

Table IV. Enthalpy of Solution of $\text{NH}_4\text{H}_2\text{PO}_4$ in 850.0 ml of 10.34*m* HCl and Stoichiometric H_2O at 40°C

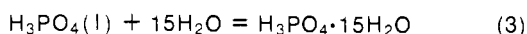
Wt sample, g	-Corr temp rise, °C	ΔH_s , cal/mol	Δ
14.90333	0.97704	5457	+4
15.00510	0.98473	5453	± 0
15.02232	0.98401	5448	-5
15.10264	0.98916	5451	-2
15.12050	0.99038	5447	-6
15.15361	0.99289	5466	+13
15.20558	0.99578	5452	-1
15.22108	0.99749	5451	-2
	Av, double SD	5453	± 4

cal (double standard deviation) for Equation 1 at 40°C. This value was adjusted by -1552 ± 2 cal to give $-15,675 \pm 32$ cal for the enthalpy of reaction at 25°C according to the equation

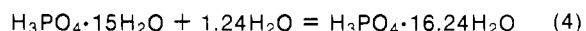
$$\Delta H_R(25^\circ\text{C}) = \Delta H_R(40^\circ\text{C}) + \int_{313.15}^{298.15} \Delta C_p dT \quad (2)$$

through use of polynomial equations for determining differences between the heat capacities of the products and the reactants. The heat capacity equations were derived from the data of Osborne et al. for water (6), of Stephenson and Zettlemyer for $\text{NH}_4\text{H}_2\text{PO}_4$ (8), of Egan et al. for phosphoric acid solutions (2), and of Wakefield and Luff for $(\text{NH}_4)_3\text{HP}_2\text{O}_7 \cdot \text{H}_2\text{O}$ (9).

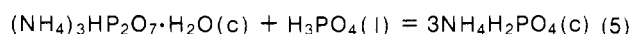
The standard enthalpies of formation of $\text{H}_3\text{PO}_4(\text{l})$, -302.8 kcal, and $\text{H}_3\text{PO}_4 \cdot 15\text{H}_2\text{O}(\text{soln})$, -307.715 kcal (5), were used to determine the enthalpy of the reaction



at 25°C, -4.9 kcal. The enthalpy of the reaction



at 25°C, -36.65 cal, was determined from the data of Egan and Luff (1). The summation of the enthalpies of reaction of Equations 1, 3, and 4 gives the enthalpy of the reaction



at 25°C, -20.61 ± 0.1 kcal.

The standard enthalpy of formation of $\text{NH}_4\text{H}_2\text{PO}_4(\text{c})$ is -345.38 kcal/mol (5). Substituting the known enthalpies of formation and the enthalpy of reaction of Equation 5 in the equation

$$\Delta H_f^\circ(\text{NH}_4)_3\text{HP}_2\text{O}_7 \cdot \text{H}_2\text{O}(\text{c}) = 3[\Delta H_f^\circ\text{NH}_4\text{H}_2\text{PO}_4(\text{c})] - \Delta H_f^\circ\text{H}_3\text{PO}_4(\text{l}) - \Delta H_R(25^\circ\text{C}) \quad (6)$$

gives -712.7 kcal/mol as the standard enthalpy of formation of $(\text{NH}_4)_3\text{HP}_2\text{O}_7 \cdot \text{H}_2\text{O}(\text{c})$ at 25°C. An estimate of the uncertainty is not given because it is largely dependent upon the uncertainty of the auxiliary enthalpies of formation taken from ref. 5.

