

# Vapor-Liquid Equilibria for the System Benzene-Thiophene-Methanol

Jaime O. Triday\* and Patricio Rodriguez

Departamento de Procesos Químicos, Universidad Técnica Federico Santa María, Valparaíso 110-V, Chile

Isothermal vapor pressure data over the whole range of composition were obtained for the system benzene-thiophene-methanol. Data were taken at temperatures of 35, 40, and 45 °C by using a static equilibrium cell. The systems benzene-methanol and thiophene-methanol are highly nonideal, while the system benzene-thiophene shows a very small deviation from ideality. The models suggested by Wilson and by Renon and Prausnitz (NRTL) and the modified equation of Abrams and Prausnitz (UNIQUAC) were used in the reduction of data. Physical parameters of these equations obtained from the binary data were used to predict the ternary system. The Wilson equation gives the best fit for the binary as well as the ternary data. Also, this equation gives the best prediction for the ternary system.

## Introduction

Vapor-liquid phase equilibria measurements continue to be of major importance in thermodynamics, not only for their direct use in process design but also for their importance in the testing and extension of fluid mixture theories.

The models suggested by Wilson (1) and by Renon and Prausnitz (NRTL) (2) and the modified equation of Abrams and Prausnitz (UNIQUAC) (3, 4) can be easily extended to multi-component mixtures without any additional assumptions beyond those for binary mixtures.

The aim of this work was to test the extension of these well-known models for the ternary system benzene-thiophene-methanol at 35, 40, and 45 °C. Also, isothermic data for this ternary system were not found in the literature (5).

The binary systems benzene-methanol and thiophene-methanol have been already measured by using the same experimental method at the same temperatures (6, 7).

## Experimental Section

**Chemicals.** Benzene was Merck analytical-grade reagent used without further purification. The certified minimum purity of this chemical was 99.7%. Thiophene and methanol were also Merck reagents and were redistilled in a high-efficiency packed column. Physical properties of the chemicals are shown in Tables I and II along with literature values.

**Vapor Pressure Measurements.** The vapor pressures of the systems were measured at constant temperature as a function of composition by using a static equilibrium cell. The apparatus, which is described in detail by Vera (8), is shown schematically in Figure 1. Briefly the major items were a large-diameter mercury manometer, measuring the difference in pressure between the reference high vacuum and measuring manifold systems, and a thermostatic bath containing the vapor pressure cell assembly. The latter consisted of a mercury null manometer connected to the static cell. Stirring of the contents of the cell was achieved with a small PTFE-coated magnet activated

Table I. Physical Properties of the Pure Compounds at 20 °C

|           | density, g cm <sup>-3</sup> |                       | refractive index |                       |
|-----------|-----------------------------|-----------------------|------------------|-----------------------|
|           | obsd                        | lit.                  | obsd             | lit.                  |
| benzene   | 0.8790                      | 0.879 01 <sup>a</sup> | 1.5011           | 1.501 08 <sup>a</sup> |
| thiophene | 1.0581                      | 1.058 87 <sup>a</sup> | 1.5290           | 1.528 7 <sup>a</sup>  |
| methanol  | 0.7911                      | 0.791 31 <sup>a</sup> | 1.3290           | 1.328 40 <sup>a</sup> |

<sup>a</sup> Reference 12.

Table II. Vapor Pressures of the Pure Compounds

|           | P, mmHg |                     |       |                     |       |                     |
|-----------|---------|---------------------|-------|---------------------|-------|---------------------|
|           | 35 °C   |                     | 40 °C |                     | 45 °C |                     |
|           | obsd    | lit.                | obsd  | lit.                | obsd  | lit.                |
| benzene   | 148.0   | 148.30 <sup>a</sup> | 182.3 | 182.77 <sup>a</sup> | 223.2 | 223.50 <sup>a</sup> |
| thiophene | 126.5   | 125.50 <sup>a</sup> | 156.4 | 155.46 <sup>a</sup> | 192.3 | 191.04 <sup>a</sup> |
| methanol  | 209.5   | 209.59 <sup>a</sup> | 265.5 | 265.76 <sup>a</sup> | 333.5 | 334.17 <sup>a</sup> |

<sup>a</sup> Reference 13.

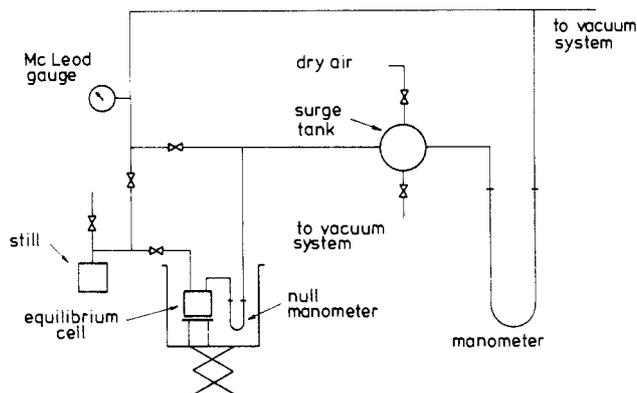


Figure 1. Schematic view of the apparatus.

by a magnetic stirrer motor sited under the bath. The mercury levels were read by using an Eberbach cathetometer.

