the saturation curve near the critical point (29). By successive trials, the value of $t_{c}$ for which ( $\mathrm{d}_{i}-\mathrm{d}_{g}$ ) showed the proper dependence on $\left(t_{c}-t\right)^{1 / 3}$ was determined to be $36.434^{\circ} \mathrm{C}$. With this value of the critical temperature, the critical pressure was calculated from Equation 2 and the critical density was calculated from the rectilinear diameter given by Equation 4. The resulting critical properties of nitrous oxide are:

$$
\begin{aligned}
t_{c} & =36.434^{\circ} \pm 0.005^{\circ} \mathrm{C} . \\
P_{c} & =71.5960 .07 \mathrm{~atm} . \\
\mathrm{d}_{\mathrm{c}} & =0.4525 \pm 0.001 \mathrm{gram} \text { per ml. } .
\end{aligned}
$$

These values are shown in comparison with the critical constants reported by other investigators in Table V.

Latent Heat of Vaporization. The observed latent heat values presented in Table IV were evaluated by use of the Clapeyron equation,

$$
\begin{equation*}
\Delta H_{v}=J T\left(v_{\mathrm{g}}-v_{L}\right)(d P / d T) \tag{6}
\end{equation*}
$$

in conjunction with the smoothed orthobaric densities of Table IV and the vapor pressure relation given by Equation 2. In evaluating the slope of the vapor pressure curve, the residual term, $r_{p}$, was differentiated and smoothed graphically. This residual derivative, $d r_{p} / d T$, contributed a maximum of $1 \%$ to the slope of the vapor pressure curve calculated from Equation 2.

In smoothing the latent heat data, the observed values were fitted to the equation:

$$
\begin{equation*}
\Delta H_{v}=a\left(t_{c}-t\right)^{b}+c\left(t_{c}-t\right)+r_{u} \tag{7}
\end{equation*}
$$

Table V. Comparison of Critical Properties

| Date | $t_{c},{ }^{\circ} \mathrm{C}$. | $P_{c}$, Atm. | $\mathrm{d}_{\mathrm{c}}, \mathrm{G} . / \mathrm{Ml}$. | Investigator |
| :---: | :---: | :---: | :---: | :---: |
| 1956 | 36.434 | 71.596 | 0.4525 | This work |
| 1953 | 36.39 | 71.4 | 0.452 | Cook (10) |
| 1929 |  |  | 0.459 | Quinn and Wernimont (27) |
| 1912 | 36.50 | 71.65 |  | Cardoso and Arni (6) |
| 1895 | 36.0 | 71.9 |  | Kuenen (24) |
| 1894 | 38.8 | 77.5 | 0.454 | Villard (33) |
| 1886 |  |  | 0.41 | Cailletet and Mathias (5) |
| 1884 | 35.4 | 75.0 |  | Dewar (13) |
| 1878 | 36.4 | 73.07 | . . | Janssen (21) |



Figure 5. Orthobaric densities of nitrous oxide
where

$$
\begin{aligned}
& a=12.9922 \\
& c=-0.082167 \\
& b=0.417796 \\
& t_{c}=36.434^{\circ} \mathrm{C}
\end{aligned}
$$

The residuals, $r_{v}$, were smoothed graphically and the smoothed latent heats calculated from Equation 7 are shown in Table IV. These latent heat data are considered to be reliable to $1 \%$ for temperatures below $35^{\circ} \mathrm{C}$.

## CONCLUSIONS

While the accuracy of the experimental $P-V-T$ measurements is discussed above, a realistic estimation of the reliability of the derived quantities is difficult. In some cases, notably the orthobaric densities and latent heat values, the above tabulations contain more significant figures than the probable accuracy warrants. These additional figures have been retained not only as an indication of the internal consistency of the smoothed tabulations, but also with a view to the possible use of these data in subsequent thermodynamic calculations wherein differences and differential coefficients must be evaluated. In using the data as such, the limitations on their reliability should be borne in mind.

## Gas Compressibility Factors at Low Pressures

The pressure range of the gas compressibility factor isotherms is extended to pressures as low as 1 atm . over the temperature range $-30^{\circ}$ to $150^{\circ} \mathrm{C}$. Also given are smoothed values of the second virial coefficient for nitrous oxide, parameters for use with the Lennard-Jones potential function which predicts values of the second virial coeffcient, and fugacity coefficients for gaseous nitrous oxide for pressures up to 315 atm . over the temperature range from $-30^{\circ}$ to $150^{\circ} \mathrm{C}$.

## EXPERIMENTAL

Nitrous Oxide Purity. The nitrous oxide used is described above. It was further purified by cooling to $-70^{\circ} \mathrm{C}$. and then discharging gas from the vapor phase until the original weight was reduced by $10 \%$.

Apparatus. The design, construction, and calibration of the Burnett apparatus used in this investigation are described by Silberberg, Kobe, and McKetta (30). The equipment was modified to extend the lower temperature limit to $-30^{\circ} \mathrm{C}$.

