07 \pm 0.03 \text{ g/cm}^3$ . Part of the discrepancy may be the result of contamination of the pycnometer sample, for example with lead carbonate ( $d = 6.6 \text{ g/cm}^3$ ).

**Phase Determination.**—The structure was solved with 286 reflections from the first data set by use of the symbolic addition procedure<sup>9</sup> to determine the phases. We used only the  $\Sigma_2$  relation,  $sE_h \approx s\sum_k E_k E_{h-k}$ , where  $s$  means "sign of." Long's program<sup>10</sup> was used to apply this relation to the 286 reflections of highest  $|E|$ . Three reflections were given plus phases in order to fix the origin and four others were assigned symbols a, b, c, or d. These are listed in Table I. Of the 16 combinations of initial signs for these symbols, three converged in 9 or 11 cycles to indications that  $a = +$ ,  $b = +$ ,  $c = -$ , and  $d = -$ . One of these gave a consistency index<sup>10</sup> of 0.49, while the next highest index was 0.39. No other starting set required less than 8 cycles to converge.

TABLE I

STARTING REFLECTIONS FOR  $\Sigma_2$  PROCEDURE

Sign	$hkl$	Sign	$hkl$
+	289	a	473
+	1,5,14	b	154
+	5,10,8	c	127
		d	1,9,11

An  $E$  map (Fourier synthesis) was computed using the signs from the most consistent set. It showed six

(8) D. T. Cromer and J. T. Waber, *Acta Cryst.*, **18**, 104 (1965); D. T. Cromer, *ibid.*, **18**, 17 (1965).

(9) I. L. Karle and J. Karle, *ibid.*, **16**, 969 (1963).

(10) R. E. Long, Thesis, University of California at Los Angeles, 1965.

TABLE II  
POSITIONAL COORDINATES AND THERMAL PARAMETERS FOR LEAD ATOMS IN  $\text{Pb}_6\text{O}(\text{OH})_6(\text{ClO}_4)_4 \cdot \text{H}_2\text{O}^a$

Atom	<i>x</i>	<i>y</i>	<i>z</i>	<i>B</i> <sub>11</sub> <sup>b</sup>	<i>B</i> <sub>22</sub>	<i>B</i> <sub>33</sub>	<i>B</i> <sub>12</sub>	<i>B</i> <sub>13</sub>	<i>B</i> <sub>23</sub>
Pb(1)	0.3391 (4)	-0.0421 (3)	0.2050 (2)	5.2 (3)	3.2 (2)	4.4 (2)	0.3 (2)	0.2 (2)	0.8 (2)
Pb(2)	0.2347 (4)	0.1505 (3)	0.1530 (2)	2.9 (2)	3.4 (2)	5.0 (2)	0.0 (2)	0.1 (2)	0.3 (2)
Pb(3)	0.5672 (4)	0.1527 (3)	0.1990 (2)	3.9 (2)	5.4 (3)	3.2 (2)	0.7 (2)	-0.2 (2)	-0.9 (2)
Pb(4)	0.5078 (4)	0.0543 (3)	0.0866 (2)	3.3 (2)	4.1 (2)	4.0 (2)	0.4 (2)	0.0 (2)	-1.2 (2)
Pb(5)	0.4734 (4)	0.2794 (3)	0.0863 (2)	3.4 (2)	3.8 (2)	4.3 (2)	-0.1 (2)	-0.2 (2)	1.1 (2)
Pb(6)	0.7958 (4)	0.2123 (3)	0.0935 (2)	3.6 (2)	5.8 (3)	4.2 (2)	-0.7 (2)	0.4 (2)	-0.5 (2)

<sup>a</sup> Standard deviations are given in parentheses and refer to the least significant digit. <sup>b</sup> Thermal parameter units are Å<sup>2</sup>.

pronounced peaks, which could readily be identified with the six lead atoms in the hexanuclear unit. The positions of the six lead atoms were refined with isotropic temperature factors by least squares using the original data set. Four cycles reduced *R* to 0.17. A Fourier synthesis of  $\Delta F$  then revealed four prominent peaks, assignable to the chlorine atoms in the four perchlorate groups, and many lesser peaks, some of which were assigned to oxygen in the perchlorate ions or bound to the lead atoms. Subsequent least-squares refinement, with anisotropic temperature factors for the lead atoms, eventually reduced *R* to 0.10. However, several oxygen atoms refused to refine properly, giving unreasonable interatomic distances or excessive thermal parameters.