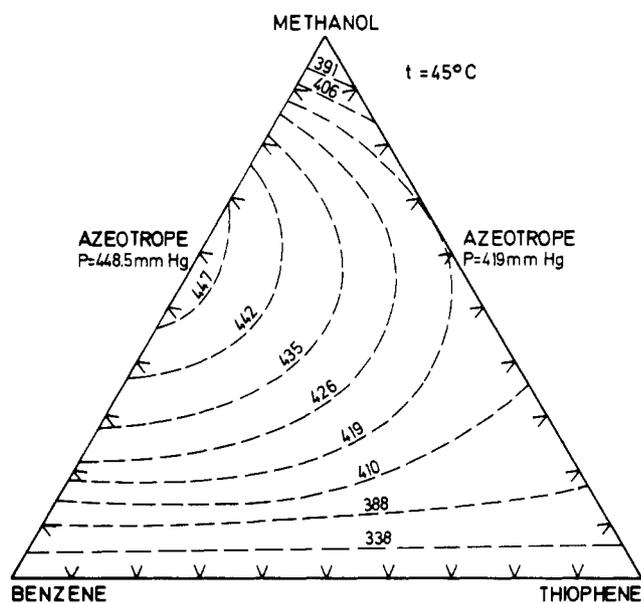
The ternary mixtures were sealed in a separate still for degassing. The air was removed by freezing the mixture with liquid nitrogen and opening the still to the vacuum system. Afterward, the mixture was melted under vigorous agitation by the magnetic stirrer. Degassing was considered complete when the vacuum gage located in the vacuum line did not detect any air at the time of opening the still with the frozen mixture. The mixture was transferred to the equilibrium cell by distilling from the still and condensing in the cell with liquid nitrogen. The cell was then gradually warmed and thermostated at the desired temperature. The small null manometer was balanced by bleeding dry air into its reference side through a needle valve. The mixture in the cell was under continuous agitation to assure uniform temperature and composition. After the vapor pressure measuring at three different temperatures, the sample was completely transferred from the equilibrium cell to the still previously evacuated and cooled with liquid nitrogen.

Ternary mixture compositions were determined by mixing

\* Address correspondence to this author at the Department of Chemical Engineering, University of California, Davis, CA 95616.

**Table III. Isothermal Vapor-Liquid Equilibrium Data for the Benzene (1)-Thiophene (2)-Methanol (3) System**

|    | $x_1$ | $x_2$ | $x_3$ | P, mmHg |       |       |
|----|-------|-------|-------|---------|-------|-------|
|    |       |       |       | 35 °C   | 40 °C | 45 °C |
| 1  | 0.516 | 0.484 | 0.000 | 139.0   | 172.9 | 210.2 |
| 2  | 0.468 | 0.439 | 0.094 | 249.9   | 309.2 | 375.4 |
| 3  | 0.411 | 0.385 | 0.204 | 270.4   | 337.1 | 411.3 |
| 4  | 0.338 | 0.317 | 0.344 | 279.0   | 346.8 | 428.5 |
| 5  | 0.212 | 0.199 | 0.589 | 284.0   | 352.7 | 436.9 |
| 6  | 0.140 | 0.132 | 0.728 | 280.4   | 351.1 | 433.3 |
| 7  | 0.088 | 0.082 | 0.830 | 268.5   | 337.7 | 418.4 |
| 8  | 0.043 | 0.041 | 0.916 | 250.0   | 313.8 | 390.5 |
| 9  | 0.000 | 0.000 | 1.000 | 209.5   | 265.5 | 333.5 |
| 10 | 0.464 | 0.000 | 0.536 | 291.8   | 364.5 | 448.1 |
| 11 | 0.429 | 0.074 | 0.497 | 289.8   | 362.0 | 446.7 |
| 12 | 0.385 | 0.170 | 0.445 | 284.3   | 355.0 | 438.6 |
| 13 | 0.302 | 0.348 | 0.350 | 275.9   | 343.6 | 426.3 |
| 14 | 0.200 | 0.568 | 0.232 | 270.4   | 337.6 | 417.3 |
| 15 | 0.136 | 0.707 | 0.157 | 255.5   | 316.7 | 388.4 |
| 16 | 0.058 | 0.874 | 0.068 | 227.0   | 278.3 | 337.5 |
| 17 | 0.000 | 1.000 | 0.000 | 126.5   | 156.4 | 192.3 |
| 18 | 0.000 | 0.504 | 0.496 | 266.5   | 335.8 | 415.0 |
| 19 | 0.149 | 0.429 | 0.422 | 271.9   | 340.1 | 422.3 |
| 20 | 0.319 | 0.344 | 0.338 | 275.4   | 345.1 | 425.8 |
| 21 | 0.512 | 0.246 | 0.242 | 275.4   | 344.6 | 425.3 |
| 22 | 0.730 | 0.136 | 0.134 | 269.9   | 334.1 | 410.3 |
| 23 | 0.862 | 0.070 | 0.069 | 254.0   | 309.8 | 375.5 |
| 24 | 1.000 | 0.000 | 0.000 | 148.0   | 182.3 | 223.2 |