## RESULTS

Compressibility. The compressibility factor is defined as

$$
\begin{equation*}
z=P V / R T \tag{8}
\end{equation*}
$$

The experimental data were treated graphically (30). Large scale plots of $P_{r} N^{r}$ vs. $P_{r}$ were made to determine $P_{o} / z_{o}$, the ordinate at zero pressure. On these plots ordinates could be read to 0.01 to $0.02 \%$ with commensurate precision for the abscissas. The compressibility factor, $z_{r}$, at each pressure, $P_{r}$, was calculated by dividing each $P_{r} N^{r}$ by $P_{0} / z_{0}$.

Compressibility factor isotherms were measured at $15^{\circ} \mathrm{C}$. intervals from $-30^{\circ}$ to $30^{\circ} \mathrm{C}$. for pressures ranging from atmospheric to slightly below the vapor pressure. Between $50^{\circ}$ and $150^{\circ} \mathrm{C}$. the isotherm increment was $25^{\circ} \mathrm{C}$. and pressures up to 65 atm . were measured. However, since the gas compressibility factors at the higher pressures agree so well with Couch's results (11), only the experimental data below 10 atm . are shown in Table VI.

The maximum error, including that from pressure and temperature, in the compressibility factor values of Table

VI is estimated to be $0.20 \%$ at $-30^{\circ}$ and $-15^{\circ} \mathrm{C} ., 0.25 \%$ at $0^{\circ} \mathrm{C} ., 0.30 \%$ at $15^{\circ} \mathrm{C} ., 0.75 \%$ at $30^{\circ} \mathrm{C} ., 0.25 \%$ at $50^{\circ} \mathrm{C}$., and $0.20 \%$ at $75^{\circ}, 100^{\circ}, 125^{\circ}$, and $150^{\circ} \mathrm{C}$.

Second Virial Coefficients. The residual volume, $\alpha$, was defined above as

$$
\begin{equation*}
\alpha=\frac{R T}{P}-V=\frac{R T}{P}(1-z) \tag{1}
\end{equation*}
$$

For each isotherm residual volumes were calculated from the experimental compressibility data by Equation 1 and plotted against pressure. Smoothed curves were drawn through the experimental points and extrapolated to zero pressure, where the intercept is the numerical value of the second virial coefficient with the sign reversed (31).

The experimental residual volume isotherms of nitrous oxide are shown in Figure 6 along with the values computed from Couch's results (11). The experimental second virial coefficients are presented in Table VII and plotted in Figure 7. Smoothed values of the second virial coefficient read from the curve in Figure 7 appear in Table VII. It is estimated that the error in the smoothed second virial coefficients does not exceed 0.025 liter per gram mole at $-30^{\circ} \mathrm{C}$. and decreases to 0.010 liter per gram mole at $150^{\circ} \mathrm{C}$.
Fugacity Coefficients. Lewis (26) defined fugacity as:

$$
\begin{equation*}
R T(d \ln f)=V d P=d G \tag{9}
\end{equation*}
$$

If Equation 9 is combined with Equation 1,

$$
\begin{equation*}
\int_{0}^{P} d \ln \left(\frac{f}{P}\right)=-\frac{1}{R T} \int_{0}^{P} \alpha d P \tag{10}
\end{equation*}
$$

Integrating the left side of Equation 10,

$$
\begin{equation*}
\ln \left(\frac{f}{P}\right)=-\frac{1}{R T} \int_{0}^{P} \alpha d P+\left.\ln \left(\frac{f}{P}\right)\right|_{P=0} \tag{11}
\end{equation*}
$$

By definition, $f / P=1.0$ at $P=0$. Therefore, the last term of Equation 11 is zero.
The value of $\alpha$ at $P=0$ is not indeterminate, as Equation 11 might indicate. Experiment shows that $\alpha$ approaches a finite value at zero pressure (Figure 6).

The ratio of fugacity to pressure is termed the fugacity coefficient, $v$, Equation 11 may be rewritten as

$$
\begin{equation*}
\nu=\frac{f}{P}=\exp \cdot\left[-\frac{1}{R T} \int_{0}^{P} \alpha d P\right] \tag{12}
\end{equation*}
$$

Fugacity coefficients for nitrous oxide were calculated by Equation 12. The experimental $\alpha$ values of Couch (11) and this work were plotted against pressure with temperature as a parameter. The scale of the plot permitted $\alpha$ to be read to 0.0001 liter per gram mole and the pressure to 0.02 atm . A smoothed curve was drawn through the data for each isotherm and residual volumes were read from the curve at intervals of 1.5 atm . The integration in Equation 12 was performed mathematically by calculating areas under the $\alpha$ vs. $P$ curve at increments of 3 atm. using Simpson's rule.

Values of the fugacity coefficient for gaseous nitrous oxide from $-30^{\circ}$ to $150^{\circ} \mathrm{C}$. are presented in Table VIII and plotted in Figure 8. The maximum error in these values is estimated to be $0.20 \%$.

## DISCUSSION

Low pressure gas compressibility measurements at $0^{\circ} \mathrm{C}$. and 1 atm. were reported by Batuecas (1), Cawood and Patterson (8), and Johnston and Weimer (22). The agreement of their results with those of this work ranges from 0.05 to $0.10 \%$.

