the diffusivity decreases very rapidly as concentration increases in the dilute region, but becomes much less dependent on concentration in the concentrated region.

Refractive indices of nickel ammonium sulfate solutions were measured at 25°C. with an Abbé refractometer. The instrument was capable of measuring refractive index with a precision of ± 0.00005 (Table II).

Densities were determined by the density bottle method, as described by Findlay (1), over the temperature range 10° to 35° C. The precision of these measurements (1) is estimated to be $\pm 0.1\%$.

Viscosities of the solutions were measured with an Ostwald viscometer, as described by Findlay (1), over the temperature range 10° to 35° C. The estimated precision is $\pm 0.3\%$. The density and viscosity results are recorded in Table IJI.

The solubility of nickel ammonium sulfate in water was measured over the temperature range 10° to 49°C. by approaching equilibrium from the under- and oversaturated states. The solutions contained in stoppered flasks were immersed in a thermostatically controlled bath ($\pm 0.1^{\circ}$ C.) and shaken at intervals over 48 hours. Samples were withdrawn through a filter and their concentrations determined by measuring the density at a temperature about 5° above the saturation temperature.

The results (Table IV) do not agree very well with those recorded in the handbooks (2, 5) or with the early work

of Tobler (6). It is, of course, difficult to explain differences between results from various sources without knowledge of the techniques used, but certain comments can be made. Two of the references (2, 5) are data handbooks, one of which (2) quotes no literature source. Neither gives any experimental detail. The work of Tobler (6) makes no mention of the purity of the salt or solvent, and saturation was approached only from the undersaturated state. The present investigation has shown that up to 48 hours is needed to approach equilibrium.

The detailed measurements of solubility in the range 37.5° to 49° C. were made in an attempt to detect any possible phase change. None was found in this region.

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Vapor-Liquid Equilibria of the Methane-Toluene System at Low Temperatures and High Pressures

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The system methane-toluene exhibits limited liquid-liquid miscibility at temperatures below the critical for methane. A quadruple point involving the two immiscible liquids, a solid phase, and a gas phase has been located visually at -149.7° F. and 358 p.s.i.a. Experimental data shown on the pressure-temperature projections permit one to classify the system as one with a Type K critical point and one with qualitatively similar behavior in all respects to the methane-heptane system. Experimental techniques were developed to sample and analyze with good precision the equilibrium gas phases containing as little as 0.001 mole % toluene. Thus, toluene K values as low as 2×10^{-5} can be reported with confidence. Binary K values for methane and toluene are reported at intervals of 20° from 0° to -100° F. for pressures from 100 to 3500 p.s.i.a. The results are reported numerically and illustrated graphically.

STUDIES on the low temperature phase behavior of the methane-n-paraffin binaries have appeared since the review of the vapor-liquid equilibria of light hydrocarbons by Price and Kobayashi (9). The equilibrium ratios and the low temperature phase behavior of the methane-n-hexane (8), methane-n-heptane (2, 6), methane-n-octane (7), methane-n-nonane (11), and methane-n-decane (12) systems have been investigated in the last few years. There are very few reports made on the study of methane-aromatic and methane-naphthenic systems up to the present time. Elbishlawi and Spencer (5) reported vapor-liquid equi-

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librium ratios of methane-toluene and methane-benzene systems at 150° F. in 1951. Sabbina and Velikovski (10) reported some results for the methane-toluene system from 40° to 150° C. in 1956. Clark (4) studied methane-cyclohexane and methane-methylcyclohexane at 150° F. in 1949. The methane-cyclohexane system has also been reported by Stepanov and Vybornov (13) at temperatures from 32° to 140° F.