**Figure 2.** Vapor-Liquid equilibrium data for the system benzene (1)-thiophene (2)-methanol (3) at 45 °C.

known amount of pure compounds. The refractive indexes of the mixtures were measured before and after the vapor pressure measurement by using a Bausch and Lomb Abbe-3L refractometer at 20 °C. Refractive index measurements were taken in order to detect any change in composition during the vapor pressure measurements. When a change in the refractive index was detected, the experimental point was disregarded.

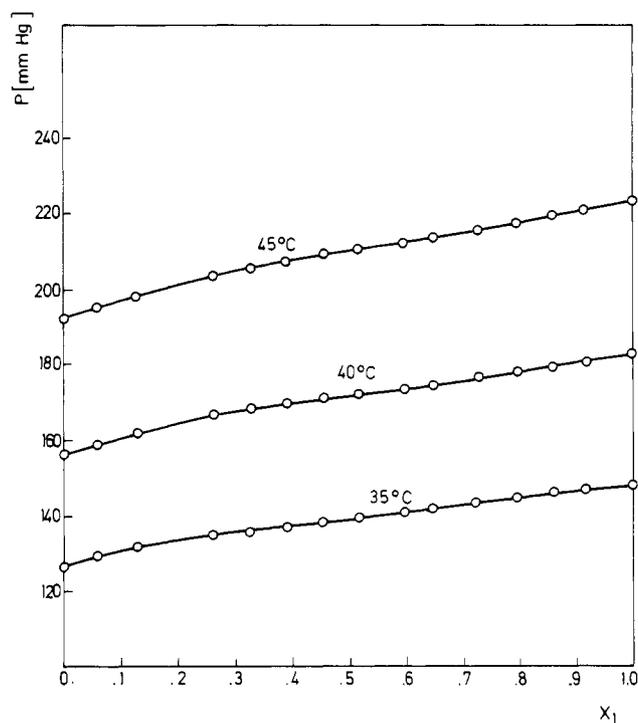
For the binary system benzene-thiophene the compositions were determined from a calibration plot of index of refraction vs. composition at 20 °C.

Considering the accuracy in the index of refraction measurement of  $\pm 0.0004$ , sample compositions were estimated to be accurate within  $\pm 0.001$  mole fraction.

In addition, the effect of the accuracy in temperature of  $\pm 0.10$  °C and a maximum error of 0.5 mmHg in measuring the

**Table IV. Isothermal Vapor-Liquid Equilibrium Data for the Benzene (1)-Thiophene (2) System**

|    | $x_1$ | P, mmHg |       |       |
|----|-------|---------|-------|-------|
|    |       | 35 °C   | 40 °C | 45 °C |
| 1  | 0.000 | 126.5   | 156.4 | 192.3 |
| 2  | 0.064 | 128.5   | 158.4 | 195.3 |
| 3  | 0.134 | 131.5   | 161.9 | 197.8 |
| 4  | 0.266 | 134.5   | 166.4 | 203.3 |
| 5  | 0.330 | 135.5   | 168.3 | 205.3 |
| 6  | 0.392 | 136.5   | 169.4 | 207.2 |
| 7  | 0.455 | 137.5   | 171.4 | 209.2 |
| 8  | 0.519 | 139.0   | 172.5 | 210.7 |
| 9  | 0.595 | 140.5   | 174.5 | 212.7 |
| 10 | 0.651 | 142.0   | 175.5 | 214.2 |
| 11 | 0.728 | 143.5   | 177.4 | 216.3 |
| 12 | 0.795 | 145.0   | 178.4 | 218.4 |
| 13 | 0.860 | 146.5   | 179.3 | 219.7 |
| 14 | 0.921 | 147.5   | 180.8 | 221.2 |
| 15 | 1.000 | 148.0   | 182.3 | 223.2 |

**Figure 3.** Vapor-liquid equilibrium data for the system benzene (1)-thiophene (2).

pressure give experimental vapor pressures better than  $\pm 1.0$  mmHg at each temperature.

## Results and Discussion

The vapor-liquid equilibrium data for the ternary system benzene-thiophene-methanol at 35, 40, and 45 °C are reported in Table III.