Second virial coefficients computed from the low pressure compressibility data of Batuecas (1), Bottomley, Massie,

Table VI. Nitrous Oxide Low Pressure Experimental Compressibility Isotherms

| Pressure, Atm. | $\begin{aligned} & \text { Volume, } \\ & \text { Liters/G. } \\ & \text { Mole } \\ & -30^{\circ} \mathrm{C} \end{aligned}$ | $\begin{gathered} z= \\ P V / R T \end{gathered}$ | Pressure, Atm. | Volume, Liters/G. Mole $30^{\circ} \mathrm{C}$. | $\begin{gathered} z= \\ P V / R T \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 9.9066 | 1.7830 | 0.8853 | 10.3712 | 2.2639 | 0.9440 |
| 7.2631 | 2.5233 | 0.9184 | 7.4627 | 3.2055 | 0.9614 |
| 5.2663 | 3.5700 | 0.9424 | 5.3329 | 4.5358 | 0.9722 |
| 3.7875 | 5.0511 | 0.9591 | 3.7997 | 6.4158 | 0.9802 |
| 2.7088 | 7.1507 | 0.9706 | 2.7013 | 9.0806 | 0.9861 |
| 1.9309 | 10.1163 | 0.9790 | 1.9171 | 12.8535 | 0.9903 |
| 1.3730 | 14.3137 | 0.9851 | 9.1635 | 2.5827 | 0.9512 |
|  |  |  | 6.5720 | 3.6526 | 0.9653 |
| 8.4645 | 2.1310 | 0.9040 | 4.6943 | 5.1716 | 0.9757 |
| 6.1674 | 3.0159 | 0.9321 | 3.3415 | 7.3139 | 0.9828 |
| 4.4496 | 4.2665 | 0.9516 | 2.3736 | 10.3525 | 0.9879 |
| 3.1929 | 6.0387 | 0.9663 | 1.6826 | 14.6558 | 0.9910 |
| 2.2781 | 8.5445 | 0.9756 | 1.1925 | 20.7255 | 0.9938 |
| 1.6218 | 12.0907 | 0.9828 |  |  |  |
| 1.1515 | 17.1071 | 0.9874 | 8.1798 5.8551 | 2.9103 4.1179 | 0.9568 0.9691 |
|  |  |  | 4.1768 | . 8.8243 | 0.9782 |
| 9.5308 | 6.0493 | 0.8903 | 2.9719 | 8.2477 | 0.9850 |
| 6.9747 | 2.6372 | 0.9220 | 2.1082 | 11.6631 | 0.9887 |
|  | $-15^{\circ} \mathrm{C}$. |  | 1.4958 | 16.5087 | 0.9927 |
| 8.3072 | 2.3524 | 0.9228 |  | $50^{\circ} \mathrm{C}$. |  |
| 6.0117 | 3.3298 | 0.9450 | 8.0016 | 3.2029 | 0.9665 |
| 4.3174 | 4.7096 | 0.9603 | 5.7136 | 4.5324 | 0.9766 |
| 3.0877 | 6.6684 | 0.9719 | 4.0644 | 6.4139 | 0.9831 |
| 2.2003 | 9.4325 | 0.9800 | 2.8868 | 9.0761 | 0.9881 |
| 1.5641 | 13.3499 | 0.9858 | 2.0474 | 12.8424 | 0.9916 |
| 1.1094 | 18.8947 | 0.9895 | 9.9677 | 2.5479 | 0.9578 |
| 10.3084 | 1.8566 | 0.9035 | 7.1362 | 3.6054 | 0.9703 |
| 7.5104 | 2.6272 | 0.9315 | 5.0900 | 5.1022 | 0.9794 |
| 5.4196 | 3.7169 | 0.9511 | 3.6187 | 7.2199 | 0.9853 |
| 3.8861 | 5.2597 | 0.9651 | 2.5682 | 10.2167 | 0.9895 |
| 2.7744 | 7.4451 | 0.9750 | 1.8207 | 14.4562 | 0.9926 |
| 1.9754 | 10.5329 | 0.9824 | 8.9511 | 2.8498 | 0.9620 |
| 1.4032 | 14.9050 | 0.9874 | 6.3966 | 4.0327 | 0.9728 |
|  |  |  | 4.5573 | 5.7068 | 0.9808 |
|  | $0^{\circ} \mathrm{C}$. |  | 3.2382 | 8.0750 | 0.9861 |
| 8.2453 | 2.5483 | 0.9376 | 2.2983 | 11.4267 | 0.9904 |
| 5.9366 | 3.6075 | 0.9553 | 1.6289 | 16.1693 | 0.9933 |
| 4.2546 | 5.1048 | 0.9688 |  | $75^{\circ} \mathrm{C}$. |  |
| 3.0348 | 7.2234 | 0.9778 |  | 75.7527 |  |
| 2.1572 | 10.2198 | 0.9836 | 10.0417 | 2.7527 | 0.9676 0.9765 |
| 1.5318 | 14.4596 | 0.9884 | 7.1621 | 3.8951 | 0.9765 |
| 1.0868 | 20.4673 | 0.9922 | 5.0969 | 5.5120 | 0.9834 |
|  |  |  | 3.6203 | 7.7996 | 0.9884 |
| 9.8028 | 2.1157 | 0.9253 | 2.5668 | 11.0376 | 0.9917 |
| 7.0882 | 2.9934 | 0.9468 |  |  |  |
| 5.0916 | 4.2372 | 0.9623 |  | $100^{\circ} \mathrm{C}$. |  |
| 3.6386 | 5.9953 | 0.9732 | 8.6398 | 3.4614 | 0.9767 |
| 2.5932 | 8.4844 | 0.9814 | 6.1473 | 4.8982 | 0.9834 |
| 1.8429 | 12.0034 | 0.9870 | 4.3685 | 6.9313 | 0.9889 |
| 1.3068 | 16.9812 | 0.9904 | $\begin{aligned} & 3.0957 \\ & 2.1934 \end{aligned}$ | $\begin{array}{r} 9.8079 \\ 13.8788 \end{array}$ | $\begin{aligned} & 0.9916 \\ & 0.9942 \end{aligned}$ |
|  | $15^{\circ} \mathrm{C}$. |  | 10.3202 | 2.8871 | 0.9731 |
| 8.2859 | 2.7016 | 0.9467 | 7.3534 | 4.0853 | 0.9811 |
| 5.9522 | 3.8237 | 0.9623 | 5.2246 | 5.7809 | 0.9864 |
| 4.2565 | 5.4079 | 0.9738 | 3.7068 | 8.1810 | 0.9904 |
| 3.0308 | 7.6565 | 0.9812 | 2.6271 | 11.5758 | 0.9932 |
| 2.1535 | 10.8305 | 0.9866 |  |  |  |
| 1.5284 | 15.3251 | 0.9908 |  | $125^{\circ} \mathrm{C}$. |  |
| 1.0841 | 21.6982 | 0.9945 | 7.9811 | 4.0255 | 0.9834 |
|  |  |  | 5.6682 | 5.6964 | 0.9883 |
| 10.2745 | 2.1489 | 0.9341 | 4.0172 | 8.0603 | 0.9911 |
| 7.4117 | 3.0409 | 0.9535 | 2.8473 | 11.4066 | 0.9941 |
| 5.3119 | 4.3046 | 0.9670 | 2.0157 | 16.1399 | 0.9958 |
| 3.7910 | 6.0891 | 0.9766 |  | $150^{\circ} \mathrm{C}$. |  |
| 2.6990 | 8.6173 12 | 0.9838 |  | 4.2106 |  |
| 1.9161 | 12.1931 | 0.9884 | 8.1284 5.7692 | 4.2106 5.9583 | 0.9857 0.9900 |
| 0.9622 | 17.2573 | 0.9914 | 5.7692 4.0878 | 5.9583 8.4320 | 0.9900 0.9927 |
|  | 24.4282 | 0.9938 | 4.0878 2.8967 | 8.4320 11.9317 | 0.9927 0.9954 |
| 9.1777 | 2.4280 | 0.9424 | 2.0520 | 16.8840 | 0.9978 |
| 6.6021 | 3.4365 | 0.9593 | 9.7801 | 3.4928 | 0.9838 |
| 4.7224 | 4.8617 | 0.9710 | 6.9447 | 4.9428 | 0.9886 |
| 3.3669 | 6.8812 | 0.9796 | 4.9243 | 6.9947 | 0.9920 |
| 2.3927 | 9.7320 | 0.9851 | 3.4873 | 9.8971 | 0.9940 |
| 1.6988 | 13.7796 | 0.9898 | 2.4711 | 14.0050 | 0.9967 |
| 1.2047 | 19.4842 | 0.9932 | 1.7492 | 19.8187 | 0.9984 |



