

## Molecular Structure of Phosphorus Trifluoride Studied by Gas Electron Diffraction

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The interatomic distances and the mean amplitudes for  $\text{PF}_3$  have been determined by the sector-microphotometer method of gas electron diffraction to be  $r_g(\text{P-F}) = 1.5700 \pm 0.0012 \text{ \AA}$ ,  $r_g(\text{F} \cdots \text{F}) = 2.3643 \pm 0.0028 \text{ \AA}$ ,  $l(\text{P-F}) = 0.0395 \pm 0.0025 \text{ \AA}$ , and  $l(\text{F} \cdots \text{F}) = 0.0653 \pm 0.0029 \text{ \AA}$ . The average structure in the ground vibrational state has been calculated from the interatomic distances ( $r_g$ ) by making correction for the effect of atomic displacements perpendicular to the equilibrium bond directions and for the centrifugal distortion. This average structure is in good correspondence with the rotational constant  $B_z$  calculated from the rotational constant  $B_0$  obtained by microwave spectroscopy. The bond angle for  $\text{PF}_3$ ,  $\theta_\alpha(\text{F-P-F}) = 97.8 \pm 0.2^\circ$ , is found to be the smallest in the series of phosphorus trihalides reported so far, and, hence, one of the subrules proposed by Gillespie has to be modified.

### Introduction

There have been appreciable differences among the structures of phosphorus trifluoride given in the literature. The structure was first reported to be  $r(\text{P-F}) = 1.52 \text{ \AA}$  and  $\theta(\text{F-P-F}) = 104^\circ$  by Brockway and his coworkers,<sup>1,2</sup> who used the visual method of electron diffraction, while the angle was later claimed to be much smaller ( $r(\text{P-F}) = 1.537 \pm 0.04 \text{ \AA}$  and  $\theta(\text{F-P-F}) = 98.2 \pm 0.6^\circ$ ) according to the sector study of Hersh.<sup>3</sup> Neither structure, however, was consistent with the rotational constant  $B_0$  obtained by microwave spectroscopy.<sup>4,5</sup>

On the other hand, it has been difficult to determine the parameters directly by spectroscopic data alone, because both phosphorus and fluorine have single stable isotopes. Accordingly, the FPF angle had to be assumed in order to derive the P-F distance from the  $B_0$  constant obtained by Gilliam, Edwards, and Gordy.<sup>5</sup> The FPF angles of 104, 102, 100, and 98° led to the P-F distances of 1.546, 1.551, 1.56, and 1.562 Å, respectively.<sup>5-8</sup> (Mirri, *et al.*,<sup>4</sup> pointed out that the P-F distance of 1.535 Å, given by Williams, *et al.*,<sup>7</sup> from the assumed FPF angle of 100°, was incorrect.)

In terms of the indirect evaluation of molecular geometry, Mirri<sup>8</sup> estimated the bond angle from the Coriolis coupling constant  $\zeta_4$  and the force constants using Meal and Polo's relation.<sup>9</sup> The upper limit for the estimated bond angle (98°) was smaller than that assumed in earlier studies<sup>4,6,10</sup> (102°); it was not only in agreement with Hersh's diffraction value<sup>3</sup> but also indicative of a force field, which brought the Coriolis

coupling constants and the centrifugal distortion constants into good consistency.

Various structures reported so far are summarized in Figure 1. As has been discussed extensively by Gillespie,<sup>11-13</sup> Bartell,<sup>14,15</sup> and others, the structure of  $\text{PF}_3$  is of basic importance in the stereochemistry of inorganic molecules. Accordingly, the present study has been undertaken to determine a more accurate structure by gas electron diffraction.

### Experimental Section

A sample of  $\text{PF}_3$  was prepared by the method cited by Brauer:<sup>16</sup>  $\text{PCl}_3 + 3\text{HF} \rightarrow \text{PF}_3 + 3\text{HCl}$ . The reaction vessels were made of brass. The system was filled with nitrogen gas and the product gas was sprayed on ice-cold water, into which hydrogen chloride was absorbed. The crude product trapped by liquid nitrogen contained a small amount of hydrogen chloride and silicon tetrafluoride. They were removed by another spray onto ice-cold water, which, however, caused considerable decomposition of  $\text{PF}_3$ . Upon redistillation under vacuum, no impurity band was observed in the infrared spectrum.

