# Measurements of VLE, $h^{E}$ , and $v^{E}$ for Binary Mixtures of Dibutyl Ether with 1-Chloropentane, 1,2-Dichloroethane, and 1,1,1-Trichloroethane

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Three binary systems of di-*n*-butyl ether with 1-chioropentane, 1,2-dichioroethane, and 1,1,1-trichioroethane were investigated first in a dynamic still, second in a flow calorimeter, and third in a densimeter. Vapor-liquid equilibria (VLE), excess enthalpies ( $h^E$ ), and excess volumes ( $v^E$ ) are reported at temperatures in the range of 283–370 K. With the results of the experiments, parameters of several "popular" expressions for the excess Gibbs energy are fitted with various fitting procedures. None of the  $g^E$  models and none of the fitting procedures is clearly superior to the others.

# Introduction

Toward better understanding of the conditions in liquid mixtures it is helpful to have available a variety of experimental data. In addition, the experimental information can be used to determine molecular parameters, coefficients in empirical correlations, or coefficients in predictive correlations such as group-interaction models (1).

For the latter methods it is important to confirm or to improve the coefficients that characterize group–group interactions. For chlorinated hydrocarbons and ethers these interactions are sensitive to details of molecular structure.

Therefore, we report here experimental data for binary mixtures containing an ether and a hydrocarbon that is chlorinated once, twice, or three times (see Table I). This work is part of a long-term program (2, 3).

### **Experimental Section**

Vapor -- Liquid Equilibrium Apparatus. VLE experiments were performed in a dynamic still, Type Stage (4), with circulating liquid and vapor. Compared to other cells, this still offers the advantage of withdrawing liguid- and vapor-phase samples without interrupting the operation (see Figure 1). The temperature was determined with a calibrated 25- $\Omega$  platinum resistance thermometer (Rosemount 162 CE) in combination with a digital voltmeter and a thermostated 25- $\Omega$  standard resistance. The inaccuracy  $\delta T$  of the system was less than ±0.01 K. A guartz Bourdon tube (Texas Instrument Model 145) pressure gauge with a sensitivity of 1 Pa and an indicating accuracy of  $\pm 10$  Pa was used to measure the system pressure. High vacuum (10<sup>-2</sup> Pa) and atmospheric pressure read on a precision barometer served as reference pressures for the calibration. The pressure in the system was regulated within  $\pm 5$  Pa with an electric contact manometer actuating a solenoid valve. Pressure fluctuations were suppressed by a buffer volume of 50 dm<sup>3</sup>. The overall inaccuracy  $\delta p_{\perp}$  in determining the system pressure is estimated to  $\pm 15$  Pa.

**Table I. Experimental Program** 

comp	onent	T/K				
1	2	VLE	$h^{\mathrm{E}}$	$v^{\mathbf{E}}$		
C <sub>5</sub> H <sub>11</sub> Cl	C <sub>8</sub> H <sub>18</sub> O	313, 323	288, 298, 313	298		
C <sub>2</sub> H <sub>4</sub> Cl <sub>2</sub>	C <sub>8</sub> H <sub>18</sub> O	330, 350, 370	288, 298	298		
$C_2H_3Cl_3$	$C_8H_{18}O$	323, 343	283, 298, 308	298		

Table II. Properties of Pure Liquids: Density, Refractive Index and Normal Boiling Point at 101.325 kPa Determined in This Work Compared with Published Data

substance	d(298.15 K)/ (g•cm <sup>-3</sup> )	n <sub>D</sub> (293.15 K)	K
C <sub>8</sub> H <sub>18</sub> O	0.76425ª	1.3989ª	414.86ª
	0.7641 (8)	1.3992 (8)	415.12 (9)
	0.76461 (9)		415.4 (8)
$C_5H_{11}Cl$	0.87699ª	1.4139ª	381.08ª
• ••	0.8769 (8)	1.4120(8)	380.91 (10)
$C_2H_4Cl_2$	1.24590°	1.4448	356.63ª
	1.2458 (8)	1.4448 (8)	356.633 (8)
C <sub>2</sub> H <sub>3</sub> Cl <sub>3</sub>	1.32985°	1.4372ª	347.20
	1.32998 (11)	1.4379 (8)	347.25 (11)
	• •	. ,	347.15 (8)

<sup>a</sup> This work.