Literature Cited

- (1) Egan, Jr., E. P., Luff, B. B., *J. Phys. Chem.*, **65**, 523 (1961).
- (2) Egan, Jr., E. P., Luff, B. B., Wakefield, Z. T., *ibid.*, **62**, 1091 (1958).
- (3) Frazier, A. W., Smith, J. P., Lehr, J. R., *J. Agr. Food Chem.*, **13**, 316 (1965).
- (4) Luff, B. B., Reed, R. B., Wakefield, Z. T., *J. Chem. Eng. Data*, **16**, 342 (1971).
- (5) National Bureau of Standards, "Selected Values of Chemical Thermodynamic Properties," Tech. Note **270-3**, 1968.
- (6) Osborne, N. S., Stimson, H. F., Ginnings, D. C., *J. Res. Nat. Bur. Stand.*, **23**, 238 (1939).
- (7) Rossini, F. D., "Experimental Thermochemistry," Vol 1, Chap. 5, Interscience, New York, N.Y., 1956.
- (8) Stephenson, C. C., Zettlemyer, A. C., *J. Amer. Chem. Soc.*, **66**, 1405 (1944).
- (9) Wakefield, Z. T., Luff, B. B., *J. Chem. Eng. Data*, **17**, 134 (1972).
- (10) Wakefield, Z. T., Luff, B. B., Reed, R. B., *ibid.*, **15**, 560 (1970).

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High-Precision Vapor-Pressure Data for Eight Organic Compounds

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Vapor-pressure data are obtained via comparative ebulliometry for butyronitrile, cyclohexene, 1,3-cyclohexadiene, methylene cyclohexane, di-*n*-propyl ether, and cyclohexanone. In addition, corrected data are presented for capronitrile and laurionitrile. Constants for Antoine and Cox equations, with their statistical uncertainties, are included. The overall average differences between calculated and observed pressures for the new data, expressed as $\Delta p/p$, are 5.6×10^{-5} for the Antoine and 4.7×10^{-5} for the Cox equation.

During a study concerning thermodynamics of solution by use of gas-liquid chromatography, the need arose for enthalpy of vaporization data for several compounds. To estimate the enthalpy of vaporization from the Clapeyron equation, we measured the vapor pressures (from about 50°C to slightly above the normal boiling point) of

five compounds for which such data are not presently available: cyclohexene, 1,3-cyclohexadiene, methylene-cyclohexane, cyclohexanone, and di-*n*-propyl ether. In addition, we are including improved data for butyronitrile and corrected data for laurionitrile and capronitrile.

Experimental

A comparative ebulliometric technique was used with an apparatus similar to that described by Ambrose (1). Instead of four bubble caps, however, only one was used in the present ebulliometer, allowing the use of significantly smaller samples (3 ml) without sacrificing the high precision characteristic of the method.

Two platinum-resistance thermometers were used to measure the temperatures of the liquid-vapor equilibria of water and the liquid under investigation. That used for the latter was calibrated (at Leeds and Northrup) according to IPTS-48. The other was calibrated in this laboratory by use of the triple point of water and several temperatures up to 108°C. The latter was accomplished by using fresh samples of deionized, degassed water in both boilers of

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the ebulliometric apparatus and by using the first thermometer for a reference temperature. (Since the second thermometer is never used outside the calibration range, its narrowness is not a handicap.) For this work both thermometers were converted to IPTS-68, in accord with the discussion of Bedford and Kirby (5). The constants in the equation

$$R_{t'} = R_o (1 + At' + Bt'^2) \quad (1)$$

were evaluated by least squares for the second thermometer. The value of unity was treated as a parameter in the analysis and was determined by the fit to be 1.00000002. The average deviation in the calibration data (a total of six points) corresponded to 0.0002°C; the maximum deviation, 0.00034°C.

The precision of the vapor-pressure data was such that correction had to be made for the difference in mass of the vapor columns above the liquid phases in the two boilers for the higher molecular-weight samples. In addition, the liquid surface in the water boiler lay 6 cm below that in the sample boiler; the condenser, through which ice water circulated, was 4 cm longer above the sample than above the water. The last two effects lead to a constant percentage error in the pressure of the sample of 0.00036%. Since the best precision in the present data amounts to 0.003%, these effects can be safely ignored. To correct for the first effect, we used the equation

$$p_s = p_w \left[1 + 2.12 \times 10^{-4} \left(\frac{M_s}{T_s} - \frac{M_w}{T_w} \right) \right] \quad (2)$$

where p , M , and T represent vapor pressure, molecular weight, and absolute temperature, and the subscripts s and w refer to sample and water, respectively. The constant includes the information that each vapor column is 18 cm high.

