

$A_1 = \int_0^1 \ln \gamma_1 dx_1$
 $A_2 = \int_0^1 \ln \gamma_2 dx_1$
 $A_H = \int_{x=0}^{x=1} (\Delta H/RT^2) dT$
 $\Delta A = A_1 - (A_2 + A_H)$
 ΣA = area sum as defined in Table V
 B_{11} = second virial coefficient for pure component 1
 B_{22} = second virial coefficient for pure component 2
 B_{12} = second virial cross coefficient
 ΔH = molar enthalpy of mixing, J/g mol
 P = total pressure
 P_1^0, P_2^0 = vapor pressures of pure components 1, 2
 R = gas constant
 T = temperature, °K
 v_1^L, v_2^L = pure component liquid molar volumes, cc/g mol
 x_1, x_2 = mole fractions of components 1, 2 in liquid phase
 y_1, y_2 = mole fractions of components 1, 2 in vapor phase

GREEK LETTERS

α^{12} = relative volatility
 γ_1, γ_2 = liquid-phase activity coefficients of components 1, 2
 $\delta_{12} = 2 B_{12} - B_{11} - B_{22}$

SUBSCRIPTS

1 = component 1
 2 = component 2
 i = component 1 or component 2

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Emf Measurements in Additive Ternary Molten Salt Systems $\text{PbCl}_2\text{-KCl-NaCl}$ and $\text{PbCl}_2\text{-CsCl-NaCl}$

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Emf measurements in the binary molten systems, $\text{PbCl}_2\text{-NaCl}$, $\text{PbCl}_2\text{-KCl}$, and $\text{PbCl}_2\text{-CsCl}$, and in the ternary systems, $\text{PbCl}_2\text{-NaCl-KCl}$ and $\text{PbCl}_2\text{-NaCl-CsCl}$, were made at mole fractions of PbCl_2 of 0.5 and 0.3. Our data (as well as some previous data) on excess free energies of solution in the three binary systems are consistent with the equation first suggested by Førlund (Equation 1) in terms of equivalent fractions, with the coefficients $\lambda = -1800, -10,300, \text{ and } -15,500 \text{ cal/mol}$ for the mixtures with NaCl , KCl , and CsCl , respectively. Measurements of $\bar{G}_{\text{PbCl}_2}^E$ at constant mole fractions of PbCl_2 in the ternary systems exhibited small negative deviations from additivity.

In this paper we present electromotive force measurements and partial molar quantities for PbCl_2 in the three binary systems $\text{PbCl}_2\text{-NaCl}$, $\text{PbCl}_2\text{-KCl}$, and $\text{PbCl}_2\text{-CsCl}$, and in the

two ternary systems, $\text{PbCl}_2\text{-NaCl-KCl}$ and $\text{PbCl}_2\text{-NaCl-CsCl}$, at mole fractions of PbCl_2 of 0.5 and 0.3. A critique of previous work on the binary systems is given, and we show that the simplest representation of the data on the activity coefficients, γ , and the partial molar excess free energy, \bar{G}^E , of PbCl_2 has a form first suggested for the binaries by Førlund (2, 6):

$$\bar{G}_{\text{PbCl}_2}^E = RT \ln \gamma_{\text{PbCl}_2} = \lambda(1 - N_{\text{PbCl}_2})^2 \quad (1)$$

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where N_{PbCl_2} is the equivalent fraction of PbCl_2 defined by the relationship

$$N_{\text{PbCl}_2} = \frac{2 N_{\text{PbCl}_2}}{2 N_{\text{PbCl}_2} + N_{\text{ACl}}} = \frac{2 n_{\text{PbCl}_2}}{2 n_{\text{PbCl}_2} + n_{\text{ACl}}}$$

where N designates mole fraction, n the number of moles, and ACl alkali chloride. Values of \bar{G}_{PbCl_2} in the ternary systems at constant mole fraction of PbCl_2 exhibit negative deviations from additive behavior. These data will be analyzed in terms of the thermodynamic treatment we have utilized previously (7, 8).

Previous work on PbCl_2 -containing systems include emf measurements of the activities of PbCl_2 in the binary systems PbCl_2 - NaCl and PbCl_2 - KCl (11, 13, 14) vapor pressure and transpiration measurements in the PbCl_2 - KCl and PbCl_2 - CsCl systems (1, 3) and calorimetric measurements of enthalpies of mixing of PbCl_2 with all the alkali halides (15). The only prior measurements in the ternary systems are for a 48-36-16 mol % PbCl_2 - KCl - NaCl mixture (4) and a dilute solution of PbCl_2 in equimolar NaCl - KCl (5).

Systematic emf studies of ternary molten salt mixtures have been seldom reported. Partial molar excess properties of NiCl_2 in 1:1 molar NaCl - KCl have been reported (10) and the ternary systems AgCl - NaCl - KCl and AgCl - NaCl - CsCl have been studied.

EXPERIMENTAL

The measurements were carried out in the reversible formation cell graphite, $\text{Pb}|\text{PbCl}_2 + \text{ACl}|\text{Cl}_2$, graphite, ($\text{A} = \text{Na}, \text{K}, \text{Cs}, \text{Na-K}, \text{Na-Cs}$) which has provided reliable emf data for the free energy of formation of PbCl_2 . The construction of the cell is identical to the one previously described (9). Except for CsCl (Penn Rare Metals, 99.9% pure), the chemicals were Baker "Analyzed" reagents and were used without any further purification. The Cl_2 gas was 99.5% pure from Matheson Co. and was bubbled through H_2SO_4 prior to being passed into the chlorine electrode.

