

Figure 4. Distribution curve at $25^{\circ} \mathrm{C}$.
Tie Lines. The three components were added one at a time to a tared, $50-\mathrm{ml}$. Erlenmeyer flask fitted with a glass stopper until approximately equal volumes of the two liquid phases were obtained. The mixture was then agitated vigorously and allowed to stand. It was then again agitated and allowed to separate into phases. The two layers were removed by use of hypodermic assemblies. Density and refractive index determinations were then made as outlined previously. Densities were used to determine compositions of the equilibrium phases. Refractive index readings were used primarily to identify phases, particularly in the region near the isopycnic (4), and secondarily to check compositions from density measurements.
Figure 1 and Table I show the compositions at the binodal curve. Figure 2 presents the variation of density of the mixtures of the components as a function of the binodal curve compositions and Figure 3 is a similar plot of refractive index. Basic data for the distribution curve, Figure 4, and the Bachman plot (2), Figure 5, were experimental tie line data (Table II). Additional points to complete


Figure 5. Bachman plot of tie line data
the distribution curve and define the plait point were extrapolated using Alders' method (1).

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# Diffusivities of Some Binary Liquid Systems Using a Diaphragm Cell 

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Diffusivity data on 25 binary systems were obtained by using a diaphragm cell at $30^{\circ} \mathrm{C}$.

P$P_{\text {resent understanding of diffusion is far from }}$ satisfactory, and reliable data are still scarce and fragmentary even for dilute binary solutions. The lack of a usable kinetic theory of liquids has resulted in dependence on simplified physical models and semiempirical correlations to predict diffusivities, and these can be used only with
certain reservations. There is, therefore, need for accurate experimental measurements. Because of the simplicity in construction and fairly high accuracy, a diaphragm cell has been used in many investigations for measuring binary liquid diffusivities. The present investigation reports data for 25 binary systems using a diaphragm cell at $30^{\circ} \mathrm{C}$.

## DIAPHRAGM CELL EQUATION

Diaphragm cell equation for the measurement of diffusion coefficient may be expressed as follows, as indicated by Gordon (2), assuming unidirectional diffusion and quasisteady state in the diaphragm:

$$
\begin{equation*}
D=\frac{1}{\beta t} \ln \frac{\Delta C_{i}^{\circ}}{\Delta C_{1}^{F}} \tag{1}
\end{equation*}
$$

| Table I. Properties of Solvents Used |  |  |  |
| :---: | :---: | :---: | :---: |
| Reagents | Mol. Wt. | $\begin{aligned} & \text { Density, } \\ & \text { G. } / \mathrm{Cc} . \text { at } \\ & 30^{\circ} \mathrm{C} \text {. } \end{aligned}$ | Viscosity, Cp . at $30^{\circ} \mathrm{C}$. |
| Amyl acetate | 130.18 | 0.876 | 0.8620 |
| Amyl alcohol | 88.15 | 0.813 | 3.3470 |
| Benzene | 78.11 | 0.779 | 0.5610 |
| Butyl acetate | 116.16 | 0.882 | 0.6880 |
| Isobutyl alcohol | 74.12 | 0.802 | 2.1223 |
| $n$-Butyl alcohol | 74.12 | 0.810 | 2.2710 |
| Ethyl acetate | 88.10 | 0.901 | 0.426 |
| Hexane | 86.17 | 0.662 | 0.2923 |
| Kerosine |  | 0.784 | , |
| Methyl acetate | 74.08 | 0.933 | 0.362 |
| Methanol | 32.04 | 0.792 | 0.5225 |
| Isopropyl acetate | 102.13 | 0.874 | 0.551 |
| 1-Propanol | 60.09 | 0.804 | 0.2004 |
| Toluene | 92.13 | 0.866 | 0.5516 |

