

The Structure of Catena- μ -ethylenediaminecadmium(II) Tetra-
cyanoniccolate(II) Dibenzene Clathrate: $\text{Cd}(\text{en})\text{Ni}(\text{CN})_4 \cdot 2\text{C}_6\text{H}_6^a$ T. Miyoshi,^b T. Iwamoto,^c and Y. Sasaki

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The crystal structure of $\text{Cd}(\text{en})\text{Ni}(\text{CN})_4 \cdot 2\text{C}_6\text{H}_6$ was determined by the single crystal X-ray diffraction method. The crystal belongs to the tetragonal system with space group of $P4/m$, $a = 7.675 \pm 0.003$ Å, $c = 8.056 \pm 0.010$ Å, and $Z = 1$ ($D_m = 1.69$, $D_c = 1.72$). The structure was solved by the Fourier method and refined by the block-diagonal least-squares method to an R-value of 0.089 for 619 reflection data. The cadmium atoms and the nickel atoms are linked cross-wise with the cyanide anions on the (001) plane to form the layers of the polymeric metal cyanide complex $[\text{CdNi}(\text{CN})_4]_\infty$, and the layers are stacked along the c-axis. Each ethylenediamine molecule bridges between two cadmium atoms in the adjacent layers to make a three-dimensional host lattice. The benzene molecules are enclathrated in the cavities formed by the host lattice. The electron density for each nitrogen atom of the ethylenediamine molecule was found to be distributed over a torus about the Cd–Cd axis. This fact and the ¹H–NMR data support the rotation of the ethylenediamine molecule about the axis at room temperature.

Introduction

In this laboratory, new benzene clathrates with the chemical formula of $\text{Cd}(\text{en})\text{M}'(\text{CN})_4 \cdot 2\text{C}_6\text{H}_6$ ($\text{M}' = \text{Ni}$ or Pd , en = ethylenediamine) have been prepared.¹ The infrared and the powder X-ray diffraction data have suggested that the ethylenediamine molecules in these compounds bridge between two cadmium atoms. Although ethylenediamine is known as a typical chelating ligand, its bridging behavior has also been reported in several coordination compounds. In most of them, the bridge structure was proposed from the infrared spectrum for which the selection rule suggested the trans conformation of en molecule about the C–C bond.²⁻⁹ Recently, Iwamoto and Shriver^{9a} have

demonstrated the mutual exclusion of the Raman and infrared spectral bands for the en molecules in several $\text{M}(\text{en})\text{X}_2$ -type complexes. However, the structure of the bridging en has been determined, so far by the single crystal X-ray diffraction method, in only four compounds: $[\text{Pt}(\text{CH}_3)_3\text{en}]_2\text{enI}_2$,¹⁰ $[\text{Pt}(\text{CH}_3)_3\text{acac}]_2\text{en}$,¹¹ $[\text{Li}(\text{en})]\text{enX}$ ($\text{X} = \text{Cl}$, Br),¹² in which the bridging en molecules always hold the trans form. The powder X-ray diffraction pattern of $\text{Hg}(\text{en})\text{Cl}_2$ also suggested an infinite bridge structure of $-(\text{Hg}-\text{NH}_2\text{CH}_2\text{CH}_2\text{NH}_2)-$.² In order to clarify the stereochemistry of the bridging en, more metal complexes must be studied by X-ray diffractometry.

The present paper deals with the single crystal structure analysis of $\text{Cd}(\text{en})\text{Ni}(\text{CN})_4 \cdot 2\text{C}_6\text{H}_6$. The preliminary results have been reported previously.¹³ The ¹H–NMR of the deuteriobenzene clathrate, $\text{Cd}(\text{en})\text{Ni}(\text{CN})_4 \cdot 2\text{C}_6\text{D}_6$, was also examined with regard to the motion of the en molecule in the crystal, because the possibility of its rotation was suggested from the diffraction data.

Experimental Section

a) *X-ray Structure Analysis.* The single crystals of $\text{Cd}(\text{en})\text{Ni}(\text{CN})_4 \cdot 2\text{C}_6\text{H}_6$ were prepared by leaving an aqueous solution of the mixture of CdCl_2 , en and $\text{K}_2\text{Ni}(\text{CN})_4$ in 1:3:1 ratio in contact with a layer of benzene for a few days. The crystals thus obtained were pale yellow and grew in prismatic form along the [001] axis.