The composition of the salt mixture was calculated from the weighed-out portions of the salts, and in some cases they were checked by wet chemical analysis after the experiments. (Lead was done by back titration with Ca^{2+} after addition of excess EDTA. Na, K, and Cs were done by flame emission spectroscopy.) Although vaporization was observed, the concentration did not change significantly during an experiment (less than ± 1 mol %). To check the electrodes, emf measurements were frequently checked in pure PbCl_2 . The contamination of these electrodes by their handling and exposure to oxygen upon opening and closing of the cell compartment led to emf values for pure PbCl_2 which differed by 1.0-2.6 mV from measurements made by using lead carefully purified by acid washing.

The absolute values of the emf given here have been corrected for this measured difference, which is due to impurities in the lead and should be the same for all cells for a given impurity level. The solution properties calculated from differences of emf values are, of course, unaffected by this shift. The emf measurements were calibrated with a standard Eppley cell and the platinum-platinum-10% rhodium thermocouple was calibrated vs. a standard thermocouple to $\pm 0.2^\circ\text{C}$. Measurements were made to $\pm 1^\circ\text{C}$.

RESULTS

Ternary mixtures of PbCl_2 - NaCl - KCl and PbCl_2 - NaCl - CsCl were examined at compositions N_{PbCl_2} equals 0.5 and 0.3. The ratio $x = n_{\text{NaCl}}/(n_{\text{NaCl}} + n_{\text{ACl}})$ was chosen equal to 0, 0.25, 0.5, 0.75, and 1.0. Data for the emf as a function of temperature are shown in Figures 1-4, where it is noted that at least two separate sets of measurements were made for each composition. The temperature range of the measurements

was chosen well above the liquidus temperature to ensure that the salt mixture was completely molten; this explains the higher temperatures for the mixtures high in NaCl , or low in PbCl_2 . The data are also given in Table I. A least-squares

Table I. Measured Values of Emf in Systems PbCl_2 - NaCl - KCl and PbCl_2 - NaCl - CsCl

| 50 PbCl_2 -50 KCl | | 50 PbCl_2 -12.5 KCl -37.5 NaCl | |
|---|--------|---|--------|
| $T, ^\circ\text{C}$ | Emf, V | $T, ^\circ\text{C}$ | Emf, V |
| 594.5 | 1.2733 | 650.5 | 1.2251 |
| 606.2 | 1.2682 | 643.1 | 1.2290 |
| 599.8 | 1.2728 | 671.1 | 1.2142 |
| 589.2 | 1.2784 | 643.3 | 1.2309 |
| 577.0 | 1.2863 | 668.3 | 1.2168 |
| 567.5 | 1.2909 | 629.1 | 1.2379 |
| 558.4 | 1.2953 | 659.8 | 1.2208 |
| 557.4 | 1.2968 | 633.9 | 1.2346 |
| 562.0 | 1.2933 | ... | ... |
| 569.9 | 1.2884 | 637.4 | 1.2341 |
| 582.2 | 1.2813 | 620.1 | 1.2428 |
| 590.2 | 1.2764 | 645.8 | 1.2298 |
| 601.8 | 1.2699 | 663.5 | 1.2205 |
| 597.7 | 1.2723 | 669.6 | 1.2171 |
| ... | ... | 657.5 | 1.2233 |
| 564.3 | 1.2922 | 628.0 | 1.2400 |
| 551.0 | 1.2999 | 652.1 | 1.2264 |
| 567.1 | 1.2912 | 50 PbCl_2 -50 NaCl | |
| 583.5 | 1.2805 | 672.3 | 1.2092 |
| 593.6 | 1.2741 | 652.9 | 1.2194 |
| 580.9 | 1.2825 | 640.2 | 1.2262 |
| 571.8 | 1.2871 | 622.3 | 1.2355 |
| 555.7 | 1.2965 | 672.8 | 1.2100 |
| 578.0 | 1.2836 | 639.6 | 1.2269 |
| 600.1 | 1.2712 | 620.9 | 1.2365 |
| 50 PbCl_2 -37.5 KCl -12.5 NaCl | | ... | ... |
| 597.7 | 1.2678 | 670.5 | 1.2103 |
| 590.0 | 1.2729 | 652.2 | 1.2199 |
| 581.1 | 1.2776 | 620.8 | 1.2333 |
| 567.7 | 1.2848 | 636.2 | 1.2283 |
| 553.3 | 1.2932 | 661.6 | 1.2150 |
| 568.5 | 1.2847 | 645.8 | 1.2227 |
| 584.1 | 1.2755 | 30 PbCl_2 -70 KCl | |
| 593.6 | 1.2701 | 686.6 | 1.2782 |
| 598.6 | 1.2668 | 689.0 | 1.2771 |
| 573.5 | 1.2816 | 699.6 | 1.2721 |
| ... | ... | 679.0 | 1.2827 |
| 604.7 | 1.2635 | 672.6 | 1.2856 |
| 592.5 | 1.2708 | 664.4 | 1.2898 |
| 582.0 | 1.2770 | 658.2 | 1.2926 |
| 572.3 | 1.2824 | 652.8 | 1.2955 |
| 50 PbCl_2 -25 KCl -25 NaCl | | 650.7 | 1.2966 |
| 595.0 | 1.2640 | 656.1 | 1.2942 |
| 603.8 | 1.2589 | 663.6 | 1.2906 |
| 586.9 | 1.2679 | ... | ... |
| 579.2 | 1.2723 | 683.4 | 1.2821 |
| 574.8 | 1.2746 | 679.0 | 1.2842 |
| 566.2 | 1.2792 | 669.7 | 1.2895 |
| 558.3 | 1.2843 | 660.4 | 1.2943 |
| 553.0 | 1.2874 | 653.9 | 1.2982 |
| 561.8 | 1.2825 | 663.3 | 1.2926 |
| 570.1 | 1.2777 | 667.6 | 1.2900 |
| 579.0 | 1.2725 | 675.5 | 1.2855 |
| 588.8 | 1.2664 | 681.2 | 1.2839 |
| ... | ... | 689.3 | 1.2798 |
| 637.7 | 1.2286 | 696.7 | 1.2763 |
| 644.9 | 1.2357 | 684.6 | 1.2813 |
| 627.3 | 1.2459 | 684.7 | 1.2821 |
| 615.5 | 1.2524 | 30 PbCl_2 -52.5 KCl -17.5 NaCl | |
| 666.9 | 1.2239 | 689.5 | 1.2704 |
| 636.1 | 1.2405 | 693.4 | 1.2683 |
| 653.1 | 1.2302 | 695.8 | 1.2670 |
| 585.8 | 1.2683 | ... | ... |