Figure 2 shows the data for the ternary system at 45 °C. The system does not exhibit a ternary azeotrope, having a maximum pressure at the binary azeotrope for the benzene-methanol system.

The vapor-liquid equilibrium data for the binary system benzene-thiophene are reported in Table IV and are shown in Figure 3. This system shows a very small deviation from ideality.

The experimental data were correlated by the Wilson (1), NRTL (2), and modified UNIQUAC (3, 4) equations.

For multicomponent systems these models give the following

equations for the molar excess Gibbs energy,  $g^E$ :

Wilson

$$g^E/RT = -\sum_i^N x_i \ln \left( \sum_j^N x_j \Lambda_{ij} \right) \quad (1)$$

where

$$\Lambda_{ij} = \frac{V_j}{V_i} \exp \left( -\frac{\lambda_{ij} - \lambda_{ji}}{RT} \right) \quad (2)$$

$\lambda_{ij}$  is the binary energy interaction parameter for the  $i$ - $j$  pair;  $V_i$  is the liquid molar volume of the component  $i$ .

NRTL

$$\frac{g^E}{RT} = \frac{\sum_i^N x_i \sum_j^N \tau_{ij} G_{ij} x_j}{\sum_k^N G_k x_k} \quad (3)$$

where

$$\tau_{ij} = (g_{ij} - g_{ji})/RT \quad (4)$$

$$G_{ij} = \exp(-\alpha_{ij} \tau_{ij}) \quad (5)$$

$g_{ij}$  is the binary energy interaction parameter for the  $i$ - $j$  pair;  $\alpha_{ij}$  is the nonrandomness parameter for the mixture  $ij$ .

The  $\alpha_{ij}$  parameters were fixed according with recommendations given by Renon (2).

UNIQUAC

$$g^E = g^E(\text{combinatorial}) + g^E(\text{residual}) \quad (6)$$

$$\frac{g^E}{RT}(\text{combinatorial}) = \sum_i^N x_i \ln \frac{\Phi_i}{x_i} + \frac{z}{2} \sum_i^N q_i x_i \ln \frac{\theta_i}{\Phi_i} \quad (7)$$

$$\frac{g^E}{RT}(\text{residual}) = -\sum_i^N q'_i x_i \ln \left( \sum_j^N \theta'_j \tau_{ij} \right) \quad (8)$$

where the coordination number,  $z$ , is set equal to 10 and the segment fraction,  $\Phi_i$ , and the area fractions  $\theta_i$  and  $\theta'_i$  are given by

$$\Phi_i = x_i r_i / \sum_j^N x_j r_j \quad (9)$$

$$\theta_i = x_i q_i / \sum_j^N x_j q_j \quad (10)$$

$$\theta'_i = x_i q'_i / \sum_j^N x_j q'_j \quad (11)$$

The parameters  $r$ ,  $q$ , and  $q'$  are pure-component molecular structure constants depending on the molecular size and the external surface area.

$$\tau_{ij} = \exp[-(u_{ij} - u_{ji})/RT] \quad (12)$$

where  $u_{ij}$  is the binary energy parameter for the  $i$ - $j$  pair; when  $q_j = q'_j$ , eq 6 reduces to the original UNIQUAC of Abrams and Prausnitz (3).

The technique used for data fitting was basically that described by Prausnitz (9). Vapor-phase nonidealities were determined from the virial equation truncated after the second term. The second virial coefficients were calculated from the generalized correlations presented by Tsonopoulos (10). The critical properties and other parameters required for estimating

Table V. Critical Properties and Parameters Characterizing Vapor-Phase Nonideality

|           | $P_c^a$<br>atm | $T_c^a$<br>K | $V_c^a$<br>$\text{cm}^3 \text{g-mol}^{-1}$ | $\omega^a$ | $a_t^b$ | $b_t^b$ |
|-----------|----------------|--------------|--|------------|---------|---------|
| benzene   | 48.3           | 562.1        | 259  | 0.212      | 0.0000  | 0.0000  |
| thiophene | 56.2           | 579.4        | 219  | 0.200      | 0.0000  | 0.0000  |
| methanol  | 79.9           | 512.6        | 118  | 0.559      | 0.0878  | 0.0560  |

<sup>a</sup>Reference 13. <sup>b</sup>Reference 10.