At this point it was judged that the intensities had been taken without proper attention to background, overlap, and absorption corrections, and it seemed evident that this inadequacy would prevent further clarification of the oxygen positions. Accordingly the final set of intensities were measured. The new data were used to refine the previously determined lead and chlorine positions, with anisotropic thermal parameters for lead. Two cycles of least squares led to *R* = 0.11. A difference Fourier synthesis was calculated, and 23 of the highest peaks could be assigned to oxygen bound to chlorine or lead. All of these oxygen atoms now refined properly, and *R* was reduced to 0.062 and *R*<sub>2</sub> to 0.073.

According to the chemical analysis<sup>5</sup> a water molecule remained to be included in the structure, and the experimental density corresponded to three additional molecules. A search for cavities in the structure revealed only one hole large enough for a water molecule. In a Fourier synthesis of  $\Delta F$ , the largest peak (of height 2.6 e<sup>-</sup>/Å<sup>3</sup>) coincided with that hole. Introduction of an oxygen atom (designated O(8)) at this location decreased *R* to 0.060 and *R*<sub>2</sub> to 0.070. This atom had been recognized in earlier Fourier maps, but had been rejected because a computational blunder caused it to have an unreasonably large thermal parameter.

Up to this time the 791 reflections had been assigned equal weight. After a few errors in the data were corrected, refinement was continued with various weighting schemes until one was found which corresponded reasonably well to the distribution of magnitudes of discrepancies as a function of observed intensity. After the final refinement, *R* was 0.055, *R*<sub>2</sub>

was 0.069, and the estimated standard deviation of an observation of unit weight was 1.09. In the last cycle, no coordinate or thermal parameter shifted more than 9% of its estimated standard deviation. A final synthesis of  $\Delta F$  showed a maximum value of 1.6 e<sup>-</sup>/Å<sup>3</sup> and 28 other peaks higher than 1.0 e<sup>-</sup>/Å<sup>3</sup>. Under these circumstances, a search for hydrogen atoms seemed unjustified.

The final values of the parameters are given in Table II for lead atom and in Table III for chlorine and oxygen atoms. Table IV contains the observed and calculated structure factors. Interatomic distances are listed in Tables V-VII. Some angles in the  $\text{Pb}_6\text{O}(\text{OH})_6^{4+}$  cluster are listed in Table VIII.

TABLE III  
FINAL COORDINATES AND THERMAL PARAMETERS FOR CHLORINE AND OXYGEN ATOMS IN  $\text{Pb}_6\text{O}(\text{OH})_6(\text{ClO}_4)_4 \cdot \text{H}_2\text{O}^a$

Atom	<i>x</i>	<i>y</i>	<i>z</i>	<i>B</i> , Å <sup>2</sup>
O(1)	0.440 (6)	0.166 (4)	0.133 (2)	6 (2)
O(2)	0.301 (5)	0.025 (3)	0.129 (2)	3 (1)
O(3)	0.309 (6)	0.096 (4)	0.222 (2)	6 (2)
O(4)	0.630 (4)	0.267 (3)	0.141 (2)	2 (1)
O(5)	0.605 (5)	0.192 (3)	0.054 (2)	4 (1)
O(6)	0.689 (5)	0.111 (3)	0.136 (2)	4 (1)
O(7)	0.519 (5)	0.012 (3)	0.176 (2)	4 (1)
O(8)	0.388 (7)	0.116 (5)	0.482 (3)	9 (2)
Cl(1)	0.890 (2)	0.296 (2)	0.233 (1)	5.0 (7)
Cl(2)	0.978 (3)	-0.002 (2)	0.162 (1)	4.9 (6)
Cl(3)	0.241 (3)	0.099 (2)	-0.002 (1)	5.5 (6)
Cl(4)	0.107 (2)	0.335 (2)	0.084 (1)	4.5 (6)
O(11) <sup>b</sup>	0.820 (6)	0.359 (4)	0.208 (2)	7 (2)
O(12)	0.884 (5)	0.222 (3)	0.207 (2)	5 (2)
O(13)	0.833 (7)	0.275 (4)	0.276 (3)	8 (2)
O(14)	0.028 (7)	0.315 (4)	0.235 (3)	7 (2)
O(21)	0.853 (7)	-0.033 (4)	0.174 (3)	7 (2)
O(22)	0.056 (8)	-0.065 (5)	0.136 (3)	10 (3)
O(23)	-0.022 (6)	0.067 (4)	0.134 (3)	7 (2)
O(24)	0.044 (6)	0.016 (4)	0.207 (2)	6 (2)
O(31)	0.315 (6)	0.028 (4)	-0.013 (2)	6 (2)
O(32)	0.135 (7)	0.074 (4)	0.026 (3)	8 (2)
O(33)	0.197 (6)	0.138 (4)	-0.044 (3)	7 (2)
O(34)	0.317 (8)	0.152 (5)	0.024 (3)	9 (2)
O(41)	0.141 (7)	0.398 (5)	0.045 (3)	9 (2)
O(42)	0.090 (6)	0.258 (4)	0.064 (2)	5 (1)
O(43)	0.000 (5)	0.365 (3)	0.109 (2)	3 (1)
O(44)	0.194 (7)	0.335 (4)	0.120 (3)	7 (2)