(Continued on next page)

fit of the data to an equation of the form

$$E(V) = a + b(t - t_0) \quad (2)$$

led to the coefficients in Table II. The standard deviations were generally less than 1 mV and always less than 2 mV.

In each case t_0 (in °C) is chosen close to the average temperature of the series of measurements. To make an isothermal comparison of the data, values for the emf were obtained by a linear extrapolation (or interpolation) to an intermediate temperature, 625°C. The emf value of the formation cell for pure $PbCl_2$, E° at 625°C was obtained by a short extrapolation.

Table I. (Continued)

| 30 $PbCl_2$ -52.5 KCl-1.75 NaCl (Contd.) | | 30 $PbCl_2$ -17.5 KCl-52.5 NaCl (Contd.) | | 50 $PbCl_2$ -37.5 CsCl-12.5 NaCl (Contd.) | | 30 $PbCl_2$ -52.5 CsCl-17.5 NaCl (Contd.) | |
|---|--------|---|--------|--|--------|--|--------|
| $T, ^\circ C$ | Emf, V | $T, ^\circ C$ | Emf, V | $T, ^\circ C$ | Emf, V | $T, ^\circ C$ | Emf, V |
| 692.9 | 1.2685 | 659.5 | 1.2561 | 679.0 | 1.2365 | 658.4 | 1.3096 |
| 687.2 | 1.2722 | 664.4 | 1.2525 | 630.1 | 1.2596 | 664.1 | 1.3068 |
| 682.3 | 1.2738 | 672.3 | 1.2485 | | | 683.6 | 1.2978 |
| 680.8 | 1.2748 | 678.1 | 1.2458 | 654.4 | 1.2466 | 701.0 | 1.2890 |
| 676.6 | 1.2770 | 685.3 | 1.2423 | 668.2 | 1.2395 | 688.5 | 1.2960 |
| 667.1 | 1.2817 | 690.9 | 1.2396 | 644.1 | 1.2511 | 676.7 | 1.2921 |
| 650.5 | 1.2895 | 681.8 | 1.2445 | 638.4 | 1.2549 | 656.8 | 1.3109 |
| 654.5 | 1.2875 | 676.4 | 1.2472 | 625.5 | 1.2605 | 670.9 | 1.3035 |
| 661.1 | 1.2851 | | | 659.8 | 1.2433 | 693.7 | 1.2929 |
| | | 685.9 | 1.2425 | | | 668.5 | 1.3048 |
| 678.4 | 1.2759 | 667.8 | 1.2515 | 50 $PbCl_2$ -25 CsCl-25 NaCl | | | |
| 663.9 | 1.2841 | 660.0 | 1.2556 | 662.9 | 1.2355 | 673.0 | 1.3034 |
| 659.5 | 1.2856 | 664.2 | 1.2526 | 674.2 | 1.2297 | 648.5 | 1.3143 |
| 650.2 | 1.2902 | 671.9 | 1.2484 | 648.6 | 1.2430 | 662.7 | 1.3081 |
| 657.2 | 1.2856 | 682.5 | 1.2436 | 663.2 | 1.2350 | 691.5 | 1.2942 |
| 670.0 | 1.2795 | 695.8 | 1.2351 | 679.7 | 1.2273 | 680.5 | 1.2996 |
| 678.4 | 1.2756 | 690.0 | 1.2392 | 655.2 | 1.2396 | 655.7 | 1.3112 |
| 688.1 | 1.2712 | 678.0 | 1.2459 | 630.2 | 1.2509 | | |
| 699.8 | 1.2651 | 650.5 | 1.2597 | 622.3 | 1.2545 | 30 $PbCl_2$ -35 CsCl-35 NaCl | |
| 688.5 | 1.2717 | | | | | 650.2 | 1.2914 |
| | | 30 $PbCl_2$ -70 NaCl | | 646.1 | 1.2428 | 656.7 | 1.2882 |
| | | 692.7 | 1.2222 | 677.4 | 1.2267 | 665.8 | 1.2837 |
| 30 $PbCl_2$ -35 KCl-35 NaCl | | 697.7 | 1.2201 | 668.6 | 1.2313 | 681.7 | 1.2765 |
| 691.1 | 1.2526 | 684.6 | 1.2270 | 633.7 | 1.2488 | 691.6 | 1.2715 |
| 687.5 | 1.2549 | 676.6 | 1.2314 | 656.6 | 1.2370 | 699.0 | 1.2686 |
| 683.3 | 1.2572 | 671.4 | 1.2341 | | | 686.4 | 1.2752 |
| 679.2 | 1.2592 | 667.8 | 1.2362 | 50 $PbCl_2$ -12.5 CsCl-37.5 NaCl | | 673.8 | 1.2816 |