Electron diffraction photographs were taken with an apparatus<sup>17,18</sup> equipped with an  $r^3$  sector at the camera lengths of  $10.778 \pm 0.002$  and  $24.322 \pm 0.002$  cm. The electron wavelength, 0.05969 Å, was calibrated with reference to the  $r_\alpha(\text{C=O})$  bond distance (1.1646 Å) of carbon dioxide measured under the same experimental condition. The gas stored in a 2-l. flask with a pressure of about 90 Torr at 22° was led into the diffraction chamber through a nozzle 0.2 mm in diameter. The pressure in the apparatus was less than  $1 \times 10^{-4}$  Torr during photographic exposure. Photographs were recorded on Fuji Process Hard plates with exposure times of about 30 sec and were developed at 20° for 5 min with ED-131 developer diluted twice.

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- (4) A. M. Mirri, F. Scappini, and P. G. Favero, *Spectrochim. Acta*, **21**, 965 (1965).
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- (14) K. W. Hansen and L. S. Bartell, *Inorg. Chem.*, **4**, 1775 (1965).
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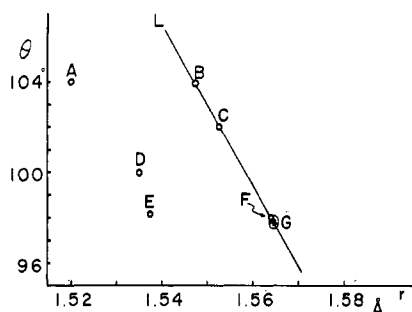


Figure 1.—Structural parameters for  $\text{PF}_3$  ( $r$  for the P-F distance and  $\theta$  for the F-P-F angle): (A) Pauling, *et al.*, ED;<sup>2</sup> (B) Gilliam, *et al.*, MW;<sup>5</sup> (C) Kisliuk, MW;<sup>6</sup> (D) Williams, *et al.*, MW;<sup>7</sup> (E) Hersh, ED;<sup>3</sup> (F) Mirri, MW;<sup>8</sup> (G) present study, ED (ED, electron diffraction; MW, microwave spectroscopy). A relation set by the rotational constant<sup>4</sup>  $B_z$  is shown by the line L.

Optical densities were measured by means of a microphotometer and an integrating digital voltmeter across the diameter of the plate with a regular interval of  $\Delta q = 1.19$ . The optical densities (0.18–0.57) were assumed to be proportional to the electron intensities. Intensity data taken from four short-distance plates and two long-distance plates were analyzed by a standard least-squares method with a diagonal weight matrix<sup>20</sup> for the  $q$  values 15–120 using the elastic and inelastic scattering factors taken from the recent literature.<sup>21–23</sup> The observed and the best-fit molecular intensities are shown in Figure 2, and the corresponding error matrix is given in Table I.<sup>24</sup>

TABLE I

ERROR MATRIX<sup>a</sup>

	$r(\text{P-F})$	$r(\text{F}\cdots\text{F})$	$l(\text{P-F})$	$l(\text{F}\cdots\text{F})$	$k$
$r(\text{P-F})$	0.0004	0.0000	-0.0000	0.0001	0.0001
$r(\text{F}\cdots\text{F})$		0.0017	0.0001	-0.0001	0.0004
$l(\text{P-F})$			0.0007	0.0004	0.0022
$l(\text{F}\cdots\text{F})$				0.0015	0.0021
$k$					0.0093

<sup>a</sup> Units for the distance  $r_a$  and the mean amplitude are Å, while the index of resolution  $k$  (average 0.84) is dimensionless. Elements of the matrix are given by  $\sigma_{ii} = \text{sgn} [(B^{-1})_{ii}] \{ [(B^{-1})_{ii}] \cdot V^*PV / (n - m) \}^{1/2}$ , where the notations correspond to those by O. Bastiansen, L. Hedberg, and K. Hedberg, *J. Chem. Phys.*, **27**, 1311 (1957). The diagonal element  $\sigma_{ii}$  represents the random standard error for the parameter  $i$ .

