that the density change per unit concentration is constant. One might assume the linear relationship for all temperatures if the data for the $0.1 M$ solution were not available. However, at higher temperatures the density change per unit concentration is greatest over the 0.0 to $0.1 M$ region (Table I), and the linear relationship between the density and the concentration of KCl solutions applied only to the 0.1 to $1.0 M$ region (Figure 2).

The densities of $1.27 \mathrm{M} \mathrm{UO} \mathrm{SO}_{4}$ at temperatures to $374^{\circ}$ C. are also shown in Figure 1, together with the data of Krohn and Wymer for $1.38 M \mathrm{UO}_{2} \mathrm{SO}_{+}$(5). The general effect of temperature on the density of the uranyl sulfate solution is similar to that on the density of the KCl solutions. However, the density of the $\mathrm{UO}_{2} \mathrm{SO}_{4}$ solution decreases much faster than the density of the KCl solutions, especially at temperatures above $250^{\circ} \mathrm{C}$. The divergence of the two sets of density data for the $\mathrm{UO}_{2} \mathrm{SO}_{4}$ solution (Figure 1) is the result of different solution concentrations at the higher temperatures. Different initial volumes of $1.27 \mathrm{M} \mathrm{UO}{ }_{2} \mathrm{SO}_{4}$ induced different vapor volumes above the solution. Therefore, the mass transfer of solvent to the vapor phase was greater for the lower initial volume, and the concentration of that solution was greater at the higher temperatures.

The densities of $0.1,0.5$, and $1.0 M \mathrm{KCl}$ and of $1.27 M$ and 1.344 molal $\mathrm{UO}_{2} \mathrm{SO}_{4}$ at various temperatures (Table II) have been determined by linear interpolation of the density $v s$. concentration plots at the various temperatures. These data for the KCl solutions were interpolated from the data in this report only. These data for $\mathrm{UO}_{2} \mathrm{SO}_{4}$ were interpolated from the data in this report and the data of Krohn and Wymer (5), obtained in numerical form from those authors.

The density change of the $\mathrm{UO}_{2} \mathrm{SO}_{4}$ solution from $25^{\circ}$ to $350^{\circ} \mathrm{C}$. is 0.464 gram per ml., whereas the corresponding change for the 1.0 M KCl solution is only 0.320 gram per ml. This difference in the change of the densities might be due to differences in the concentrations or the molecular weights of the two salts. However, the linear relationship between the density and concentration of the KCl solutions indicates that the densities of $1.27 M \mathrm{KCl}$ solution at all temperatures would be higher than the densities of the 1.0 M KCl ; but the rate of

Table II. Interpolated Densities of Solutions Having Constant Concentrations at Temperatures to $370^{\circ} \mathrm{C}$.

|  | Density, Grams per Ml. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Temp., | $0.1 M$ | $0.5 M$ | $1.0 M$ | $1.27 M$ | $1.344 m$ |
| ${ }^{\circ} \mathrm{C}$. | KCl | KCl | KCl | $\mathrm{UO}_{2} \mathrm{SO}_{4}$ | $\mathrm{UO}_{2} \mathrm{SO}_{4}$ |
| 25 | 1.003 | 1.018 | 1.039 | 1.411 | 1.411 |
| 100 | 0.971 | 0.985 | 1.004 | 1.370 | 1.363 |
| 150 | 0.933 | 0.947 | 0.964 | 1.319 | 1.314 |
| 200 | 0.882 | 0.900 | 0.922 | 1.278 | 1.253 |
| 225 | 0.858 | 0.876 | 0.899 | 1.258 | 1.223 |
| 250 | 0.823 | 0.848 | 0.878 | 1.233 | 1.189 |
| 275 | 0.788 | 0.867 | 0.856 | 1.207 | 1.144 |
| 285 | 0.773 | 0.804 | 0.846 | 1.186 | 1.124 |
| 300 | 0.743 | 0.780 | 0.816 | 1.149 | 1.088 |
| 350 | 0.618 | 0.674 | 0.744 |  |  |
| 370 | 0.525 | 0.586 | 0.659 |  |  |

density change would not approach that observed for $\mathrm{UO}_{2} \mathrm{SO}_{4}$. Also, normalizing the concentrations in terms of molality and normality and plotting the densities against these terms does not change the trends of, and the differences in, the densities of the KCl and $\mathrm{UO}_{2} \mathrm{SO}_{4}$ solutions.

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# Vapor-Liquid Equilibrium Relations of Binary Systems. The Propane-n-Alkane Systems. n-Butane and n-Pentane 

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I
[N THE COURSE of a long-range study of the critical properties of hydrocarbon mixtures, $P-V-T-x$ data have been obtained for a series of binary systems of the normal and branched-chain hydrocarbons. In the selection of the systems of study, members of the homologous series of the paraffin hydrocarbons have been paired with a member of the same series, but of lower molecular weight. By this method, the effect of such variables as
molecular weight and molecular structure on the phase behavior can be investigated as parameters for the correlation of the $P-V-T$ data. This first paper summarizes the data obtained for the two binary systems composed of $n$-butane and $n$-pentane, with propane as the common component. The work has been carried out by graduate students, each binary system serving as the thesis problem for the M.S. degree in chemical engineering.