The vapor pressure of the water (p_w) is calculated from the temperature of the vapor-liquid equilibrium by use of a Chebyshev polynomial (4) with constants determined by Ambrose and Sprake (3).

The resistances of both thermometers at the triple point of water were measured during the course of the work; the sample thermometer exhibited a resistance 0.0002 ohm higher than its original value and the other, 0.0001 ohm higher (0.0001 ohm corresponds to 0.001°).

The coils of the thermostated Mueller bridge used for resistance measurements were also recalibrated by use of a Leeds and Northrup standard resistance of 10.0100 ohms. In no case was the total correction to a bridge reading greater than 0.0001 ohm different from the original calibration values received with the instrument four years ago. The new corrections were used for this work.

Subsequent to an earlier publication from this laboratory (7), it was pointed out (2) that the Chebyshev constants used therein were based on IPTS-68, whereas the thermometer had been calibrated according to IPTS-48. This leads to significant, though small, errors in the data for capronitrile and lauronitrile presented in that paper. (The remaining vapor-pressure data published in ref. 7, for which manometers were used, are consistent but based on IPTS-48.) Consequently, we include here corrected data for these two compounds, based on IPTS-68. In addition, we have repeated the measurements for butyronitrile by use of the comparative ebulliometric apparatus.

Recent suggestions in the literature give rise to the possibility of further changes in the practical temperature scale (6). To preserve the value of good data measured on a practical scale, provision should be made for ready conversion from one scale to another. Thus, we include

in Table I values of the characteristic constants for the thermometers used in this work.

In the event that the vapor pressure-temperature relationship used herein for water should prove unsatisfactory, the temperature of the water equilibrium is included with the presentation of the temperature and pressure in Table II for each sample.

All compounds on which new measurements were made were obtained from ChemSampCo (Columbus, Ohio) except cyclohexene, which was from Eastman. Butyronitrile and methylenecyclohexene did not require purification; the remainder were distilled on a Teflon spinning band column. All were better than 99.9% pure by gas-liquid chromatography and were dried over a molecular sieve before use. Helium was used to apply the external pressure to the boiling liquids.

Results

The results are presented in Table II. Tables III and IV give the values of the Antoine and Cox constants, respectively, for the data in Table II, as well as the temperature range of the data, average deviations in pressure, and the normal boiling points of the compounds studied. Evaluation of the constants was accomplished by the iterative approach to rigorous least-squares analysis described by Wentworth (9). The standard deviation in temperature was taken to be 0.001, and that in pressure was calculated from the expression

$$\sigma_p = \left[\left(\frac{dp}{dT} \right)_w^2 + \left(\frac{dp}{dT} \right)_s^2 \right]^{1/2} \sigma_T \quad (3)$$

where σ represents standard deviation, and w and s refer to water and sample, respectively. Weighing the data was accomplished following the paper of Wentworth (9).

Discussion

One of the most important uses of accurate vapor-pressure data is in the estimation of enthalpies of vaporization or, if calorimetric values are available, evaluation of second-virial coefficients for the vapors in question. Both involve the derivative of $\log p$ with respect to T :

$$\left(\frac{d \log p}{dT} \right)_{\text{Antoine}} = \frac{B}{(C + t)^2} \quad (4)$$

$$\left(\frac{d \log p}{dT} \right)_{\text{Cox}} = \left[\frac{T_{\text{bp}}}{T^2} + 2.303 \left(1 - \frac{T_{\text{bp}}}{T} \right) (b + 2cT) \right] \cdot 10^{(a+b+cT^2)} \quad (5)$$

These expressions point out one of the reasons for the relative popularity of the Antoine equation. It is of interest to compare the precision of enthalpies of vaporization derived from these two equations. To this end, we have calculated the standard deviation of the enthalpies of vaporization at the boiling point and at a temperature near the low end of the experimental data from the elements of the variance-covariance matrices produced in fitting the data. For both equations the statistical uncertainty averages 0.5 cal/mol and is never greater than 1.1 cal/mol. Since the error introduced through second-virial coefficients in the Clapeyron equation is probably not

