

### Even the Fifth Ionization Potentials of the Lanthanides follow the "Inclined W" Theory

SHYAMA P. SINHA

*Eidgenössische Technische Hochschule, Laboratorium für Biochemie, Universitätstrasse 16, CH-8006 Zürich, Switzerland*

Received January 25, 1977

Recently Sugar [1] has derived the fifth ionization potentials ( $IP_5$ ) for the lanthanide series. These data along with the previously published [2] third ( $IP_3$ ) and fourth ( $IP_4$ ) ionization potentials and the experimentally determined [3] first ( $IP_1$ ) and second ( $IP_2$ ) ionization potentials provide interesting sets of properties for the lanthanide series to test the validity of the "Inclined W" theory [4].

In 1975 I have proposed [4] plotting the properties ( $P_i$ ) of the f-ions vs. the free ion orbital angular quantum numbers ( $L$ ) at the ground state. Such plots show linear variation of  $P_i$  within each of the four tetrads, often exhibiting the profile of an inclined W. Recently, a wide variety of properties for the lanthanides and the actinides in different oxidation states have been examined [5] confirming the general validity of the "Inclined W" theory ( $P_i = w_i L + k_i$ , where  $w_i$  is the slope and  $k_i$  is the intercept of the least square straight line for a given tetrad ( $i$ ), having  $i = 1-4$ ). In Ref. 5, I have examined among others, the  $L$ (originating ion) dependence plots of  $IP_1$ ,  $IP_2$  and  $IP_3$  for the lanthanides as calculated and

quoted by Faktor and Hanks [6] and the validity of linearization within each of the four tetrads was proved. Here, I wish to show that the data of Sugar and his coworkers [1, 2] on  $IP_3$ ,  $IP_4$  and  $IP_5$  for the lanthanide series vary linearly within each tetrad and follow the Inclined W theory extremely well.

The plots of  $IP_3$ ,  $IP_4$  and  $IP_5$  vs. the free ion ground state  $L$  quantum numbers are shown in Fig. 1 (a-c). The straight lines within each tetrad are drawn as least square lines having the following values of the parameters.

For  $IP_3$ : First tetrad (La-Pr)  $w_1 = 0.5491$ ,  $k_1 = 17.9535$ ; Second tetrad (Nd-Eu)  $w_2 = -0.4445$ ,  $k_2 = 24.7034$ ; Third tetrad (Gd-Dy)  $w_3 = 0.5138$ ,  $k_3 = 19.55$ ; Fourth tetrad (Ho-Yb)  $w_4 = -0.3921$ ,  $k_4 = 24.945$ .

For  $IP_4$ : First tetrad (La-Nd)  $w_1 = 1.2021$ ,  $k_1 = 33.106$ ; Second tetrad (Pm-Gd)  $w_2 = -0.5038$ ,  $k_2 = 44.0434$ ; Third tetrad (Tb-Ho)  $w_3 = 0.8886$ ,  $k_3 = 37.10$ ; Fourth tetrad (Er-Lu)  $w_4 = -0.4464$ ,  $k_4 = 45.13$ .

For  $IP_5$ : First tetrad (Pr-Pm)  $w_1 = 1.365$ ,  $k_1 = 53.37$ ; Second tetrad (Sm-Tb)  $w_2 = -0.6426$ ,  $k_2 = 66.527$ ; Third tetrad (Dy-Er)  $w_3 = 0.995$ ,  $k_3 = 59.06$ ; Fourth tetrad (Tm-Lu)  $w_4 = -0.4779$ ,  $k_4 = 68.16$ .

The inclined W parameters for the experimental data [3] are as follows. For  $IP_1$ : First tetrad (La-Pr)  $w_1 = -0.0393$ ,  $k_1 = 5.646$ ; Second tetrad (Nd-Eu)  $w_2 = -0.0291$ ,  $k_2 = 5.6867$ ; Third tetrad (Gd-Dy)  $w_3 = -0.06$ ,  $k_3 = 6.23$ ; Fourth tetrad (Ho-Yb)  $w_4 = -0.0371$ ,  $k_4 = 6.2683$ .