The P-V-T-x relations of the binary systems of $n$-butane and $n$-pentane, with propane as a common component, have been determined. The experimental results cover a range from about 200 p.s.i.a. and room temperature to the highest pressure and temperature at which liquid and vapor can coexist. The data are presented in tabular form. P-T-x, density-T-x, and isobaric $T$-x diagrams are given.

## EXPERIMENTAL

To determine the $P-V-T-x$ relations for the binary propane- $n$-alkane systems, the $P-T$ border curves and density-temperature curves were obtained for a series of mixtures of known composition for each system. The relationships between any set of variables were then derived by appropriate cross plots of the curves.

The apparatus and experimental procedures were the


Figure 1. Pressure-temperature-composition diagram for propane-n-butane system


Figure 2. Temperature-density-composition diagram for propane-n-butane system
same as those employed in earlier studies (5,6). A fluid mixture, prepared by combining measured amounts of the pure air-free components, was confined over mercury in the sealed end of a thick-walled glass tube. The tube was heated to a constant temperature by the vapors of a series of pure organic compounds which were confined in a jacket surrounding the tube. The temperature was measured to within $0.02^{\circ} \mathrm{C}$. by a thermocouple projecting into the jacket. The tube was held in one leg of a mercury-in-steel U-tube, the other leg of which was connected to a source of high-pressure nitrogen gas for pressurizing the sample. The pressure on the system was measured to within 0.5 p.s.i. by a precision spring gage. Both the thermocouple and pressure gage were calibrated, the former by comparison with a platinum re-


Figure 3. Isobaric temperature-composition diagram for propane-n-butane system


Figure 4. Pressure-temperature-composition diagram for propane-n-pentane system


Figure 5. Temperature-density-composition diagram for propane-n-pentane system


Figure 6. Isobaric temperature-composition diagram for propane-n-pentane system

Table I. Summary of Temperature, Pressure, and Density Relations of the Propane-n-Butane System at the Phase Boundaries (1)

|  | Liquid |  | Vapor |  | Pressure, P.S.I.A. | Liquid |  | Vapor |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Pressure, P.S.I.A. | Temp., ${ }^{\circ} \mathrm{C}$. | Density, g./cc. | Temp., ${ }^{\circ} \mathrm{C}$. | Density, g./ce. |  | Temp., ${ }^{\circ} \mathrm{C}$ | Density, g. /cc. | Temp., ${ }^{\circ} \mathrm{C}$. | Density, g. $/ \mathrm{cc}$. |
| Composition. 14.68 Mole \% Propane |  |  |  |  | Composition. 52.11 Mole \% Propane |  |  |  |  |
| 225.0 | 89.9 |  | 95.8 | 0.0382 | 250.0 | $71.0{ }^{\text {a }}$ |  | 82.8 | 0.0402 |
| 250.0 | 95.6 | 0.4556 | 101.1 | 0.0436 | 300.0 | 81.8 | 0.4397 | 91.7 | 0.0499 |
| 300.0 | 105.3 | 0.4372 | 110.0 | 0.0480 | 350.0 | 90.4 | 0.4213 | 99.4 | 0.0603 |
| 350.0 | 114.1 | 0.4171 | 118.3 | 0.0660 | 400.0 | 98.1 | 0.4030 | 106.2 | 0.0724 |
| 400.0 | 122.1 | 0.3950 | 125.8 | 0.0796 | 450.0 | 105.1 | 0.3844 | 112.3 | 0.0863 |
| 450.0 | 129.5 | 0.3719 | 132.5 | 0.0968 | 500.0 | 111.7 | 0.3629 | 117.8 | 0.1034 |
| 500.0 | 136.0 | 0.3450 | 138.6 | 0.1191 | 525.0 | 114.9 | 0.3504 | 120.3 | 0.1142 |
| 525.0 | 139.2 | 0.3279 | 141.4 | 0.1337 | 550.0 | 117.9 | 0.3361 | 122.7 | 0.1266 |
| 540.0 | 141.1 | 0.3140 | 142.9 | 0.1449 | 570.0 | 120.3 | 0.3221 | 124.4 | 0.1380 |
| 550.0 | 142.4 | 0.3029 | 143.9 | 0.1554 | 590.0 | 122.7 | 0.3034 | 126.0 | 0.1562 |
| 560.0 | 143.6 | 0.2890 | 144.8 | 0.1710 | 600.0 | 124.0 | 0.2899 | 126.6 | 0.1674 |
| 565.0 | 144.2 | 0.2783 | 145.2 | 0.1806 | 605.0 | 124.6 | 0.2820 | 126.9 | 0.1726 |
| 567.5 570.0 | 144.5 144.9 | 0.2720 0.2616 | 145.4 | 0.1870 0.196 | 610.0 | 125.35 | 0.2696 | 127.1 | 0.1880 |
|  |  |  |  |  | 614.8 max. p. | 126.5 | 0.2482 |  |  |
|  |  |  |  |  |  |  |  |  |  |
| 250.0 | $84.9{ }^{\text {a }}$ |  | 94.1 | 0.0421 |  | Composition. | 75.45 Mole | \% Propane |  |
| 300.0 | 94.8 | 0.4418 | 103.4 | 0.0522 | 300.0 | $69.9^{\text {a }}$ | 0.4364 | 78.2 | 0.0484 |
| 350.0 | 103.5 | 0.4227 | 111.0 | 0.0631 | 350.0 | 77.9 | 0.4199 | 85.3 | 0.0584 |
| 400.0 | 111.5 | 0.4029 | 117.9 | 0.0758 | 400.0 | 85.5 | 0.4019 | 91.9 | 0.0696 |
| 450.0 | 118.7 | 0.3800 | 124.2 | 0.0914 | 450.0 | 92.3 | 0.3832 | 97.9 | 0.0830 |
| 500.0 | 125.3 | 0.3559 | 129.9 | 0.1114 | 500.0 | 98.4 | 0.3625 | 103.2 | 0.0984 |
| 525.0 | 128.6 | 0.3407 | 132.5 | 0.1234 | 525.0 | 101.4 | 0.3498 | 105.6 | 0.1084 |
| 550.0 | 131.6 | 0.3238 | 134.8 | 0.1385 | 550.0 | 104.2 | 0.3360 | 108.0 | 0.1198 |
| 560.0 570.0 | 132.8 134.0 | 0.3148 0.3042 | 135.7 136.6 | 0.1460 0.1562 | 570.0 | 106.4 | 0.3240 | 109.8 | 0.1308 |
| 580.0 | 135.2 | 0.2916 | 137.5 | 0.1710 | 590.0 | 108.6 | 0.3079 | 111.4 | 0.1441 |
| 585.0 | 135.9 | 0.2820 | 137.8 | 0.1804 | 600.0 | 109.7 | 0.2974 | 112.1 | 0.1530 |
| 590.0 | 136.8 | 0.2646 | 137.9 | 0.1876 | 610.0 | 110.8 | 0.2844 | 112.8 | 0.1662 |