<sup>a</sup> Standard deviations, estimated by least squares, are given in parentheses and refer to the least significant digits. <sup>b</sup> O(*ij*) refers to the *j*th oxygen bound to the *i*th chlorine in the perchlorate groups.

TABLE IV

OBSERVED AND CALCULATED STRUCTURE FACTORS FOR Pb6O(OH)6(ClO4)4 · H2O [FCA(0, 0, 0) = 2645]

Table with multiple columns containing observed and calculated structure factors for Pb6O(OH)6(ClO4)4 · H2O. The table lists various hkl reflections and their corresponding structure factor values.

TABLE V

INTERATOMIC DISTANCES (Å) IN Pb6O(OH)64+

Table listing interatomic distances (Å) in Pb6O(OH)64+. It includes pairs of atoms and their respective distances, such as Pb(3)-Pb(4) at 3.440 (5) Å.

Standard deviations in parentheses refer to the least significant digit.

Discussion

Apart from the perchlorate ions, the asymmetric unit contains 8 oxygen atoms of three distinct types. These atoms possess 8 hydrogen atoms according to the chemical stoichiometry. On the basis of the structure we assign these as an oxide ion, O(1), a water molecule, O(8), and six hydroxide ions.

The lead atoms occur in discrete clusters of six, with

TABLE VI

CHLORINE-OXYGEN DISTANCES (Å) IN PERCHLORATE GROUPS

Table listing chlorine-oxygen distances (Å) in perchlorate groups. It shows Cl-O distances for various Cl-O bonds, such as Cl(1)-O(11) at 1.45 (6) Å.

Standard deviations in parentheses refer to the least significant digits.

TABLE VII

DISTANCES (Å) INVOLVING THE WATER MOLECULE

Table listing distances (Å) involving the water molecule. It shows distances between atoms and the water molecule, such as O(8)-Pb(6) at 2.74 (7) Å.

TABLE VIII  
 SOME ANGLES (IN DEG) IN THE  $\text{Pb}_6\text{O}(\text{OH})_6^{4+}$  CLUSTER<sup>a</sup>

