



**Figure 7.** Miscibility relationships for hydrocarbon mixtures (wt % 1-butanol required for miscibility at 1:1 wt ratio of hydrocarbon to 2.5 *m* aqueous sodium *p*-cymenesulfonate solution; 25 °C).

The relatively simple dependence on EACN, whose applicability the Texas group demonstrated for hydrocarbon mixtures in their interfacial tension measurements, does not seem to apply to the miscibility relationships. Figure 6 compares 1-butanol–2.5 *m* cymenesulfonate systems containing octane, phenyloctane, and a 1:1 mixture of toluene and pentadecane. All three systems have, for the hydrocarbon, EACN = 8. The toluene–pentadecane system requires much more butanol for miscibility than the other two.

We were interested in establishing the basic mixing rules for the miscibility relationship. The studies were limited to the central portion of the phase diagrams where the weight ratio of hydrocarbon to aqueous cymenesulfonate solutions was one. The

amount of butanol required for miscibility was established for the following four systems: hexane–pentadecane; hexane–1-phenyltridecane; toluene–pentadecane; toluene–1-phenyltridecane. The results are summarized in Figure 7. It may be noted that the amount of butanol required in all four systems varies approximately linearly with the weight fraction of one hydrocarbon in the hydrocarbon mixtures. Since some of the phase boundary diagrams are not completely symmetrical, one does not expect the linearity rule to hold generally at other hydrocarbon–aqueous ratios. However there is little doubt that the phase boundaries for the various hydrocarbon mixtures lie between those of the “pure” hydrocarbon systems.

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## Excess Thermodynamic Properties of Binary Liquid Mixtures of 1,2-Dichloroethane with Normal Alkanes

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**Excess volumes and isentropic compressibilities for binary liquid mixtures of 1,2-dichloroethane with hexane, heptane, octane, and nonane were determined at 303.15 K. Isothermal compressibilities were computed from isentropic compressibilities, heat capacities at constant pressure, and thermal coefficients of expansion. Excess isothermal compressibility was then calculated and the  $\kappa_T^E$  data were analyzed in light of both the original and modified versions of the Flory theory. The original theory fails to predict even the sign of  $\kappa_T^E$  while the modified theory correctly predicts the sign of  $\kappa_T^E$  in two systems.**

A survey of the literature has shown that a number of attempts (1–3) have been made to predict excess volumes of binary liquid mixtures by using the values of the Flory interaction parameter derived from experimental excess enthalpy. Several attempts have also been made to predict excess enthalpy by employing the values of the Flory interaction parameter derived from experimental excess volume. However, very few attempts have been made to predict excess isothermal compressibility by employing the values of the interaction parameter from either experimental excess volume or excess enthalpy. These thermodynamic data have an important place in industrial and academic work. Hence an effort has been made to predict excess

Table I. Densities of the Pure Components

| component          | temp, K | $\rho/g\text{ cm}^{-3}$ |                   |
|--------------------|---------|-------------------------|-------------------|
|                    |         | present work            | lit. <sup>5</sup> |
| 1,2-dichloroethane | 303.15  | 1.238 30                | 1.238 31          |
| hexane             | 303.15  | 0.650 64                | 0.650 70          |
| heptane            | 303.15  | 0.675 30                | 0.675 38          |
| octane             | 303.15  | 0.694 59                | 0.694 50          |
| nonane             | 303.15  | 0.709 98                | 0.709 99          |

isothermal compressibility by using the values of the interaction parameter computed from the original Flory theory and that derived from experimental excess volumes. The mixtures studied include 1,2-dichloroethane + hexane, 1,2-dichloroethane + heptane, 1,2-dichloroethane + octane, and 1,2-dichloroethane + nonane. These mixtures have been chosen because they come under the category of *n*-alkane mixtures for which the Flory theory has been designed. The new experimental data reported here are excess volumes and isentropic compressibilities determined at 303.15 K.