Table I. (Continued)

|  | Liquid |  | Vapor |  | Pressure, P.S.I.A. | Liquid |  | Vapor |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Pressure, P.S.I.A. | Temp., ${ }^{\circ} \mathrm{C}$. | Density, <br> g. cc . | Temp., ${ }^{\circ} \mathrm{C}$. | Density, g. /cc. |  | Temp., ${ }^{\circ} \mathrm{C}$. | Density, g. $/ \mathrm{cc}$. | Temp., ${ }^{\circ} \mathrm{C}$. | Density, g. /cc. |
| 615.0 | 111.3 | 0.2766 | 113.1 | 0.1750 | 525.0 | 91.6 | 0.3440 | 93.5 | 0.1072 |
| 620.0 | 112.0 | 0.2630 | 113.3 | 0.1868 | 550.0 | 94.3 | 0.3298 | 96.0 | 0.1184 |
| 622.5 | 112.4 | 0.2524 | 113.36 | 0.1960 | 570.0 | 96.4 | 0.3165 | 97.8 | 0.1292 |
|  | Composition. | 92.58 Mol | $C_{c}$ Propane |  | 590.0 | 98.4 | 0.3011 | 99.6 | 0.1424 |
| 350.0 | $69.6{ }^{\text {c }}$ |  | 72.9 | 0.0577 | 600.0 | 99.4 | 0.2911 | 100.4 | 0.1523 |
| 400.0 | 76.6 | 0.3948 | 79.6 | 0.0694 | 610.0 | 100.4 | 0.2764 | 101.2 | 0.1656 |
| 450.0 | 83.1 | 0.3755 | 85.5 | 0.0824 | 615.0 | 100.9 | 0.2658 | 101.6 | 0.1768 |
| 500.0 | 88.8 | 0.3563 | 91.0 | 0.0980 | 620.0 | 101.4 | 0.2514 | 101.9 | 0.1822 |

a Extrapolated value.
sistance thermometer which had been calibrated by the National Bureau of Standards, and the latter by comparison with a calibrated dead weight gage. A previous calibration of the tube made it possible to determine the volume of the sample by measuring the length of the tube which it occupied with a cathetometer reading to 0.02 mm . Equilibrium between the liquid and vapor phases was attained by moving a small steel ball enclosed in the tube, by means of a magnet, around the outside of the jacket. Pressure and volume were observed at a series of constant temperatures covering the range desired.

## MATERIALS AND PREPARATION OF MIXTURES

The propane, $n$-butane, and $n$-pentane from which the mixtures were prepared were supplied with a purity of 99.9 mole $\%$ or better by the Phillips Petroleum Co. and
used without further purification except for the removal of air. Deaeration was accomplished by a series of operations which involved freezing with liquid nitrogen and pumping off residual gas over the solid, followed by melting of the solid sample and distillation at low pressure. The purity of the components was checked by measuring the difference between their isothermal dew and bubble points. The maximum pressure difference was less than 2.0 p.s.i. Mixtures of propane with $n$-butane were prepared by injecting measured amounts of each gas into the experimental tube, previously filled with pure air-free mercury. For mixtures containing $n$-pentane, a measured amount of the air-free liquid component was transferred by molecular distillation to the experimental tube, which was attached to a high-vacuum line. Measured quantities of pure propane gas were then injected to make a mixture of the desired composition.