Table VI. Parameters for the System Benzene (1)-Thiophene (2)

|                                 | 35 °C  | 40 °C  | 45 °C  |
|---------------------------------|--------|--------|--------|
| Wilson                          |        |        |        |
| $\lambda_{12} - \lambda_{11}^a$ | 249.8  | 319.3  | 247.7  |
| $\lambda_{12} - \lambda_{22}^a$ | -68.2  | -82.4  | -69.5  |
| $\sigma_p(\%)^b$                | 0.40   | 0.27   | 0.22   |
| NRTL ( $\alpha_{12} = 0.30$ )   |        |        |        |
| $g_{12} - g_{22}^a$             | 265.7  | 264.9  | 309.2  |
| $g_{12} - g_{11}^a$             | -121.3 | -75.7  | -165.3 |
| $\sigma_p(\%)^b$                | 0.40   | 0.32   | 0.26   |
| UNIQUAC                         |        |        |        |
| $u_{12} - u_{22}^a$             | 489.6  | 502.1  | 514.7  |
| $u_{21} - u_{11}^a$             | -384.1 | -374.9 | -407.1 |
| $\sigma_p(\%)^b$                | 0.45   | 0.35   | 0.29   |

<sup>a</sup>Units: J/mol. <sup>b</sup> $\sigma_p(\%) = 100\{[\sum_k^{\text{NEX}}((p - p^*)/p)_k^2]/(\text{NEX} - \text{NP})\}^{1/2}$ .

Table VII. Parameters for the System Benzene (1)-Methanol (3)

|                                 | 35 °C  | 40 °C  | 45 °C  |
|---------------------------------|--------|--------|--------|
| Wilson                          |        |        |        |
| $\lambda_{13} - \lambda_{11}^a$ | 753.2  | 870.3  | 845.2  |
| $\lambda_{13} - \lambda_{33}^a$ | 7418.6 | 7167.2 | 6857.9 |
| $\sigma_p(\%)^b$                | 0.26   | 0.33   | 0.33   |
| NRTL ( $\alpha_{13} = 0.47$ )   |        |        |        |
| $g_{13} - g_{33}^a$             | 5033.6 | 4820.2 | 4531.5 |
| $g_{13} - g_{11}^a$             | 2970.8 | 3079.6 | 3046.1 |
| $\sigma_p(\%)^b$                | 0.38   | 0.41   | 0.43   |
| UNIQUAC                         |        |        |        |
| $u_{13} - u_{33}^a$             | 7866.3 | 7585.9 | 7268.0 |
| $u_{31} - u_{11}^a$             | -472.8 | -443.5 | -464.4 |
| $\sigma_p(\%)^b$                | 0.33   | 0.39   | 0.40   |

<sup>a</sup>Units: J/mol. <sup>b</sup> $\sigma_p(\%) = 100\{[\sum_k^{\text{NEX}}((p - p^*)/p)_k^2]/(\text{NEX} - \text{NP})\}^{1/2}$ .

the second virial coefficients by the correlation of Tsonopoulos are listed in Table V.

The physical parameters were obtained by minimizing the objective function

$$S^2 = 100 \sum_i^{\text{NEX}} \left( \frac{P - P^*}{P} \right)^2 = \text{minimum} \quad (13)$$

where  $P$  and  $P^*$  are respectively the experimental and calculated values of the total vapor pressure and NEX is the total number of experimental points.

The secant method for simultaneous nonlinear equations was used for solving the objective function (11).

All the regression analyses were carried out by using double precision arithmetic upon a DEC-2020 computer.

The resulting binary interaction parameters obtained from the binary data are listed in Tables VI-VIII together with the estimated variance of the fit,  $\sigma_p(\%)$ .

$$\sigma_p(\%) = 100 \left\{ \left[ \sum_i^{\text{NEX}} \left( \frac{P - P^*}{P} \right)^2 \right] / (\text{NEX} - \text{NP}) \right\}^{1/2} \quad (14)$$

where NP is the number of parameters to be fitted.

**Table VIII. Parameters for the System Thiophene (2)-Methanol (3)**

|                                 | 35 °C  | 40 °C  | 45 °C  |
|---------------------------------|--------|--------|--------|
| Wilson                          |        |        |        |
| $\lambda_{23} - \lambda_{22}^a$ | 631.8  | 631.8  | 652.7  |
| $\lambda_{23} - \lambda_{33}^a$ | 7912.3 | 7661.3 | 7422.8 |
| $\sigma_p(\%)^b$                | 0.76   | 0.69   | 0.41   |
| NRTL ( $\alpha_{23} = 0.47$ )   |        |        |        |
| $g_{23} - g_{33}^a$             | 5481.3 | 5318.1 | 5154.9 |
| $g_{23} - g_{22}^a$             | 2627.7 | 2615.1 | 2627.1 |
| $\sigma_p(\%)^b$                | 0.82   | 0.86   | 0.51   |
| UNIQUAC                         |        |        |        |
| $u_{23} - u_{33}$               | 8456.3 | 8180.1 | 7908.1 |
| $u_{32} - u_{22}$               | -493.7 | -510.5 | -510.5 |
| $\sigma_p(\%)$                  | 0.77   | 0.70   | 0.43   |

<sup>a</sup> Units: J/mol. <sup>b</sup>  $\sigma_p(\%) = 100\{[\sum_k^{NEX}(p - p^*)/p]^2\}/(NEX - NP)^{1/2}$ .