| 673.6 | 1.2622 | 664.8 | 1.2379 | 625.7 | 1.2506 | 681.9 | 1.2763 |
| 669.4 | 1.2644 | 655.4 | 1.2427 | 656.8 | 1.2338 | 698.0 | 1.2686 |
| 662.7 | 1.2677 | | | 680.0 | 1.2209 | 685.6 | 1.2749 |
| 656.7 | 1.2710 | 692.3 | 1.2224 | 669.6 | 1.2260 | 671.7 | 1.2819 |
| 649.3 | 1.2747 | 689.2 | 1.2242 | 649.6 | 1.2361 | 657.6 | 1.2886 |
| 644.7 | 1.2770 | 675.3 | 1.2321 | 630.0 | 1.2469 | 610.5 | 1.2817 |
| 647.9 | 1.2754 | 663.0 | 1.2388 | 617.5 | 1.2540 | | |
| 654.3 | 1.2722 | 657.6 | 1.2417 | 641.0 | 1.2414 | 671.9 | 1.2809 |
| 660.3 | 1.2693 | 651.9 | 1.2448 | 660.6 | 1.2306 | 660.0 | 1.2866 |
| 667.1 | 1.2662 | 655.1 | 1.2433 | | | 648.5 | 1.2923 |
| 677.6 | 1.2609 | 667.6 | 1.2360 | 630.5 | 1.2474 | 682.0 | 1.2763 |
| | | 682.0 | 1.2286 | 665.5 | 1.2289 | 697.0 | 1.2691 |
| 684.6 | 1.2558 | 687.5 | 1.2257 | 678.9 | 1.2209 | 688.4 | 1.2733 |
| 673.8 | 1.2612 | 695.5 | 1.2213 | 671.8 | 1.2254 | | |
| 652.1 | 1.2722 | | | 651.1 | 1.2356 | 30 $PbCl_2$ -17.5 CsCl-52.5 NaCl | |
| 640.5 | 1.2779 | 50 $PbCl_2$ -50 CsCl | | 640.1 | 1.2418 | 686.6 | 1.2567 |
| 644.7 | 1.2753 | 678.4 | 1.2395 | 653.7 | 1.2355 | 698.2 | 1.2508 |
| 657.1 | 1.2695 | 661.0 | 1.2487 | 646.0 | 1.2387 | 685.9 | 1.2559 |
| 673.1 | 1.2610 | 642.7 | 1.2584 | | | 671.2 | 1.2627 |
| 684.1 | 1.2562 | | | 30 $PbCl_2$ -70 CsCl | | 663.5 | 1.2672 |
| 688.4 | 1.2536 | 625.7 | 1.2669 | 676.7 | 1.3207 | 656.5 | 1.2706 |
| 699.1 | 1.2477 | 644.8 | 1.2565 | 688.6 | 1.3152 | 668.7 | 1.2645 |
| 694.1 | 1.2499 | 662.4 | 1.2474 | 673.5 | 1.3229 | 682.9 | 1.2575 |
| 690.9 | 1.2517 | 679.9 | 1.2387 | 663.0 | 1.3286 | 691.9 | 1.2522 |
| 687.6 | 1.2537 | 667.6 | 1.2454 | 672.2 | 1.3234 | 679.8 | 1.2580 |
| 683.2 | 1.2557 | 656.9 | 1.2505 | | | | |
| 679.2 | 1.2579 | 650.1 | 1.2539 | 669.6 | 1.3257 | 677.6 | 1.2582 |
| 670.0 | 1.2625 | 635.2 | 1.2611 | 700.0 | 1.3099 | 663.6 | 1.2654 |
| 662.9 | 1.2666 | 613.2 | 1.2732 | 692.0 | 1.3139 | 649.0 | 1.2733 |
| 658.0 | 1.2681 | 631.4 | 1.2639 | 680.5 | 1.3195 | 671.7 | 1.2612 |
| 676.5 | 1.2589 | | | 663.8 | 1.3276 | 688.1 | 1.2531 |
| 686.5 | 1.2537 | 50 $PbCl_2$ -37.5 CsCl-12.5 NaCl | | 654.8 | 1.3317 | 700.5 | 1.2467 |
| 695.3 | 1.2496 | 650.2 | 1.2493 | 648.5 | 1.3358 | 686.5 | 1.2542 |
| | | 672.7 | 1.2387 | 689.0 | 1.3162 | 673.1 | 1.2610 |
| 30 $PbCl_2$ -17.5 KCl-52.5 NaCl | | 655.3 | 1.2477 | 700.5 | 1.3100 | 656.8 | 1.2693 |
| 687.9 | 1.2407 | 632.5 | 1.2591 | 640.7 | 1.3393 | 680.3 | 1.2570 |
| 692.0 | 1.2381 | 614.0 | 1.2678 | 30 $PbCl_2$ -52.5 CsCl-17.5 NaCl | | 698.0 | 1.2486 |
| 694.3 | 1.2371 | 643.8 | 1.2517 | 650.9 | 1.3142 | 689.1 | 1.2526 |
| 663.6 | 1.2527 | 667.1 | 1.2417 | | | | |

tion of the values for E° in the range 500–620°C from a previous paper (9).

