

crystals (item 51) that gave two long spacings, one for the A form (10 orders) and the other for the B form (4 orders), but the short-spacing pattern differed from the A pattern only by an additional strong spacing at 3.74 Å. Therefore, a strong short spacing at 3.74 Å can be taken as characteristic of the B form.

A review of the long-spacing data based on the X-ray powder-diffraction data of Kurokawa (11), five values, and those calculated ( $c \sin \beta$ ) from the single-crystal data of Turner and Lingafelter (12), six values, and of Sakurai (9), three values, indicates that the A modification has been the only form observed for even-carbon amides up to myristamide. When plotted against  $n$ , these data were satisfied by eq 3 with an average deviation

$$L = 1.755n + 3.263 \quad (3)$$

of 0.16 Å. The calculated angle of tilt is therefore  $\sin^{-1} 1.755/2.54 = 43^\circ 42'$ .

Because only limited X-ray data were published on four long-chain methyl ketones reported in a previous publication (13), these four compounds (2-tridecanone, 2-pentadecanone, 2-heptadecanone, and 2-nonadecanone) are listed in Table I with complete X-ray data. When the long spacings of these compounds are plotted vs. number of carbons, the three longer compounds fall squarely on a straight line (the C<sub>13</sub> compound is slightly off the line) represented by eq 4. The calculated angle

$$L = 2.40n + 6.60 \quad (4)$$

of tilt of these long-chain methyl ketones is therefore  $\sin^{-1} 2.40/2.54 = 70^\circ 53'$ .

Item 21 in Table I, prepared by melting an equimolar mixture of morpholine stearate and cyclohexylamine palmitate and allowing it to crystallize from the melt, gave a long spacing characteristic of cyclohexylamine stearate (item 16) and none for the other combination possible from the four ions present.

Mod et al. (14) have studied the ternary reciprocal salt pair system involving the cyclohexylamine and morpholine salts of stearic and palmitic acids and prepared a freezing-point diagram for this system. A study of this diagram indicates that the first crystals to form from the melt of a 50:50 mixture would be cyclohexylamine stearate. The first crystals would tend to grow and be larger and better formed than those coming out later when components of eutectic mixtures were crystallizing. It is therefore not surprising that the long spacing for only cyclohexylamine stearate was observed in the X-ray data for the mixture.

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#### Literature Cited

- (1) Mod, R. R.; Magne, F. C.; Skau, E. L. *J. Am. Oil Chem. Soc.* **1959**, *36*, 616.
- (2) Mod, R. R.; Magne, F. C.; Skau, E. L. *J. Chem. Eng. Data* **1960**, *5*, 478.
- (3) Mod, R. R.; Magne, F. C.; Skau, E. L. *J. Chem. Eng. Data* **1962**, *7*, 31.
- (4) Mod, R. R.; Harris, J. A.; Skau, E. L. *J. Chem. Eng. Data* **1968**, *13*, 115.
- (5) Mod, R. R.; Magne, F. C.; Skau, E. L. *J. Phys. Chem.* **1956**, *60*, 1651.
- (6) Mod, R. R.; Magne, F. C.; Skau, E. L. *J. Am. Oil Chem. Soc.* **1959**, *36*, 102.
- (7) O'Connor, R. T.; Mod, R. R.; Murray, M. D.; Skau, E. L. *J. Am. Chem. Soc.* **1955**, *77*, 892.
- (8) Skau, E. L. *J. Am. Oil Chem. Soc.* **1973**, *50*, 245.
- (9) Sakurai, T. *J. Phys. Soc. Jpn.* **1955**, *10*, 1040.
- (10) Sakurai, T.; Yabe, M. *J. Phys. Soc. Jpn.* **1958**, *13*, 5.
- (11) Kurokawa, S. *Bull. Chem. Soc. Jpn.* **1955**, *28*, 660.
- (12) Turner, J. D.; Lingafelter, E. C. *Acta Crystallogr.* **1955**, *8*, 549.
- (13) Bailey, A. V.; Mltcham, D.; Skau, E. L. *J. Chem. Eng. Data* **1970**, *15*, 542.
- (14) Mod, R. R.; Magne, F. C.; Skau, E. L. *J. Am. Oil Chem. Soc.* **1958**, *35*, 688.