Table I. Thermometer Constants

	R_o	α_{68}	δ_{68}
Sample thermometer	25.5404	0.003926394	1.496947
Water thermometer	25.5412	0.003926841	1.500461

Table II. Vapor-Pressure Data

Butyronitrile			1,3-Cyclohexadiene			Methylene cyclohexane			Di- <i>n</i> -propyl ether		
t_{w1} , °C	t_{s1} , °C	p_{s1} , kPa	t_{w1} , °C	t_{s1} , °C	p_{s1} , kPa	t_{w1} , °C	t_{s1} , °C	p_{s1} , kPa	t_{w1} , °C	t_{s1} , °C	p_{s1} , kPa
52.310	59.807	13.831	59.464	34.185	19.444	63.374	58.645	23.240	55.789	39.703	16.358
57.229	65.615	17.513	64.718	39.995	24.711	68.715	65.013	29.486	61.361	45.857	21.223
62.298	71.638	22.151	69.336	45.146	30.293	73.249	70.444	35.827	66.669	51.773	26.953
66.802	77.023	27.111	74.272	50.687	37.406	78.447	76.742	44.476	71.984	57.749	33.952
72.269	83.599	34.366	78.843	55.860	45.201	83.782	83.247	55.114	76.849	63.263	41.649
77.117	89.462	42.109	79.259	56.332	45.973	94.186	96.128	82.034	82.132	69.298	51.617
82.501	96.022	52.382	83.990	61.740	55.567	99.466	102.755	99.414	87.254	75.199	63.121
87.606	102.279	63.984	89.626	68.233	69.131	103.702	108.117	115.468	89.614	77.936	69.101
93.198	109.175	79.081	94.628	74.045	83.383	108.015	113.619	133.958	92.764	81.601	77.811
98.417	115.651	95.737	99.142	79.332	98.263				95.004	84.221	84.548
103.373	121.838	114.148	104.042	85.113	116.841				100.778	91.016	104.174
108.055	127.707	134.135	108.287	90.160	135.198				106.810	98.183	128.564
Cyclohexene			Cyclohexanone			Capronitrile			Lauronitrile		
59.947	36.875	19.885	50.612	89.628	12.725	50.799	98.079	12.843	30.682	167.746	4.4151
65.930	43.560	26.084	54.701	94.896	15.528	53.729	101.861	14.818	38.171	178.991	6.6921
71.453	49.795	33.189	59.255	100.807	19.257	60.560	110.711	20.455	45.585	190.226	9.8833
76.707	55.785	41.404	64.507	107.664	24.477	69.081	121.896	29.960	49.343	195.963	11.949
82.582	62.537	52.551	69.552	114.303	30.580	74.855	129.534	38.332	53.230	201.926	14.465
87.993	68.815	64.943	73.635	119.712	36.416	81.883	138.897	51.106	61.957	215.426	21.810
93.580	75.354	80.213	77.814	125.282	43.337	85.316	143.510	58.538	68.678	225.921	29.438
98.425	81.075	95.764	81.826	130.659	50.990	94.495	155.936	82.975	73.722	233.873	36.550
102.658	86.112	111.325	85.620	135.774	59.239	99.285	162.487	98.770	78.002	240.657	43.673
107.053	91.378	129.633	90.022	141.742	70.181	103.669	168.510	115.335	83.216	248.970	53.893
			93.054	145.880	78.656				87.770	256.297	64.392
			97.458	151.916	92.474				92.318	263.605	76.526
			97.493	151.969	92.593				97.218	271.578	91.674
			101.081	156.917	105.300				103.684	282.147	115.399
			101.112	156.966	105.417						
			107.454	165.769	131.422						