Pb(2)–Pb(1)–Pb(3)	58.3	Pb(1)–Pb(4)–Pb(5)	111.3	Pb(3)–O(1)–Pb(5)	114
Pb(2)–Pb(1)–Pb(4)	59.4	Pb(1)–Pb(4)–Pb(6)	125.5	Pb(4)–O(1)–Pb(5)	109
Pb(3)–Pb(1)–Pb(4)	50.7	Pb(2)–Pb(4)–Pb(3)	63.1	Pb(1)–O(2)–Pb(2)	105
Pb(1)–Pb(2)–Pb(3)	66.3	Pb(2)–Pb(4)–Pb(5)	60.2	Pb(1)–O(2)–Pb(4)	108
Pb(1)–Pb(2)–Pb(4)	63.9	Pb(2)–Pb(4)–Pb(6)	107.5	Pb(2)–O(2)–Pb(4)	103
Pb(1)–Pb(2)–Pb(5)	117.4	Pb(3)–Pb(4)–Pb(5)	62.9	Pb(1)–O(3)–Pb(2)	108
Pb(3)–Pb(2)–Pb(4)	54.0	Pb(3)–Pb(4)–Pb(6)	60.7	Pb(1)–O(3)–Pb(3)	98
Pb(3)–Pb(2)–Pb(5)	59.8	Pb(5)–Pb(4)–Pb(6)	55.4	Pb(2)–O(3)–Pb(3)	92
Pb(4)–Pb(2)–Pb(5)	59.8	Pb(2)–Pb(5)–Pb(3)	60.2	Pb(3)–O(4)–Pb(5)	105
Pb(1)–Pb(3)–Pb(2)	55.4	Pb(2)–Pb(5)–Pb(4)	60.0	Pb(3)–O(4)–Pb(6)	103
Pb(1)–Pb(3)–Pb(4)	62.6	Pb(2)–Pb(5)–Pb(6)	116.8	Pb(5)–O(4)–Pb(6)	106
Pb(1)–Pb(3)–Pb(5)	108.3	Pb(3)–Pb(5)–Pb(4)	54.2	Pb(4)–O(5)–Pb(5)	101
Pb(1)–Pb(3)–Pb(6)	128.5	Pb(3)–Pb(5)–Pb(6)	62.2	Pb(4)–O(5)–Pb(6)	109
Pb(2)–Pb(3)–Pb(4)	62.9	Pb(4)–Pb(5)–Pb(6)	66.6	Pb(5)–O(5)–Pb(6)	107
Pb(2)–Pb(3)–Pb(5)	60.1	Pb(3)–Pb(6)–Pb(4)	51.3	Pb(3)–O(6)–Pb(4)	92
Pb(2)–Pb(3)–Pb(6)	112.4	Pb(3)–Pb(6)–Pb(5)	60.3	Pb(3)–O(6)–Pb(6)	115
Pb(4)–Pb(3)–Pb(5)	62.9	Pb(4)–Pb(6)–Pb(5)	58.0	Pb(4)–O(6)–Pb(6)	115
Pb(4)–Pb(3)–Pb(6)	68.0	Pb(2)–O(1)–Pb(3)	115	Pb(1)–O(7)–Pb(3)	118
Pb(5)–Pb(3)–Pb(6)	57.5	Pb(2)–O(1)–Pb(4)	109	Pb(1)–O(7)–Pb(4)	113
Pb(1)–Pb(4)–Pb(2)	56.7	Pb(2)–O(1)–Pb(5)	112	Pb(3)–O(7)–Pb(4)	88
Pb(1)–Pb(4)–Pb(3)	66.7	Pb(3)–O(1)–Pb(4)	98		

<sup>a</sup> The estimated standard deviations of the Pb–Pb–Pb and the Pb–O–Pb angles are  $\pm 0.1$  and  $\pm 2^\circ$ , respectively.

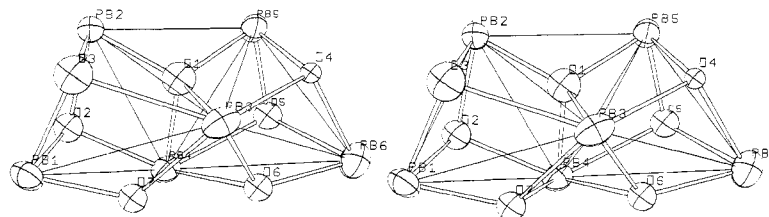


Figure 1.—Stereoscopic view of the  $\text{Pb}_6\text{O}(\text{OH})_6^{4+}$  complex. The stick bonds connect oxygen and lead atoms; the lines define the lead polyhedra. Interatomic distances are given in Table V and angles in Table VIII.

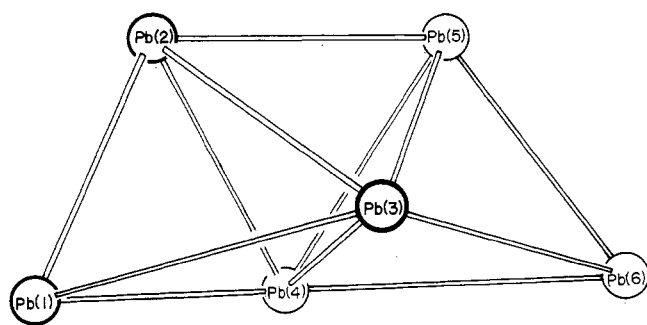


Figure 2.—The three face-sharing tetrahedra of Pb atoms in the  $\text{Pb}_6\text{O}(\text{OH})_6^{4+}$  cluster.

single tetrahedron, and to that<sup>12</sup> of  $\text{Sn}_2\text{OSO}_4$ , in which an isolated  $\text{Sn}_3$  unit has four tin atoms at the corners of a central tetrahedron all four faces of which are covered by the remaining tin atoms.