The  $r_a$  distances of P-F and F $\cdots$ F and their mean amplitudes derived from this analysis are listed in Table II. The limits of uncertainty ( $2.5\sigma$ ) were estimated from the internal consistency and the reproducibility of the results including the consideration of systematic errors, among which the error in the scale factor was the only significant one for the distance parameters, while for the mean amplitudes those due to extraneous scattering and the correlation with the index of resolution were the most important

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(24) Numerical data have been deposited as Document No. NAPS-00216 with the ASIS National Auxiliary Publications Service, c/o CCM Information Sciences, Inc., 22 West 34th St., New York, N. Y. 10001. A copy may be secured by citing the document number and by remitting \$3.00 for photocopies or \$1.00 for microfiche. Advance payment is required. Make checks or money orders payable to: ASIS-NAPS.

TABLE II

STRUCTURAL PARAMETERS AND MEAN AMPLITUDES FROM ELECTRON DIFFRACTION<sup>a</sup>

	P-F, Å	F $\cdots$ F, Å	$\theta(\text{P-F-F})$ , deg
$r_a$	$1.5689 \pm 0.0012$	$2.3624 \pm 0.0028$	(97.7)
$r_g$	$1.5700 \pm 0.0012$	$2.3643 \pm 0.0028$	(97.8)
$r_\alpha$	$1.5644 \pm 0.0012$	$2.3578 \pm 0.0028$	$97.8 \pm 0.2$
$r_\alpha^0$	$1.5647 \pm 0.0012$	$2.358 \pm 0.006^b$	$97.8^b$
$l_{\text{obsd}}$	$0.0395 \pm 0.0025$	$0.0653 \pm 0.0029$	
$l_{\text{calcd}}$	0.0412	0.0698	

<sup>a</sup> See ref 17 for various definitions of the structure of a molecule exerting vibration and rotation. Convenient measures of structure may be "the thermal-average values of interatomic distances,"  $r_g$ , and "the angles measured with regard to the average positions of atoms,"  $\theta_\alpha$  and  $\theta_\alpha^0$  for thermal and zero-point averages, respectively. <sup>b</sup> Estimated; see text.

contributors. The errors in the asymmetry parameters  $\kappa$  ( $\kappa_{\text{P-F}}$  and  $\kappa_{\text{F-F}}$  assumed to be  $7 \times 10^{-7}$  Å<sup>3</sup> and zero, respectively) were insignificant.

The thermal averages of the instantaneous internuclear distances  $r_g$  were calculated by<sup>25</sup>

$$r_g = r_a + (l^2/r_a) \quad (1)$$

The mean amplitudes are compared in Table II with those calculated from the quadratic force constants which were determined by Mirri<sup>8</sup> from vibrational frequencies, centrifugal distortion, and Coriolis coupling constants. The agreement is within the errors in the experimental and theoretical values, the latter being estimated to be about  $\pm 0.003$  Å. Similar values for the amplitudes have been calculated by several authors.<sup>26–28</sup>

## Molecular Structure

Average Structure ( $r_\alpha^0$ ) from Electron Diffraction.—

In order to compare the structure determined in the present analysis with spectroscopic results, the zero-point average distances<sup>29</sup> ( $r_\alpha^0$ ) were derived from  $r_g$  by the use of the quadratic force constants. Following the usual steps, the  $r_\alpha$  and  $r_\alpha^0$  distances were calculated by<sup>17</sup>

$$r_\alpha = r_g - [(\langle \Delta x^2 \rangle + \langle \Delta y^2 \rangle) / 2r] - \delta r \quad (2)$$

$$r_\alpha^0(\text{P-F}) = \lim_{T \rightarrow 0^\circ \text{K}} r_\alpha(\text{P-F}) = r_\alpha(\text{P-F}) - \Delta \langle \Delta z \rangle \quad (3)$$

where

$$\begin{aligned} \Delta \langle \Delta z \rangle &\equiv \Delta z (\text{room temperature}) - \langle \Delta z \rangle (0^\circ \text{K}) \\ &= 3/2 a \Delta \langle \Delta z^2 \rangle - [\Delta (\langle \Delta x^2 \rangle + \langle \Delta y^2 \rangle) / 2r] \end{aligned} \quad (4)$$