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## Densities of NaCl, MgCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub>, and MgSO<sub>4</sub> Aqueous Solutions at 1 atm from 0 to 50 °C and from 0.001 to 1.5 m

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The relative densities ( $d - d_0$ ) of NaCl, MgCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub>, and MgSO<sub>4</sub> aqueous solutions have been determined at 1 atm with a vibrating flow densimeter from 0.001 to 1.5 m and from 0 to 35 °C. The data have been combined with our earlier measurements at temperatures up to 55 °C and fitted to equations of the following form (precisions better than  $15 \times 10^{-6} \text{ g cm}^{-3}$ ):  $d - d_0 = Am + Bm^{3/2} + Cm^2 + Dm^{5/2}$ , where  $d$  and  $d_0$  are the densities of solution and pure water, respectively,  $m$  is the molality, and  $A$ ,  $B$ ,  $C$ , and  $D$  are temperature-dependent parameters. The equations agree well with the results of other workers.

#### Introduction

The basic pressure-volume-temperature-concentration properties of NaCl, MgCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub>, and MgSO<sub>4</sub> aqueous solutions

are of prime importance for various thermodynamic calculations in solution chemistry, geochemistry, and oceanography. They are also important in the engineering calculations such as those concerning the process of converting salty water to potable water and the process of assessing salty water intrusion in the freshwater aquifers. A survey of the literature (14) reveals the scarcity of reliable experimental 1-atm density data for these solutions at temperatures other than 25 °C. The present paper provides precise 1-atm density data from 0 to 55 °C and from 0 to 1.5 m for the major sea salts. The results have been fitted to equations that are simple polynomial functions of  $t$  (°C) and  $m^{1/2}$  (molality).

#### Experimental Section

Densities of NaCl, MgCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub>, and MgSO<sub>4</sub> aqueous solutions have been measured at various temperatures and concentrations on a high-precision digital readout flow densimeter

Table I. Relative Density of NaCl, MgCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub>, and MgSO<sub>4</sub> Aqueous Solutions