#### Experimental Section

**Materials.** 1,2-Dichloroethane, hexane, and heptane, supplied by B.D.H. Chemicals, England, and octane and nonane supplied by Veb Chemicals, West Germany, were purified by the methods

Table II. Parameters of the Pure Components at 303.15 K

| component          | $10^3\alpha/\text{deg}^{-1}a$ | $K_T/\text{TPa}^{-1}b$ | $V/\text{cm}^3\text{mol}^{-1}a$ | $\tilde{v}^c$ | $V^*/\text{cm}^3\text{mol}^{-1}$ | $P^*/\text{Jcm}^{-3}d$ | $\tilde{T}^c$ |
|--------------------|-------------------------------|------------------------|---------------------------------|---------------|----------------------------------|------------------------|---------------|
| 1,2-dichloroethane | 1.189                         | 856.7                  | 79.92                           | 1.289         | 62.00                            | 699.1                  | 0.062 95      |
| hexane             | 1.404                         | 1791.7                 | 132.45                          | 1.329         | 99.65                            | 419.7                  | 0.068 09      |
| heptane            | 1.260                         | 1526.3                 | 148.39                          | 1.303         | 113.92                           | 424.7                  | 0.064 76      |
| octane             | 1.195                         | 1373.5                 | 164.46                          | 1.290         | 127.47                           | 439.0                  | 0.063 11      |
| nonane             | 1.062                         | 1217.3                 | 180.65                          | 1.264         | 142.94                           | 422.5                  | 0.059 41      |

<sup>a</sup> Experimentally determined. <sup>b</sup> Computed from eq 3. <sup>c</sup> Computed from the thermal expansion coefficient. <sup>d</sup> Computed from isothermal compressibility.

Table III. Experimental Values of  $V^E$  for the Binary Systems of 1,2-Dichloroethane + *n*-Alkanes<sup>a</sup>

| 1,2-dichloroethane + hexane |       | 1,2-dichloroethane + heptane |       | 1,2-dichloroethane + octane |       | 1,2-dichloroethane + nonane |       |
|-----------------------------|-------|------------------------------|-------|-----------------------------|-------|-----------------------------|-------|
| $x_1$                       | $V^E$ | $x_1$                        | $V^E$ | $x_1$                       | $V^E$ | $x_1$                       | $V^E$ |
| 0.1225                      | 0.312 | 0.1452                       | 0.471 | 0.1472                      | 0.542 | 0.1502                      | 0.605 |
| 0.2058                      | 0.453 | 0.2561                       | 0.712 | 0.2360                      | 0.773 | 0.2793                      | 0.911 |
| 0.3609                      | 0.598 | 0.3821                       | 0.844 | 0.4078                      | 1.015 | 0.4385                      | 1.090 |
| 0.4826                      | 0.597 | 0.5295                       | 0.854 | 0.4802                      | 1.043 | 0.5431                      | 1.097 |
| 0.6105                      | 0.525 | 0.6230                       | 0.775 | 0.5775                      | 1.021 | 0.6746                      | 0.974 |
| 0.7255                      | 0.409 | 0.7250                       | 0.643 | 0.6797                      | 0.898 | 0.8154                      | 0.698 |
| 0.8328                      | 0.265 | 0.8154                       | 0.468 | 0.8012                      | 0.654 | 0.8732                      | 0.532 |
| 0.9020                      | 0.162 | 0.9090                       | 0.247 | 0.9216                      | 0.289 | 0.9263                      | 0.337 |

<sup>a</sup>  $x_1$  indicates mole fraction of 1,2-dichloroethane;  $V^E$  in  $\text{cm}^3\text{mol}^{-1}$ .

described by Reddick and Bunger (4). The purity of the samples was checked by comparing the measured densities of the samples with those reported in literature (5). The densities were measured by using a bicapillary pycnometer. The measured data of densities along with the literature values are reported in Table I.

**Excess Volumes and Compressibilities.** The excess volumes were determined by using a single composition per loading type dilatometer described by Rao and Naidu (6). The values were accurate to  $\pm 0.003\text{ cm}^3\text{mol}^{-1}$ .