The parameter  $a$  characterizing the anharmonicity of the P-F bond stretching vibration was assumed to be equal to that of the PF diatomic molecule,<sup>30</sup>  $1.89 \text{ \AA}^{-1}$ . Minor corrections for the centrifugal distortion,  $\delta r$ ,

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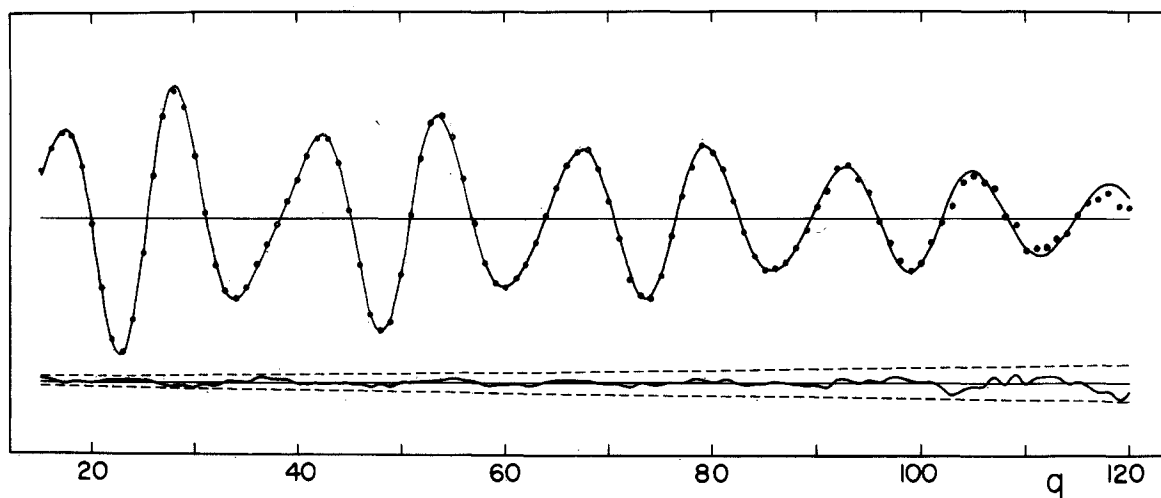


Figure 2.—Reduced molecular intensity  $qM(q)$  for  $\text{PF}_3$ . The observed and the best-fit values from one of the photographic plates are shown by dots and a solid curve, respectively. The lower solid and broken curves represent the residual and the error in the  $qM(q)$  due to the relative error of  $1 \times 10^{-3}$  in the original photocurrent, respectively.

were calculated by the method of Iwasaki and Hedberg<sup>31</sup> to be  $4 \times 10^{-4}$  Å for P–F and F···F.

The zero-point average angle,  $\theta_{\alpha}^0$ , was set equal to the temperature-average angle,  $\theta_{\alpha}$ , for the following reason. It seems plausible, as a first-order approximation, to assume a linear and additive relation in regard to the angle corresponding to the average positions of atoms for a certain vibrational state  $v(v_1, v_2, v_3, v_4)$ , designated as

$$\theta_z^v = \theta_e + \sum_{i=1} \beta_i(v_i + d_i/2) + \dots \quad (5)$$

where  $d_i$  represents degeneracy. Since the  $\theta_{\alpha}$  angle is essentially equal to the Boltzmann average of  $\theta_z^v$ , it follows that

$$\theta_{\alpha} \approx \sum_v \theta_z^v w_v(T) \approx \theta_e + \sum_i \beta_i d_i T_i / 2 \quad (6)$$

where

$$w_v(T) = \exp(-E_{vib}(v)/kT) / \sum_v \exp(-E_{vib}/kT) \quad (7)$$

and

$$T_i = \coth(hc\nu_i/2kT) \quad (8)$$

Accordingly, the difference is shown to be

$$\theta_{\alpha} - \theta_{\alpha}^0 \approx \sum_i \beta_i d_i (T_i - 1) / 2 \quad (9)$$