The oxide ion is near the center of the central tetrahedron, at an average distance 2.29 Å from its lead neighbors. The oxygen atoms in tetragonal  $\text{PbO}$

have similar tetrahedral coordination, with lead neighbors at 2.30 Å.<sup>13</sup> Thus the central tetrahedron of the cluster can be considered as a fragment of the  $\text{PbO}$  structure. Oxygen with four metal neighbors in isolated complexes is relatively rare, but some examples are  $\text{Be}_4\text{O}(\text{CH}_3\text{COO})_6$  and  $\text{Zn}_4\text{O}(\text{CH}_3\text{COO})_6$ ,<sup>14</sup>  $\text{Mg}_4\text{OBr}_6 \cdot 4\text{C}_4\text{H}_{10}\text{O}$ ,<sup>15</sup> and  $\text{Cu}_4\text{OCl}_6((\text{C}_6\text{H}_5)_3\text{PO})_4$ .<sup>16</sup>

Each of the six hydroxide ions is adjacent to three lead atoms on an external face of a noncentral tetrahedron, and all such faces are covered in this way. This topology gives the three lead atoms in each face of every tetrahedron one, and only one, oxygen neighbor in common. The oxide ion fills this role for four faces, while each hydroxide ion is involved with only one face.

The water molecule is only loosely bonded to this complex, at a distance 2.74 Å from Pb(6) on one corner. It is remote from any other lead atoms. Its nearest oxygen neighbor is O(32) at  $2.77 \pm 0.09$  Å and in a

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direction  $116^\circ$  from Pb(6); this distance and direction suggest hydrogen bonding. Other oxygen neighbors are at distances of 3.15 Å or more.

There is considerable variation in the Pb–Pb distances. The shortest one, 3.44 Å, is unique in that it is the only edge shared by all three tetrahedra. It may be compared with the distance 3.50 Å found in metallic lead. The other Pb–Pb neighbor distances in the cluster range from 3.67 to 4.09 Å, compared with 3.85 Å found in the  $\text{Pb}_4(\text{OH})_4^{4+}$  complex.<sup>11</sup> The cluster conforms only approximately to the symmetry  $\text{mm}2$  ( $C_{2v}$ ) which is permitted by its topology, but the lead positions are very close to symmetry 2 ( $C_2$ ). The hydroxide ions are expected to have their protons directed outward from the cluster, and they will tend to form hydrogen bonds to the surrounding perchlorate ions. Evidently such bonding or some other packing force prevents exact symmetry for the cluster. Each hydroxide ion has one or two perchlorate oxygen neighbors at distances between 2.94 and 3.15 Å to which it could form weak hydrogen bonds. We cannot make any unique assignment of hydrogen bonds on the basis of our results. The low accuracy of oxygen–oxygen distances (*ca.* 0.08 Å) tends to obscure the distinction between bonds and nonbonds, and the bonds may involve disorder or bifurcation.

The perchlorate ions are not significantly coordinated, the closest distance from a lead to a perchlorate oxygen being 2.9 Å. This is in accord with the Raman and infrared spectra,<sup>17</sup> which show bands characteristic of unbound  $\text{ClO}_4^-$ . The observed distortions of perchlorate geometry are within the rather large standard deviations of the oxygen positions (see Table VI).

On the basis of its Raman spectrum the hexanuclear unit was predicted to have octahedral geometry.<sup>2b</sup> The main evidence was the occurrence of three Raman bands

in the metal–metal stretching region, analogous to those found for the known octahedral species  $\text{Bi}_6(\text{OH})_{12}^{6+}$ . The actual geometry revealed here (idealized point symmetry  $C_{2v}$ , lowered by the deviations in the Pb–O distances, and in the Pb–Pb distances around the base of the complex) requires 12 Raman-active vibrational modes in the metal–metal region. Evidently there is a good deal of accidental degeneracy in these frequencies. Preliminary calculations<sup>18</sup> show that this is a plausible consequence of the observed geometry.

An interesting question is whether the rather unusual structure found here for the hexameric complex is intrinsically more stable than others which can be envisaged, or whether it is stabilized by crystal forces. The results of a solution X-ray scattering study by Johannson and Olin<sup>19</sup> point to the former conclusion. The Pb–Pb peak in the radial distribution function, which occurs at 3.85 Å in solutions containing tetrahedral  $\text{Pb}_4(\text{OH})_4^{4+}$ , simply broadens without change in position as the OH:Pb ratio is increased toward 1.33. Weak next nearest neighbor peaks are found at 6.37 and 7.14 Å. (Nonadjacent Pb–Pb distances in  $\text{Pb}_6\text{O}(\text{OH})_6^{4+}$  occur at 6.36 and 7.14 Å.) These observations rule out an octahedral complex in solution and are entirely consistent with the structure reported here. In fact a radial distribution function calculated on the basis of our structure is in quantitative agreement with the solution scattering data.<sup>19</sup>

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