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# Partial Miscibility Phenomena in the Ternary System Ethane-n-Nonadecane-n-Eicosane

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> Pressure, composition, and molar volumes of the two liquid phases which coexist for constant molar ratio mixtures of n-nonadecane and n-eicosane in solution with ethane are presented at representative temperatures along the three phase  $(L_1$ - $L_2$ -V) border curves. The lower critical solution temperature (LCST) points and the type-K singular points for the ternary mixtures represent nearly linear interpolations of the behavior of the ethane-n-nonadecane and ethane-n-eicosane binary systems. Both coexisting liquid phases were sampled at several temperatures and at overall mole fractions of n-eicosane of approximately 0.25, 0.50, and 0.75 on an ethanefree basis. The analysis of these samples indicated that the distribution coefficients of the n-nonadecane and n-eicosane were independent of over-all composition but depended only on the temperature.

 $\mathbf{I}_{\mathrm{N}}$  THE binary system study on partial miscibility of ethane with high molecular weight paraffinic hydrocarbons reported by Kohn (3), *n*-nonadecane was shown to be the lowest molecular weight normal paraffin hydrocarbon which is partially immiscible with ethane. The extension of the partial miscibility work to ternary systems seems necessary if further understanding of the immiscibility phenomenon is to be attained. This paper reports the immiscibility behavior of one ternary system in which the two high molecular weight paraffin hydrocarbons both form partially miscible liquid phases with ethane. Further work will report the immiscibility behavior of a ternary system in which only one of the high molecular weight components is partially immiscible with ethane.

### EXPERIMENTAL

The apparatus, techniques, and experimental materials were identical to those reported previously (1-5). The constant molar ratio mixtures of *n*-nonadecane and *n*-eicosane were prepared from the pure components by weighing techniques. The mixtures were kept in closed bottles. Each sample bottle was heated prior to use so that the entire sample material was in the completely melted condition. The liquid sample was withdrawn from the sample bottle by means of a pipet having a hypodermic needle extension, which permitted the liquid to be introduced into the equilibrium cell through its long capillary neck. The mass added to the cell was determined by accurately weighing the cell on an analytical balance.

During the experimental runs, accurate amounts of pure ethane gas were added to the glass equilibrium cell from a high pressure bomb, through use of a positive displacement mercury pump. As the pressure rose in the thermostated cell and ethane dissolved into the liquid phase, a pressure was reached at which a trace of the second liquid  $(L_2)$ phase appeared on top of the original liquid  $(L_1)$  phase. At this point, the over-all mixture was essentially at the  $(L_1-L_2-V)$  phase border curve. The molar ratio of n-nonadecane to *n*-eicosane in the  $L_1$  phase was thus identical to that originally charged to the equilibrium cell.

In a similar manner during experimental runs in which smaller amounts of the heavy hydrocarbon liquids were charged to the cell, the composition and molar volume of the  $L_2$  phase were determined under conditions at which only trace amounts of  $L_1$  phase were present. The sampling technique and method of analysis were presented in detail by McCaffrey (5). Experimental sampling was accomplished by using a 90-ml. Jerguson gage cell fitted with two sampling ports. The lower sampling port was at the bottom of the equilibrium cell and the second was above the  $L_1$ - $L_2$  interface and below the  $L_2$ -V interface when the three phases were present in the cell. The sampling ports were connected via hypodermic tubing to  $\frac{1}{16}$ -inch needle valves. When these valves were opened very slowly, samples of the liquid phases passed to a small glass receptacle. The ethane was allowed to flash to the atmosphere while the n-nonadecane and n-eicosane were collected as a liquid phase. Samples of approximately 15 to 20 µl. were taken. The samples were analyzed on a Beckman GC-2A gas-liquid chromatograph. The column packing was 20% by weight silicone gum rubber on a firebrick substrate, and the chromatograph was operated at a constant temperature of 250° C.