The activity of a component, i , in solution (here, $i = \text{PbCl}_2$), a_i , may be defined through the relationship

$$RT \ln a_i = \bar{G}_i - \bar{G}_i^\circ = -2F(E - E^\circ) \quad (3)$$

where R is the gas constant in cal/mol-degree, T is the temperature in degrees Kelvin, $\bar{G}_i - \bar{G}_i^\circ$ is the partial molar free energy of solution of PbCl_2 ; the Faraday constant, $F = 23,062$ cal/V, and $E - E^\circ$ is the difference in emf between a cell

containing i in solution and a cell containing pure i , respectively. The activity coefficient, γ_i , is related to the activity by Equation 4:

$$\gamma_i = a_i/N_i \quad (4)$$

where N_i is the mole fraction of PbCl_2 in the system. The partial molar excess free energy,

$$\bar{G}_i^E \equiv RT \ln \gamma_i = \bar{G}_i - G_i^\circ - RT \ln N_i \quad (5)$$

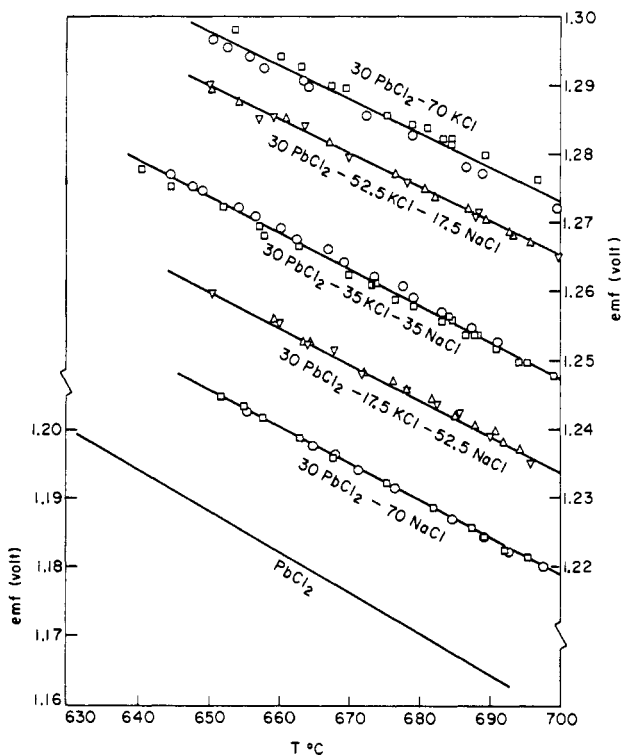


Figure 1. Emf vs. temperature in PbCl_2 - NaCl - KCl system

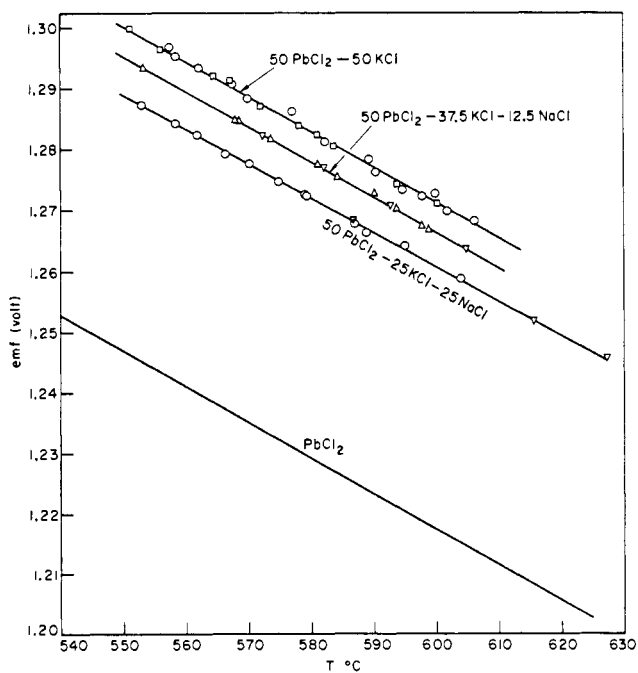


Figure 2. Emf vs. temperature in PbCl_2 - NaCl - KCl system

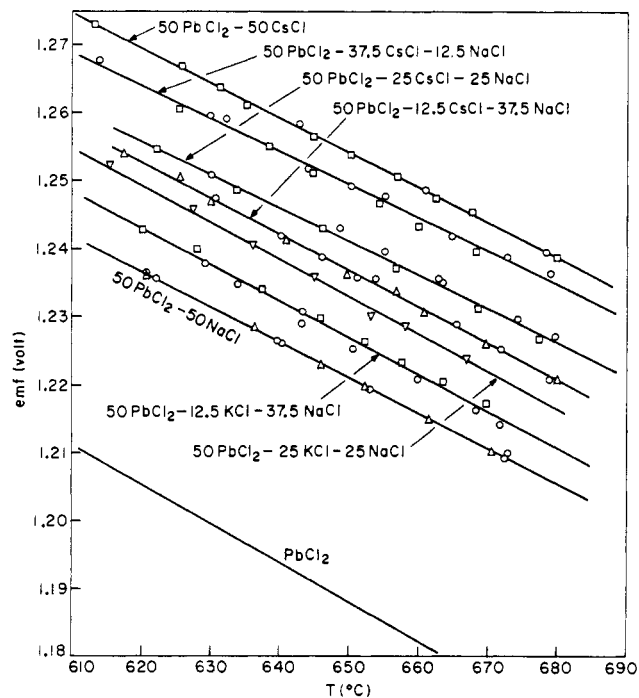


Figure 3. EMF vs. temperature in PbCl_2 - NaCl - CsCl system

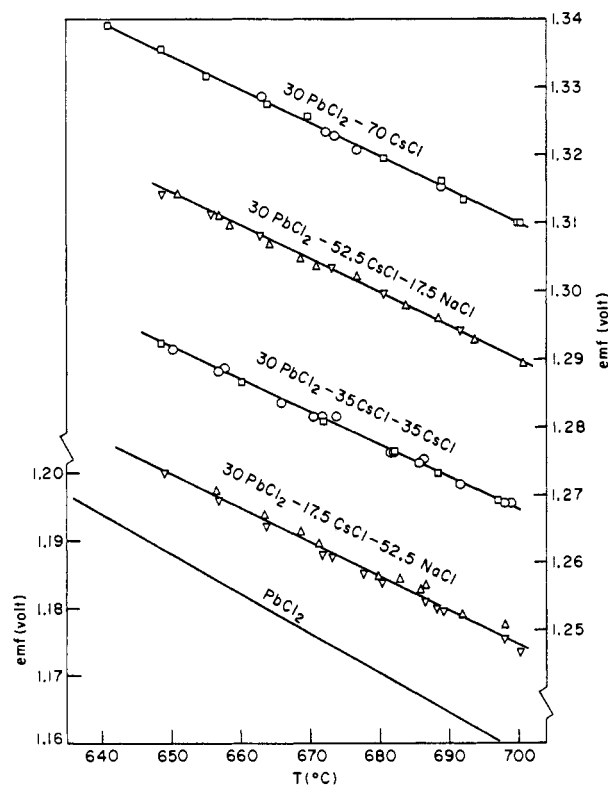


Figure 4. EMF vs. temperature in PbCl_2 - NaCl - CsCl system

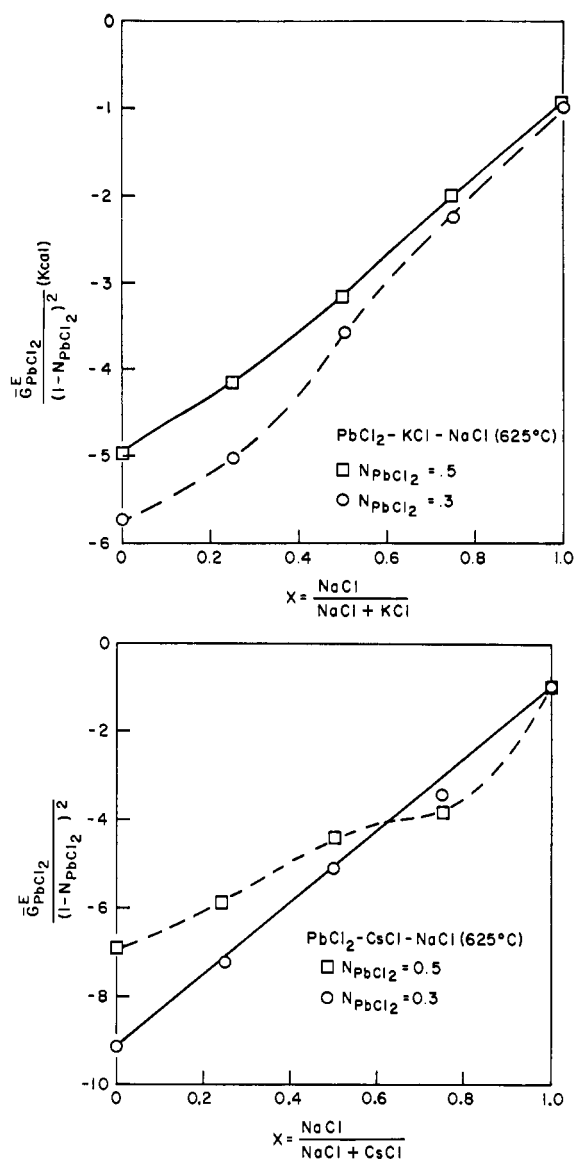