Samples of the liquid and the condensed vapor were collected after steady-state operation and equilibrium was reached. The composition was determined by a gas chromatograph (GC, Hewlett Packard 5830 A) with a thermal conductivity detector calibrated with reference mixtures prepared gravimetrically. Each sample was analyzed at least three times. The precision of the analyzing instrument in mole fraction is  $\pm 0.0002$ .

Considering all inaccuracies in taking and handling the samples, the concentrations can be determined with an accuracy in mole fraction of  $\delta x = 0.002$  in the liquid and of  $\delta y = 0.003$  in the vapor.

Due to inaccuracies in the calibration procedure of each instrument, due to fluctuations in the operation of the still and due to error propagation for the interdependent variables, there will be a total uncertainty for each T, p, x, y point. The values of these uncertainties depend also on the properties of the mixture. For the systems investigated the uncertainty in pressure  $\delta p$  is calculated according to the error propagation formula; the values are given later in Table VII with the results of the consistency test.

**Calorimeter.** The heat of mixing was determined with a Picker flow calorimeter (5, 6). The principle of the measurement is shown in Figure 2. The calorimeter was operated for defined mixing ratios until the signal from the  $\Delta T$  detector was indicating steady-state conditions. The temperature in the thermostat fluctuated less than  $\pm 0.001$  K. The Picker pumps were always operated with a constant total of the two flows  $\dot{V}_1$  +  $\dot{V}_2$  = 0.013 cm<sup>3</sup> s<sup>-1</sup>. Fluctuations in the flow rate were less than  $\pm 0.1\%$ , and the inaccuracy of the ratio of the two flow rates at the same setting of the pumps was  $\pm 0.01\%$ . Measurements of the heat of mixing could be reproduced within  $\pm 2\%$ . The inaccuracy of the results is, therefore, expected

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Table III. Parameters of the Antoine Equation (1) and Standard Deviations between Experimental and Correlated Vapor Pressures SIG(Dp) as well as Relative Deviations in Pressure Calculated by Using the Antoine Constants of this Work and of the Literature D(AEQ), where  $D(AEQ) = \int (AEQ_1 - AEQ_2)^2 dT)^{0.5} / (T_{max} - T_{min})$ 

	• / ·						
component	ref	$(T_{\rm max} - T_{\rm min})/{ m K}$	A	В	С	SIG(Dp)/kPa	D(AEQ)/%
C <sub>8</sub> H <sub>18</sub> O	а	110	13.8340	3137.49	74.48	0.054	
	12	60	13.6341	2987.123	82.12		0.52
	8		14.8294	3795.581	43.15		0.44
$C_5H_{11}Cl$	а	86	13.9946	3037.315	57.15	0.031	
	10	25	16.0771	4356.491	0.0		0.91
	8	87	14.0252	3069.093	54.65		0.17
$C_2H_4Cl_2$	а	59	14.1424	2896.480	52.51	0.011	
	13		14.5275	3127.970	40.95		0.05
	14	129	14.1614	2927.171	50.22		0.08
	15	29	14.1176	2882.031	53.27		0.08
$C_2H_3Cl_3$	а	58	13.8574	2757.407	48.74	0.031	
	13		13.9876	2802.246	48.15		0.17

<sup>a</sup> This work.

Table IV. T, p, x, y Data and Relative Volatilities  $\alpha_{12}$  for Coexisting Vapor and Liquid Phases of Binary Mixtures of Di-*n*-butyl Ether (2) with Three Chlorohydrocarbons