The precession photographs of the crystal, $0.3 \times 0.3 \times 0.6$ mm, mounted in a soft glass capillary for preventing the escape of benzene, were taken with Zr-filtered Mo $K\alpha$ radiation. The reflection data were recorded about [110] and [100] axis up to the sixth and the second layer, respectively. The Laue group was found to be 4/m. The intensity of 619 independent reflections was measured with a flying-spot microdensitometer, Joyce and Loebel Co. Visual

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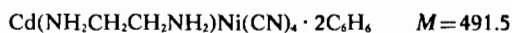
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tetragonal

$$a=7.675 \pm 0.003 \text{ \AA}, \quad c=8.056 \pm 0.010 \text{ \AA}$$

space group $P4/m - C_{4h}^1$

$$Z=1$$

$$D_c=1.72, \quad D_m=1.69$$

b) *NMR Studies.* The $^1\text{H-NMR}$ spectra of the polycrystalline samples were recorded with a JEOL 30W spectrometer and a Varian Associate VF-16 spectrometer. The temperature of the sample was varied from room temperature to -120°C .

Structure Refinement. Since the unit cell contains only one unit of $\text{Cd}(\text{en})\text{Ni}(\text{CN})_4 \cdot 2\text{C}_6\text{H}_6$, the center of the en molecule must lie on the fourfold axis in order to satisfy the crystal symmetry. A certain amount of randomness must, therefore, be assumed. The positions of all the atoms except the hydrogen atoms were determined by three-dimensional Fourier syntheses, assuming that the cadmium atom is at 0,0,0 and that the nickel atom is at $\frac{1}{2}, \frac{1}{2}, 0$ as in the case of $\text{Cd}(\text{NH}_3)_2\text{Ni}(\text{CN})_4 \cdot 2\text{C}_6\text{H}_6$.¹⁴ The atomic parameters obtained gave a minus sign to only one structure factor, $F(2\bar{1}1)$, since the heaviest atom, cadmium, is situated at the point of origin. Some sections of the Fourier maps, calculated with the use of this sign, are presented in Figure 1. As Figure 1 shows, the electron density for the nitrogen atom of the en molecule is distributed uniformly over a torus about the Cd–Cd axis (fourfold axis), while that for the carbon atom exists on the axis with the shape of a distorted oblate-spheroid. This fact suggests that the en molecule is rotating about the Cd–Cd axis, or that each en molecule is distributed in random orientations about the axis in the crystal. As will be described later, the NMR data support the rotation of the en molecule. The en molecule has three conformational isomers, *trans*, *cis* and *gauche*, depending on the change in the torsional angle about the central C–C bond. In the present compound, however, the conformation of the en can not be determined by X-ray diffraction method,

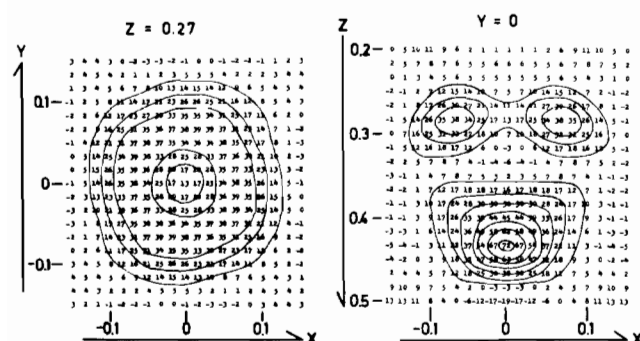


Figure 1. The Three-dimensional Fourier Maps (in an arbitrary scale). The section at $y = 0$ along the (010) plane and at $z = 0.27$ along the (001) plane, showing the electron densities for the nitrogen atom and the carbon atom of the ethylenediamine molecule.

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because any conformation gives the same features upon rotation.