The objectives of this study were to: obtain vapor-liquid equilibria data on the methane-toluene system which could be related to the methane-n-heptane (2) and methanemethylcyclohexane systems (3) recently studied, all systems with a different solvent type of the same carbon number; and provide basic data on binary systems which would

	Methane- <i>n</i> -Heptane		Methane-Methylcyclo- hexane		Methane-Toluene		
Phases	<i>T</i> , ° F.	P, p.s.i.a.	$T, \circ F.$	P, p.s.i.a.	$T, \circ F.$	P, p.s.i.a.	
L_1L_2G					-117.0	650	
L_1L_2G	-126.0	570	-155.0	318	-125.0	570	
L_1L_2G	-130.0	519	-177.5	190	-131.0	502	
L_1L_2G	-140.0	435	-194.0	1'25	-139.0	443	
L_1SG	-136.7	155	-207.0	50	-142.5	144	
L_1SG	-139.5	98	-209.5	65	-143.5	203	
L_2SG			-216.0	66			
L_2SG			-223.0	53	-168.6	246	
L_1L_2S			-213.5	100			
L_1L_2S			-214.0	400			
L_1L_2SG	-154.2	331	-213.5	73	-149.7	358	
K_{sing}^{a}	-114.7	694	-113.8	687	-115.9	671	
U							

 Table I. Observed Three- and Four-Phase Conditions of the Methane–n-Heptane, Methane-Methylcyclohexane, and Methane-Toluene Systems

 $K_{sing} = Type K singular point.$





for the methane-toluene system

Figure 3. Pressure-temperature projection for the methane-toluene system

serve as a basis for multicomponent vapor-liquid equilibrium studies at both infinitesimal and finite concentrations of the intermediate components by gas-liquid partition chromatography methods.

PHASE BEHAVIOR IN THE METHANE-TOLUENE BINARY

As previously noted (2) the binary phase behavior of methane with other *n*-paraffin hydrocarbons through *n*-decane offers three types of phase behavior: complete liquid phase miscibility, limited liquid phase miscibility, and intersection of the solubility curve with the critical locus. This study showed that the low temperature phase behavior of the methane-toluene system falls in the middle category and is quite similar to the methane-*n*-heptane binary system, which is characterized by liquid-liquid