<i>m</i>	1000Δ <i>d</i>	<i>m</i>	1000Δ <i>d</i>	<i>m</i>	1000Δ <i>d</i>	<i>m</i>	1000Δ <i>d</i>	<i>m</i>	1000Δ <i>d</i>	<i>m</i>	1000Δ <i>d</i>
NaCl, 0 °C		NaCl, 35 °C		MgCl <sub>2</sub> , 25 °C		0.16373	21.547	0.70189	83.141	MgSO <sub>4</sub> , 25 °C	
0.01029	0.470	0.04120	1.670	0.00469	0.372	0.19951	26.097	0.72018	85.166	0.00099	0.128
0.04120	1.864	0.09485	3.817	0.00978	0.785	0.30182	38.931			0.00549	0.688
0.16630	7.429	0.16630	6.673	0.00989	0.797	0.50208	63.252	Na <sub>2</sub> SO <sub>4</sub> , 35 °C		0.01177	1.458
0.50190	21.845	0.50190	19.740	0.00989	0.802	0.56760	71.015	0.00340	0.443	0.02231	2.742
0.99920	42.290	0.99920	38.413	0.01972	1.576	0.70189	86.634	0.01055	1.339	0.02786	3.426
				0.04851	3.854			0.05050	6.331	0.03855	4.726
NaCl, 5 °C		MgCl <sub>2</sub> , 0 °C		0.05038	3.994	Na <sub>2</sub> SO <sub>4</sub> , 15 °C		0.05553	6.961	0.03855	4.727
0.01029	0.455	0.00469	0.391	0.05038	3.999	0.00340	0.458	0.10019	12.461	0.07019	8.526
0.04120	1.819	0.00469	0.397	0.07890	6.212	0.01055	1.388	0.16373	20.184	0.07019	8.528
0.09485	4.154	0.00978	0.822	0.09970	7.845	0.01399	1.850	0.30182	36.603	0.11669	14.048
0.16630	7.257	0.01972	1.645	0.09970	7.850	0.01399	1.859	0.33307	40.251	0.12010	14.459
0.19849	8.631	0.04137	3.423	0.19500	15.185	0.03178	4.171	0.40356	48.438	0.12010	14.463
0.50120	21.347	0.04851	4.018	0.19525	15.172	0.05050	6.583	0.50208	59.687	0.21211	25.246
0.50190	21.360	0.07890	6.478	0.19893	15.476	0.05553	7.234	0.56760	67.098	0.21211	25.253
0.72467	30.469	0.09627	7.909	0.19893	15.475	0.10019	12.941			0.23758	28.188
0.99920	41.420	0.19500	15.811	0.28278	21.818	0.16373	20.922	MgSO <sub>4</sub> , 0 °C		0.00099	0.129
1.00120	41.512	0.19525	15.856	0.37485	28.701	0.19951	25.387	0.00549	0.730	0.39375	46.132
1.49986	60.719	0.28278	22.731	0.49487	37.572	0.30182	37.908	0.01177	1.538	0.64325	74.089
		0.37485	29.875	0.49487	37.575	0.33307	41.680	0.02786	3.584	0.88167	100.043
NaCl, 15 °C		0.40811	32.434	0.55193	41.719	0.40356	50.095	0.03855	4.944	0.88167	100.049
0.01029	0.437	0.55193	43.342	0.63404	47.644	0.50208	61.705	0.07019	8.908	1.23320	137.220
0.04120	1.751	0.63404	49.489	0.71531	53.503	0.56760	69.311	0.11669	14.678	1.23320	137.223
0.09485	4.004	0.79758	61.551	0.79758	59.328	0.70189	84.640			1.35795	150.078
0.16630	6.986	0.97410	74.252	0.99097	72.852	Na <sub>2</sub> SO <sub>4</sub> , 25 °C		MgSO <sub>4</sub> , 5 °C		1.35795	150.082
0.19849	8.312			0.99097	72.850	0.00259	0.335	0.00099	0.131	1.42400	156.831
0.50120	20.610	MgCl <sub>2</sub> , 5 °C		1.47531	105.418	0.00340	0.436	0.00549	0.717	1.42400	156.843
0.50190	20.634	0.00469	0.384	1.47531	105.422	0.00504	0.651	0.01177	1.515	1.48251	162.740
0.72467	29.457	0.00978	0.816			0.01055	1.361	0.02231	2.851	1.48251	162.748
0.99920	40.087	0.01972	1.615	MgCl <sub>2</sub> , 35 °C		0.01270	1.591	0.02786	3.551		
1.00120	40.168	0.04137	3.381	0.00469	0.362	0.01682	2.162	0.03855	4.883	MgSO <sub>4</sub> , 35 °C	
1.49986	58.848	0.04851	3.967	0.04851	3.805	0.03022	3.867	0.07019	8.797	0.00099	0.115
		0.07890	6.388	0.09627	7.547	0.03581	4.575	0.11669	14.503	0.00549	0.675
NaCl, 25 °C		0.09627	7.805	0.28278	21.689	0.04293	5.477	0.12010	14.905	0.01177	1.444
0.00992	0.414	0.19500	15.624	0.37485	28.558	0.05050	6.437	0.21211	26.013	0.02231	2.718
0.01011	0.420	0.19525	15.624	0.40811	30.988	0.05553	7.075	0.23758	29.092	0.02786	3.399
0.01029	0.426	0.37485	29.484	0.55193	41.473	0.05958	7.569	1.48251	166.290	0.03855	4.704
0.04120	1.696	0.40811	32.016	Na <sub>2</sub> SO <sub>4</sub> , 0 °C		0.07698	9.753			0.07019	8.452
0.05002	2.068	0.55193	42.831	0.00340	0.481	0.08861	11.205	MgSO <sub>4</sub> , 15 °C		0.11669	13.960
0.05003	2.066	0.63404	48.895	0.01055	1.464	0.09850	12.443	0.00099	0.133	0.12010	14.321
0.09485	3.894			0.01399	1.954	0.10019	12.652	0.00549	0.698	0.23758	27.997
0.09989	4.101	MgCl <sub>2</sub> , 15 °C		0.03178	4.381	0.11256	14.185	0.01177	1.488	0.39375	45.770
0.10039	4.129	0.00469	0.377	0.05050	6.918	0.13651	17.137	0.02231	2.792	0.64325	73.548
0.19849	8.096	0.00978	0.790	0.05553	7.610	0.16801	20.993	0.02786	3.486	0.88167	99.331
0.20009	8.162	0.01972	1.593	0.10019	13.584	0.19951	24.841	0.03855	4.793	1.23320	136.281
0.29972	12.145	0.04137	3.319	0.10019	13.584	0.24072	29.799	0.07019	8.629	1.35795	149.108
0.40009	16.116	0.04851	3.886	0.16373	21.944	0.30182	37.131	0.11669	14.242	1.42400	155.833
0.49946	20.012	0.07890	6.275	0.19951	26.583	0.33307	40.842	0.12010	14.641	1.48251	161.662
0.50120	20.097	0.09627	7.665	0.50208	64.261	0.35894	43.890	0.21211	25.561		
0.50190	20.113	0.19525	15.334	0.56760	72.106	0.40356	49.122	0.23758	28.575		
0.59971	23.907	0.37485	28.994	0.70189	87.887	0.50061	60.360	0.39375	46.690		
0.69917	27.740	0.40811	31.464	Na <sub>2</sub> SO <sub>4</sub> , 5 °C		0.50208	60.537	0.64325	74.884		
0.72467	28.740	0.55193	42.109	0.00340	0.468	0.56760	68.027	0.88167	101.076		
0.79957	31.578	0.63404	48.105	0.01055	1.438			1.23320	138.504		
0.90125	35.435			0.01399	1.905						
0.99920	39.126	0.97410	72.309	0.03178	4.302						
1.00010	39.156			0.05050	6.780						
1.00120	39.215			0.05553	7.446						
1.49986	57.520										

