Table I. Experimental Data for Naphthalene Vapor Pressure

| Liquid |  | Solid |  |
| :---: | :---: | :---: | :---: |
| $t,{ }^{\circ} \mathrm{C}$. | $P$, torr | $t,{ }^{\circ} \mathrm{C}$. | $P$, torr |
| $80.33{ }_{4}$ | $7.51{ }_{\\|}$ | 40.33: | 0.35 |
| 82,88 | 8.55- | 49.45 | 0.74 , |
| $83.35{ }^{\text {i }}$ | 8.80 | 54.170 | 1.11; |
| 85.69 | 9.71 | 60.22 ; | 1.836 |
| 88.85 | $11.30_{2}$ | 61.200 | 1.90. |
| 92.74; | $13.58{ }_{1}$ | 65.05, | 2.54 , |
| 93.28 | 13.85 | 66.35 . | $2.88{ }_{6}$ |
| $94.31_{9}$ | 14.64 | 70.18: | 3.75; |
| 98.66; | 17.67; | 70.98 | 3.914 |
| 102.93 | 21.25 ; | $75.61{ }_{4}$ | 5.44* |
| $106.19{ }_{6}$ | 24.33: | $76.70{ }_{6}$ | 5.92: |
| $109.23_{0}$ | 27.731 | 79.34; | 6.99 i |
| 109.49 | 27.88 |  |  |
| $109.80_{4}$ | 28.28 |  |  |
| 115.55; | 35.639 |  |  |
| 115.57, | 35.67, |  |  |
| 119.22. | 41.03, |  |  |
| 124.44, | 50.0515 |  |  |
| 124.91* | 50.98 ; |  |  |
| 125.91. | 52.95 |  |  |
| 133.28 | 69.06* |  |  |
| 133.69 4 | 69.97 " |  |  |
| 138.48 | 82.63 |  |  |
| $139.61^{\prime \prime}$ | 86.08: |  |  |
| 140.83* | 89.64: |  |  |
| 149.64 | 120.0: |  |  |
| 150.38 | 122.8 |  |  |
| 158.01. | $155.7{ }_{7}$ |  |  |
| 159.08 | $161.3{ }_{1}$ |  |  |
| 159.54 | 163.62 |  |  |
| $168.70_{4}$ | 214.8 |  |  |
| 179.51; | 290.9 |  |  |

At the triple point, $80.27^{\circ} \mathrm{C}$. (4), Equations 1 and 4 give values of 7.47 ; and $7.49_{4}$ torr, respectively. These values agree within the calculated precision. The use of a nonlinear regression and minimization of the deviation of $P$ rather than of $\log P$ is feasible only with the aid of the computer. This method was chosen because it fits the experimental condition of a relatively constant error in the measurement of $P$, rather than the constant percentage error in $P$ implied in the minimization of the deviation of $\log P$. Trial calculations showed that the two methods do not lead to large differences in calculated values of the constants or of $P$. However, the authors believe there is a real gain in obtaining the value of the deviation in $P$ directly from the calculation of the interpolating equation.

## ACKNOWLEDGMENT

The authors acknowledge the assistance of R. F. Brooks and A. W. Dickinson for devising and implementing the computer programs.

## literature cited

(1) Camin, D.L., Rossini, F.D., J. Phys. Chem. 59, 1173 (1955).
(2) Gil'denblat, I.A., Furmanov, A.S., Zhavoronkov, N.M., J. Appl. Chem., U.S.S.R.33, 246 (1960).
(3) Mastrangelo, S.V.R., Anal. Chem. 29, 841 (1957).
(4) McCullough, J.P., Finke, H.L., Messerly, J.F., Todd, S.S., Kincheloe, T.C., Waddington, G., J. Phys. Chem. 61, 1105 (1957).
(5) Stull, D.R., Ind. Eng. Chem. 39, 517 (1947).
(6) Timmermans, J., "Physico-Chemical Constants of Pure Organic Compounds," p. 177, Elsevier, New York, 1950.
(7) Ibid., Vol. 2, p. 130, 1965.

# Liquid Phase Density in the System Helium-Nitrogen 

W. B. STREETT ${ }^{1}$<br>Inorganic Chemistry Laboratory, University of Oxford, Oxford, England


#### Abstract

Densities have been measured at 25 points in the compressed liquid region of the helium-nitrogen system at $77.38^{\circ}, 100.61^{\circ}$, and $117.30^{\circ} \mathrm{K}$. at pressures up to 544 atm. Density vs. pressure curves have been extrapolated to the saturation curves to obtain densities for the saturated liquid.