Table II. Isobaric Temperature-Composition Relations of Propane-n-Butane System


| Composition, <br> Mole $\%$ <br> Propane | Temperature, ${ }^{\circ} \mathrm{C}$ |  |
| :--- | :--- | :--- |
|  | Vapor |  |


| Composition, Mole \% Propane | Temp |
| :---: | :---: |
|  | Liquid |

## Pressure. 300 P.S.I.A.

| 0 | 116.2 | 116.2 |
| ---: | ---: | ---: |
| 10 | 108.6 | 112.0 |
| 20 | 101.7 | 107.8 |
| 30 | 95.2 | 103.4 |
| 40 | 88.9 | 98.7 |
| 50 | 82.9 | 93.6 |
| 60 | 77.4 | 88.1 |
| 70 | 72.4 | 81.9 |
| 80 | 67.8 | 75.1 |
| 90 | 63.3 | 67.5 |
| 100 | 59.3 | 59.3 |


| 0 | 146.0 | 146.0 |
| ---: | :---: | :---: |
| 10 | 139.2 | 141.1 |
| 20 | 132.5 | 135.8 |
| 30 | 125.85 | 130.4 |
| 40 | 119.25 | 124.8 |
| 50 | 113.0 | 119.1 |
| 60 | 107.0 | 113.1 |
| 70 | 101.2 | 106.8 |
| 80 | 95.55 | 100.0 |
| 90 | 90.25 | 92.9 |
| 100 | 85.5 | 85.5 |

Pressure. 570 P.S.I.A.

| 20 | 140.7 | 142.6 |
| ---: | ---: | ---: |
| 30 | 134.4 | 137.0 |
| 40 | 128.2 | 131.4 |
| 50 | 121.9 | 125.6 |
| 60 | 115.6 | 119.7 |
| 70 | 109.4 | 113.5 |
| 80 | 103.5 | 106.8 |
| 90 | 97.8 | 100.0 |
| 100 | 92.7 | 92.7 |

Pressure. 590 P.S.I.A.
Pressure. 400 P.S.I.A.

| 0 | 132.7 | 132.7 |
| ---: | :---: | ---: |
| 10 | 125.4 | 128.1 |
| 20 | 118.6 | 123.3 |
| 30 | 112.0 | 118.3 |
| 40 | 105.6 | 113.0 |
| 50 | 99.4 | 107.4 |
| 60 | 93.7 | 101.6 |
| 70 | 88.3 | 95.5 |
| 80 | 83.05 | 88.8 |
| 90 | 77.9 | 81.5 |
| 100 | 73.5 | 73.5 |


| Pressure. 550 P.S.I.A. |  |  |
| ---: | ---: | ---: |
| 0 | 152.2 | 152.2 |
| 10 | 145.5 | 146.5 |
| 20 | 138.8 | 140.9 |
| 30 | 132.3 | 135.3 |
| 40 | 125.6 | 129.7 |
| 50 | 119.3 | 124.0 |
| 60 | 113.2 | 118.0 |
| 70 | 107.2 | 111.6 |
| 80 | 101.4 | 104.8 |
| 90 | 95.8 | 97.7 |
| 100 | 90.4 | 90.4 |


| Pressure. 590 P.S.I.A. |  |  |
| :---: | :---: | ---: |
| 30.85 | 136.8 | 137.9 |
| 40 | 130.7 | 132.8 |
| 50 | 124.1 | 127.2 |
| 60 | 117.8 | 121.2 |
| 70 | 111.8 | 115.0 |
| 80 | 105.9 | 108.4 |
| 90 | 99.9 | 101.4 |
| 100 | 94.6 | 94.6 |
| Pressure. $625.0^{\circ}$ |  |  |
| P.S.I.A. |  |  |
| 82.6 | 108.1 | 108.1 |

[^0]Table III. Vapor-Liquid Equilibrium Ratios for Propane-n-Butane System

| $\begin{gathered} \text { Temp., } \\ \text { © } \mathrm{C} . \end{gathered}$ | Pressure, P.S.I.A. | $K_{\mathrm{C}_{2}}$ | $K_{\mathrm{C}_{4}}$ | Temp., ${ }^{\circ} \mathrm{C}$. | Pressure, P.S.I.A. | $K \mathrm{c}_{3}$ | $K_{\text {c }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 300 | 1.48 | 0.70 | 110 | 350 | 1.58 | 0.85 |
|  | 350 | 1.30 | 0.66 |  | 400 | 1.37 | 0.82 |
|  | 400 | 1.17 | 0.65 |  | 450 | 1.26 | 0.79 |
|  | 450 | 1.09 | 0.66 |  | 500 | 1.18 | 0.78 |
| 100 | 300 | 1.65 | 0.81 |  | 550 | 1.11 | 0.79 |
|  | 350 | 1.42 | 0.76 |  | 590 | 1.07 | 0.83 |
|  | 400 | 1.28 | 0.73 | 120 | 350 | 1.83 | 0.94 |
|  | 450 | 1.18 | 0.71 |  | 400 | 1.49 | 0.89 |
|  | 500 | 1.11 | 0.72 |  | 450 | 1.33 | 0.87 |
|  | 550 | 1.05 | 0.75 |  | 500 | 1.25 | 0.84 |
|  | 590 | 1.02 | 0.79 |  | 550 | 1.16 | 0.84 |
| 110 | 300 | 1.84 | 0.93 |  | 590 | 1.10 | 0.87 |