(10, 13). The data have been combined with the results of our earlier measurements (15–17) to give reliable equations of state for the four major sea salts at 1 atm over the total range 0–55 °C and 0–1.5 *m*.

All of the solutions have been made by weight with reagent-grade (Baker Analyzed) chemicals (without further purification) and ion-exchanged water (Millipore Super Q System). The concentrations of NaCl and Na<sub>2</sub>SO<sub>4</sub> stock solutions have been analyzed by heating to dryness, whereas the concentration of the MgCl<sub>2</sub> stock solution has been analyzed for Cl<sup>-</sup> by titration with AgNO<sub>3</sub>; the concentration of the MgSO<sub>4</sub> stock solution has been analyzed for SO<sub>4</sub><sup>2-</sup> by titration with BaCl<sub>2</sub>.

The vibrating flow densimeter used to make the density measurements is described in detail elsewhere (1, 10, 13). The instrument applies the principle of the vibrating tube. By

measuring the resonance frequency of a hollow metallic tube filled with the solution, one can readily determine the density of the solution. In this study, only relative densities (Δ*d*) are desired

$$\Delta d = d - d_0 = k(\tau^2 - \tau_0^2) \quad (1)$$

where *d* and *d*<sub>0</sub> are respectively the densities of the unknown and reference fluids, *k* is a constant (at a given *T* and *P*), and  $\tau$  and  $\tau_0$  are the periods of the natural frequency of the oscillator containing the unknown and reference fluids, respectively. The instrument constant, *k*, is determined by measuring the  $\tau$  in pure water (ion-exchanged, Millipore Super Q System) and N<sub>2</sub>. The densities of pure water are taken from Kell (9), and the densities of nitrogen are obtained from the van der Waals equation (8). The temperature of the densimeter has been controlled to ±0.001 °C. The temperature has been set to ±0.002 °C with