Figure 6. Residual volume isotherms of nitrous oxide
and Whytlaw-Gray (3), Cawood and Patterson (8), Johnston and Weimer (22), Leduc and Sacerdote (25), and Rayleigh (28) appear in Figure 7 along with the experimental values of the present work. The ICT value (20) was calculated from Rayleigh's work. Smoothed second


Figure 7. Experimental second virial coefficients of nitrous oxide

Table VII. Second Virial Coefficients of Nitrous Oxide
$-B$, Liter/G. Mole

| Temp., ${ }^{\circ} \mathrm{C}$. | Exptl. | Smoothed | Berthelot ${ }^{\circ}$ | LennardJones ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: |
| -30 | 0.2120 | 0.2132 | 0.2180 | 0.1970 |
| -15 | 0.1869 | 0.1842 | 0.1902 | 0.1760 |
| 0 | 0.1609 | 0.1609 | 0.1675 | 0.1576 |
| 15 | 0.1423 | 0.1423 | 0.1477 | 0.1418 |
| 30 | 0.1278 | 0.1272 | 0.1312 | 0.1276 |
| 50 | 0.1091 | 0.1095 | 0.1134 | 0.1113 |
| 75 | 0.0920 | 0.0920 | 0.0944 | 0.0939 |
| 100 | 0.0794 | 0.0788 | 0.0790 | 0.0791 |
| 125 | 0.0680 | 0.0688 | 0.0650 | 0.0666 |
| 150 | 0.0582 | 0.0582 | 0.0548 | 0.0560 |
| rom Eq aramete | on 13. <br> $e / k=189$ | $b_{0}=0.122$ | er/g. mole. |  |

virial coefficients obtained in this study agree with the work of these other investigators within the estimated experimental accuracy, 0.025 liter per gram mole.