The atomic parameters were refined by least-squares methods, using the block-diagonal approximation, to an R value of 0.089. The calculated and the observed structure factors are listed in Table I. In calculating the structure factors of the nitrogen atom of the en, by assuming the rotational motion of the nitrogen atom about the [001] axis the following equation was used:¹⁵

$$F = f \cdot \exp[-B_{11}(h^2 + k^2) - B_{33}l^2] \cdot J_0(2\pi \frac{r}{a} \sqrt{h^2 + k^2}) \cdot \exp(2\pi i \frac{z}{c})$$

where J_0 is the Bessel function of the zeroth order and where r is the radius of the circular electron density for the nitrogen atom. The carbon atoms of the en were assumed to be fixed on the [001] axis. The atomic parameters thus obtained by the least-squares refinement gave rise to the unusual bond distances and angles in the en molecule as follows: C–N = 1.33 Å, C–C = 1.38 Å, Cd–N–C = 136° , and N–C–C = 152° . As may be seen in Figure 1, the electron density for the carbon atom of the en has a considerably distorted shape, showing the motion of the en more complicated than that assumed. These chemically-unacceptable values appear to be caused from the assumption that the carbon atoms are fixed on the axis.* Therefore, the atomic parameters given in Table II can be referred approximately with regard to those values for the carbon atom C(2) of the en.

All the calculations were performed by the use of the Hitac 5020E computer in the computation center of the University of Tokyo. The LP corrections were carried out with the ACACA program, while the Fourier syntheses, the least-squares refinement, and the calculations of the bond lengths and angles were done with programs in UNICS.¹⁶ The atomic scattering factors used were those listed in International Tables for X-ray Crystallography.¹⁷ The $\sum w(|F_o| - |F_c|)^2$ function was minimized in the least-squares calculations, and the weight of the reflections was set 1 for $|F_o| > 8.6$, and 0.5 for $|F_o| \leq 8.6$ because of the low reliabilities of photometer-readings for the weak reflections. The least-squares refinements with the space groups of $P4$ and $P\bar{4}$ were also examined respectively, but the standard deviations of the atomic parameters became significantly larger. Therefore, it is unnecessary to consider the possibility of $P4$ or $P\bar{4}$.

Results and Discussion

a) *Description and Discussion of the Structure.* The structure obtained is shown in Figs. 2 and 3, while

* The calculations of the least-squares refinement with another assumption that the both carbon and nitrogen atoms of the en move around the axis, gave, however, large standard deviations of the atomic parameters and did never converge into the model in which the electron density for the carbon atom is also distributed on a torus.

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Table II. Atomic Coordinates of the Asymmetric Unit ($\times 10^4$). (The numbers in parentheses are standard deviations in the last significant figures).

Atom	Wychoff's notation	x/a	y/b	z/c
Cd	a	0000(0)	0000(0)	0000(0)
Ni	c	5000(0)	5000(0)	0000(0)
C(1)	j	3306(26)	3263(27)	0000(0)
N(1)	j	2209(23)	2200(23)	0000(0)
C(2)	g	0000(0)	0000(0)	4145(39)
N(2)				2693(52)
C(3)	i	5000(0)	0000(0)	3188(33)
C(4)	l	4865(29)	1583(26)	4129(23)

* r is the radius of the torus of the electron density for the nitrogen atom of the en molecule.

Table III. Anisotropic Thermal Parameters ($\times 10^4$). (The thermal parameters are of the form: $T = \exp\{-(B_{11}h^2 + B_{22}k^2 + B_{33}l^2 + 2B_{12}hk + 2B_{13}hl + 2B_{23}kl)\}$).

Atom	B_{11}	B_{22}	B_{33}	B_{12}	B_{13}	B_{23}
Cd	59(3)	59(3)	60(3)	000(0)	000(0)	000(0)
Ni	43(6)	43(6)	89(8)	000(0)	000(0)	000(0)
C(1)	72(29)	87(31)	144(33)	-24(48)	000(0)	000(0)
N(1)	92(32)	104(34)	134(28)	16(45)	000(0)	000(0)
C(2)	315(104)	315(104)	52(47)	000(0)	000(0)	000(0)
N(2)	124(123)	124(123)	80(60)	000(0)	000(0)	000(0)
C(3)	343(84)	86(43)	158(41)	-13(95)	000(0)	000(0)
C(4)	161(39)	271(52)	181(34)	-5(69)	8(62)	0(69)

The numbers in parentheses are estimated standard deviations

Table IV. Interatomic Distances and Bond Angles with Their Estimate Standard Deviations (in Parentheses). (Those distances longer than 4.0 Å are not presented).