Table II. Coefficients for Eq 2<sup>a</sup>

variables	NaCl	MgCl <sub>2</sub>	Na <sub>2</sub> SO <sub>4</sub>	MgSO <sub>4</sub>
<i>m</i>	45.872	84.223	140.89	131.174
<i>mt</i>	-0.243	-0.290	-0.608	-0.3261
<i>mt</i> <sup>2</sup>	4.05E-3	8.36E-3	7.88E-3	1.88E-3
<i>mt</i> <sup>3</sup>	-4.39E-5	-1.48E-4	-3.67E-5	8.43E-5
<i>mt</i> <sup>4</sup>	2.91E-7	1.34E-6	6.70E-8	-1.12E-6
<i>m</i> <sup>3/2</sup>	-2.766	-6.215	-15.710	-17.615
<i>m</i> <sup>3/2</sup> <i>t</i>	0.0534	0.0816	0.272	0.1629
<i>m</i> <sup>3/2</sup> <i>t</i> <sup>2</sup>	-6.02E-4	-1.38E-3	-3.11E-3	-1.96E-3
<i>m</i> <sup>2</sup>	-0.793	-1.909	-3.598	5.395
<i>m</i> <sup>2</sup> <i>t</i>				-1.35E-2
<i>m</i> <sup>5/2</sup>				-2.665
validity range	0-1.5 <i>m</i> , 0-55 °C	0-1 <i>m</i> , 0-50 °C	0-1 <i>m</i> , 0-50 °C	0-1.5 <i>m</i> , 0-50 °C
std dev (10 <sup>-6</sup> g cm <sup>-3</sup> )	11.6	10.0	8.9	15.2

<sup>a</sup> The terms *E*-*a*, given for each variable, mean the coefficient is times 10<sup>-*a*</sup>.

a platinum resistance thermometer and a G-2 Mueller bridge (IPST 1968 temperature scale).

### Results

The relative densities of NaCl, MgCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub>, and MgSO<sub>4</sub> aqueous solutions have been measured over the range 0.001-1.5 *m* and 0-35 °C. The results are tabulated in Table I. The values given in Table I are combined with the magnetic float data obtained earlier in this laboratory (15-17) and fitted into equations of the form (g cm<sup>-3</sup>)

$$10^3 \Delta d = 10^3(d - d_0) = Am + Bm^{3/2} + Cm^2 + Dm^{5/2} \quad (2)$$

where *A*, *B*, *C*, and *D*, the temperature dependent parameters, are given in Table II along with the standard deviations of the fit and *m* is the molality.

In order to calculate the density of the solutions, one needs the densities of pure water. We have thus refitted the pure water density equation given by Kell (9) to a polynomial equation which is precise to 0.044 × 10<sup>-6</sup> g cm<sup>-3</sup> (one standard deviation) over the range 0-55 °C (3)

$$d_0 \text{ (g cm}^{-3}\text{)} = 0.9998395 + 6.7914 \times 10^{-5}t - 9.0894 \times 10^{-6}t^2 + 1.0171 \times 10^{-7}t^3 - 1.2846 \times 10^{-9}t^4 + 1.1592 \times 10^{-11}t^5 - 5.0125 \times 10^{-14}t^6 \quad (3)$$

### Discussion and Conclusion

The relative densities of NaCl aqueous solutions (*d* - *d*<sub>0</sub>) calculated from eq 2 at various concentrations and temperatures are compared with the data of Dunn (5, 6), Lee (11), and Desnoyers and co-workers (7, 12) in Figure 1 over the temperature range 0.05-45 °C and the concentration range 0-0.85 *m*. The data of Dunn are precise to 20 × 10<sup>-6</sup> g cm<sup>-3</sup> (duplicate measurements) and ours to 12 × 10<sup>-6</sup> g cm<sup>-3</sup> (one standard deviation of the fit). The agreement is within the combined precision of 32 × 10<sup>-6</sup> g cm<sup>-3</sup> over most of the concentration and temperature ranges.