Figure 5. Top, free energy function at constant N_{PbCl_2} in $\text{PbCl}_2\text{-NaCl-KCl}$ system at 625°C . Bottom, free energy function at constant N_{PbCl_2} in the $\text{PbCl}_2\text{-NaCl-CsCl}$ system at 625°C

Values of $\bar{G}_{\text{PbCl}_2}^E$ at 625°C are given in the last column of Table II.

In Figures 5a and 5b, $\bar{G}_{\text{PbCl}_2}^E/(1 - N_{\text{PbCl}_2})^2$ is shown as a function of x at constant N_{PbCl_2} . With an uncertainty of ± 1 mV in $E - E^\circ$, the error in $\bar{G}_{\text{PbCl}_2}^E/(1 - N_{\text{PbCl}_2})^2$ is ± 200 cal at $N = 0.5$ and ± 100 cal at $N_{\text{PbCl}_2} = 0.3$. Within the limits of experimental error, $\bar{G}_{\text{PbCl}_2}^E/(1 - N_{\text{PbCl}_2})^2$ is not a linear function of x at constant N_{PbCl_2} . In the systems $\text{PbCl}_2\text{-NaCl-KCl}$, the negative deviation from linearity seems to be greater at smaller values of x , whereas the opposite is observed to be the case in the system $\text{PbCl}_2\text{-NaCl-CsCl}$ where the negative deviation is at x close to 1. A short extrapolation of the emf measurements of Delimarskii and Roms (4) for the 48 mol % $\text{PbCl}_2\text{-36\% KCl-16\% NaCl}$ systems gives $\bar{G}_{\text{PbCl}_2}^E/(1 - N_{\text{PbCl}_2})^2 = -4800$ cal for $x = 0.31$ and $N = 0.5$ at 625°C . This is 900 cal more negative than is calculated in the present work, although it supports the negative deviation from linearity observed in Figure 5a.