The virial form of the Berthelot equation of state may be used to calculate second virial coefficients. The expression for $B$ derived from the Berthelot equation is

$$
\begin{equation*}
B=\frac{9 R T_{c}}{128 P_{c}}\left[1-\frac{6}{T_{R}^{2}}\right] \tag{13}
\end{equation*}
$$

Couch's critical constants (11) were used in Equation 13 to calculate values of $B$ from $-30^{\circ}$ to $150^{\circ} \mathrm{C}$. (Table VII). The maximum deviation of the calculated second virial coefficients from the smoothed values of this work is 0.007 liter per gram mole.

Another theoretical relation for computing the second virial coefficients of nonpolar gases is the Lennard-Jones " $6-12$ " potential function described by Hirschfelder, Curtiss, and Bird (16). Hirschfelder's suggested parameters (17) for nitrous oxide were used- $e / k=189^{\circ} \mathrm{K}$. and $b_{0}=0.122$ liter per gram mole. The maximum difference between the calculated second virial coefficients (Table VII) and the smoothed values is 0.016 liter per gram mole at $-30^{\circ} \mathrm{C}$., which is within the experimental accuracy of this work.

Other values for the parameters in the Lennard-Jones function, such as $e / k=195^{\circ}, 180^{\circ}$, and $175^{\circ} \mathrm{K}$. and $b_{0}=$ $0.120,0.145$, and 0.149 liter per gram mole, led to calculated second virial coefficients which gave larger deviations from the experimental results than Hirschfelder's values.

For polar gases, the Stockmayer potential function usually gives good predictions of the second virial coefficient. The Stockmayer function depends not only of the reduced temperature but also on the dipole moment of the gas. For nitrous oxide the dipole moment is so small ( 0.14 debye) that the function ( $\left.T^{*} / t^{*}\right) B^{*}(16)$ cannot be evaluated. Consequently, the Stockmayer potential function is not satisfactory for predicting the second virial coefficients of nitrous oxide, a relatively nonpolar gas.