Little, if any, density data with precisions better than 100 × 10<sup>-6</sup> g cm<sup>-3</sup> at 1 *m* are available in the literature for MgCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub>, and MgSO<sub>4</sub> aqueous solutions at temperatures other than 25 °C. Therefore, it is only attempted to compare our density results for MgCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub>, and MgSO<sub>4</sub> solutions with the data of other workers at 25 °C. The data of Lee (11) were chosen for comparisons because they cover wide concentration ranges and have good precisions (concentrations up to 3.4, 1.3, 1.3, and 1.0 *m* for NaCl, MgCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub>, and MgSO<sub>4</sub> aqueous solutions, respectively, with standard deviations of 13 × 10<sup>-6</sup>, 6 × 10<sup>-6</sup>, 12 × 10<sup>-6</sup>, and 12 × 10<sup>-6</sup> g cm<sup>-3</sup>). It is shown in Figure 2 that our NaCl relative densities agree with the data of

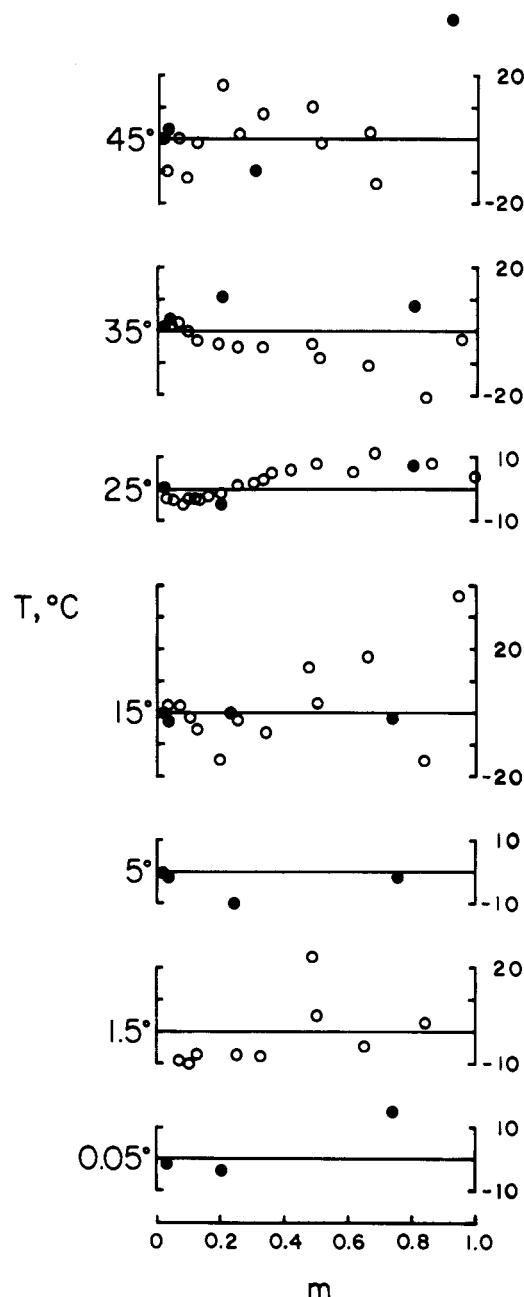


Figure 1. Comparisons of the relative densities (*d* - *d*<sub>0</sub> in 10<sup>-6</sup> g cm<sup>-3</sup>) of NaCl aqueous solutions with the data of Dunn (5, 6) (solid circles) and Fortier et al. (7) and Perron et al. (12) (open circles) at various temperatures.