#### RESULTS

Table I presents smoothed composition, pressure, and molar volume data on the liquid phases for three molar ratios of *n*-nonadecane and *n*-eicosane. The raw experimental data on the liquid phases were reproducible to  $\pm 0.0005$  mole fraction,  $\pm 0.02^{\circ}$  C., and  $\pm 0.05$  atm. The molar volumes of the  $L_2$  liquid phase were reproducible to  $\pm 0.2$  ml. per gram mole while those of the  $L_1$  liquid phase were reproducible to  $\pm 0.06$  ml. per gram mole.

Figure 1 shows the smoothed composition data for the three constant molar ratios of *n*-nonadecane to *n*-eicosane and includes the curves for the two pure components in binary solution with ethane. Figure 1 and Table I show that the partial miscibility temperature range is reduced



in an almost linear fashion by addition of n-nonadecane to n-eicosane.

The results of the sampling work are presented in Table II. The temperature, pressure, mole fraction of *n*-nonadecane in *n*-eicosane charged to the cell, and molar ratio of *n*-nonadecane to *n*-eicosane in each liquid phase were observed experimentally. The difference of the molar ratios of the heavy hydrocarbons in the two liquid phases shows the existence of a small separational effect. A distribution coefficient  $(\beta)$ , which is a measure of this effect, was defined as follows:

$$\beta = R_2/R_1 \tag{1}$$

		$L_1$ Phase		$L_2$ Phase						
Temp., °C.	Press., Atm.	Comp. mole fract. ethane	Mol. vol., ml./g. mole	Comp. mole fract. ethane	Mol. vol., ml./g. mole					
R = 0.333										
34.49° 34.80 35.20 35.60 36.00 36.40	$\begin{array}{c} 49.590 \\ 49.942 \\ 50.400 \\ 50.858 \\ 51.313 \\ 51 \\ 772 \end{array}$	$\begin{array}{c} 0.9718 \\ 0.9554 \\ 0.9489 \\ 0.9448 \\ 0.9413 \\ 0.9385 \end{array}$	93.90 93.38 94.17 94.69 94.80 94.56	0.9718 0.9849 0.9892 0.9917 0.9938 0.9954	$\begin{array}{c} 93.90\\97.07\\99.30\\101.53\\104.30\\108.43\end{array}$					
36.80 37.02*	52.230 52.479	0.9363 0.9354	93.78 92.88	0.9970 0.9977	$115.23 \\ 125.60$					
R = 1.000										
35.19 <sup>a</sup> 35.40 35.80 36.00 36.40 36.80 37.26 <sup>b</sup>	$50.318 \\ 50.554 \\ 51.013 \\ 51.241 \\ 51.701 \\ 52.158 \\ 52.688$	$\begin{array}{c} 0.9722\\ 0.9604\\ 0.9532\\ 0.9507\\ 0.9468\\ 0.9431\\ 0.9396\end{array}$	$\begin{array}{c} 95.10\\ 94.23\\ 94.32\\ 94.41\\ 94.43\\ 94.12\\ 92.50\\ \end{array}$	0.9722 0.9834 0.9888 0.9902 0.9923 0.9944 0.9968	$\begin{array}{c} 95.10\\ 97.80\\ 100.23\\ 101.62\\ 104.84\\ 109.50\\ 123.60\end{array}$					
R = 3.00										
35.89° 36.20 36.40 36.80 37.20 37.47°	51.063 51.418 51.645 52.107 52.563 52.880	$\begin{array}{c} 0.9735 \\ 0.9570 \\ 0.9534 \\ 0.9489 \\ 0.9456 \\ 0.9435 \end{array}$	95.70 94.18 94.10 93.81 92.97 92.07	$\begin{array}{c} 0.9735 \\ 0.9864 \\ 0.9891 \\ 0.9922 \\ 0.9946 \\ 0.9960 \end{array}$	95.70 99.23 100.52 103.60 108.70 119.00					

Table I. Smoothed Values of Pressure, Composition, and Molar Volume of the Two Liquid Phases Coexisting along the Three-Phase (L<sub>1</sub>-L<sub>2</sub>-V) Border Curves

<sup>a</sup>L.C.S.T. point. <sup>b</sup>Type-K singular point.