## NOMENCLATURE

[^0]Table VIII. Fugacity Coefficients for Gaseous Nitrous Oxide

|  | Temptrature ${ }^{\circ} \mathrm{C}$. |  |  |  |  | $\begin{gathered} \text { Pressure, } \\ \text { Atm. } \\ 123 \end{gathered}$ | Temperature, ${ }^{\circ} \mathrm{C}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Pressure, Atm. | Fugaci y Coefficient, $v=f / P$ |  |  |  |  |  | Fugacity Coefficient, $v=f / P$ |  |  |  |  |
| 0 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |  | 0.5139 | 0.6323 | 0.7119 | 0.7705 | 0.8162 |
| 3 | 0.9683 | 0.9740 | 0.9784 | 0.9819 | 0.9847 | 126 | 0.5054 | 0.6245 | 0.7058 | 0.7656 | 0.8123 |
| 6 | 0.9372 | 0.9482 | 0.9570 | 0.9639 | 0.9694 | 129 | 0.4972 | 0.6168 | 0.6998 | 0.7608 | 0.8084 |
| 9 | 0.9063 | 0.9226 | 0.9357 | 0.9460 | 0.9542 | 132 | 0.4895 | 0.6092 | 0.6938 | 0.7560 | 0.8045 |
| 12 | 0.8752 | 0.8970 | 0.9144 | 0.9281 | 0.9391 | 135 | 0.4820 | 0.6018 | 0.6870 | 0.7512 | 0.8007 |
| 13.052 | $0.8642^{\text {a }}$ |  |  |  |  | 138 | 0.4749 | 0.5946 | 0.6820 | 0.7465 | 0.7969 |
| 15 |  | 0.8712 | 0.8931 | 0.9102 | 0.9240 | 141 | 0.4680 | 0.5876 | 0.6763 | 0.7419 | 0.7931 |
| 18 |  | 0.8456 | 0.8721 | 0.8924 | 0.9089 | 144 | 0.4615 | 0.5807 | 0.6706 | 0.7373 | 0.7894 |
| 20.559 |  | $0.7864^{\text {a }}$ |  |  |  | 147 | 0.4552 | 0.5740 | 0.6650 | 0.7328 | 0.7857 |
| 21 |  |  | 0.8508 | 0.8746 | 0.8939 | 150 | 0.4492 | 0.5675 | 0.6594 | 0.7283 | 0.7820 |
| 24 |  |  | 0.8295 | 0.8568 | 0.8789 |  |  |  |  |  |  |
| 27 |  |  | 0.8081 | 0.8390 | 0.8639 | 153 | 0.4434 | 0.5612 | 0.6540 | 0.7238 | 0.7784 |
| 30 |  |  | 0.7864 | 0.8212 | 0.8489 | 156 | 0.4378 | 0.5551 | 0.6486 | 0.7195 | 0.7748 |
| 30.786 |  |  | $0.7806^{\text {a }}$ |  |  | 159 | 0.4324 | 0.5491 | 0.6434 | 0.7151 | 0.7712 |
| 33 |  |  |  | 0.8033 | 0.8340 | 162 | 0.4273 | 0.5433 | 0.6382 | 0.7108 | 0.7677 |
| 36 |  |  |  | 0.8033 0.7853 | 0.8340 0.8190 | 165 | 0.4223 | 0.5377 | 0.6331 | 0.7066 0.7024 | 0.7643 |
| 39 |  |  |  | 0.7672 | 0.8041 | 168 171 | 0.4175 0.4128 | 0.5323 0.5270 | 0.6281 0.6233 | 0.7024 0.6983 | 0.7608 0.7574 |
| 42 |  |  |  | 0.7487 | 0.7891 | 174 | 0.4128 0.4084 | 0.5219 | 0.6185 | 0.6943 | 0.7574 0.7541 |
| 44.438 |  |  |  | $0.7334^{\text {a }}$ |  | 174 177 | 0.4084 0.4041 | 0.5219 0.5170 | 0.6185 0.6138 | 0.6943 0.6903 | 0.7541 0.7507 |
| 45 |  |  |  |  | 0.7740 | 180 | 0.3999 | 0.5122 | 0.6092 | 0.6863 | 0.7474 |
| 48 |  |  |  |  | 0.7589 | 180 | 0.399 | 0.512 | 0.6032 | 0.6863 | 0.747 |
| 51 |  |  |  |  | 0.7436 |  |  |  |  |  |  |
| 54 |  |  |  |  | 0.7281 | 183 | 0.3959 | 0.5075 | 0.6047 | 0.6824 | 0.7442 |
| 57 |  |  |  |  | 0.7124 | 186 | 0.3920 | 0.5030 | 0.6003 | 0.6786 | 0.7410 |
| 60 |  |  |  |  | 0.6961 | 189 | 0.3882 | 0.4986 | 0.5960 | 0.6748 | 0.7379 |
| 62.359 |  |  |  |  | $0.6828^{\text {a }}$ | 192 | 0.3846 | 0.4943 | 0.5918 | 0.6712 | 0.7348 |
|  | Temperature, ${ }^{\circ} \mathrm{C}$. |  |  |  |  | 195 | 0.3811 | 0.4902 | 0.5876 | 0.6675 | 0.7317 |
|  | 50 | 75 | 100 | 125 | 150 | 201 | 0.3744 | 0.4823 | 0.5796 | 0.6604 | 0.7256 |
| 0 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 204 | 0.3712 | 0.4785 | 0.5758 | 0.6569 | 0.7227 |
| 3 | 0.9876 | 0.9904 | 0.9923 | 0.9938 | 0.9950 | 207 | 0.3681 | 0.4748 | 0.5720 | 0.6535 | 0.7198 |
| 6 | 0.9754 | 0.9808 | 0.9846 | 0.9876 | 0.9901 | 210 | 0.3651 | 0.4712 | 0.5683 | 0.6502 | 0.7169 |
| 9 | 0.9631 | 0.9712 | 0.9770 | 0.9815 | 0.9852 |  |  |  |  |  |  |
| 12 | 0.9509 | 0.9616 | 0.9694 | 0.9753 | 0.9803 | 213 | 0.3622 | 0.4677 | 0.5647 | 0.6469 | 0.7141 |
| 15 | 0.9387 | 0.9521 | 0.9618 | 0.9693 | 0.9755 | 216 | 0.3594 | 0.4643 | 0.5612 | 0.6437 | 0.7113 |