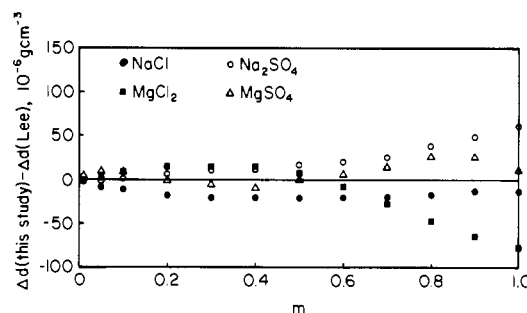


Figure 2. Comparisons of the relative densities (*d* - *d*<sub>0</sub> in 10<sup>-6</sup> g cm<sup>-3</sup>) of NaCl, MgCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub>, and MgSO<sub>4</sub> aqueous solutions with the data of Lee (11) at 25 °C.

Lee to within ±20 × 10<sup>-6</sup> g cm<sup>-3</sup> from 0 to 1 *m*. Our MgCl<sub>2</sub> density agrees with the data of Lee to within ±15 × 10<sup>-6</sup> g cm<sup>-3</sup> up to 0.6 *m* and is 76 × 10<sup>-6</sup> g cm<sup>-3</sup> lower than the data of Lee

at 1 *m*. The densities of Na<sub>2</sub>SO<sub>4</sub> agree to within  $\pm 20 \times 10^{-6}$  g cm<sup>-3</sup> from 0 to 0.6 *m*. Our value is higher than the data of Lee by  $60 \times 10^{-6}$  g cm<sup>-3</sup> at 1 *m*. The measured densities of MgSO<sub>4</sub> agree with the data of Lee to within  $25 \times 10^{-6}$  g cm<sup>-3</sup>.

The 1-atm density equations obtained in this study have been combined with the high-pressure sound speeds (2) to derive high-pressure equations of state for NaCl, MgCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub>, and MgSO<sub>4</sub> aqueous solutions. The results will be presented in a future publication (4).

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#### Literature Cited

- (1) Chen, C. T. Ph.D. Dissertation, University of Miami, Coral Gables, FL, 1977.
- (2) Chen, C. T.; Chen, L. S.; Millero, F. J. *J. Acoust. Soc. Am.* **1978**, *63*, 1795.

- (3) Chen, C. T.; Millero, F. J. *Nature (London)* **1977**, *266*, 707.
- (4) Chen, C. T.; Millero, F. J., unpublished data, University of Miami, 1978.
- (5) Dunn, L. A. *Trans. Faraday Soc.* **1968**, *64*, 1898.
- (6) Dunn, L. A. *Trans. Faraday Soc.* **1968**, *64*, 2951.
- (7) Fortier, J. L.; Leduc, P. A.; Picker, P.; Desnoyers, J. E. *J. Solution Chem.* **1974**, *3*, 323.
- (8) Weast, R. C., Ed. "Handbook of Chemistry and Physics"; CRC Press: Cleveland, 1974.
- (9) Kell, G. S. *J. Chem. Eng. Data* **1975**, *20*, 97.
- (10) Kratky, O.; Leopold, H.; Stabinger, H. Z. *Angew. Phys.* **1969**, *27*, 273.
- (11) Lee, S. Ph.D. Dissertation, Yale University, New Haven, CT, 1966.
- (12) Perron, G.; Fortier, J. L.; Desnoyers, J. E. *J. Chem. Thermodyn.* **1975**, *7*, 1177.
- (13) Picker, P.; Tremblay, E.; Jolicoeur, C. *J. Solution Chem.* **1974**, *3*, 377.
- (14) Millero, F. J. "Water and Aqueous Solution, Structure, Thermodynamics and Transport Processes"; Wiley: New York, 1972; Chapter 13.
- (15) Millero, F. J. *J. Phys. Chem.* **1970**, *74*, 356.
- (16) Millero, F. J.; Knox, J. *J. Chem. Eng. Data* **1973**, *18*, 407.
- (17) Millero, F. J.; Knox, J., unpublished data, University of Miami, 1973.