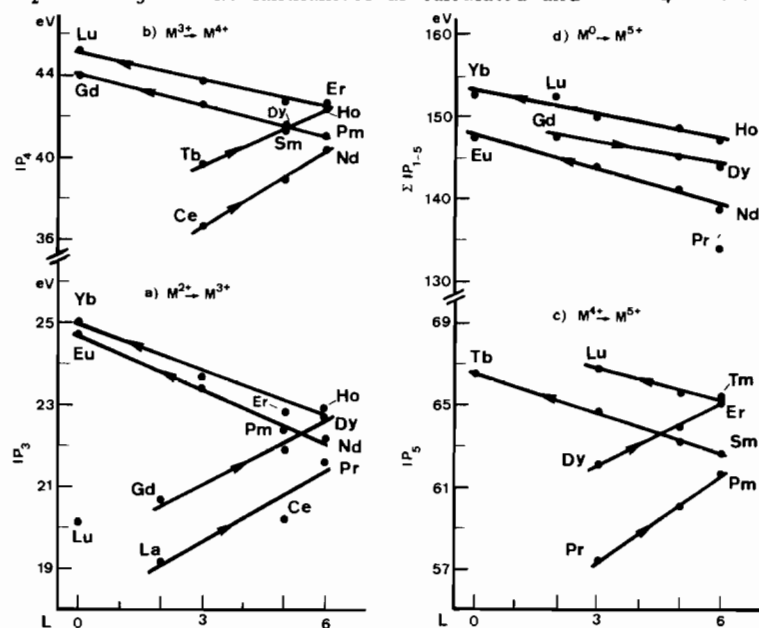
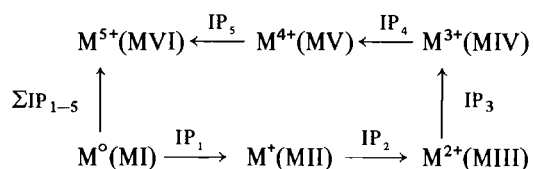


Fig. 1. Plots of the ionization potentials against the orbital angular quantum numbers ( $L$ ) of the originating lanthanide ions; (a) third ionization potentials [2] ( $IP_3$ ) vs.  $L$  of  $M^{2+}$  ions, (b) fourth ionization potentials [2] ( $IP_4$ ) vs.  $L$  of  $M^{3+}$  ions, (c) fifth ionization potentials [1] ( $IP_5$ ) vs.  $L$  of  $M^{4+}$  ions, and (d) sum of the five ionization potentials [1-3] ( $\sum IP_{1-5}$ ) vs.  $L$  of the neutral lanthanide atoms [3].

For  $IP_2$ : First tetrad (La-Pr)  $w_1 = -0.1607$ ,  $k_1 = 11.57$ ; Second tetrad (Nd-Eu)  $w_2 = -0.0838$ ,  $k_2 = 11.2783$ ; Third tetrad (Gd-Dy)  $w_3 = -0.1273$ ,  $k_3 = 12.315$ ; Fourth tetrad (Ho-Yb)  $w_4 = -0.05833$ ,  $k_4 = 12.1917$ .

The average deviations from the least square line are never higher than 0.1 eV, except for the first tetrad of  $IP_3$ , where it is around 0.3 eV.

We have earlier shown [5] that the sum of the ionization potentials (e.g.  $\Sigma IP_{1-3}$ ) could be plotted against the L-values of the neutral lanthanides ( $M^0(MI)$ ). This also results in an inclined W plot. Here, I have plotted the sum of all five ionization potentials ( $\Sigma IP_{1-5}$ ) for the process  $M^0 \rightarrow M^{5+}$ , against the L quantum numbers of the neutral atoms (Fig. 1d) and I have observed the linearity within



the second through fourth tetrad. In this case, only one point (i.e. Pr) is available for the first tetrad. The least square inclined W parameters are as fol-

lows. For  $IP_{1-5}$ : Second tetrad (Nd-Eu)  $w_2 = -1.3860$ ,  $k_2 = 147.8434$ ; Third tetrad (Gd-Dy)  $w_3 = -0.8738$ ,  $k_3 = 149.49$ ; Fourth tetrad (Ho-Yb)  $w_4 = -0.9174$ ,  $k_4 = 152.8067$ .

We are at present examining the plots of the system difference [7] (SD) energies vs. the L quantum numbers of the originating lanthanide ions, in an attempt to systematize the inclined W concept. The main advantage of this concept is the linearization within each of the four tetrads, which enables us to predict the property of a missing member with greater accuracy than that is usually possible in a non-linear plot of a given property vs. the atomic numbers of the lanthanides or the actinides.

## References

- 1 J. Sugar, *J. Opt. Soc. Am.*, **65**, 1366 (1975).
- 2 J. Sugar and J. Reader, *J. Chem. Phys.*, **59**, 2083 (1973).
- 3 C. E. Moore, "Ionization Potentials and Ionization Limits Derived from the Analyses of Optical Spectra", *Natl. Bur. Std. (U.S.) Circ. NSRDS-NBS 34*, Sept. 1970.
- 4 S. P. Sinha, *Helv. Chim. Acta*, **58**, 1978 (1975).
- 5 S. P. Sinha, "Struct. Bonding", Springer-Verlag, Berlin, Heidelberg, New York (1976), vol. 30, pp. 1-64.
- 6 M. M. Faktor and R. Hanks, *J. Inorg. Nucl. Chem.*, **31**, 1649 (1969).
- 7 W. C. Martin, *J. Opt. Soc. Am.*, **61**, 1682 (1971).