T/K	p/hPa	<i>x</i> <sub>1</sub>	У1	α <sub>12</sub>	T/K	p/hPa	<i>x</i> <sub>1</sub>	<i>y</i> <sub>1</sub>	α <sub>12</sub>	T/K	p/hPa	<i>x</i> <sub>1</sub>	<i>y</i> <sub>1</sub>	α <sub>12</sub>
	1-Chl	oropentar	ne (1)			267.4	0.5424	0.9109	8.63		1,1,1-Tri	chloroeth	ane (1)	
313.15	20.3	0.0000	0.0000			288.6	0.6096	0.9285	8.32	323.15	33.8	0.0000	0.0000	
	25.5	0.0774	0.2646	4.29		329.2	0.7350	0.9547	7.60		39.5	0.0141	0.1523	12.56
	28.5	0.1209	0.3734	4.33		355.8	0.8277	0.9664	5.99		46.8	0.0335	0.2990	12.31
	35.3	0.2242	0.5539	4.30		375.6	0.9060	0.9810	5.36		53.6	0.0517	0.4008	12.27
	39.2	0.2877	0.6294	4.20		396.9	0.9700	0.9940	5.12		78.8	0.1152	0.6222	12.65
	43.5	0.3549	0.6949	4.14		406.8	1.0000	1.0000			95.3	0.1575	0.7003	12.50
	46.4	0.3978	0.7334	4.16		114.5	0.0000	0.0000			155.7	0.3082	0.8512	12.84
	56.1	0.5515	0.8337	4.08		129.1	0.0163	0.1245	8.58		178.4	0.3613	0.8807	13.05
	56.9	0.5678	0.8409	4.02	350.00	144.7	0.0340	0.2300	8.49		206.7	0.4270	0.9087	13.36
	64.2	0.6810	0.8960	4.04		166.5	0.0578	0.3450	8.59		228.8	0.4821	0.9258	13.40
	65.2	0.6964	0.9029	4.05		232.9	0.1382	0.5704	8.28		253.2	0.5367	0.9412	13.82
	70.4	0.7793	0.9345	4.04		418.5	0.3671	0.8232	8.03		272.8	0.5861	0.9515	13.85
	73.1	0.8225	0.9490	4.02		520.6	0.5069	0.8880	7.71		303.7	0.6558	0.9648	14.39
	78.1	0.8985	0.9726	4.01		577.6	0.5908	0.9144	7.40		326.0	0.7065	0.9726	14.75
	80.1	0.9307	0.9817	3.99		653.9	0.7080	0.9446	7.03		352.1	0.7656	0.9804	15.31
	84.6	1.0000	1.0000			693.1	0.7754	0.9571	6.46		377.9	0.8271	0.9865	15.28
323.15	34.1	0.0000	0.0000			725.3	0.8334	0.9668	5.82		397.4	0.8707	0.9906	15.65
	40.7	0.0631	0.2131	4.02		754.2	0.8843	0.9774	5.66		432.6	0.9492	0.9968	16.67
	48.5	0.1416	0.3951	3.96		773.8	0.9197	0.9830	5.05		434.5	0.9544	0.9971	16.43
	60.9	0.2652	0.5870	3.94		783.0	0.9337	0.9862	5.07		442.6	0.9771	0.9986	16.72
	69.3	0.3509	0.6786	3.91		803.0	0.9692	0.9931	4.57		451.2	1.0000	1.0000	
	76.8	0.4291	0.7436	3.86		808.1	0.9788	0.9953	4.59	343.15	86.3	0.0000	0.0000	
	88.0	0.5460	0.8207	3.81		815.7	0.9896	0.9976	4.37		114.4	0.0380	0.2724	9.48
	93.3	0.5990	0.8507	3.81		820.3	1.0000	1.0000			155.2	0.0955	0.4976	9.38
	95.4	0.6220	0.8614	3.78		1 2-Dick	nloroethai	ne (1)			203.2	0.1557	0.6440	9.81
	98.7	0.6552	0.8779	3.78		248.8	0.0000	0.0000			252.8	0.2194	0.7373	9.99
	102.7	0.6952	0.8969	3.81		264.1	0.0097	0.0669	7.32		306.7	0.2889	0.8032	10.05
	110.7	0.7789	0.9303	3.79	370.00	326.6	0.0502	0.2765	7.23		359.4	0.3538	0.8484	10.22
	117.0	0.8443	0.9536	3.79	010.00	380.0	0.0842	0.3960	7.13		468.9	0.4870	0.9093	10.56
	$122.7 \\ 126.8$	0.9042	0.9725	3.75		473.3	0.1490	0.5530	7.07		533.4	0.5616	0.9337	10.99
		0.9474	0.9855	3.77		680.6	0.2902	0.7381	6.89		535.3	0.5664	0.9344	10.90
	130.6	0.9860	0.9960	3.54		758.1	0.3475	0.7836	6.80		602.0	0.6444	0.9533	11.26
	131.9	1.0000	1.0000			828.5	0.3999	0.8171	6.70		650.8	0.7002	0.9639	11.43
	1.2-Dic	hloroetha	ne (1)			902.3	0.4571	0.8491	6.68		673.1	0.7246	0.9684	11.65
330.00	47.9	0.0000	0.0000			957.8	0.5032	0.8692	6.56		739.1 792.7	0.7979	0.9798	12.29
	64.8	0.0374	0.2877	10.40		1040.3	0.5690	0.8951	6.46		800.4	0.8533 0.8665	$0.9872 \\ 0.9884$	13.26
	79.2	0.0695	0.4376	10.42		1119.2	0.6366	0.9162	6.24		800.4 822.3		0.9898	13.13
	95.2	0.1046	0.5497	10.45		1282.8	0.7851	0.9512	5.34		851.4	0.8795		13.30
	103.5	0.1272	0.5959	10.12		1357.5	0.8555	0.9666	4.89		851.4 870.7	$0.9223 \\ 0.9506$	$0.9936 \\ 0.9962$	13.08
	138.3	0.2073	0.7241	10.04		1432.5	0.9259	0.9822	4.42		870.7 875.5	0.9506	0.9962	13.62
	191.5	0.3339	0.8308	9.80		1505.2	0.9899	0.9975	4.07		884.1	0.9631	0.9971	13.17 13.46
	218.6	0.4304	0.8673	9.67		1515.3	1.0000	1.0000			889.6	0.9778	0.9983	13.46
	248.0	0.4817	0.8948	9.15							893.1	1.0000	1.0000	10.04
											020.1	1.0000	1.0000	