Table IV. Composition and Critical Constants of Propane-n-Butane Mixtures

| $\underset{\mathrm{C}_{3}}{\text { Mole }} \%$ | Critical Point |  |  | Point of Maximum Pressure |  |  | Point of Maximum Temperature |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} \text { Temp., } \\ T_{c}, \\ { }^{\circ} \mathrm{C} . \end{gathered}$ | Pressure, $P_{c}$, P.S.I.A | Density, <br> $p_{c}$, | Temp., <br> $T_{P},{ }_{\text {max }}$ <br> ${ }^{\circ} \mathrm{C}$. | Pressure, $P_{P}$, ${ }_{\text {max }}$ P.S.I.A. | Density, $\rho_{P},{ }_{\text {max }}$ <br> g./ce. | Temp. $T_{T}$, ${ }_{\text {max }}$ C. | Pressure, $P_{T}$, ${ }^{\text {max }}$ P.S.I.A. | Density, ${ }^{{ }_{T} T_{\text {max }}}$ g./cc. |
| 0 | $152.2^{\text {a }}$ | $550.8^{\text {a }}$ | 0.228 |  |  |  |  |  |  |
| 14.7 | 145.4 | 570.8 | 0.225 | 145.2 | 571.0 | 0.251 | 145.5 | 570.0 | 0.201 |
| 30.9 | 137.7 | 590.9 | 0.223 | 137.5 | 591.7 | 0.241 | 138.0 | 587.7 | 0.190 |
| 52.1 | 126.6 | 614.4 | 0.222 | 126.4 | 614.8 | 0.235 | 127.1 | 609.8 | 0.184 |
| 75.5 | 113.0 | 624.5 | 0.223 | 113.0 | 624.5 | 0.222 | 113.4 | 622.8 | 0.192 |
| 82.6 | 108.3 | 624.7 | 0.223 | 108.4 | 624.7 | 0.233 | 108.6 | 623.6 | 0.196 |
| 92.6 | 101.8 | 621.5 | 0.225 | 101.9 | 621.5 | 0.220 | 101.9 | 620.4 | 0.204 |
| 100 | $96.87^{\text {b }}$ | $617.9^{\text {b }}$ | $0.226^{6}$ |  |  |  |  |  |  |
| ${ }^{a}(3) . \quad{ }^{\text {b }}$ (2). |  |  |  |  |  |  |  |  |  |

Table V. Summary of Temperature, Pressure, and Density Relations for the Propane-n-Pentane System at the Phase Boundaries (8)