Cd-N(1)	2.39(2) Å	N(2)-N(1) ^a	2.80(4) Å
Cd-N(2)	2.26(4)	C(3)-C(1)	3.85(2)
Ni-C(1)	1.86(2)	C(3)-N(1)	3.75(2)
C(1)-N(1)	1.17(3)	C(3)-C(2)	3.91(1)
C(2)-N(2)	1.33(5) ^b	C(3)-N(2) ^a	3.23(4)
C(2)-C(2')	1.38(6) ^b	C(4)-C(1)	3.79(2)
C(3)-C(4)	1.44(2)	C(4)-C(1')	3.83(2)
C(4)-C(4')	1.40(4)	C(4)-N(1)	3.93(2)
		C(4)-C(2)	3.93(2)
N(2)-Cd-C(2)	16(1) ^o	C(4)-N(2) ^a	3.49(5)
Cd-N(2)-C(2)	136(3) ^b	C(4)-C(4')	3.71(4)
N(2)-C(2)-C(2')	152(2) ^b	C(4')-N(2) ^a	3.68(5)
Ni-C(1)-N(1)	178(2)		
Cd-N(1)-C(1)	179(2)		
C(3)-C(4)-C(4')	122(2)		

^a The shortest distance attainable by the rotation of ethylenediamine molecule. ^b No great faith can be placed in these parameters. See text for further discussion.

the final coordinates of the asymmetric unit and the anisotropic thermal parameters are listed in Tables II and III respectively. The bond lengths and the bond angles are given in Table IV. As may be seen in Figs. 2 and 3, the cadmium atoms and the nickel atoms are at 0,0,0 and $\frac{1}{2}, \frac{1}{2}, 0$ respectively, and they are bridged together with the cyanide anions on the (001) plane to make a square-planar network. Moreover, the en molecules are along the [001] axis. Each of the en molecules links between two cadmium atoms in the neighboring networks, thus forming a three-dimensional host lattice of the polymeric metal complex structure. The guest benzene molecules are trapped in the cavities formed by the host lattice with their ring planes vertical to the (001) plane. The en molecule is surrounded by four planes

of the benzene molecules, while the ring plane of the benzene molecule is placed between two en molecules in such an orientation as to avoid the steric repulsion from the en molecules. If the en molecule is replaced by two ammonia molecules, this structure is almost the same as that of $\text{Cd}(\text{NH}_3)_2\text{Ni}(\text{CN})_4 \cdot 2\text{C}_6\text{H}_6$ ¹⁴.

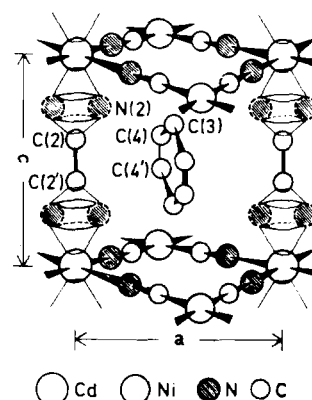


Figure 2. The Illustration of the Structure of $\text{Cd}(\text{en})\text{Ni}(\text{CN})_4 \cdot 2\text{C}_6\text{H}_6$.

The en molecule, with its center situated at 0,0, $\frac{1}{2}$, bridges between two cadmium atoms at 0,0,0 and 0,0,1. The nitrogen atoms of the en molecule are 0.6 Å from the [001] axis, while the carbon atoms lie approximately on the axis. The angle between the axis and the direction of the Cd-N(en) bond is 16°. With regard to the orientation of the en molecule, the previous idea that was shown in Fig. 2 of ref. 1 should be corrected.

Table V. Bond Lengths and Angles in the Ethylenediamine Complexes.

Compound	C—N	C—C'	M—N	M—N—C	N—C—C'	M—M ^a
Present compound	1.33 A ^b	1.38 A ^b	2.26 A	136° ^b	152° ^b	8.06 A
[Li(en)]enCl ¹²	1.48	1.50	2.07	122.2	109.4	6.39
[Li(en)]enBr ¹²	1.47	1.53	2.06	122.1	109.7	6.37
[Pt(CH ₃) ₃ acac] ₂ en ¹¹	1.38	1.70	2.31	111	104	7.68
[Pt(CH ₃) ₃ en] ₂ enI ₂ ¹⁰						7.79
Hg(en)Cl ₂ ²						7.59
[Co(en) ₃]Cl ₃ ·H ₂ O ¹⁹	1.50	1.51	1.98	108.3	105.7	— ^c

^a The interatomic distance between the bridged metal atoms. ^b No great faith can be placed in these parameters. ^c The complex with chelating en molecules.