Table II. Vapor-Liquid Equilibrium Data for the Methane-Toluene System

Р					P.				
P.S.I.A.	\mathcal{Y}_{7}	x. 0.0° F.	K_1	K_{\pm}	P.S.I.A.	\mathcal{Y}_7	<i>x</i> ₇ −60.0° F.	K_1	K_7
100.0 200.0 400.0 600.0 800.0 1250.0 1500.0 1750.0 2000.0 2500.0 3000.0 3500.0	$\begin{array}{c} 0.0021\\ 0.0012\\ 0.0009\\ 0.0009\\ 0.0009\\ 0.0010\\ 0.0010\\ 0.0011\\ 0.0014\\ 0.0018\\ 0.0027\\ 0.0041\\ 0.0063\\ \end{array}$	$\begin{array}{c} 0.9807\\ 0.9610\\ 0.9260\\ 0.8880\\ 0.8505\\ 0.8139\\ 0.7770\\ 0.7340\\ 0.6960\\ 0.6500\\ 0.5670\\ 0.5050\\ 0.4600\end{array}$	51.75 26.00 13.20 8.92 6.68 5.36 4.48 3.75 3.28 2.85 2.30 2.01 1.84	$\begin{array}{c} 0.00215\\ 0.00122\\ 0.00097\\ 0.00105\\ 0.00121\\ 0.00135\\ 0.00150\\ 0.00204\\ 0.00284\\ 0.00284\\ 0.00480\\ 0.00810\\ 0.0137 \end{array}$	$100.0 \\ 200.0 \\ 400.0 \\ 600.0 \\ 800.0 \\ 1000.0 \\ 1250.0 \\ 1500.0 \\ 1750.0 \\ 2000.0 \\ 2500.0 \\ 3000.0 \\ 3500.0 \\ 3500.0 \\ 3500.0 \\ 3500.0 \\ 3500.0 \\ 3500.0 \\ 3500.0 \\ 3500.0 \\ 3500.0 \\ 3500.0 \\ 3500.0 \\ 3500.0 \\ 3500.0 \\ 3000.0 \\ 3500.0$	$\begin{array}{c} 0.00030\\ 0.00017\\ 0.00011\\ 0.00010\\ 0.00010\\ 0.00012\\ 0.00015\\ 0.00015\\ 0.00019\\ 0.00025\\ 0.00032\\ 0.00052\\ 0.00089\\ 0.00160\\ \end{array}$	$\begin{array}{c} 0.9749\\ 0.9501\\ 0.9028\\ 0.8575\\ 0.8080\\ 0.7672\\ 0.7160\\ 0.6700\\ 0.6240\\ 0.5802\\ 0.5021\\ 0.4330\\ 0.3749 \end{array}$	$\begin{array}{c} 39.80\\ 20.00\\ 10.30\\ 7.00\\ 5.25\\ 4.25\\ 3.51\\ 3.00\\ 2.62\\ 2.36\\ 2.00\\ 1.75\\ 1.58\end{array}$	$\begin{array}{c} 0.00029\\ 0.00018\\ 0.00013\\ 0.00012\\ 0.00013\\ 0.00021\\ 0.00029\\ 0.00040\\ 0.00025\\ 0.00105\\ 0.00105\\ 0.00210\\ 0.00210\\ 0.00430\\ \end{array}$
		−20.0° F.					−80.0° F.		
$\begin{array}{c} 100.0\\ 200.0\\ 400.0\\ 600.0\\ 800.0\\ 1000.0\\ 1250.0\\ 1500.0\\ 1750.0\\ 2000.0\\ 2500.0\\ 3000.0\\ 3500.0 \end{array}$	$\begin{array}{c} 0.0012\\ 0.0007\\ 0.0005\\ 0.0004\\ 0.0004\\ 0.0005\\ 0.0006\\ 0.0007\\ 0.0009\\ 0.0011\\ 0.0017\\ 0.0026\\ 0.0041 \end{array}$	$\begin{array}{c} 0.9791\\ 0.9590\\ 0.9185\\ 0.8789\\ 0.8391\\ 0.8011\\ 0.7535\\ 0.7100\\ 0.6700\\ 0.6350\\ 0.5550\\ 0.4900\\ 0.4350\\ \end{array}$	$\begin{array}{c} 47.82\\ 24.43\\ 12.25\\ 8.25\\ 6.20\\ 5.00\\ 4.10\\ 3.42\\ 3.00\\ 2.71\\ 2.21\\ 1.91\\ 1.70\end{array}$	$\begin{array}{c} 0.00119\\ 0.00070\\ 0.00052\\ 0.00050\\ 0.00054\\ 0.00064\\ 0.00080\\ 0.00099\\ 0.00137\\ 0.00173\\ 0.00173\\ 0.00315\\ 0.0053\\ 0.0095 \end{array}$	$\begin{array}{c} 