Isentropic compressibilities ( $\kappa_s$ ) were computed from ultrasonic sound velocities ( $u$ ) and densities ( $\rho$ ) by using the relation

$$\kappa_s = u^{-2}\rho^{-1} \quad (1)$$

Ultrasonic sound velocities were determined with a single-crystal ultrasonic interferometer at a frequency of 2 MHz and were accurate to  $\pm 0.15\%$  (7). The densities were computed from experimental  $V^E$ , using the relation

$$\rho = \frac{\chi_1 M_1 + \chi_2 M_2}{V + V^E} \quad (2)$$

where  $\chi_1$  and  $\chi_2$  and  $M_1$  and  $M_2$  denote the mole fractions and molecular weights of 1,2-dichloroethane and normal alkanes, respectively.  $V$  stands for molar volume and  $V^E$  for excess molar volume. Isothermal compressibilities ( $\kappa_T$ ) were calculated by using the relation

$$\kappa_T = \kappa_s + \alpha^2 VT/C_p \quad (3)$$

where  $\alpha$ ,  $V$ ,  $T$ , and  $C_p$  denote thermal expansion coefficient, molar volume, temperature, and heat capacity at constant pressure. In the case of mixtures the thermal coefficient of expansion and heat capacity at constant pressure were assumed to be additive in terms of volume fraction and mole fraction, respectively.

The excess isothermal compressibilities were evaluated from the relation

$$\kappa_T^E = \kappa_T - \phi_1 \kappa_{T,1} - \phi_2 \kappa_{T,2} \quad (4)$$

Table IV. Values of the Parameters in Equation 12 and the Standard Deviation

| system                       | $a_0$ | $a_1$  | $a_2$  | $\sigma(V^E)/\text{cm}^3\text{mol}^{-1}$ |
|------------------------------|-------|--------|--------|--|
| 1,2-dichloroethane + hexane  | 2.378 | -0.699 | -0.037 | 0.003                                    |
| 1,2-dichloroethane + heptane | 3.466 | -0.548 | -0.046 | 0.004                                    |
| 1,2-dichloroethane + octane  | 4.185 | -0.154 | 0.009  | 0.004                                    |
| 1,2-dichloroethane + nonane  | 4.389 |        | 0.727  | 0.006                                    |

where  $\kappa_T$ ,  $\kappa_{T,1}$ , and  $\kappa_{T,2}$  are isothermal compressibilities of the mixture and pure components and  $\phi_1$  and  $\phi_2$  are volume fractions of 1,2-dichloroethane and *n*-alkanes.

### Theory and Calculations

Flory (8, 9) formulated the following theoretical equations for excess volume and excess isothermal compressibility:

$$V^E = \tilde{v}^E(\chi_1 V_1^* + \chi_2 V_2^*) \quad (5)$$

$$\kappa_T^E = \frac{3\tilde{v}^2(\tilde{v}^{1/3} - 1)}{P^*[1 - 3(\tilde{v}^{1/3} - 1)]} - \frac{1}{\tilde{v}}(\phi_1 \tilde{v}_1 \kappa_{T,1} + \phi_2 \tilde{v}_2 \kappa_{T,2}) \quad (6)$$

where

$$\tilde{v}^E = (\tilde{v}^0)^{7/3} [4/3 - (\tilde{v}^0)^{1/3}]^{-1} (\tilde{T} - \tilde{T}^0) \quad (7)$$

$$\tilde{T} = \frac{(\phi_1 P_1^* \tilde{T}_1 + \phi_2 P_2^* \tilde{T}_2)}{(\phi_1 P_1^* + \phi_2 P_2^* - \phi_1 \theta_2 X_{12})} \quad (8)$$

$$\theta_2 = \frac{\phi_2}{\phi_1(S_1/S_2) + \phi_2} \quad (9)$$

$$X_{12} = P_1^*[1 - (S_1/S_2)^{1/2}(P_2^*/P_1^*)^{1/2}]^2 \quad (10)$$

$$P^* = (\phi_1 P_1^* + \phi_2 P_2^* - \phi_1 \theta_2 X_{12}) \quad (11)$$

The quantities in eq 5-11 have the same significance described by Flory (8, 9).