|  | Liquid |  | Vapor |  | Pressure, P.S.I.A. | Liquid |  | Vapor |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Pressure, P.S.I.A. | Temp., ${ }^{\circ} \mathrm{C}$. Composition | Density, g. /cc. <br> 14.70 Mol | Temp., ${ }^{\circ} \mathrm{C}$. | Density, g./ce. |  | $\begin{array}{r} \text { Temp., }{ }^{\circ} \mathrm{C} . \\ \text { Composition. } \end{array}$ | Density, g./ce. <br> 1.62 Mole | Temp., ${ }^{\circ} \mathrm{C}$. <br> \% Propane | Density, g./cc. |
| 100 |  |  | 103.4 |  | 300 | 85.3 | 0.480 | 118.2 |  |
| 150 | 101.0 | 0.520 | 121.2 |  | 350 | 95.1 | 0.462 | 124.6 |  |
| 200 | 117.0 | 0.497 | 134.8 |  | 400 | 103.5 | 0.444 |  |  |
| 250 | 131.5 | 0.474 | 146.5 |  | 450 | 111.5 | 0.424 | 134.8 | 0.085 |
| 300 | 143.4 | 0.451 | 155.8 |  | 500 | 118.8 | 0.404 | 139.4 | 0.100 |
| 350 | 153.2 | 0.430 | 164.4 | 0.075 | 550 | 126.2 | 0.380 | 143.2 | 0.119 |
| 400 | 162.1 | 0.406 | 172.0 | 0.093 | 600 | 132.9 | 0.352 | 146.2 | 0.145 |
| 450 | 170.8 | 0.378 | 179.0 | 0.117 | 650 | 140.8 | 0.299 | 146.8 | 0.155 |
| 500 | 179.2 | 0.341 | 184.7 | 0.147 | Composition. 78.62 Mole \% Propane |  |  |  |  |
| 510 | 180.8 | 0.332 | 185.8 | 0.157 |  |  |  |  |  |
| 520 | 182.5 | 0.320 | 186.6 | 0.170 | 150 |  |  | 71.2 |  |
| 530 | 184.2 | 0.302 | 187.2 | 0.186 | 200 | 52.2 | 0.491 | 81.6 | $\ldots$ |
| Composition. 38.73 Mole \% Propane |  |  |  |  | 250 | 63.5 | 0.474 | 90.2 |  |
|  |  |  |  |  | 300 | 73.2 | 0.458 | 97.5 |  |
| 100 |  |  | 90.9 |  | 350 | 81.6 | 0.442 | 104.0 | 0.056 |
| 150 | 67.9 | 0.5396 | 106.8 | $\ldots$ | 400 | 89.3 | 0.426 | 109.8 | 0.067 |
| 200 | 83.7 | 0.518 | 118.5 | . . | 450 | 96.5 | 0.408 | 115.2 | 0.079 |
| 250 | 96.7 | 0.499 | 128.1 |  | 500 | 103.2 | 0.389 | 119.9 | 0.094 |
| 300 | 108.4 | 0.4805 | 136.7 |  | 550 | 109.8 | 0.367 | 124.0 | 0.112 |
| 350 | 119.1 | 0.461 | 144.0 |  | 600 | 115.9 | 0.341 | 127.1 | 0.135 |
| 400 | 128.3 | 0.441 | 151.2 | 0.082 | 650 | 122.8 | 0.287 | 128.5 | 0.173 |
| 450 | 136.8 | 0.421 | 156.9 | 0.097 | Composition. 87.78 Mole \% Propane |  |  |  |  |
| 500 | 144.8 | 0.398 | 162.0 | 0.115 |  |  |  |  |  |
| 550 | 152.8 | 0.371 | 166.5 | 0.143 | 250 | 56.9 | 0.467 | 79.7 | $\ldots$ |
| 600 | 161.2 | 0.325 | 168.4 | 0.178 | 300 | 66.3 | 0.449 | 86.3 |  |
| 610 | 163.3 | 0.305 | 167.7 | 0.158 | 350 | 74.5 | 0.433 | 92.2 |  |
| Composition. 61.62 Mole \% Propane |  |  |  |  | 400 | 82.2 89.2 | 0.415 | 97.0 | 0.078 |
| 100 |  |  | 80.1 |  | 500 | 95.4 | 0.379 | 106.5 | 0.092 |
| 150 | 48.2 | 0.539 | 93.5 | . . | 550 | 101.3 | 0.357 | 110.5 | 0.110 |
| 200 | 62.3 | 0.518 | 103.2 | $\cdots$ | 600 | 107.1 | 0.328 | 113.9 | 0.135 |
| 250 | 74.5 | 0.499 | 111.6 | , . | 650 | 113.4 | 0.255 | 115.5 | 0.200 |

Table VI. Isobaric Temperature-Composition Relations of Propane-n-Pentane System

| Composition, Mole \% Propane | Liquid, ${ }^{\circ} \mathrm{C}$. | Vapor, ${ }^{\circ} \mathrm{C}$. | Composition, Mole \% Propane | Liquid, <br> ${ }^{\circ} \mathrm{C}$. | Vapor, ${ }^{\circ} \mathrm{C}$. | Composition, Mole \% Propane | Liquid, C. | Vapor, ${ }^{\circ} \mathrm{C}$. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Pressure. 300 P.S.I.A. |  |  | Pressure. 400 P.S.I.A. |  |  | Pressure. 600 P.S.I.A. |  |  |
|  |  |  | 50 | 114.9 | 140.9 |  |  |  |
| 0 | 165.2 | 165.2 | 60 | 105.0 | 131.1 | 33.7 | 171.1 | 171.1 |
| 10 | 150.4 | 157.94 | 70 | 96.1 | 120.6 | 38.73 | 161.4 | 168.4 |
| 20 | 135.7 | 150.6 | 80 | 88.1 | 108.1 | 40 | 159.4 | 167.2 |
| 30 | 121.1 | 142.8 | 90 | 80.4 | 92.9 | 50 | 146.1 | 158.0 |
| 40 | 106.6 | 134.7 | 100 | 73.0 | 73.0 | 60 | 134.5 | 148.2 |
| 50 | 95.4 | 126.7 | Pressure. 500 P.S.I.A. |  |  | 70 | 124.3 | 137.2 |
| 60 | 86.6 | 118.1 |  |  |  | 80 | 114.6 | 125.0 |
| 70 | 78.9 | 108.3 | 3.2 | 194.6 | 194.6 | 90 | 105.0 | 110.6 |
| 80 | 71.9 | 96.7 | 10 | 185.0 | 188.7 | 100 | 95.2 | 95.2 |
| 90 | 65.3 | 81.7 | 20 | 171.1 | 179.9 | 10 | 9.2 | 95.2 |
| 100 | 58.8 | 58.8 | 30 | 157.1 | 170.6 | Pressure. 650 P.S.I.A. |  |  |
| Pressure. 400 P.S.I.A. |  |  | 40 | 143.2 | 160.7 |  |  |  |
|  |  |  | 50 | 131.3 | 150.8 | 55 | 151.7 | 151.7 |
| 0 | 183.3 | 183.3 | 60 | 120.1 | 140.9 | 60 | 142.7 | 148.3 |
| 10 | 168.9 | 175.8 | 70 | 110.6 | 130.4 | 70 | 131.7 | 138.6 |
| 20 | 154.4 | 167.7 | 80 | 101.9 | 117.9 | 80 | 121.6 | 126.9 |
| 30 | 140.2 | 158.9 | 90 | 93.3 | 103.2 | 87.76 | 113.3 | 115.6 |
| 40 | 126.4 | 150.0 | 100 | 85.00 | 85.0 | 88.6 | 113.3 | 113.3 |