Table II. The Separational Effect in the Ethane-n-Nonadecane-n-Eicosane System

		Mole Fraction	Molar Ratio of n-Nonadecane to n-Eicosane			
Temp., ° C.	Pressure, Atm.	<i>n</i> -Nonadecane Charged to Cell	Liquid 1 $R_1$	Liquid 2 R <sub>2</sub>	Distribution Coefficient, $\beta$	Reduced Temperature, $T^*$
$35.10 \\ 35.10$	50.19 50.16	0.2718 0.2718	$0.454 \\ 0.455$	0.492	$1.094 \\ 1.068$	0.241 0.241
35.40	50.72	0.2718	0.350	0.378	1.080	0.360
35.40 35.60	50.71	0.2718 0.5082	0.343 0.979	0.380	1.08	0.360
36.10 36.10	51.30 51.32	0.2718 0.2718	0.458	0.507	1.106 1.097	0.636
36.20	51.25	0.7481	3.063	3.226	1.053	0.196
36.20 36.40	51.46 51.86	$0.5082 \\ 0.2718 \\ 0.2718$	0.988 0.388	1.089 0.412 0.280	1.102 1.219 1.124	0.488 0.755 0.755
36.40 36.80 36.80	51.83 51.97 52.10	0.2718 0.7481 0.5082	0.343 3.112 1.006	0.389 3.390 1.130	1.134 1.089 1.123	0.755 0.575 0.777
37.20	52.38	0.7481	3.102	3.512	1.132	0.827



Figure 2. Distribution coefficient vs. reduced temperature for  $C_2$ - $C_{19}$ - $C_{20}$ 

The distribution coefficient was correlated empirically as a function of a reduced temperature defined as follows:

$$T^* = (T - T_{\text{LCST}}) / (T_{\text{type } K} - T_{\text{LCST}})$$
(2)

The critical temperatures  $(T_{\text{LCST}} \text{ and } T_{\text{type } K})$  used were those of a binary mixture whose composition is the same as that of the over-all ethane-free composition in the cell. The values of the distribution coefficient ( $\beta$ ) and the reduced temperature ( $T^*$ ) are also presented in Table II. The distribution coefficient is plotted against the reduced temperature in Figure 2, and a smooth curve has been drawn through the data. Figure 2 shows that the distribution coefficient is not a function of the over-all heavy hydrocarbon composition in the cell. The average deviation of the experimental distribution coefficients from the smooth curve is  $\pm 0.019$ .

#### NOMENCLATURE

- $L_1$  = liquid phase less rich in ethane
- $L_2$  = liquid phase richer in ethane
- LCST = lower critical solution temperature ( $L_1$  is in critical identity with  $L_2$  in the presence of vapor phase) R = molar ratio of *n*-nonadecane to *n*-eicosane
  - $R_1$  = molar ratio of *n*-nonadecane to *n*-elcosane in the  $L_1$
  - phase  $R_2 = \text{molar ratio of$ *n*-nonadecane to*n* $-eicosane in the <math>L_2$ 
    - $_{2}$  = motar ratio of *n*-nonadecane to *n*-elecosane in the  $L_{2}$  phase
  - T = temperature in °C.
  - $T^*$  = reduced temperature defined in Equation 2
- $T_{\text{LCST}}$  = temperature of LCST critical phenomenon for the *n*-nonadecane-*n*-eicosane composition charged to the cell
- $T_{\text{type }K}$  = temperature of type K critical phenomena for the *n*-nonadecane-*n*-eicosane composition charged to the cell
- Type K = singular point ( $L_2$  is in critical identity with V in the presence of  $L_1$  phase)
  - V = vapor phase
  - $\beta$  = distribution coefficient defined in Equation 1

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