| 18 | 0.9266 | 0.9426 | 0.9542 | 0.9632 | 0.9706 | 219 | 0.3567 | 0.4610 | 0.5578 | 0.6405 | 0.7085 |
| 21 | 0.9145 | 0.9332 | 0.9467 | 0.9572 | 0.9658 | 222 | 0.3540 | 0.4578 | 0.5544 | 0.6374 | 0.7058 |
| 24 | 0.9024 | 0.9238 | 0.9392 | 0.9512 | 0.9610 | 225 | 0.3515 | 0.4547 | 0.5511 | 0.6343 | 0.7032 |
| 27 | 0.8903 | 0.9144 | 0.9318 | 0.9452 | 0.9563 | 228 | 0.3490 | 0.4517 | 0.5479 | 0.6313 | 0.7005 |
| 30 | 0.8783 | 0.9050 | 0.9243 | 0.9393 | 0.9515 | 231 | 0.3466 | 0.4488 | 0.5448 | 0.6284 | 0.6979 |
| 33 | 0.8663 | 0.8956 | 0.9169 | 0.9334 | 0.9468 | 234 | 0.3442 | 0.4459 | 0.5418 | 0.6255 | 0.6954 |
| 36 | 0.8544 | 0.8863 | 0.9095 | 0.9275 | 0.9421 | 237 | 0.3419 | 0.4431 | 0.5388 | 0.6226 | 0.6929 |
| 39 | 0.8424 | 0.8770 | 0.9022 | 0.9216 | 0.9375 | 240 | 0.3397 | 0.4404 | 0.5358 | 0.6198 | 0.6904 |
| 42 | 0.8305 | 0.8678 | 0.8948 | 0.9158 | 0.9330 |  |  |  |  |  |  |
| 45 | 0.8186 | 0.8585 | 0.8876 | 0.9100 | 0.9284 | 243 | 0.3375 | 0.4378 | 0.5330 | 0.6171 | 0.6880 |
| 48 | 0.8067 | 0.8493 | 0.8803 | 0.9043 | 0.9238 | 246 | 0.3354 | 0.4352 | 0.5302 | 0.6144 | 0.6856 |
| 51 | 0.7948 | 0.8402 | 0.8731 | 0.8985 | 0.9192 | 249 | 0.3333 | 0.4327 | 0.5275 | 0.6118 | 0.6832 |
| 54 | 0.7830 | 0.8310 | 0.8659 | 0.8928 | 0.9146 | 252 | 0.3313 | 0.4302 | 0.5248 | 0.6092 | 0.6809 |
| 57 | 0.7711 | 0.8220 | 0.8588 | 0.8872 | 0.9100 | 255 | 0.3294 | 0.4278 | 0.5223 | 0.6067 | 0.6786 |
| 60 | 0.7592 | 0.8129 | 0.8517 | 0.8815 | 0.9055 | 258 | 0.3275 | 0.4255 | 0.5197 | 0.6042 | 0.6764 |
| 63 | 0.7474 | 0.8039 | 0.8446 | 0.8759 | 0.9010 | 261 | 0.3256 | 0.4233 | 0.5172 | 0.6018 | 0.6742 |
| 66 | 0.7355 | 0.7950 | 0.8376 | 0.8703 | 0.8965 | 264 | 0.3238 | 0.4211 | 0.5148 | 0.5994 | 0.6720 |
| 69 | 0.7235 | 0.7860 | 0.8306 | 0.8648 | 0.8920 | 270 | 0.3221 0.3204 | 0.4189 0.4168 | 0.5125 0.5102 | 0.5971 0.5948 | 0.6699 0.6678 |
| 72 | 0.7115 | 0.7771 | 0.8236 | 0.8592 | 0.8876 | 270 | 0.3204 | 0.4168 | 0.6102 | 0.5048 | 0.6678 |
| 75 | 0.6994 | 0.7683 | 0.8167 | 0.8538 | 0.8832 | 273 | , 0.3187 | 0.4148 | 0.5079 | 0.5926 | 0.6657 |
| 78 | 0.6871 | 0.7594 | 0.8098 | 0.8483 | 0.8788 | 276 | -0.3171 | 0.4128 | 0.5057 | 0.5904 | 0.6637 |
| 81 | 0.6784 | 0.7506 | 0.8030 | 0.8428 | 0.8744 | 279 | 0.3156 | 0.4108 | 0.5035 | 0.5882 | 0.6617 |
| 84 | 0.6622 | 0.7419 | 0.7962 | 0.8374 | 0.8701 | 282 | 0.3140 | 0.4089 | 0.5014 | 0.5861 | 0.6598 |
| 87 | 0.6500 | 0.7332 | 0.7894 | 0.8321 | 0.8658 | 285 | 0.3125 | 0.4071 | 0.4994 | 0.5841 | 0.6578 |
| 90 | 0.6377 | 0.7245 | 0.7827 | 0.8268 | 0.8615 | 288 | 0.3110 | 0.4053 | 0.4974 | 0.5820 | 0.6560 |
| 93 | 0.6245 | 0.7158 | 0.7760 | 0.8214 | 0.8572 | 291 | 0.3096 | 0.4035 | 0.4954 | 0.5801 | 0.6541 |
| 96 | 0.6114 | 0.7072 | 0.7694 | 0.8162 | 0.8530 | 294 | 0.3082 | 0.4018 | 0.4935 | 0.5781 | 0.6523 |
| 99 | 0.5986 | 0.6986 | 0.7628 | 0.8110 | 0.8488 | 297 | 0.3069 | 0.4002 | 0.4916 | 0.5762 | 0.6505 |
| 102 | 0.5862 | 0.6901 | 0.7563 | 0.8058 | 0.8446 | 300 | 0.3056 | 0.3985 | 0.4898 | 0.5744 | 0.6488 |
| 105 | 0.5744 | 0.6816 | 0.7498 | 0.8006 | 0.8405 |  |  |  |  |  |  |
| 108 | 0.5631 | 0.6732 | 0.7434 | 0.7955 | 0.8364 | 303 | 0.3043 | 0.3969 | 0.4880 | 0.5725 | 0.6471 |
| 111 | 0.5523 | 0.6649 | 0.7370 | 0.7904 | 0.8323 | 306 | 0.3030 | 0.3954 | 0.4862 | 0.5708 | 0.6454 |
| 114 | 0.5420 | 0.6566 | 0.7306 | 0.7854 | 0.8282 | 309 | 0.3018 | 0.3938 | 0.4845 | 0.5690 | 0.6437 |
| 117 | 0.5322 | 0.6484 | 0.7243 | 0.7804 | 0.8242 | 312 | 0.3006 | 0.3924 | 0.4829 | 0.5673 | 0.6421 |
| 120 | 0.5228 | 0.6403 | 0.7181 | 0.7754 | 0.8202 | 315 | 0.2995 | 0.3909 | 0.4812 | 0.5656 | 0.6406 |