DISCUSSION

Measured values of $\bar{G}_{\text{PbCl}_2}^E$ in the three binary systems are plotted in Figure 6 vs. $(1 - N_{\text{PbCl}_2})^2$. Our measurements

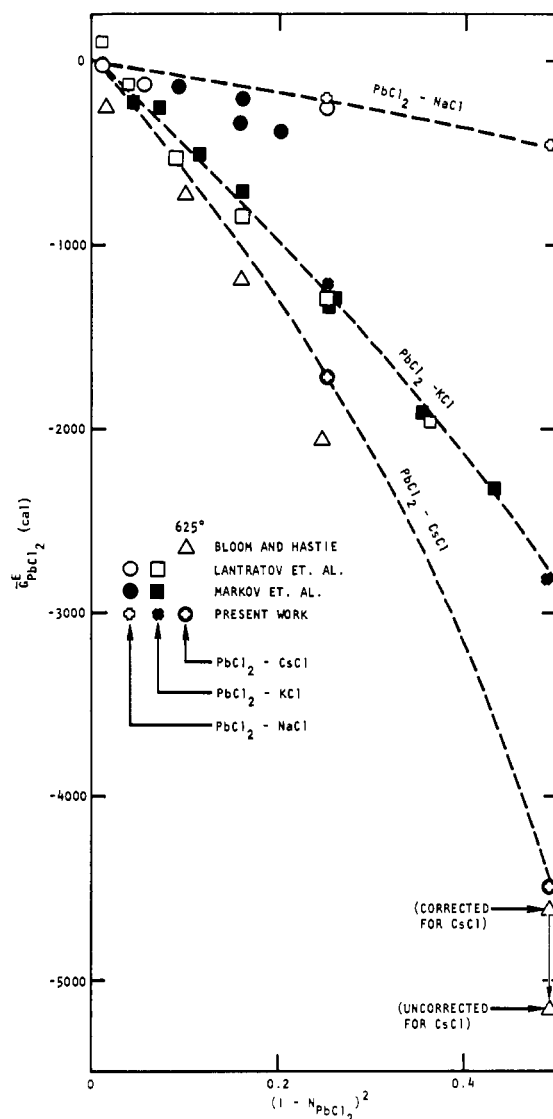


Figure 6. Plot of $\bar{G}_{\text{PbCl}_2}^E$ vs. $(1 - N_{\text{PbCl}_2})^2$ at 625°C

on the $\text{PbCl}_2\text{-NaCl}$ and $\text{PbCl}_2\text{-KCl}$ systems are consistent with those of Lantratov and Alabyshev (13) and those of Markov et al. (14). The vapor pressure measurements in the $\text{PbCl}_2\text{-KCl}$ system by Barton and Bloom (1) are inconsistent with the other results and were not plotted. The transpiration measurement of Bloom and Hastie (3) on the $\text{PbCl}_2\text{-CsCl}$ system are plotted in Figure 6 and differ from ours. Re-examination of their data reveals two possible reasons for these discrepancies. First, the measurements at $N_{\text{PbCl}_2} = 0.299$ were uncorrected for a significant partial pressure of the species CsCl indicating a higher activity of PbCl_2 than they report. Second, they used a value for the pressure of pure PbCl_2 at 650°C of 9.860 mm which is higher than the value given in the JANAF Tables (12). If their points are thus corrected, they correspond closely to our emf measurements.

The curvature of the plots of $\bar{G}_{\text{PbCl}_2}^E$ in Figure 6 suggests the dependence upon concentration first suggested by Førlund (6) and given in Equation 1. A replot of the data vs. $(1 - N_{\text{PbCl}_2})^2$ in Figure 7 indicates no curvature within experimental precision and supports this form for these data with $\lambda = -1800, -10,300,$ and $-15,500$ cal/mol for the $\text{PbCl}_2\text{-NaCl}$, $\text{PbCl}_2\text{-KCl}$, and $\text{PbCl}_2\text{-CsCl}$ systems, respectively. Values of $\bar{H}_{\text{PbCl}_2}^E$ were calculated from the data of McCarty and Kleppa (15), and with values of $\bar{G}_{\text{PbCl}_2}^E$ at 665°C from our data, we calculated the small values of $\bar{S}_{\text{PbCl}_2}^E$ given in Table III, which are consistent with findings in many other systems.