Table III. Antoine Constants^a

Compound	Temp range, °C	A	B	C	T_{bp} , K	$\frac{\Delta p}{p} \times 10^5$
Butyronitrile	59.8–127.7	6.129067 ± 0.000400	1452.076 ± 0.804	224.1855 ± 0.0277	390.770	4.1
1,3-Cyclohexadiene	34.2–90.2	5.865445 ± 0.000481	1205.995 ± 0.866	222.3226 ± 0.1020	353.489	6.7
Methylenecyclohexane	58.6–113.6	5.803367 ± 0.001935	1253.192 ± 1.171	216.0562 ± 0.1409	376.578	5.8
Di- <i>n</i> -propyl ether	39.7–98.2	5.894812 ± 0.000458	1227.468 ± 0.824	215.7007 ± 0.0950	363.246	3.1
Cyclohexene	36.9–91.4	5.872420 ± 0.001757	1221.899 ± 1.011	223.1720 ± 0.1186	356.095	5.9
Cyclohexanone	89.6–165.8	5.978401 ± 0.000987	1495.511 ± 0.666	209.5517 ± 0.0747	428.572	8.0
Capronitrile	98.1–168.5	6.071220 ± 0.001304	1553.811 ± 0.888	207.3386 ± 0.0968	436.613	15
Lauronitrile	167.7–282.1	6.081293 ± 0.000592	1859.981 ± 0.464	166.6944 ± 0.0486	549.258	21

^a $\log p$ (cm Hg) = $A - \frac{B}{C + t}$. To convert to kPa, add 0.124903 to A.

Table IV. Cox Constants^a

Compound	α	$-b \times 10^3$	$c \times 10^6$	T_{bp} , K	$\frac{\Delta p}{p} \times 10^5$
Butyronitrile	0.846124 ± 0.00317	0.667751 ± 0.0178	0.662990 ± 0.0250	390.7717 ± 0.00068	2.5
1,3-Cyclohexadiene	0.845439 ± 0.00416	0.804445 ± 0.0256	0.854257 ± 0.0391	353.4899 ± 0.00065	5.5
Methylenecyclohexane	0.846896 ± 0.00550	0.762546 ± 0.0314	0.741997 ± 0.0448	376.5779 ± 0.00073	6.3
Di- <i>n</i> -propyl ether	0.866715 ± 0.00375	0.812825 ± 0.0226	0.809693 ± 0.0339	363.2462 ± 0.00061	3.2
Cyclohexene	0.833958 ± 0.00485	0.742586 ± 0.0130	0.767278 ± 0.0450	356.0954 ± 0.00065	6.6
Cyclohexanone	0.852046 ± 0.00340	0.612660 ± 0.0175	0.504661 ± 0.0225	428.5716 ± 0.00069	4.0
Capronitrile	0.863202 ± 0.00362	0.597309 ± 0.0185	0.475389 ± 0.0236	436.6137 ± 0.00072	17
Lauronitrile	0.984965 ± 0.00110	0.792482 ± 0.00465	0.553941 ± 0.00488	549.2613 ± 0.00079	9.7

^a $\log p$ (atm) = $A' \left(1 - \frac{T_{bp}}{T}\right)$, where $\log A' = (\alpha + bT + cT^2)$. T_{bp} was treated as a parameter in fitting the data. To convert atm to kPa, multiply by 101.325.

smaller than this, either equation may be used when an enthalpy of vaporization is to be estimated from vapor pressures within the range of experimental data.

However, if one calculates the enthalpy of vaporization at 25°C, there is a real discrepancy between the two equations under discussion, which increases with the length of extrapolation below the experimental data. For example, the difference varies from 4 cal/mol for 1,3-cyclohexadiene to 2500 cal/mol for laurionitrile. Scott (8) pointed out that the Cox equation is to be preferred when such an extrapolation becomes necessary, since it behaves properly as temperature decreases, an advantage the Antoine equation does not share.

Conclusions

Accurate vapor-pressure data have been measured and fitted to Antoine and Cox equations for eight compounds. Within the range of the data, there is no clear advantage to either equation. The statistical uncertainty in enthalpies of vaporization derived from them by use of the Clausius-Clapeyron equation is of the order of 1 cal/mol.