**Table IX. Prediction of the VLE for the System Benzene (1)-Thiophene (2)-Methanol (3)**

|       | $\sigma_p(\%)^a$ |                   |         |
|-------|------------------|-------------------|---------|
|       | Wilson           | NRTL <sup>b</sup> | UNIQUAC |
| 35 °C | 1.21             | 1.49              | 1.44    |
| 40 °C | 1.07             | 1.26              | 1.31    |
| 45 °C | 1.32             | 1.34              | 1.64    |

<sup>a</sup>  $\sigma_p(\%) = 100\{[\sum_i^{NEX}((p - p^*)/p)^2]\}/(NEX - NP)^{1/2}$ . <sup>b</sup>  $\alpha_{12} = 0.30$ ;  $\alpha_{13} = \alpha_{23} = 0.47$ .

**Table X. Fit of the VLE Data for the System Benzene (1)-Thiophene (2)-Methanol (3)**

|       | $\sigma_p(\%)^a$ |                   |         |
|-------|------------------|-------------------|---------|
|       | Wilson           | NRTL <sup>b</sup> | UNIQUAC |
| 35 °C | 0.58             | 0.79              | 0.65    |
| 40 °C | 0.50             | 0.66              | 0.58    |
| 45 °C | 0.56             | 0.66              | 0.64    |

<sup>a</sup>  $\sigma_p(\%) = 100\{[\sum_i^{NEX}((p - p^*)/p)^2]\}/(NEX - NP)^{1/2}$ . <sup>b</sup>  $\alpha_{12} = 0.30$ ;  $\alpha_{13} = \alpha_{23} = 0.47$ .

The Wilson equation gives the best fit for the binary systems at each temperature. With these parameters, the ternary system was predicted and compared to the experimental data. Table IX shows the estimated variance for the predictions by Wilson, NRTL, and UNIQUAC models. These variances are larger than those obtained when binary data were fitted. This lack of fit indicates that predictions obtained by the Wilson, NRTL, and UNIQUAC equations do not represent the ternary system as well as the binaries. Even though, the predictions still represent a good agreement with the experimental data. Again, the Wilson equation gives the best prediction for the ternary system.

Furthermore, binary parameters were also obtained from the ternary data by using the same procedure already described. The obtained variances of the fit are shown in Table X and the resulting parameters are reported in Table XI. These variances compared well with those obtained when binary data are fitted. And once again, the Wilson equation gives the best fit for the ternary data.

### Glossary

|          |   |
|----------|---|
| $g^E$    | excess Gibbs energy, J/mol                                      |
| $g_{ij}$ | NRTL binary parameter for the $i$ - $j$ pair interaction, J/mol |
| $G_{ij}$ | defined by eq 5   |
| $N$      | number of components  |
| NEX      | total experimental points                                       |

**Table XI. Parameters<sup>a</sup> for the System Benzene (1)-Thiophene (2)-Methanol (3)**

|                               | 35 °C  | 40 °C  | 45 °C  |
|-------------------------------|--------|--------|--------|
| Wilson                        |        |        |        |
| $\lambda_{12} - \lambda_{11}$ | 251.3  | 314.0  | 245.6  |
| $\lambda_{12} - \lambda_{22}$ | -61.8  | -81.9  | -66.7  |
| $\lambda_{13} - \lambda_{11}$ | 610.9  | 627.6  | 573.2  |
| $\lambda_{13} - \lambda_{33}$ | 7941.6 | 7732.4 | 7611.1 |
| $\lambda_{23} - \lambda_{22}$ | 732.2  | 811.7  | 861.9  |
| $\lambda_{23} - \lambda_{33}$ | 7238.7 | 7037.8 | 6816.1 |
| NRTL <sup>b</sup>             |        |        |        |
| $g_{12} - g_{22}$             | 257.9  | 259.6  | 310.6  |
| $g_{12} - g_{11}$             | -120.4 | -79.8  | -171.6 |
| $g_{13} - g_{33}$             | 5167.5 | 5046.1 | 4970.8 |
| $g_{13} - g_{11}$             | 2941.5 | 2941.5 | 2874.5 |
| $g_{23} - g_{33}$             | 4975.0 | 4841.1 | 4665.4 |
| $g_{23} - g_{22}$             | 2610.9 | 2682.1 | 2732.3 |
| UNIQUAC                       |        |        |        |
| $u_{12} - u_{22}$             | 493.4  | 520.1  | 509.7  |
| $u_{12} - u_{11}$             | -381.6 | -381.4 | -409.8 |
| $u_{13} - u_{33}$             | 8644.6 | 8330.7 | 8201.0 |
| $u_{13} - u_{11}$             | -522.3 | -543.9 | -577.4 |
| $u_{23} - u_{33}$             | 7640.3 | 7506.4 | 7217.7 |
| $u_{23} - u_{22}$             | -431.0 | -443.5 | -426.8 |