One may further assume that substantial contributions come from bending modes  $\nu_2$  ( $487 \text{ cm}^{-1}$ ) and  $\nu_4$  ( $344 \text{ cm}^{-1}$ )<sup>32</sup> and that the orders of magnitude of  $\beta_2$  and  $\beta_4$  are equal. Then the difference may be estimated in terms of that between the zero-point average and equilibrium angles.

$$\theta_{\alpha} - \theta_{\alpha}^0 \approx 0.37(\theta_z - \theta_e) \quad (10)$$

While the  $\theta_z - \theta_e$  for  $\text{PF}_3$  is unknown, it can be esti-

mated from analogous molecules to be only a small fraction of  $1^\circ$ . (For example, the corresponding differences are  $+6'$  and  $+2'$  for  $\text{OF}_2$  and  $\text{SO}_2$ , respectively.<sup>33</sup>) Consequently, it seems plausible to regard the  $\theta_{\alpha}^0$  as equal to  $\theta_{\alpha}$  to within the experimental uncertainty of the latter ( $\pm 0.2^\circ$ ). The  $r_{\alpha}^0(\text{F} \cdots \text{F})$  distance was derived from the  $r_{\alpha}^0(\text{P-F})$  distance and the  $\theta_{\alpha}^0$  angle.

Various average distances and angles are listed in Table II.

**Rotational Constant from Spectroscopy.**—The rotational constant  $B_z$ , which corresponds to the average structure in the ground vibrational state, was calculated from the rotational constant for the ground vibrational state  $B_0$  by correcting for rotation-vibration interactions.<sup>17</sup> The difference between  $B_z$  and  $B_0$  was found to be  $-5.70 \times 10^{-3} \text{ cm}^{-1}$ . Thus the rotational constant  $B_0$  (7819.99 MHz) obtained by Mirri, *et al.*,<sup>4</sup> gave a  $B_z$  constant of 7802.9 MHz.

**Average Structure.**—The rotational constant  $B_z$  sets a relation between the  $r_z(\text{P-F})$  distance and the  $\theta_z(\text{F-P-F})$  angle. This is illustrated in Figure 1 as a nearly straight line L. No unique  $r_z$  structure can be obtained from spectroscopy alone since the other rotational constant  $C_z$  is yet unknown.

On the other hand, the  $r_{\alpha}^0$  structure, which should be essentially equivalent to the spectroscopic  $r_z$  structure,<sup>17</sup> derived from electron diffraction is shown by G with an estimated uncertainty indicated by an ellipse. Since the point G is very closely on the line L, the result of electron diffraction is consistent with the rotational constant  $B_z$ . This consistency may be restated from a slightly different standpoint. The  $\theta_z$  angle can be obtained from  $B_z$  based on spectroscopy and the  $r_{\alpha}^0(\text{P-F})$  distance based on electron diffraction. The resulting  $\theta_z$ ,  $97.9 \pm 0.3^\circ$ , agrees with  $\theta_{\alpha}$ ,  $97.8 \pm 0.2^\circ$ , within experimental uncertainties, and, hence, the above-mentioned

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estimation,  $\theta_{\alpha}^0 \approx \theta_{\alpha}$ , within a few tenths of  $1^{\circ}$ , is justified.

### Discussion

In the light of the structural parameters determined in the present investigation, the long-standing confusion in regard to the  $\text{PF}_3$  structure may be elucidated in the following way.

(a) The initial study of Brockway and Wall<sup>1</sup> by means of visual intensity measurements ( $r(\text{P-F}) = 1.65 \text{ \AA}$  and  $\theta(\text{F-P-F}) = 99^{\circ}$ ) estimated the structure nearly correctly. However, a subsequent study of Pauling and Brockway<sup>2</sup> by the radial distribution method gave a different set of parameters including much larger errors ( $r = 1.47 \text{ \AA}$  and  $\theta = 110^{\circ}$ ). Unfortunately, the latter authors recommended average values of the above two with equal weights ( $r = 1.52 \text{ \AA}$  and  $\theta = 104^{\circ}$ ). Similar situations are encountered in the structures of  $\text{PCl}_3$ ,  $\text{AsCl}_3$ , and  $\text{Cl}_2\text{O}$ .