Table II. Solutes Used

| Reagents | Mol. Wt. | Density | Mol. Vol., |
| :--- | ---: | :---: | :---: |
| Cc. Gole |  |  |  |
| Methyl ethyl ketone | 72.10 | 0.805 | 96.2 |
| Adipic acid | 146.14 | 1.360 | 173.8 |
| Butyric acid | 88.10 | 0.958 | 112.8 |
| Cinnamic acid | 148.15 | 1.284 | 181.8 |
| Malic acid | 134.09 | 1.601 | 141.4 |
| Oleic acid | 282.45 | 0.891 | 405.0 |
| Tartaric acid | 150.09 | 1.737 | 153.4 |

where

$$
\begin{aligned}
\beta & =\text { cell constant equal to } A_{\mathrm{e}} / l_{\mathrm{e}}\left[\frac{1}{V_{A}}+\frac{1}{V_{B}}\right] \\
\Delta C_{1}^{\mathrm{i}} & =\text { initial concentration difference, } C_{1 A}^{\circ}-C_{B} \\
\Delta C_{1}^{F} & =\text { final concentration difference, } C_{i A}^{F}-C_{I B}^{F}
\end{aligned}
$$

The diffusion coefficient as defined by Equation 1 is the time-averaged integral diffusion coefficient. Gordon (3) has shown that this coefficient can be treated without any serious error as the ordinary integral diffusion coefficient taken over the concentration range

$$
C_{1 A M}=1 / 2\left(C_{1 A}^{\circ}+C_{1 A}^{F}\right)
$$

and

$$
C_{I B M}=1 / 2\left(C_{i B}+C_{1 B}^{F}\right)
$$

The relationship between the integral diffusion coefficient and the true or differential diffusion coefficient may thus be expressed as

$$
\begin{equation*}
D=\frac{1}{C_{\mathrm{L} A M}-C_{1 B M}} \times \int_{C_{B B M}}^{C_{\mathrm{L} K M}} D d c \tag{2}
\end{equation*}
$$

where $\bar{D}$ is the true or differential diffusion coefficient. Gordon (3) has shown that if the original concentration is small, the integral diffusion coefficient calculated by using a diaphragm cell is approximately equal to the true or differential diffusion coefficient, if bulk transport due to volume changes or mixing can be neglected.

The use of Equation 1 is subject to the following conditions: quasi-steady state in the diaphragm, cell constant $\beta$ remaining constant, solutions in the two compartments being homogeneous, and mechanism of transport only by diffusion and not by surface transport. These requirements were assumed to be met by the following considerations and the use of diaphragm cells of normal dimensions similar to the one used by Krishnan and Laddha (4).

The use of a unidirectional form of diffusion equation has been shown by Toor (8) to be rigorously valid, in the sense that $A_{e} / l_{e}$ depends only upon the internal path of the diaphragm. The assumption of quasi- or pseudo-steady

Table III. Diffusivity Data at $30^{\circ} \mathrm{C}$.