<sup>a</sup> All values in J/mol. <sup>b</sup>  $\alpha_{12} = 0.3$ ;  $\alpha_{13} = \alpha_{23} = 0.47$ .

|          |   |
|----------|---|
| NP       | number of parameters  |
| $P$      | pressure, mmHg  |
| $q_i$    | molecular-geometric area parameter for the pure component $i$                 |
| $q'_i$   | molecular-interaction area parameter for the pure component $i$               |
| $r_i$    | molecular volume parameter for the pure component $i$                         |
| $R$      | gas constant, J mol <sup>-1</sup> K <sup>-1</sup>                             |
| $S^2$    | objective function defined by eq 13   |
| $T$      | absolute temperature, K   |
| $u_{ij}$ | UNIQUAC binary parameter for the $i$ - $j$ pair interaction, J/mol            |
| $v_j$    | liquid molar volume for the component $i$ , cm <sup>3</sup> mol <sup>-1</sup> |
| $x_i$    | liquid mole fraction for the component $i$                                    |
| $y_i$    | vapor mole fraction for the component $i$                                     |
| $z$      | coordination number   |

### Greek Letters

|                |   |
|----------------|---|
| $\alpha_{ij}$  | NRTL nonrandomness parameter                                      |
| $\lambda_{ij}$ | Wilson binary parameter for the $i$ - $j$ pair interaction, J/mol |
| $\Delta_{ij}$  | defined by eq 2   |
| $\tau_{ij}$    | defined by eq 4 and 12  |
| $\Phi_i$       | volume fraction defined by eq 9                                   |
| $\theta_i$     | area fraction defined by eq 10                                    |
| $\theta'_i$    | area fraction defined by eq 11                                    |
| $\sigma_p(\%)$ | estimated variance of the fit defined by eq 14                    |

Registry No. Benzene, 71-43-2; thiophene, 110-02-1; methanol, 67-56-1.

### Literature Cited

- (1) Wilson, G. M. *J. Am. Chem. Soc.* **1964**, *86*, 127.
- (2) Renon, H.; Prausnitz, J. M. *AIChE J.* **1968**, *14*, 135.
- (3) Abrams, D. S.; Prausnitz, J. M. *AIChE J.* **1975**, *21*, 116.
- (4) Anderson, T. F.; Prausnitz, J. M. *Ind. Eng. Chem. Process Des. Dev.* **1978**, *17*, 552.
- (5) Wichterle, F.; Linek, J.; Hála, E. "Vapor-Liquid Equilibrium Data Bibliography"; Elsevier: Amsterdam, 1973. Supplement 1, 1976. Supplement 2, 1979.

- (6) Triday, J. O. *J. Chem. Eng. Data* 1983, 28, 307.  
 (7) Triday, J. O. Chemical Engineer Thesis, Universidad Técnica Federico Santa María, Valparaíso, Chile, 1977.  
 (8) Vera, J. H.; Prausnitz, J. M. *J. Chem. Eng. Data* 1971, 16, 149.  
 (9) Prausnitz, J. M.; Eckert, C. A.; Orye, R. V.; O'Connell, J. P. "Computer Calculations for Multicomponent Vapor-Liquid Equilibria", 1st ed.; Prentice-Hall: Englewood Cliffs, NJ, 1965.  
 (10) Tsonopoulos, C. *AIChE J.* 1974, 20, 263.  
 (11) Wolfe, P. *Commun. ACM* 1959, 2 (12), 12-3.

- (12) "Selected Values of Physical and Thermodynamic Properties of Hydrocarbons and Related Compounds", API Research Project 44; American Petroleum Institute: Washington, DC, 1962.  
 (13) Reid, C. R.; Prausnitz, J. M.; Sherwood, T. K. "The Properties of Gases and Liquids", 3rd ed.; McGraw-Hill: New York, 1977.

Received for review February 3, 1984. Accepted July 11, 1984. Financial support for this work was provided by the "Dirección General de Desarrollo Científico y Tecnológico", Universidad Técnica Federico Santa María.

## Vapor-Liquid Equilibria in Toluene + *m*-Xylene, Toluene + *n*-Decane, and *n*-Decane + *m*-Xylene Mixtures

Bert Willman and Amyn S. Teja\*

School of Chemical Engineering, Georgia Institute of Technology, Atlanta, Georgia 30332-0100

**Isothermal vapor-liquid equilibria at three temperatures between 373.5 and 394.3 K were measured for the binary systems toluene + *m*-xylene, toluene + *n*-decane, and *n*-decane + *m*-xylene by using a recirculating still. The data reported were found to be thermodynamically consistent and were correlated with four well-known activity coefficient models. The maximum likelihood method was used to estimate the parameters of the models.**

### Introduction

As part of a continuing study of phase equilibria involving coal chemicals, isothermal vapor-liquid equilibria (VLE) were measured for the binary systems toluene + *m*-xylene, toluene + *n*-decane, and *n*-decane + *m*-xylene at three temperatures between 373.5 and 394.3 K.