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Literature Cited

- (1) Ambrose, D., *J. Sci. Instrum.*, **1968**, p 41.
- (2) Ambrose, D., National Physical Laboratory, Teddington, Middlesex, England, private communication, May 4, 1971.
- (3) Ambrose, D., Sprake, C. H. S., *J. Chem. Thermodyn.*, **1972**, p 603.
- (4) Ambrose, D., Counsell, J. F., Davenport, A. J., *ibid.*, **1970**, 283.
- (5) Bedford, R. E., Kirby, C. G. M., *Metrologia*, **1969**, p 83.
- (6) Haar, L., *Science*, **176**, 1293 (1972) and references therein.
- (7) Meyer, E. F., Renner, T. A., Stec, K. S., *J. Phys. Chem.*, **75**, 642 (1971).
- (8) Scott, D. W., U.S. Bureau of Mines, Bartlesville, Okla., private communication, March 22, 1971.
- (9) Wentworth, W. E., *J. Chem. Educ.*, **42**, 96 (1965).

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Vapor Pressures of Aqueous Solutions of Beryllium Sulfate

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Water vapor pressures over saturated, aqueous BeSO₄ solutions were measured with a differential mercury manometer at 25–93°C for BeSO₄·4H₂O as solid phase and at 90–110°C for BeSO₄·2H₂O as solid phase. The transition temperature of BeSO₄·4H₂O to BeSO₄·2H₂O in contact with saturated solution was 88.3 ± 0.5°C. The compositions of saturated solutions in the above temperature ranges were obtained from the best fit of selected literature data. A correlation of relative vapor pressure lowering with relative saturation was developed which predicts the vapor pressures of undersaturated BeSO₄ solutions in the range 0–90°C.

The vapor pressures of saturated, aqueous solutions of beryllium sulfate reported here form part of a thermodynamic study (1) of the system BeSO₄-H₂O. The disagreement existing among several authors (3, 8, 12) on the compositions of the stable hydrates and their transition temperatures in contact with saturated solution is now resolved. Vapor pressures and compositions of saturated solutions may be used as a basis for the prediction of the vapor pressures of undersaturated BeSO₄ solutions over wide ranges of temperature and composition.

Experimental

A differential mercury manometer was constructed of 12-mm i.d. borosilicate glass tubing with side arms for sample and reference solutions. Water was distilled into both side arms, and an excess of BeSO₄·4H₂O was added to one side. The purity of the salt was previously reported (1). After several freeze-thaw degassing cycles, the entire manometer was evacuated and sealed under a

vacuum of 1 × 10⁻³ mm Hg. An oil bath controlled to ±0.01°C was used, and the temperature was measured to 0.01°C at both side arms with quartz thermometers.

The manometer levels were measured to 0.05 mm with a cathetometer, and the difference in levels was corrected to 0°C and $g = 9.80665 \text{ m sec}^{-2}$. In this paper 1 mm Hg ≡ 1 Torr = (101.325/760) kN m⁻². Occasional shaking ensured saturated solutions, and there was no significant difference between pressures obtained with heating and cooling. For measurements with a BeSO₄·2H₂O solid phase, a second run was carried out with a saturated sodium chloride solution as reference instead of water. The water vapor pressures over saturated aqueous NaCl were obtained from a least-squares fit of the data of several workers in the range 90–110°C (11), and the pressures over pure water were taken from standard tables (13).

Results and Discussion

The measured water vapor pressures over saturated solutions in the range 25–89°C (Table I) are fitted by the least-squares relation:

$$\ln p_s = -15.3437 \ln T - 9927.89/T + 123.707 \quad (1)$$

where p_s is the pressure in mm Hg, and T is the absolute temperature. The maximum deviation in p_s is 0.95 mm Hg, and the standard deviation is 0.55 mm Hg. In the range 89–93°C the measured pressures are slightly lower than values predicted by Equation 1, the difference increasing to 3.5 mm Hg at 93°C.

On raising the temperature to 110°C, a period of 15 hr was required to reach a steady pressure, indicating a change to a lower solid hydrate. The measured water