EXPERIMENTAL studies of liquid-vapor phase equilibria have been published for many low temperature binary systems; however, few of these include data on the densities of the coexisting phases. Such data are required for performing meaningful thermodynamic analyses and correlations of the phase data, but they are difficult to obtain because of the low temperature and sometimes high pressure at which these systems exist. Often the vapor phase density can be estimated from an equation of state, but estimates of the liquid density are far less reliable, especially when one of the pure components is a supercritical gas. In this paper, experimental measurements of densities in the compressed liquid region of the helium-nitrogen system are
${ }^{1}$ Present address: Department of Chemistry, U. S. Military Academy, West Point, N. Y. 10996
presented at temperatures of $77.38^{\circ}, 100.61^{\circ}$, and $117.30^{\circ} \mathrm{K}$. and at pressures from just above saturation to 544 atm . Density vs. pressure curves have been extrapolated to the saturation line to obtain saturated liquid densities.

## EXPERIMENTAL

Liquid densities reported here have been measured by the method of gas expansion. In this method a small quantity of the fluid under study is confined in a cell of known volume at fixed pressure and temperature, and expanded into a large volume, thermostatically controlled at room temperature. The mass of gas is determined from known low pressure $P V T$ relations in the large volume, and used to calculate the density under conditions in the cell. A detailed description of the experimental equipment and its
use in measuring densities of pure liquids has been given (2). A brief discussion of the procedure used in measuring mixture densities is reported here.

The experimental method is explained by Figure 1. Curve $a-b$ is the saturated liquid line for the helium-nitrogen system at temperature $T_{1}$. [The saturated liquid lines for the three temperatures of interest were determined earlier, and have been reported (1).] After this phase boundary curve has been determined, a series of gas mixtures of known compositions ( $X_{1}-X_{3}$ ) are prepared. A mixture such as $X_{1}$ is then pumped into the high pressure cell of known volume, at temperature $T_{1}$, to a pressure well above the saturation pressure, such as point $c$. The high pressure cell is fitted with a soft iron stirring bar, actuated by an electromagnet wound on the outside of the cell, which is used to stir the mixture and ensure complete mixing. After the cell and its contents reach pressure and temperature equilibrium, the pressure is lowered, in steps of 50 to 100 atm ., by expanding the contents into the low pressure expansion volume, thermostatically controlled


Figure 1. Method of density determination for mixtures


Figure 2. Density-pressure

## diagram

盲, experimental curves
$\square$, saturated liquid
$\Delta$. pure nitrogen density

Table I. Density and Molar Volume of Helium-Nitrogen Liquid Mixtures

| $T=77.38^{\circ} \mathrm{K}$ |  |  |
| :---: | :---: | :---: |
| 1.66 Molerc ${ }^{r} \mathrm{He}$ |  |  |
| $P$, | $\rho$, | $V$, |
| atm. | g. $/ \mathrm{cc}$. | cc. $/$ mole |
| 282.3 | 0.853 | 32.38 |
| 190.5 | 0.839 | 32.94 |
| 102.0 | 0.821 | 33.66 |
| $95.2^{\circ}$ | 0.819 | 33.72 |


| $T=117.30^{\circ} \mathrm{K}$ |  |  |
| :---: | :---: | :---: |
| 12.81 |  | Moler $\%$ |
| $P$. | $\rho$, | $V$ |
| atm. | g.. cc. | $\mathrm{cc} . /$ mole |
| 282.3 | 0.649 | 38.45 |
| 204.1 | 0.607 | 41.11 |
| 136.1 | 0.556 | 44.83 |
| $125.9^{2}$ | 0.548 | 45.51 |


| 19.21 Mole \% He |  |  |
| :---: | :---: | :---: |
| $P$, | $\rho$, | $V$, |
| atm. | g. cc. | ce. $/$ mole |
| 346.9 | 0.636 | 36.81 |
| 272.2 | 0.602 | 38.86 |
| 204.1 | 0.560 | 41.81 |
| 190.5 | 0.547 | 42.78 |