100.0\\ 200.0\\ 400.0\\ 600.0\\ 800.0\\ 1000.0\\ 1250.0\\ 1500.0\\ 1750.0\\ 2000.0\\ 2500.0\\ 3000.0\\ 3500.0 \end{array}$	$\begin{array}{c} 0.00012\\ 0.00007\\ 0.00005\\ 0.00005\\ 0.00005\\ 0.00006\\ 0.00006\\ 0.00007\\ 0.00001\\ 0.00011\\ 0.00015\\ 0.00025\\ 0.00045\\ 0.00087\\ \end{array}$	$\begin{array}{c} 0.9713\\ 0.9449\\ 0.8939\\ 0.8395\\ 0.7949\\ 0.7490\\ 0.6946\\ 0.6946\\ 0.5985\\ 0.5500\\ 0.4700\\ 0.3988\\ 0.3381 \end{array}$	$\begin{array}{c} 34.90\\ 18.14\\ 9.40\\ 6.30\\ 4.88\\ 3.99\\ 3.27\\ 2.80\\ 2.49\\ 2.21\\ 1.88\\ 1.66\\ 1.50\end{array}$	$\begin{array}{c} 0.00012\\ 0.00007_{+}\\ 0.00005_{8}\\ 0.00005_{8}\\ 0.00005_{8}\\ 0.00007_{3}\\ 0.00010\\ 0.00014\\ 0.00019\\ 0.00027\\ 0.00024\\ 0.00113\\ 0.00258 \end{array}$
		-40.0° F.					−100.0° F.		
$\begin{array}{c} 100.0\\ 200.0\\ 400.0\\ 600.0\\ 800.0\\ 1000.0\\ 1250.0\\ 1500.0\\ 1750.0\\ 2000.0\\ 2500.0\\ 3000.0\\ 3500.0 \end{array}$	$\begin{array}{c} 0.0006\\ 0.0003\\ 0.0002\\ 0.0002\\ 0.0002\\ 0.0002\\ 0.0003\\ 0.0003\\ 0.0004\\ 0.0005\\ 0.0006\\ 0.0010\\ 0.0016\\ 0.0026\\ \end{array}$	$\begin{array}{c} 0.9770\\ 0.9548\\ 0.9133\\ 0.8704\\ 0.8271\\ 0.7850\\ 0.7372\\ 0.6901\\ 0.6460\\ 0.6049\\ 0.5350\\ 0.4685\\ 0.4180\end{array}$	$\begin{array}{c} 43.06\\ 22.12\\ 11.53\\ 7.70\\ 5.78\\ 4.65\\ 3.80\\ 3.23\\ 2.82\\ 2.51\\ 2.15\\ 1.88\\ 1.71\end{array}$	$\begin{array}{c} 0.00061\\ 0.00037\\ 0.00026\\ 0.00025\\ 0.00027\\ 0.00032\\ 0.00045\\ 0.00060\\ 0.00060\\ 0.00080\\ 0.00107\\ 0.00186\\ 0.00337\\ 0.00632 \end{array}$	$\begin{array}{c} 100.0\\ 200.0\\ 400.0\\ 600.0\\ 800.0\\ 1000.0\\ 1250.0\\ 1500.0\\ 1750.0\\ 2000.0\\ 2500.0\\ 3000.0\\ 3500.0 \end{array}$	$\begin{array}{c} 0.00004\\ 0.00003\\ 0.00002\\ 0.00002\\ 0.00002\\ 0.00003\\ 0.00003\\ 0.00003\\ \overline{0.00004}\\ \overline{0.00005}\\ \overline{0.00006}\\ 0.00011\\ 0.00021\\ 0.00045 \end{array}$	$\begin{array}{c} 0.9678\\ 0.9379\\ 0.8816\\ 0.8249\\ 0.7721\\ 0.7255\\ 0.6699\\ 0.6168\\ \overline{0.5650}\\ 0.5510\\ 0.4290\\ 0.3551\\ 0.2924 \end{array}$	$\begin{array}{c} 31.05\\ 16.10\\ 8.44\\ 5.70\\ 4.39\\ 3.62\\ 3.10\\ 2.60\\ 2.26\\ 2.04\\ 1.75\\ 1.55\\ 1.40\end{array}$	$\begin{array}{c} 0.00004,\\ 0.00002,\\ 0.00002,\\ 0.00002,\\ 0.00002,\\ 0.00003,\\ 0.00003,\\ 0.00004,\\ 0.00006,\\ 0.00006,\\ 0.00006,\\ 0.00026,\\ 0.00060,\\ 0.00160,\\ 0.0000,\\ 0.0000,\\ 0.0000,\\ 0.0000,\\ 0.0000,\\ 0.0000,\\ 0.0000,\\ 0.0000,\\ 0.0000,\\ 0.0000,\\ 0.0000,\\ 0.0000,\\ 0.0000,\\ 0.000,$