| Solute | Solvent | Cell No. | Initial <br> Conen., CiA | Concn. Difference |  | $\begin{gathered} t \times 10^{-5} \\ \text { Sec. } \end{gathered}$ | $\begin{aligned} & D \times 10^{5} \\ & \text { Sq. Cm. } \\ & \text { Sec. } \end{aligned}$ | $\begin{gathered} D_{u} \times 10^{5} \\ \text { Sq. } \mathrm{Cm} . \\ / \mathrm{Sec} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\Delta C_{i}$ | $\Delta C_{1}^{F}$ |  |  |  |
| Methyl ethyl ketone | Amyl acetate | 1 | 0.2311 | 0.2311 | 0.0925 | 1.819 | 2.012 | 1.916 |
| Methyl ethyl ketone | Amyl alcohol | 1 | 0.2200 | 0.2200 | 0.1340 | 1.647 | 1.230 | 1.284 |
| Methyl ethyl ketone | Benzene | 1 | 0.2410 | 0.2400 | 0.1054 | 1.582 | 2.086 | 2.281 |
| Methyl ethyl ketone | Butyl acetate | 1 | 0.2271 | 0.2271 | 0.1072 | 1.625 | 1.852 | 2.216 |
| Methyl ethyl ketone | Isobutyl alcohol | 2 | 0.2355 | 0.2355 | 0.1753 | 1.626 | 0.5962 | 0.5873 |
| Methyl ethyl ketone | $n$-Butyl alcohol | 2 | 0.2436 | 0.2436 | 0.1819 | 1.652 | 0.5802 | 0.5488 |
| Methyl ethyl ketone | Ethyl acetate | 2 | 0.0481 | 0.0481 | 0.0106 | 1.692 | 2.932 | 3.190 |
| Methyl ethyl ketone | Hexane | 2 | 0.0596 | 0.0596 | 0.0102 | 1.560 | 3.740 | 4.595 |
| Methyl ethyl ketone | Kerosine | 1 | 0.2087 | 0.2087 | 0.1446 | 1.549 | 0.9478 | ... |
| Methyl ethyl ketone | Methanol | 3 | 0.2659 | 0.2659 | 0.1007 | 1.616 | 1.870 | 2.127 |
| Methyl ethyl ketone | Methyl acetate | 2 | 0.0471 | 0.0471 | 0.01005 | 1.608 | 3.15 | 3.442 |
| Methyl ethyl ketone | Isopropyl acetate | 2 | 0.2995 | 0.2995 | 0.1015 | 1.605 | 2.211 | 2.655 |
| Methyl ethyl ketone | Propyl alcohol | 3 | 0.1636 | 0.1636 | 0.1234 | 1.592 | 0.552 | 0.5538 |
| Methyl ethyl ketone | Toluene | 1 | 0.2447 | 0.2447 | 0.1003 | 2.031 | 2.21 | 2.519 |
| Adipic acid | Methanol | 1 | 0.02343 | 0.02343 | 0.01328 | 1.640 | 1.382 | 1.492 |
| Butyric acid | Methanol | 1 | 0.03010 | 0.03010 | 0.01387 | 1.710 | 1.810 | 1.934 |
| Cinnamic acid | Methanol | 2 | 0.02721 | 0.02721 | 0.01003 | 1.642 | 2.52 | 2.711 |
| Malic acid | Methanol | 2 | 0.02469 | 0.02469 | 0.01030 | 1.732 | 1.712 | 1.689 |
| Oleic acid | Methanol | 3 | 0.0220 | 0.0220 | 0.01333 | 1.82 | 0.902 | 0.899 |
| Tartaric acid | Methanol | 3 | 0.03419 | 0.03419 | 0.01423 | 1.652 | 1.652 | 1.608 |
| Adipic acid | 1-Butanol | 1 | 0.04679 | 0.04679 | 0.01014 | 1.514 | 0.3992 | 0.3849 |
| Butyric acid | 1-Butanol | 3 | 0.02322 | 0.02322 | 0.01788 | 1.589 | 0.5120 | 0.4889 |
| Cinnamic acid | 1-Butanol | 2 | 0.02040 | 0.02040 | 0.01591 | 1.568 | 0.4462 | 0.3746 |
| Malic acid | 1-Butanol | 2 | 0.02040 | 0.02040 | 0.01591 | 1.830 | 0.4462 | 0.4356 |
| Oleic acid | 1-Butanol | 1 | 0.03103 | 0.03103 | 0.01050 | 1.792 | 0.2513 | 0.2816 |
| Tartaric acid | 1-Butanol | 3 | 0.02131 | 0.02131 | 0.01581 | 1.812 | 0.4050 | 0.4149 |

state condition in the pores-i.e., a linear concentration gra-dient-was proved to be valid by Barnes (1) as long as the following two conditions are met: The total pore volume is less than $1 \%$ of the total cell volume and the preliminary diffusion period has lasted long enough for the effect of the original constant cross section in the diaphragm to disappear, which takes about 4 to 5 hours with a $D$ value of $2 \times 10^{-5} \mathrm{sq}$. cm . per second. The first condition is usually met by using a diaphragm of normal dimensions and the second condition by proper experimentation. The constancy of the cell factor, $\beta$, was checked by a number of experiments with 0.1 N HCl diffusing into pure water at a temperature of $30^{\circ} \mathrm{C}$. The solutions in the two compartments were assumed to be homogeneous, since with the denser solution in the top chamber, the solutions in the two compartments tended to be density-stirred. It was, however, found necessary to have the diaphragm placed perfectly horizontal. The assumption of diffusion-controlled transport will be invalidated by a defective diaphragm having a relatively enormous area of the pores, which may permit streaming. The possibility of such transport can be neglected if a proper diaphragm is used.