| $T=100.61^{\circ} \mathrm{K}$. |  |  | 26.99 Mole ${ }^{-} \cdot \mathrm{He}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4.67 Mole ${ }^{\circ} \mathrm{c}$ - He |  |  |  |  |  |
| $P$ <br> atm. | $\stackrel{\rho}{\text { g. } / \mathrm{cc} .}$ | $V$, cc. mole | $P_{\text {. }}$ <br> atm. | $\stackrel{\rho}{\mathrm{g}} / \mathrm{cc}$ | $V$, cc. mole |
| 272.2 | 0.756 | 35.58 | 425.2 | 0.614 | 35.06 |
| 190.5 | 0.733 | 36.70 | 373.5 | 0.595 | 36.19 |
| 102.0 | 0.696 | 38.67 | 306.1 | 0.564 | 38.19 |
| $91.8^{\text {c }}$ | 0.689 | 39.03 | 292.5 " | 0.557 | 38.66 |
| 9.50 Mole ${ }^{\sim} \mathrm{c} \mathrm{He}$ |  |  | 35.31 Mole $\% \mathrm{He}$ |  |  |
| $P_{1}$ atm. | $\begin{aligned} & \rho, \\ & \text { g./cc. } \end{aligned}$ | $V$. <br> cc. /mole | $\begin{gathered} P, \\ \text { atm. } \end{gathered}$ | $\stackrel{\rho}{\mathrm{g} \cdot \mathrm{cc} .}$ | $V$, cc. mole |
| 363.9 | 0.751 | 34.26 | 544.2 | 0.596 | 32.81 |
| 272.2 | 0.728 | 35.33 | 476.2 | 0.575 | 33.96 |
| 217.7 | 0.712 | 36.15 | 469.4* | 0.574 | 34.03 |
| 210.9* | 0.710 | 36.25 |  |  |  |
| 15.12 Mole ${ }^{\circ} \mathrm{HHe}$ |  |  |  |  |  |
| $\begin{gathered} P, \\ \mathrm{a} \text { tm. } \end{gathered}$ | $\rho$, <br> g. cc . | V, cc. mole |  |  |  |
| 510.2 | 0.768 | 31.74 |  |  |  |
| 455.8 | 0.751 | 32.46 |  |  |  |
| 438.8* | 0.745 | 32.73 |  |  |  |

"Saturation pressure.


Figure 3. Saturated liquid lines plotted as molar volume vs. composition
at room temperature, from which the quantity of gas removed in each pressure step is determined. When a pressure just above saturation is reached (point $e$ ), the entire cell contents are expanded, to give the density at that pressure. The densities at higher pressures (points $c, d$ ) are then obtained by adding the increments for each pressure step. This procedure is repeated for other mixtures $\left(X_{2}\right.$, $X_{3}$ ), resulting in a network of $P-\rho-X$ points in the compressed liquid region at temperature $T_{1}$. Temperatures have been measured by a platinum resistance thermometer calibrated by the National Bureau of Standards, and are accurate to within $\pm 0.02^{\circ} \mathrm{K}$. Pressures have been measured by a calibrated Heise bourdon gage, with an accuracy of $\pm 0.5 \mathrm{~atm}$. The unit of pressure is the international atmosphere.

## RESULTS AND DISCUSSION

The experimental density measurements are shown in Table I with the equivalent molar volumes. Experimental density us. pressure curves have been plotted in Figure 2 and extrapolated to the saturation pressure to give the saturation density for each mixture composition. Pure nitrogen density points in Figure 2 have been taken from reported data (2) and are estimated to be accurate to within $\pm 0.1 \%$. The expansion of each mixture in steps, as outlined above, reduces the accuracy of the mixture densities, as compared with those for pure liquid nitrogen, for which the entire cell contents were expanded from each $P-T$ point. The mixture densities are estimated to be accurate to within $\pm 1.0 \%$.

A smooth curve has been drawn through the saturated liquid density points at each temperature. These curves for the $100.61^{\circ}$ and $117.30^{\circ} \mathrm{K}$. isotherms have an inflection point at pressures around 300 to 400 atm ., but it is not clear whether this is a feature of the system or whether it is a result of scatter in the data. These curves might reasonably be expected to be complicated, since increasing pressure is accompanied by increasing helium content, and these two factors produce opposite effects on the density of the mixture. A plot of molar volume us. composition for the saturated liquid is better behaved (Figure 3).