immiscibility and a quadruple point involving the coexistence of four phases. The four three-phase lines emanating from the quadruple point are L_1 - L_2 -S, L_1 - L_2 -G, L_1 -S-G, and L_2 -S-G. The $L_2 \equiv G$ critical locus runs from the critical of pure toluene to the "three phase critical" in which L_1 = L_2 with solid toluene present. A study of the phase behavior indicated that the $L_2 \equiv G$ critical locus is higher in pressure than would be the case if the critical locus proceeded from the critical point of pure toluene to the critical point of pure methane. Also, the critical locus of the methane-toluene system is much higher than the methane-n-heptane system, but the low temperature phase behavior of these two systems is qualitatively similar. The higher critical pressures can be explained qualitatively by the difference in vapor pressure of n-heptane and toluene and the positive deviation from ideal solution laws exhibited by the methane-aromatic system.

Comparisons of the observed three- and four-phase conditions of the methane-toluene system with the methanen-heptane and methane-methylcyclohexane systems are shown in Table I. The Type K singular points for the three systems are quite close, but the quadruple point of the methane-methylcyclohexane system is far below the other two systems. An explanation of these phenomena is presented elsewhere (3).

EXPERIMENTAL

The experimental equipment, an error analysis, and the analytical techniques have been described by Chang *et al.* (2). The equipment is discussed in detail by Chang (1). The error analysis gave a maximum percentage error in the heavy component to be less than 5% of the amount present.

MATERIALS USED

The methane was purchased from the Matheson Co., Inc., with a certified purity of 99.99 mole %, the toluene was obtained from the Phillips Petroleum Co. with a reported purity of 99.96 mole %. Methane was passed through drying tubes packed with silica gel, activated charcoal, and Ascarite before it was introduced into the equilibrium cell. The toluene was used without further purification.

EXPERIMENTAL RESULTS AND DISCUSSION

Equilibrium measurements were made on a large number of mixtures involving methane and toluene for the temperatures from 0° to -100° F. and pressures from 100 to about 3500 p.s.i.a. Table 1 presents a comparison of the observed three- and four-phase conditions of the methanetoluene and methane-n-heptane and methane-methylcyclohexane binaries. Table II presents a complete tabulation of all binary phase compositions and K values determined in this investigation at the experimental conditions. Plots of K value vs. pressure for the six isotherms studied are presented in Figure 1. Minimum K values of toluene are at approximately 600 p.s.i.a. as shown in Figure 1. A plot of the K values of toluene vs. the reciprocal absolute temperature is shown in Figure 2. The critical locus in Figure 3 is estimated using the toluene critical point and the data of Elbishlawi and Spencer (5) and Sabbina and Velikovski (10). Great care was taken to have the experimental conditions at even temperature and pressure increments (Table II).

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Vapor-Liquid Equilibria of the Methane-Methylcyclohexane System at Low Temperatures and High Pressures

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The methane-methylcyclohexane system exhibits limited liquid miscibility at temperatures below the critical of methane. A quadruple point involving a gas phase, two liquid phases, and a solid phase has been located visually at -213.5° F. and 73 p.s.i.a. Experimental data on the pressure-temperature projection show that the low temperature phase behavior of this system is qualitatively similar to the methanen-heptane system with the exception that a minimum point appears in the critical locus. Binary K values of methane and methylcyclohexane are reported at intervals of 20° from 0° to -100° F. for pressures from 100 p.s.i.a. to the critical of the system. The lowest K value of methylcyclohexane determined was 0.000044 at 100 p.s.i.a. and -100° F.

THE EQUILIBRIUM ratio and the low temperature phase behavior of the several methane-n-paraffin binary systems studied in the last few years have recently been reviewed (2). There are only a few references on the study of methane-aromatic or methane-naphthenic systems (7, 8, 11). The only literature data found for the methanemethylcyclohexane system was the study by Clark (6) in 1949.

The objectives of this study were: to obtain vapor-liquid equilibrium data on the methane-methylcyclohexane system over a temperature range comparable with that made for the methane-*n*-heptane (4) and the methane-toluene (5)systems-i.e., from 0° to -100° F. inclusive- and to reveal the effect of solvent types on the vapor-liquid equilibrium behavior of these systems; to provide basic data on binary systems which would serve as a basis for subsequent multicomponent vapor-liquid equilibrium studies at both infinitesimal and finite concentrations of the intermediate components both by classical and gas-liquid partition chro-

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matography methods; and to provide basic data to permit theoretical studies on the effects of molecular size and structure of the solvent on the vapor-liquid equilibria behavior of hydrocarbon systems at low temperatures and elevated pressures (2, 3).

PHASE BEHAVIOR IN METHANE-METHYLCYCLOHEXANE BINARY SYSTEM

The binary phase behavior of methane with other *n*-paraffin hydrocarbons through *n*-decane offers three types of phase behavior: complete liquid phase miscibility, limited liquid miscibility, and the intersection of the three-phase solid-liquid-gas solubility curve locus with the gas-liquid critical locus, which causes an interruption in the latter. This study showed that the low temperature phase behavior of methane-methylcyclohexane system falls in the middle category and is qualitatively similar to methane-n-heptane binary system, which is characterized by liquid-liquid immiscibility and a quadruple point involving the coexistence of four phases, $G-L_1-L_2-S$. The four three-phase