As the four cyanide anions around the cadmium atom are fixed on the (001) plane, the cadmium atom has the ligand configuration of a considerably distorted octahedron in this compound. Although the bond angles around the six-coordinated metal atoms seldom deviate so greatly from 90°, an angle of 68° has been reported for the N—Cd—O angle Cd(NH₂—NHCO₂)₂·H₂O¹⁸. Ligand arrangements around the d¹⁰ ions may be distorted rather easily from a regular octahedron, since the ligand-field energy does not affect the symmetry of the arrangement in the d¹⁰ complexes.

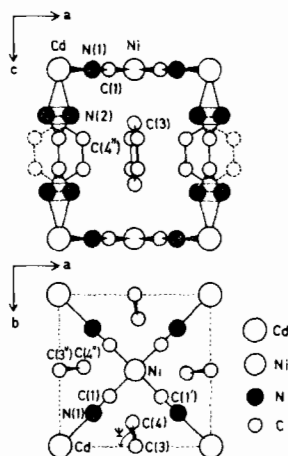


Figure 3. The Projection of the Structure on the (010) and the (001) Planes. The en molecules are not presented in the projection on the (001) plane.

The structures of the bridging en - metal systems in the present compound, in [Pt(CH₃)₃acac]₂en¹¹, and in [Li(en)]enX (X = Cl, Br)¹² are illustrated in Fig. 4, and the structural data concerned are listed in Table V along with that for an en chelate complex (+)-[Co(en)₃]Cl₃·H₂O¹⁹. All the bridging en molecules so far studied are in the trans conformation about the central C—C bond. On the other hand, considering the M—N—C—C set of chemical bonds in the complexes with bridging en molecules, there is another conformational isomerism about the N—C—C bond. As Fig. 4 shows, the present compound, as like the platinum complex, has a trans conformation about the N—C bond, while a cis one is observed in the li-

thium complexes. The difference in the conformation affects the interatomic distance between the bridged metal atoms (the M—M distance in Table V). Indeed, very short M—M distances are reported in the lithium complexes with the cis conformation. That of the present compound, 8.06 Å, is significantly longer than those of the other complexes with the trans conformation. The longer M—M distance can be caused from the smaller angle formed between the line combining the two M atoms and the direction of the C—C bond of the en molecule. In the present compound, the guest benzene molecule rules the lower limit of the Cd—Cd distance, and moreover, the steric repulsion between the guest molecule and the host lattice may make the C—C bond of the en molecule be approximately on the [001] axis. Accordingly, the observed distance, 8.06 Å, is shorter than that, 8.32 Å, in Cd(NH₃)₂Ni(CN)₄·2C₆H₆¹⁴ owing to the en-bridging structure, but is longer than those M—M distances, observed for the other en-bridged metal complexes in Table V.

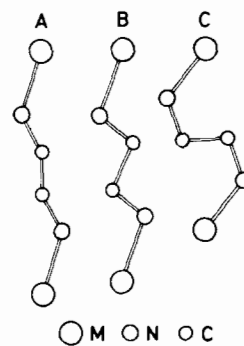


Figure 4. The Structure of the Bridging en Molecules.

- A: Cd(en)Ni(CN)₄·2C₆H₆
 B: [Pt(CH₃)₃acac]₂en
 C: [Li(en)]enCl or [Li(en)]enBr

As Table V shows, the interatomic distances between the benzene molecule and the networks, or those between the benzene molecules, are 3.7 Å or more, except those of C(3)—N(2) (3.23 Å) and C(4)—N(2) (3.49 Å). Since the latter two are the shortest distances at the closest approach of the en to the benzene molecule, even they become longer with the rotation of the en molecule. It can be concluded, therefore, that no direct bonds exist between the guest benzene and its surroundings. The benzene molecule is en-

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clathrated in the three-dimensional host lattice with its sixfold axis parallel to the (001) plane as in the case of the Hofmann-type clathrates.^{14,20} A projection of the structure on the (001) plane is presented in Figure 3, where Ψ is the angle between the ring plane of benzene and the *a*-axis. The orientation of the guest benzene in the (001) plane appears to depend considerably upon the surroundings. The benzene molecule in this clathrate is arranged with the Ψ angle of 85° , which is much larger than that of 59° observed for the corresponding Hofmann-type clathrate $\text{Cd}(\text{NH}_3)_2\text{Ni}(\text{CN})_4 \cdot 2\text{C}_6\text{H}_6$.¹⁴ The increment in the Ψ angle is deduced from the replacement of the ammonia molecules by more bulky en molecule, because the Ψ angle must become larger in order for the electron cloud of the guest benzene to be in contact with that of the en molecule.