## ACKNOWLEDGMENT

The author is indebted to L. A. K. Staveley of the Inorganic Chemistry Laboratory, Oxford, for much useful advice on the design and conduct of the experiment.

## literature Cited

(1) Streett, W.B., Chem. Eng. Progr. Symp. Ser. 63, No. 81, 37 (1967).
(2) Streett, W.B., Staveley, L.A.K., Advan. Cryog. Eng. 13, to be published.

Received for review October 18, 1967. Accepted January 31, 1968. This work was made possible by a NATO Postdoctoral Research Fellowship in Science, awarded to the author by the National Science Foundation. Financial support was provided, in part, by the U.S. Army Research Office, Durham, N. C.

# Heat of Formation of Hydroxylammonium Perchlorate by Combustion Calorimetry 

M. F. ZIMMER, E. E. BAROODY, G. A. CARPENTER, and R. A. ROBB<br>Research and Development Department, Naval Ordnance Station, Indian Head, Md. 20604


#### Abstract

The energy of combustion of solid hydroxylammonium perchlorate with diethyl oxalate as fuel was determined in a rotating bomb calorimeter. The standard heat of formation of hydroxylammonium perchlorate at $25^{\circ} \mathrm{C}$. and 1 atm , is $-66.16 \pm 0.65 \mathrm{kcal}$. per mole ( $\pm 0.65$ is estimated standard deviation of the mean) and was calculated using a computer program which was developed for compounds containing carbon, hydrogen, nitrogen, oxygen, and chlorine.


Combustion reaction of hydroxylammonium perchlorate was carried out in an oxygen atmosphere using diethyl oxalate as the fuel. The idealized reaction equation from which the heat of formation is determined is:

$$
\begin{array}{r}
\mathrm{H}_{4} \mathrm{O}_{5} \mathrm{~N}_{1} \mathrm{Cl}_{1}(\mathrm{c})+\mathrm{C}_{6} \mathrm{H}_{10} \mathrm{O}_{4}(\mathrm{l})+4.75 \mathrm{O}_{2}(\mathrm{~g})+143.5 \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow \\
6 \mathrm{CO}_{2}(\mathrm{~g})+\mathrm{HCl} \cdot 150 \mathrm{H}_{2} \mathrm{O}(\mathrm{l})+0.5 \mathrm{~N}_{2}(\mathrm{~g}) \tag{1}
\end{array}
$$

The chlorine gas liberated in the reaction was converted to the chloride ion by adding arsenious acid solution to the bomb (5). The heats of formation of perchlorates or other highly oxygenated compounds are usually obtained from heat of solution experiments. For such reactions, however, the heats of formation of the other reactants and reaction products must be known. The reactants and products will vary for each different compound of the general formula $\mathrm{C}_{a} \mathrm{H}_{b} \mathrm{O}_{c} \mathrm{~N}_{d} \mathrm{Cl}_{e}$ and so will their thermal data that must be obtained either from literature or experiments that subjects the final results to other possible sources
of errors. The combustion of hydroxylammonium perchlorate with diethyl oxalate according to Equation 1 is equivalent to burning a compound of the general formula $\mathrm{C}_{a} \mathrm{H}_{b} \mathrm{O}_{\mathrm{c}} \mathrm{N}_{d} \mathrm{Cl}_{e}$ in the presence of oxygen and water. The reaction products, $\mathrm{CO}_{2}, \mathrm{H}_{2} \mathrm{O}, \mathrm{HCl}$, and $\mathrm{N}_{2}$ are always the same and no auxiliary data besides the heat of formation for diethyloxalate are necessary. Thus with a slight modification for chlorine compounds, the "Washburn corrections" used for $\mathrm{C}_{6} \mathrm{H}_{6} \mathrm{O}_{c} \mathrm{~N}_{d}$ compounds can be applied. Since the final combustion products for all compounds are the same, a computer program has been set up for data reduction (5).

## EXPERIMENTAL

Material. Hydroxylammonium perchlorate was synthesized at this laboratory. After synthesis, the material was dissolved in ethyl ether, filtered, and precipitated by the rapid addition of benzene, yielding fine needles. The very fine needles were desirable to provide the most intimate contact between the oxidizer and fuel to obtain good combustion. The precipitate was filtered and dried at $50^{\circ} \mathrm{C}$.