Table VII. Vapor-Liquid Equilibrium Ratios for Propane-n-Pentane System

| Temp., ${ }^{\circ} \mathrm{C}$. | Pressure, P.S.I.A. | $K \mathrm{c}_{3}$ | $K \mathrm{c}_{5}$ | $\begin{gathered} \text { Temp., } \\ { }^{\circ} \mathrm{C} . \end{gathered}$ | Pressure, P.S.I.A. | $K \mathrm{c}_{3}$ | $K_{\text {Cs }}$ | $\begin{aligned} & \text { Temp., } \\ & { }^{\circ} \mathrm{C} . \end{aligned}$ | Pressure, P.S.I.A. | $K_{\text {C3 }}$ | $K_{\text {cs }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 300 | 1.52 | 0.342 | 110 | 300 | 1.82 | 0.506 | 120 | 650 | 1.044 | 0.808 |
|  | 400 | 1.18 | 0.371 |  | 400 | 1.44 | 0.472 | 150 | 300 | 2.03 | 0.882 |
|  | 500 | 1.036 | 0.425 |  |  | 1.21 | 0.490 |  | 400 | 1.74 | 0.779 |
|  |  |  |  |  | $600$ | 1.067 | 0.627 |  | 500 | 1.45 | 0.757 |
| 100 | 300 | 1.69 | 0.416 | 120 | 300 | 1.88 | 0.609 |  | 600 | 1.24 | 0.791 |
|  | 400 | 1.31 | 0.417 |  | 400 | 1.85 | 0.541 |  | 650 | 1.05 | 0.933 |
|  | 500 | 1.12 | 0.458 |  | 500 | 1.30 | 0.544 | 180 | 400 | 1.96 | 0.976 |
|  | 600 | 1.02 | 0.626 |  | 600 | 1.125 | 0.634 |  | 500 | 1.46 | 0.928 |

Table VIII. Critical Constants of Propane-n-Pentane Mixtures

|  | Critical Point |  |  | Point of Maximum Pressure |  |  | Point of Maximum Temperature |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mole \% Propane | Temp., ${ }^{\circ} \mathrm{C}$. | Pressure, P.S.I.A. | $\begin{gathered} \text { Density, } \\ \text { g./ce. } \end{gathered}$ | $T_{P \text { max }}$ temp., C. | $\begin{aligned} & P_{P \max } \\ & \text { pressure, } \\ & \text { P.S.I.A. } \end{aligned}$ | Density, g. $/ \mathrm{cc}$. | $\underset{T_{T \max }}{\mathrm{Temp}_{2}}{ }^{\circ} \mathrm{C} .$ | $\begin{aligned} & P_{T} \max \\ & \text { P.S.I.A. } \end{aligned}$ | Density, g./cc. |
| 0 | $196.6^{\text {a }}$ | $489.7{ }^{\text {a }}$ | $0.232^{\text {a }}$ |  |  |  |  |  |  |
| 14.7 | 187.0 | 538.1 | 0.241 | 186.3 | 539.1 | 0.326 | 187.4 | 533.7 | 0.190 |
| 38.7 | 166.8 | 614.0 | 0.244 | 165.4 | 616.3 | 0.278 | 168.5 | 595.0 | 0.190 |
| 61.6 | 144.7 | 657.7 | 0.240 | 144.3 | 658.0 | 0.259 | 147.3 | 636.0 | 0.180 |
| 78.6 | 126.1 | 662.0 | 0.235 | 126.5 | 662.0 | 0.242 | 128.6 | 650.0 | 0.170 |
| 87.8 | 114.3 | 651.8 | 0.231 | 115.0 | 652.0 | 0.246 | 115.7 | 643.0 | 0.180 |
| 100 | $96.87{ }^{\text {b }}$ | $617.9^{\text {b }}$ | $0.226^{5}$ |  |  |  |  | . . . |  |

${ }^{a}(3) . \quad{ }^{b}(2)$.

The estimated error in the composition of the mixture prepared in this manner was about $0.5 \%$.