Owing to the rotation of en molecule in the crystal at room temperature, the conformation about the C–C' bond of the en could not be determined from the present data. Although the infrared data suggested the trans form,¹ Raman studies are necessary to establish the conformation.

b) *NMR Studies.* The ^1H -NMR spectra and the temperature dependence of the line width for the powder sample of $\text{Cd}(\text{en})\text{Ni}(\text{CN})_4 \cdot 2\text{C}_6\text{D}_6$ are shown in Figure 5. The second moments of the spectra

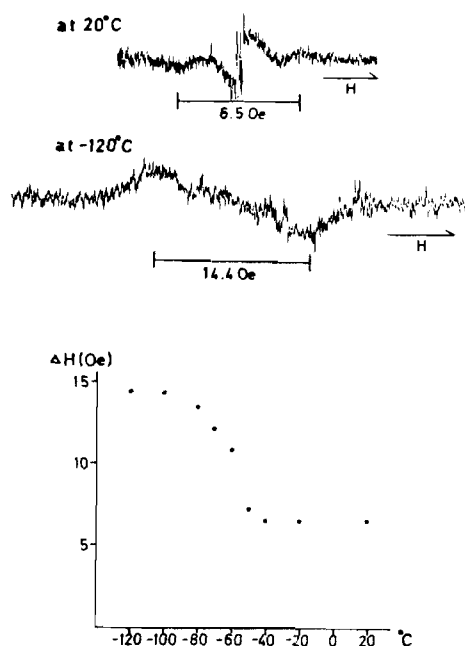


Figure 5. The ^1H -NMR Spectra of $\text{Cd}(\text{en})\text{Ni}(\text{CN})_4 \cdot 2\text{C}_6\text{D}_6$ and the Temperature Dependence of the Line Width of the Spectra.

could not be calculated owing to the weak intensities of the signals. As the temperature increases from -100° to -40°C , the line width of the spectrum decreases drastically with the change in the line shape. This fact supports that the motion of the en molecule begins in this temperature range. The line shape and the line width of the proton signal depend mainly on the magnetic dipole-dipole interactions among the resonant nuclei. The spin system of the present compound is too complicated for the line shape to be analyzed. The line width of 14.4 Oe at -120°C , however, indicates a rigid en molecule, while that of 6.5 Oe at room temperature may support the rotation of en molecule about the Cd–Cd axis. This feature resembles that of 1,2-dichloroethane where the rotation about an axis perpendicular to the H–H line on the CH_2 group narrows the line width to a half of the rigid one.²¹

The en molecule appears to be rotating at room temperature with little hindrance so that the electron density for the nitrogen atom is almost uniformly spread along the torus. The symmetry of the crystal shows a fourfold potential barrier against the rotation of the en molecule. The height of the barrier may be determined by the repulsion from four sets of two nearest-neighboring atoms, *i.e.*, the nitrogen atom of the cyanide anion, N(1), and the carbon atom of the benzene molecule, C(3). When the nitrogen atom of the en is on the (010) plane upon rotation, it is 2.95 Å from the former and 3.23 Å from the latter. These distances become 2.80 Å and 3.45 Å respectively when it is on the (110) plane. Although the repulsive forces from each atom vary considerably with the rotation of the en molecule, their variations may mostly offset each other. Therefore, a nearly-free rotation of en appears to be allowed in the present compound at room temperature. This may be the first observation of the rotating ethylenediamine molecule in the coordination compounds.

Although diffuse scatterings due to the rotation of the en molecule may be expected,^{15,22} the X-ray photographs did not show any features except the thermal diffuse scatterings due to the vibration. It is not known, therefore, whether the en molecules rotate with any correlation with each other or not.

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