(b) Hersh's study,<sup>3</sup> on the other hand, estimated the bond angle correctly, whereas an appreciable systematic error (about 2%) involved in the scale factor caused the bond distance to appear unreasonably short. This is probably the reason for a similar systematic shortening in the P-F bond distances of  $\text{PF}_5$  studied contemporaneously by Hersh in comparison with the corresponding distances reported more recently by Hansen and Bartell.<sup>14</sup>

(c) The P-F distance of  $1.535 \text{ \AA}$ , which was presented by Williams, *et al.*,<sup>7</sup> as derived from the rotational constant  $B_0$  by assuming the bond angle of  $100^{\circ}$  and which has frequently been referred to,<sup>34</sup> is in fact incompatible with the rotational constant, as first pointed out by Mirri.<sup>4</sup> This value was compared by Hansen and Bartell<sup>14</sup> with the axial and equatorial P-F distances in  $\text{PF}_5$ , where the latter bond ( $1.534 \text{ \AA}$ ) was thought to be "surprisingly close to the P-F bond in  $\text{PF}_3$ ." It turns out, however, that a more correct P-F bond distance in  $\text{PF}_3$  ( $1.570 \text{ \AA}$ ) is apparently much closer to the *axial* P-F distance ( $1.577 \text{ \AA}$ ). The P-F bond of  $\text{PF}_3\text{BH}_3$  measured by Kuczkowski and Lide<sup>35</sup> is shorter than that of  $\text{PF}_3$  by about  $0.03 \text{ \AA}$ , while the P-F bond in  $\text{HPF}_2$ <sup>36</sup> is longer by  $0.01 \text{ \AA}$ . The latter increase has been discussed by Kuczkowski,<sup>36</sup> although he cited Hersh's value for the P-F bond in  $\text{PF}_3$ .

The above differences in the P-F bond distances for related molecules (Figure 3) may be understood systematically in terms of the structural characteristics of  $\text{PF}_5$ ,  $\text{CH}_3\text{PF}_4$ , and  $(\text{CH}_3)_2\text{PF}_3$ , as discussed by Bartell and Hansen<sup>15</sup> and by Gillespie.<sup>12,37</sup> The P-F bond distance in  $\text{PF}_3\text{BH}_3$  should be shorter than that in  $\text{PF}_3$  as a result of the diminution of the lone-pair repulsion by  $\text{BH}_3$  coordination, which should cause an

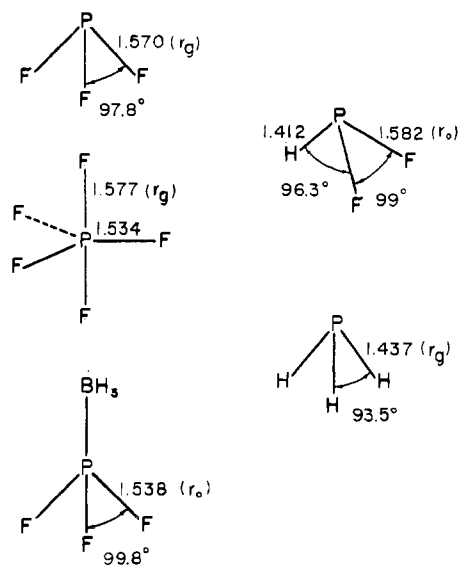


Figure 3.—Comparison of the structures of phosphorus-fluorine compounds. All bond lengths are in  $\text{\AA}$ .

increase in the FPF angle at the same time. A similar shortening has been observed for the equatorial P-F bond in  $\text{PF}_5$ , where the unshared pair in  $\text{PF}_3$  is replaced by two axial P-F bonds. As for  $\text{HPF}_2$ , substitution of a fluorine atom in  $\text{PF}_3$  by hydrogen should increase the remaining P-F bonds, since the repulsion of the P-H bonding electron pair is larger than that of the P-F pair because of the lower electronegativity of hydrogen in comparison with that of fluorine. A similar relation holds for the P-H bond distances of  $\text{PH}_3$ <sup>38</sup> and  $\text{HPF}_2$ . Table III lists the bond angles in group V trihalides, which increase from fluorides to iodides and decrease from nitrogen to antimony compounds.<sup>39-51</sup> These systematic changes in bond angles have been accounted for by Gillespie<sup>11-13</sup> on the basis of his valence-shell electron-pair repulsion theory. In his table, however, the angles of  $104$  and  $102^{\circ}$  for  $\text{PF}_3$  and  $\text{AsF}_3$ , respectively, were cited, and, hence, it seemed as if phosphorus and arsenic trifluorides had shown anomalously large angles. In order to explain this behavior, Gillespie invoked a subrule (postulate 5 in ref 11) assuming a