## EQUILIBRIUM DATA

The pressure-temperature and density-temperature diagrams for mixtures of constant composition, and the isobaric temperature-composition diagrams for propane-$n$-butane and propane- $n$-pentane systems are shown in Figures 1 through 6. From large plots of these figures, Tables I through VIII were constructed, giving smoothed values of the temperatures and densities at the bubble and dew points for mixtures of constant composition at regular intervals of pressure, the bubble and dew points
at regular intervals of the composition at a series of constant pressures, the vapor-liquid equilibrium ratio $K=y / x$, as a function of pressure at a series of selected temperatures, and the pressure, temperature, and density at the critical point, maximum pressure point, and maximum temperature points on the $P-T$ border curves for each of the mixtures of the two binary systems that were studied. The tables for each system are grouped together and appropriately marked. The critical point was determined visually by the disappearance-of-themeniscus method, whereas the pressure and temperature at the maximum pressure and maximum temperature points were obtained graphically from large plots of the
$P-T$ border curves in the critical region of the mixture. The accuracy of the tabulated data is estimated as follows: temperature, $\pm 0.5^{\circ} \mathrm{C}$.; pressure, $\pm 2.0$ p.s.i.; density, $\pm 0.001$ gram per cc. for the liquid and $\pm 0.0001$ gram per cc. for the vapor. However, in the critical region, the uncertainty in the values reported may be somewhat greater, because of the difficulty in assessing the accuracy of measurements in this region.

## COMPARISON OF RESULTS WITH LITERATURE DATA

The propane- $n$-butane system was studied by Nysewander et al. (7) and the propane-n-pentane system by Sage and Lacey (9). An apparatus similar to that employed in this study was used. In Table IX (deposited with ASIS) a comparison is made between the values of the temperature and pressure at the critical point, maximum pressure point, and maximum temperature point reported for these systems and those found in this study. The agreement is moderately good for both systems, but noticeably better for the propane- $n$-pentane system. Table X (deposited with ASIS) compares bubble and dew point data for the propane- $n$-butane system. The dew point pressures of mixtures of low propane content agree moderately well with those found in this study; for mixtures of high propane content, the agreement is less satisfactory. The bubble point pressures show fairly large deviations. This is due to the greater sensitivity of the bubble point pressure, compared to the dew point pressure, to small traces of noncondensable gas in the sample.

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Received for review April 10, 1969. Accepted October 3, 1969. For Tables IX and X, order NAPS Document NAPS00651 from ASIS National Auxiliary Publications Service, c/o CCM Information Sciences, Inc., 22 West 34th St., New York, N. Y. 10001 . Remit $\$ 1.00$ for microfiche or $\$ 3.00$ for photocopies.

# Low Temperature Heat Capacities of 15 Inorganic Compounds 

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#### Abstract

Smoothed low temperature heat capacities and derived thermodynamic functions for $\mathrm{KOH}, \mathrm{K}_{2} \mathrm{CO}_{3}, \mathrm{~K}_{2} \mathrm{SiO}_{3}, \mathrm{~K}_{2} \mathrm{~S}_{2} \mathrm{O}_{8}, \mathrm{KBH}_{4}, \mathrm{LiCl}, \mathrm{LiBO}_{2}, \mathrm{Li}_{2} \mathrm{SiO}_{3}, \mathrm{MgS}, \mathrm{Mg}\left(\mathrm{CO}_{2} \mathrm{H}\right)_{2}, \mathrm{P}_{4} \mathrm{O}_{10}$, $\mathrm{BPO}_{4}, \mathrm{SnSO}_{4}, \mathrm{Na}_{2} \mathrm{SiF}_{6}$, and $\mathrm{AlCl}_{3} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ are presented at even temperatures. Comparisons with literature data indicate the entropies at $298.15^{\circ} \mathrm{K}$. are accurate to at least $1 \%$. Such values are useful in thermodynamic calculations, as evidenced by comparison with estimates based on ion contributions.


DURING THE PAST DECADE and a half, the pioneer automatic adiabatic low-temperature calorimeter described by Stull (13) was used for the measurement of the heat capacity of a number of inorganic solids. The precision of measurement attained with this calorimeter was somewhat less than could be achieved with manually operated apparatus. Samples used were the best available within the time limitations of an industrial laboratory; in some cases this meant relatively low purity and in others incomplete characterization. Heat capacity measurements are not highly sensitive to impurities, however, and the smoothed heat capacity

[^1]data led to third-law entropies of good accuracy as shown by some comparisons with data from other laboratories. Therefore, although the measurements may not warrant a detailed account of individual data points, smoothed tables of thermodynamic functions at even temperatures should prove useful in thermodynamic calculations.

## MATERIALS

Reagent grade potassium hydroxide was dried under vacuum at $425^{\circ} \mathrm{C}$. Analysis by acid titration indicated $97.8 \% \mathrm{KOH}$ and $2.2 \% \mathrm{~K}_{2} \mathrm{CO}_{3}$.

Reagent grade potassium carbonate was dried at $300^{\circ} \mathrm{C}$. The manufacturer's analysis indicating $99.9 \%$ purity was accepted.

A sample of potassium metasilicate was prepared from


[^0]:    a Maximum critical pressure for propane-n-butane system.

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