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## Thermodynamic Properties of Magnesium Potassium Orthophosphate Hexahydrate

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The low-temperature heat capacity of magnesium potassium orthophosphate hexahydrate, MgKPO<sub>4</sub>·6H<sub>2</sub>O, was measured by adiabatic calorimetry over the temperature range 10–316 K. The standard enthalpy of formation at 298.15 K was determined with a solution calorimeter. Related thermodynamic properties and the solubility product constant were derived.

#### Introduction

Magnesium potassium orthophosphate hexahydrate, MgKPO<sub>4</sub>·6H<sub>2</sub>O, may occur as a soil-fertilizer reaction product (3) or as a precipitate in liquid fertilizers containing potassium and prepared from wet-process phosphoric acid (1). It also is an excellent source of potassium and phosphorus for plants (8). Presented here are measurements of the heat capacity of magnesium potassium orthophosphate hexahydrate from 10 to 316 K, entropies and enthalpies at 298.15 K derived therefrom, and the enthalpy of formation at 298.15 K. The entropy and enthalpy of formation are combined with other values from the literature in the calculation of the solubility product constant, which is compared with the value derived from the direct measurements of solubilities.

**Materials.** Magnesium potassium orthophosphate hexahydrate was prepared by the method of Lehr et al. (2). Chemical analyses showed it to contain 17.4% K<sub>2</sub>O, 15.2% MgO, and 26.8% P<sub>2</sub>O<sub>5</sub> (stoichiometric: 17.68% K<sub>2</sub>O, 15.13% MgO, and 26.63% P<sub>2</sub>O<sub>5</sub>); microscopic examination showed it to comprise an essentially homogeneous phase of MgKPO<sub>4</sub>·6H<sub>2</sub>O.

Monopotassium orthophosphate was prepared by recrystallizing the reagent-grade salt from distilled water and drying it by vacuum desiccation over MgClO<sub>4</sub>. It contained 34.6% K<sub>2</sub>O and 52.1% P<sub>2</sub>O<sub>5</sub> (stoichiometric: 34.61% K<sub>2</sub>O and 52.15%

P<sub>2</sub>O<sub>5</sub>). The magnesium chloride solution was prepared by dissolving the reagent-grade salt in distilled water. It contained 14.6% MgO and 25.2% Cl (MgCl<sub>2</sub>·10.05H<sub>2</sub>O, based on the MgO analysis).

**Low-Temperature Heat Capacity.** The adiabatic calorimeter and the method of operation have been described previously (10), and the overall accuracy of our technique has been reported (5). The defined calorie was taken as 4.1840 absolute J and the ice point as 273.15 K.

The calorimeter was charged with 35.8460 g or 0.134 518 mol. The weight was corrected for buoyancy in air on the basis of a density of 1.83 g cm<sup>-3</sup> (2), and the gram formula weight was taken as 266.4774. The air in the calorimeter was replaced with helium by evacuating to a pressure of 100 torr and then relieving to atmospheric pressure with helium. This cycle was repeated twice, and then the pressure was adjusted to give the same mass of helium as was used in the measurements on the empty calorimeter. The final observed weight of the calorimeter was 5 mg greater than the summation of the masses in each step of the preparation, evacuation, and sealing of the calorimeter. This difference (+0.01% based on the sample weight) was considered sufficiently small to assure that no appreciable alteration of the sample occurred during evacuation and sealing of the calorimeter. The heat capacity of the sample ranged from 28% of the total at 10 K to 49% at 300 K.

The measured heat capacities were corrected for curvature and for small differences in the amount of eutectic solder relative to the empty calorimeter. Because small temperature differences were important, temperatures were measured to four decimal places; but these were rounded to two decimal places in the final tabulation. The heat capacities below 10 K were read from a large-scale plot of  $C_p/T$  against  $T^2$  that extrapolated smoothly to 0 K. Observed molal heat capacities are shown in Table I. Heat capacity and derived functions at round values