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TABLE III  
BOND ANGLES IN GROUP V TRIHALIDES<sup>a</sup>

Halide	N		P		As		Sb	
	Angle, deg	Method	Angle, deg	Method	Angle, deg	Method	Angle, deg	Method
F	102.17 ± 0.04	MW <sup>39</sup>	97.8 ± 0.2	ED <sup>b</sup>	96.1 ± 0.2	ED <sup>40</sup>	(88)	XD <sup>42</sup>
Cl	...		100.27 ± 0.09	ED <sup>43</sup>	95.8 ± 0.7	ED <sup>41</sup>	99.5 ± 1.5	MW <sup>6</sup>
			100.1	MW <sup>44</sup>	98.7 ± 0.3	ED <sup>46</sup>		
Br	...		(101.5)	ED <sup>46</sup>	98.4	MW <sup>44</sup>	(97)	ED <sup>48, 49</sup>
					99.66 ± 0.26	ED <sup>47</sup>		
I	...		(102)	ED <sup>49</sup>	100.2 ± 0.4	ED <sup>50</sup>	99.1 ± 2	ED <sup>51</sup>

<sup>a</sup>Abbreviations: ED, electron diffraction; MW, microwave spectroscopy; XD, X-ray diffraction (crystal). <sup>b</sup>Present study.

considerable contribution of double-bond character for the fluorides; according to his argument,<sup>12</sup> the above anomaly may be attributed to "the unshared pairs of fluorine having a strong tendency to delocalize into the incomplete shell of the central atom, thereby giving the bonds some double-bond character and, therefore,

increasing the size of the bonding orbitals and hence the bond angle." From the present result for PF<sub>3</sub>, along with the recent results for AsF<sub>3</sub> by Bartell and Clip-pard<sup>40</sup> and by Konaka and Kimura,<sup>41</sup> their bond angles fit in regular series, so that the rules governing the bond angles in group V trihalides can be simplified.

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## The Characterization of Metal-Oxygen Bridge Systems<sup>1</sup>

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The vibrational spectra of various types of metal-oxygen bridge systems are assigned by normal-coordinate analysis and discussed in terms of geometry. The results of this analysis are shown to be a powerful tool for the characterization of metal-oxygen bridged complexes. The synthesis of a new dioxo-bridged molybdenum(V) complex is described and a structure is proposed on the basis of its infrared spectrum.

### Introduction

In the course of our work on molybdenum(V) chemistry we have frequently been faced with the problem of distinguishing between the several types of oxygen-bridged dimers that occur in this system.<sup>2-4</sup> Infrared spectral measurements were thought to be the solution to this problem.

However, the infrared characteristics of metal-to-oxygen multiply bonded systems have been discussed in detail only for those compounds in which the oxo ligand is in a terminal position.<sup>5-7</sup> An abbreviated analysis of monooxo bridged systems, both linear and bent, was discussed by Cotton and Wing,<sup>8</sup> and Hewkin and Griffith<sup>9</sup> have tabulated a considerable amount of

infrared and Raman data for compounds containing a single oxo bridge.

It is the purpose of this paper to present a general analysis of the mono- and dioxo-bridged systems and to illustrate how infrared spectra in the bridge metal-oxygen region (*ca.* 850–200 cm<sup>-1</sup>) can be used to predict structures. Of prime importance in a consideration of these bridge systems is the fact that the vibrational frequencies are strongly sensitive to the M–O–M bond angle. It is in fact this angular dependence which permits one to distinguish between mono- and dioxo-bridged systems.

### Normal-Coordinate Analyses and Angular Dependence of Frequencies

The general monooxo-bridged metal dimer, treated for simplicity as a three-body system, is bent at an angle  $\phi$  and exhibits two bridge vibrations. Such a system can be characterized by a two-constant potential field. The first constant pertains to the metal-oxygen

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