## EXPERIMENTAL

The cells consisted of two equal compartments separated by a No. 4 sintered glass diaphragm (porosity 5 to 10 microns) about 30 mm . in diameter and 2 to 3 mm . thick. Each compartment was provided with a filling and draining capillary tube with stopcocks. In order to measure the diffusion coefficient, the lower chamber of the vertical cell and the diaphragm were filled with the denser solution and the upper chamber with the less dense solution. The cell was then placed in the constant temperature bath in an inverted vertical position so as to have the dense solution in the top chamber. The initial concentration of the solute in the chamber from which diffusion occurred was $C_{i A}^{\circ}$. The initial concentration of the solute in the other compartment, $C_{i B}^{\circ}$, was taken to be zero. Diffusion was then allowed to occur for a preliminary period of 4 to 5 hours to establish the concentration gradient across the diaphragm. Then the cells were emptied and refilled with fresh solutions to begin the experiment. It was assumed that the solutions in the compartments were density-stirred, so that the concentration was uniform throughout each compartment. After a known time the solutions from each compartment were drained and analyzed.

The cell constant, $\beta$, was found by calibrating the cells with $0.1 N \mathrm{HCl}$ diffusing into pure water at a temperature of $30^{\circ} \mathrm{C}$. in a constant temperature bath. The value of $3.078 \times 10^{-5}$ sq. cm. per second from Stokes' data (7) was used for the diffusion coefficient in the diaphragm cell equation. The average values of the cell constants thus determined are

$$
\begin{aligned}
& \beta(\text { cell 1) } 0.2496 \\
& \beta(\text { cell 2) } 0.3049 \\
& \beta(\text { cell 3) } 0.3209
\end{aligned}
$$

The $95 \%$ confidence limit values obtained by the analysis of independent experimental runs for each cell using the procedure suggested by Mickley, Sherwood, and Reed (5) were $\pm 0.000765, \pm 0.000089$, and $\pm 0.0004$, respectively.

Ketone was determined by the method suggested by Morasco (6). Carboxylic acid in solution was estimated by titration with 0.02 N potassium hydroxide using phenolphthalein as an indicator.

## RESULTS

Diffusion coefficients were measured for 25 binary systems involving methyl ethyl ketone, adipic acid, butyric acid, cinnamic acid, malic acid, oleic acid, and tartaric acid as diffusing solutes. The properties of the solvents and the solutes are given in Tables I and II, respectively. Experimental data on binary diffusivities are recorded in Table III and compared with the predicted values according to the following empirical correlation of Wilke and Chang (9).

$$
\begin{equation*}
D_{u}=\frac{7.4 \times 10^{-8}\left(\bar{x} \cdot M_{s}\right)^{0.5} T}{\eta\left(V_{m}\right)^{06}} \tag{3}
\end{equation*}
$$

The agreement between the experimental and predicted values is satisfactory.

## NOMENCLATURE

$A_{e}=$ effective cross-sectional area of all pores
$C_{1 A}=$ concentration of component 1 in A , compartment from which component 1 diffuses, g. mole/liter
$C_{1 B}=$ concentration of component 1 in B , compartment to which component 1 diffuses, g. mole/liter
$C_{\text {LAM }}=$ mean concentration of component 1 in compartment A
$C_{\text {LBM }}=$ mean concentration of component 1 in compartment B
$\Delta C_{1}=$ molar concentration difference of component 1
$D=$ binary diffusivity as defined by Equation 1, sq. $\mathrm{cm} . / \mathrm{sec}$.
$D_{w}=$ diffusivity as calculated by Wilke and Chang's equation
$l_{e}=$ effective pore length
$M_{s}=$ molecular weight of solvent
$T=$ absolute temperature, ${ }^{\circ} \mathrm{K}$.
$t=$ time, sec.
$V_{A}=$ volume of compartment $\mathrm{A}, \mathrm{cc}$.
$V_{B}=$ volume of compartment $\mathrm{B}, \mathrm{cc}$.
$V_{m}=$ molar volume of solute
$\bar{x}=$ association parameter

## Greek Letters

$\beta=$ cell factor
$\eta=$ viscosity of solvent, centipoises

## Superscripts

$\circ=$ initial condition
$F=$ final condition
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