In application of the original theory of Flory to excess isothermal compressibilities, the numerical evaluation of characteristic and reduced parameters for the pure components and mixtures was carried out according to the procedure adopted by Flory (8, 9). The values of the parameters for pure components are included in Table II. To predict  $\kappa_T^E$  on the basis of the modified Flory theory, we obtained the values of the interaction parameter from experimental  $V^E$  at each composition.

### Results and Discussion

The experimental excess volumes for the four binary mixtures determined at 303.15 K are given in Table III. The experimental values of  $V^E$  are represented by an empirical equation

$$V^E/\text{cm}^3\text{mol}^{-1} = \chi_1 \chi_2 \sum_{i=0}^k a_i (\chi_1 - \chi_2)^i \quad (12)$$

Table V. Experimental and Predicted Values of  $\kappa_T^E$  for the Binary Systems of 1,2-Dichloroethane + Alkanes at 303.15 K<sup>a</sup>

| system                       | $\phi_1$ | $\kappa_s$ | original theory   |              | modified theory   |              | $\kappa_T^E$<br>(exptl) |
|------------------------------|----------|------------|-------------------|--------------|-------------------|--------------|-------------------------|
|                              |          |            | $\theta_2 X_{12}$ | $\kappa_T^E$ | $\theta_2 X_{12}$ | $\kappa_T^E$ |                         |
| 1,2-dichloroethane + hexane  | 0.0777   | 1329       | 16.5250           | -47          | 53.5708           | -4           | 2                       |
|                              | 0.1352   | 1286       | 15.3142           | -75          | 49.1883           | -8           | 5                       |
|                              | 0.2541   | 1194       | 12.8980           | -114         | 41.4447           | -14          | 8                       |
|                              | 0.3601   | 1112       | 10.8385           | -132         | 34.4640           | -31          | 10                      |
|                              | 0.4860   | 1010       | 8.4984            | -134         | 27.0549           | -44          | 9                       |
|                              | 0.6146   | 902        | 6.2218            | -119         | 19.9433           | -49          | 4                       |
|                              | 0.7503   | 791        | 3.9322            | -89          | 12.7152           | -43          | 2                       |
|                              | 0.8474   | 711        | 2.3620            | -59          | 7.7562            | -30          | 1                       |
| 1,2-dichloroethane + heptane | 0.0838   | 1152       | 11.8064           | -25          | 54.1383           | 25           | 6                       |
|                              | 0.1564   | 1111       | 10.7385           | -42          | 48.6228           | 34           | 10                      |
|                              | 0.2498   | 1058       | 9.3477            | -59          | 41.1726           | 34           | 15                      |
|                              | 0.3774   | 982        | 7.5415            | -71          | 32.6802           | 25           | 17                      |
|                              | 0.4709   | 922        | 6.2812            | -73          | 26.8137           | 15           | 13                      |
|                              | 0.5867   | 849        | 4.7881            | -68          | 20.5186           | 5            | 11                      |
|                              | 0.7040   | 772        | 3.3463            | -56          | 14.2747           | -3           | 7                       |
|                              | 0.8432   | 684        | 1.7232            | -34          | 7.3434            | -6           | 2                       |
| 1,2-dichloroethane + octane  | 0.0774   | 1061       | 7.1467            | -19          | 58.3895           | 17           | 9                       |
|                              | 0.1305   | 1040       | 6.6409            | -30          | 53.2869           | 47           | 15                      |
|                              | 0.2507   | 981        | 5.5472            | -47          | 42.9387           | 59           | 17                      |
|                              | 0.3099   | 952        | 5.0345            | -61          | 38.5884           | 59           | 19                      |
|                              | 0.3991   | 906        | 4.2862            | -56          | 32.7922           | 56           | 18                      |
|                              | 0.5077   | 850        | 3.4205            | -47          | 25.8367           | 45           | 17                      |
|                              | 0.6620   | 767        | 2.2647            | -40          | 17.1839           | 28           | 11                      |
|                              | 0.8511   | 667        | 0.9564            | -22          | 7.2124            | 9            | 7                       |
| 1,2-dichloroethane + nonane  | 0.0725   | 985        | 7.2005            | -3           | 49.5117           | 30           | 17                      |
|                              | 0.1463   | 963        | 6.4889            | -4           | 44.6741           | 51           | 26                      |
|                              | 0.2568   | 922        | 5.4784            | -8           | 44.2345           | 62           | 31                      |
|                              | 0.3446   | 886        | 4.7170            | -10          | 28.8268           | 60           | 31                      |
|                              | 0.4784   | 826        | 3.6244            | -12          | 21.3552           | 52           | 27                      |
|                              | 0.6615   | 741        | 2.2458            | -12          | 13.5004           | 36           | 16                      |
|                              | 0.7529   | 700        | 1.6030            | -10          | 9.9674            | 28           | 13                      |
|                              | 0.8476   | 656        | 0.9669            | -7           | 6.1672            | 19           | 8                       |