[^1]

Figure 8. Fugacity coefficients for gaseous nitrous oxide
$\Delta H_{v}=$ latent heat of vaporization, cal./g.
$J=$ mechanical equivalent of heat, $0.0242179 \mathrm{cal} . / \mathrm{ml}$. atm.
$\mathrm{M}=$ molecular weight (44.016 for nitrous oxide)
$N=$ Burnett apparatus constant
$P=$ absolute pressure, atm.
$R=$ gas constant, 0.0820545 liter atm./g. mole ${ }^{\circ} \mathrm{K}$.
$r_{d}=$ density residual, g. $/ \mathrm{ml}$.
$r_{e}=$ density residual, g. $/ \mathrm{ml}$.
$r_{P}=$ logarithmic vapor pressure residual
$r_{v}=$ residual latent heat of vaporization, cal. $/ \mathrm{g}$.
$T=$ absolute temperature, ${ }^{\circ} \mathrm{K}$. (ice point $=273.16^{\circ} \mathrm{K}$.)
$t=$ temperature, ${ }^{\circ} \mathrm{C}$.
$V=$ molal volume, liter/g. mole
$v=$ specific volume, ml. g .
$z=$ compressibility factor, $z=P V / R T$
$\alpha=$ residual volume, liter $/ \mathrm{g}$. mole
$\nu=$ fugacity coefficient, $f / p$

## Subscripts

$c=$ critical state
$g=$ saturated gas phase
$L=$ saturated liquid phase
$0=$ initial state of a run
$r=$ number of the expansion

## Superscript

* = parameter in Stockmayer potential function


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## literature cited

(1) Batuecas, T., J. chim. phys. 28, 572-86 (1931).
(2) Beattie, J.A., Proc. Am. Acad. Arts Sci. 69, 389-405 (1934).
(3) Bottomley, G.A., Massie, D.S., Whytlaw-Gray, R., Proc. Roy. Soc. (London) A200, 201-18 (1950).
(4) Britton, G.T., Trans. Faraday Soc. 25, 520-5 (1929).
(5) Cailletet, L., Mathias, E., Compt. rend. 102, 1202-7 (1886).
(6) Cardoso, E., Arni, E., J. chim. phys. 10, 504-8 (1912).
(7) Carlton-Sutton, T., Ambler, H.R., Williams, G.W., Proc. Phys. Soc. (London) 48, 189-202 (1936).
(8) Cawood, W., Patterson, H.S., J. Chem. Soc. 1933, pp. 619-24.
(9) Cherney, B.J., Marchman, H., York., R., Ind. Eng. Chem. 41, 2653-8 (1949).
(10) Cook, D., Trans. Faraday Soc. 49, 716-23 (1953).
(11) Couch, E.J., "Thermodynamic Properties of Nitrous Oxide," Ph. D. dissertation in chemical engineering, University of Texas, Austin, Tex., 1956.
(12) d'Andréeff, E., Ann. chim. phys. 56, 317-33 (1859).
(13) Dewar, J., Phil. Mag. 18, 210-6 (1884).
(14) Grunmach, L., Ann. Physik. 15, 401-6 (1904).
(15) Hellwig, L.R., "Pressure-Volume-Temperature Properties of Sulfur Dioxide," Ph. D. dissertation in chemical engineering, University of Texas, Austin, Tex., 1955.
(16) Hirschfelder, J.O., Curtiss, C.F., Bird, R.B., "Molecular Theory of Gases," pp. 162-70, Wiley, New York, 1954.
(17) Ibid., p. 1111.
(18) Hirth, L.J., "Gas Compressibility of Nitrous Oxide and of Sulfur Dioxide by the Burnett Method," Ph. D. dissertation in chemical engineering, University of Texas, Austin, Tex., 1958.
(19) Hoge, H.J., J. Research Natl. Bur. Standards 34, 281-93 (1945).
(20) "International Critical Tables," Vol. III, p. 229, McGrawHill, New York, 1928.
(21) Janssen, W.J., Beibl. Ann. Physik. 2, 136-41 (1878).
(22) Johnston, H.L., Weimer, H.R., J. Am. Chem. Soc. 56, 625-30 (1934).
(23) Keyes, F.G., Proc. Am. Acad. Arts Sci. 68, 505 (1933).
(24) Kuenen, J.P., Phil. Mag. 40, 173-94 (1895).
(25) Leduc, A., Sacerdote, P., Compt. rend. 125, 297-9 (1897).
(26) Lewis, G.N., Proc. Am. Acad. Arts Sci. 37, 36-9 (1901).
(27) Quinn, E.L., Wermimont, G., J. Am. Chem. Soc. 51, 2002-8 (1929).
(28) Rayleigh, L., Phil. Trans. 204, 351-72 (1905).
(29) Rice, O.K., J. Chem. Phys. 23, 164-73 (1955).
(30) Silberberg, I.H., Kobe, K.A., McKetta, J.J., J. Chem. Eng. Data 4, 314-23 (1959).
(31) Ibid., pp. 323-9.
(32) Villard, P., Ann. chim. phys. 10 (7), 387-432 (1897).
(33) Villard, P., Compt. rend. 118, 1096-9 (1894).

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[^0]:    $B=$ second virial coefficient
    $b_{0}=$ parameter in Lennard-Jones and Stockmayer potential functions
    $\mathrm{d}=$ density, g./ml.
    $e / k=$ parameter in Lennard-Jones and Stockmayer potential functions
    $f=$ fugacity
    $G=$ molal free energy

[^1]:    ${ }^{a}$ Value at saturation.