### Experimental Section

The VLE still that was used in this work was an all-glass Stage-Muller recirculating still described recently by Gutsche and Knapp (7). The prominent features of the still are shown in Figure 1 and a schematic of the whole apparatus is given in Figure 2. The important features of the still are the magnetic sampling valves, the Cottrell pump, and the silver-plated vacuum jacket. The valves allow sampling of the equilibrium phases without disrupting the operation of the still. The vacuum jacket surrounds the equilibrium chamber and prevents partial condensation of the vapor separating from the liquid at the exit from the Cottrell pump. Heating of the fluid mixture was achieved with a heating mantle while a magnetic stirrer was used to mix the contents of the boiling flask. The temperature outside the equilibrium chamber was maintained approximately 1 K lower than the equilibrium temperature by means of a thermostated heating jacket.

The temperature was measured by a thermometer calibrated by the National Bureau of Standards and graduated in increments of 0.2 K. Pressure was measured by a mercury manometer graduated in 0.13 kPa increments. An electronic pressure regulator (constructed by Fischer of West Germany) positioned between the still and a vacuum pump maintained the pressure constant to 0.068 kPa. All experiments were carried out under an inert atmosphere of nitrogen (Matheson Co., purity > 99.99%) to minimize contact with moisture and to accurately control the pressure.

Table I. Physical Properties of Pure Compounds

| property            | this work          | lit. <sup>a</sup> | $\Delta$ , % |
|---------------------|--------------------|-------------------|--------------|
| <i>m</i> -Xylene    |                    |                   |              |
| $n_d$ (293 K)       | 1.4930             | 1.4972            | 0.28         |
| nbp, <sup>d</sup> K | 412.1 <sup>b</sup> | 412.3             | 0.07         |
| <i>n</i> -Decane    |                    |                   |              |
| $n_d$ (293 K)       | 1.4080             | 1.4102            | 0.16         |
| nbp, K              | 447.0 <sup>b</sup> | 447.3             | 0.06         |
| Toluene             |                    |                   |              |
| $n_d$ (293 K)       | 1.4904             | 1.4961            | 0.38         |
| nbp, K              | 383.9              | 383.9             | 0.01         |
| Benzene             |                    |                   |              |
| $n_d$ (293 K)       | 1.4960             | 1.5011            | 0.34         |
| nbp, K              | 353.4              | 353.3             | 0.01         |

<sup>a</sup>Literature values taken from ref 12. <sup>b</sup>Extrapolated from data in 373-393 K range. <sup>c</sup> $\Delta = 100(\text{measured property} - \text{literature property})/(\text{literature property})$ . <sup>d</sup>nbp is the normal boiling point.

Table II. Constants of Eq 1 for Pure Compounds

| compd            | A       | B        | C       |
|------------------|---------|----------|---------|
| <i>m</i> -xylene | 15.4744 | 4305.195 | -15.437 |
| <i>n</i> -decane | 14.8129 | 3864.601 | -65.932 |
| toluene          | 15.175  | 3946.675 | -9.824  |

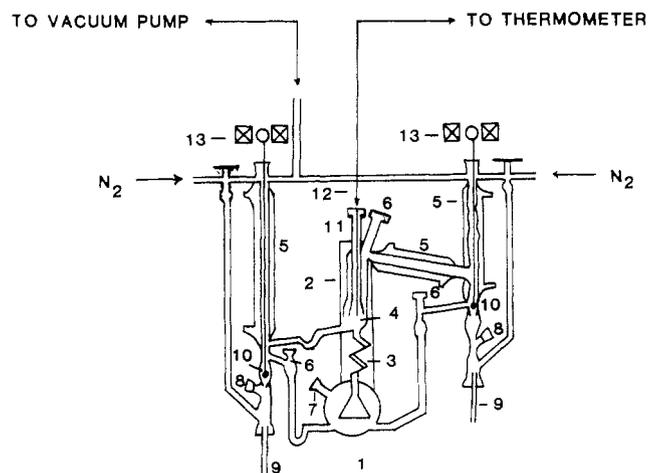


Figure 1. Sketch of Stage-Muller still used in this work: (1) boiling flask, (2) vacuum jacket, (3) Cottrell pump, (4) equilibrium chamber, (5) condensers, (6) injection ports, (7) filling spout and thermometer well, (8) Teflon valves, (9) sample tubes, (10) glass ball valves, (11) equilibrium thermometer well, (12) equilibrium thermometer, (13) solenoid devices (actuates 10).