Table II. Least Squares Fit to Emf Data and Partial Molar Excess Free Energy of PbCl₂ at 625°C

| System | Emf, V | | $\bar{G}_{\text{PbCl}_2}^E$ (625°C), cal/mol |
|--------------------------------------|-----------------------------|-----------------------|---|
| | a + b | (t - t ₀) | |
| 50 PbCl ₂ -50 KCl-0 NaCl | 1.2858-585·10 ⁻⁶ | (t - 575) | -1240 |
| -37.5 KCl-12.5 NaCl | 1.2809-576·10 ⁻⁶ | (t - 575) | -1040 |
| -25 KCl-25 NaCl | 1.2748-562·10 ⁻⁶ | (t - 575) | -790 |
| -25 KCl-25 NaCl | 1.2329-556·10 ⁻⁶ | (t - 650) | ... |
| -12.5 KCl-37.5 NaCl | 1.2269-540·10 ⁻⁶ | (t - 650) | -500 |
| -0 KCl-50 NaCl | 1.2211-521·10 ⁻⁶ | (t - 650) | -210 |
| 30 PbCl ₂ -70 KCl-0 NaCl | 1.2837-490·10 ⁻⁶ | (t - 675) | -2810 |
| -52.5 KCl-17.5 NaCl | 1.2777-497·10 ⁻⁶ | (t - 675) | -2450 |
| -35 KCl-35 NaCl | 1.2607-526·10 ⁻⁶ | (t - 675) | -1740 |
| -17.5 KCl-52.5 NaCl | 1.2468-523·10 ⁻⁶ | (t - 675) | -1100 |
| -0 KCl-70 NaCl | 1.2323-545·10 ⁻⁶ | (t - 675) | -470 |
| 50 PbCl ₂ -50 CsCl-0 NaCl | 1.2541-516·10 ⁻⁶ | (t - 650) | -1720 |
| -37.5 CsCl-12.5 NaCl | 1.2494-488·10 ⁻⁶ | (t - 650) | -1480 |
| -50 CsCl-50 NaCl | 1.2412-488·10 ⁻⁶ | (t - 650) | -1100 |
| -12.5 CsCl-37.5 NaCl | 1.2368-535·10 ⁻⁶ | (t - 650) | -950 |
| 30 PbCl ₂ -70 CsCl-0 NaCl | 1.3223-493·10 ⁻⁶ | (t - 675) | -4500 |
| -52.5 CsCl-17.5 NaCl | 1.3020-480·10 ⁻⁶ | (t - 675) | -3530 |
| -35 CsCl-35 NaCl | 1.2798-474·10 ⁻⁶ | (t - 675) | -2500 |
| -17.5 CsCl-52.5 NaCl | 1.2605-499·10 ⁻⁶ | (t - 675) | -1670 |
| 100 PbCl ₂ | 1.2320·596·10 ⁻⁶ | (t - 575) | |
| | 1.2028-585·10 ⁻⁶ | (t - 625) | |
| | 1.1881-580·10 ⁻⁶ | (t - 650) | |
| | 1.1734-575·10 ⁻⁶ | (t - 675) | |

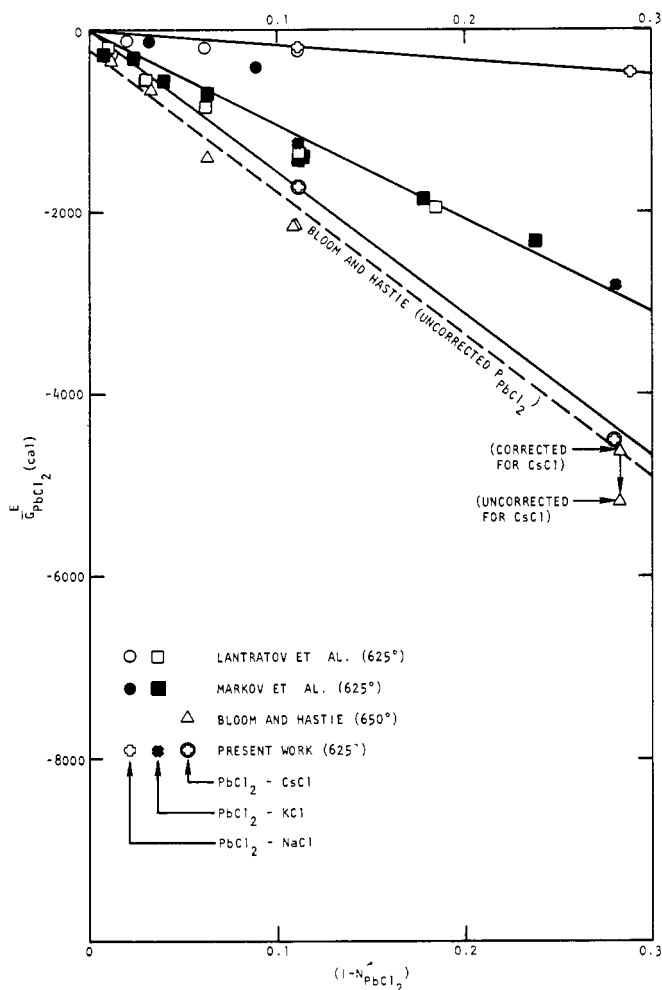


Figure 7. Plot of $\bar{G}_{\text{PbCl}_2}^E$ vs. $(1 - N_{\text{PbCl}_2})^2$ at 625°C

$N_{\text{PbCl}_2}' = \left(\frac{2 n_{\text{PbCl}_2}}{n_{\text{NaCl}} + 2 n_{\text{PbCl}_2}} \right)$ is the equivalent fraction of PbCl₂

Table III. Partial Excess Thermodynamic Quantities of PbCl₂ at 665°C and at N_{PbCl_2} Equals 0.5

| System | $\bar{H}_{\text{PbCl}_2}^E$, cal ^a | $\bar{G}_{\text{PbCl}_2}^E$, cal ^b | $\bar{S}_{\text{PbCl}_2}^E$, cal/deg |
|-------------------------|---|---|--|
| PbCl ₂ -NaCl | -125 | -280 | 0.2 |
| PbCl ₂ -KCl | -750 | -1200 | 0.5 |
| PbCl ₂ -CsCl | -1540 | -1810 | 0.3 |

^a Reference 15. ^b Extrapolated from present data.

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