<sup>a</sup>  $\phi_2 X_{12}$  in J mol<sup>-1</sup>,  $V^E$  in cm<sup>3</sup> mol<sup>-1</sup>,  $\kappa_s$  and  $\kappa_T^E$  in TPa<sup>-1</sup>, and  $\phi_1$  indicates the volume fraction of 1,2-dichloroethane.

where  $a_0, a_1, \dots, a_k$  are adjustable parameters. The values of the parameters, obtained by the least-squares method, are included in Table IV along with the standard deviation,  $\sigma(V^E)$ .

The experimental isentropic compressibilities determined at 303.15 K are included in column 3 of Table V. The predicted and experimental isothermal compressibilities for the four binary systems are shown in columns 5, 7, and 8 of Table V. The data show that the original theory fails even to predict the correct sign of  $\kappa_T^E$  in all cases. Further, the modified theory correctly predicts the sign of  $\kappa_T^E$  in the systems of 1,2-dichloroethane with octane and nonane and fails to predict even the sign of  $\kappa_T^E$  for the system of 1,2-dichloroethane with heptane in mixtures rich in 1,2-dichloroethane and over the whole range of composition for the system 1,2-dichloroethane with hexane. This shows though the modified theory is superior to original theory it fails to predict correctly the sign of  $\kappa_T^E$  which is sensitive to molecular geometry unlike excess enthalpy.

### Glossary

|            |  |
|------------|--|
| $\rho$     | density, g cm <sup>-3</sup>                      |
| $\kappa_T$ | isothermal compressibility, TPa <sup>-1</sup>    |
| $\kappa_s$ | isentropic compressibility, TPa <sup>-1</sup>    |
| $\alpha$   | thermal expansion coefficient, deg <sup>-1</sup> |
| $T$        | temperature, K                                   |
| $V$        | molar volume, cm <sup>3</sup> mol <sup>-1</sup>  |

|             |  |
|-------------|--|
| $V^E$       | excess molar volume, cm <sup>3</sup> mol <sup>-1</sup>                     |
| $C_p$       | heat capacity at constant pressure, J mol <sup>-1</sup>                    |
| $\phi_i$    | segment fraction of component $i$  |
| $\theta_2$  | site fraction  |
| $\bar{v}_i$ | reduced volume of component $i$  |
| $\bar{v}^0$ | ideal reduced volume of mixture  |
| $\bar{v}^E$ | excess reduced volume  |
| $V_i^*$     | characteristic volume of component $i$ , cm <sup>3</sup> mol <sup>-1</sup> |
| $P_i^*$     | characteristic pressure of component $i$ , J cm <sup>-3</sup>              |
| $\bar{T}_i$ | reduced temperature of component $i$                                       |
| $S_i$       | site fraction of component $i$   |
| $X_{12}$    | interaction parameter, J mol <sup>-1</sup>                                 |

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