to be  $\pm 2\%$ , provided complete mixing was assured. It was, however, sometimes difficult to accomplish complete mixing.

erence (7). The temperature of the bath liquid was controlled within  $\pm 0.01$  K. The relative inaccuracy of the densities is  $10^{-4}$ .

**Densimeter.** Densities of pure liquids and their mixtures were determined with two vibrating U-tube instruments, Type A.Paar (DMA 602/60), one filled with the gravimetrically prepared mixture and the other with a pure component as a ref-

**Pure Substances.** The substances were purified according to recommendations of Riddick et al. (8). The ether was dried with sodium hydroxide and distilled at subatmospheric pressure in a high-efficiency spinning band column to remove peroxides

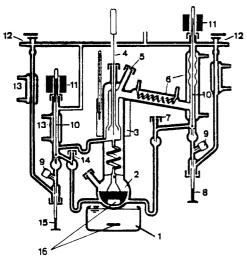
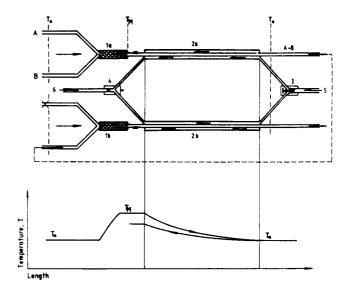


Figure 1. Schematic diagram of the Stage equilibrium still: 1, heating bath; 2, boiling vessel with Cottrell pump; 3, heating mantle; 4, temperature sensor; 5, vapor sampling spout; 6, cooler for the vapor phase; 7, sample take-off for the condensed vapor; 8, sample receiver for the vapor; 9, PTFE valve; 10, solenoid valve; 11, solenoid coil; 12, receiver's evacuation; 13, cooler for the liquid phase; 14, sample take-off for the liquid phase; 15, sample receiver for the liquid phase; 16, magnetic stirrers.

and high-boiling impurities. The chlorinated alkanes were treated with concentrated sulfuric acid, washed with distilled water, dried with calcium chloride, and finally distilled in the spinning band column with a reflux ratio of 50:1. The purity of the products was checked by gas chromatography. Purification was continued until trace impurities were no longer detectable.



**Figure 2.** Schematic flow diagram of Picker calorimeter with temperature profile. A and B, inlet of reagents from thermostat at  $T_0$ : 1a and b, mixer; 2a and b, heat exchanger for mixture and auxiliary liquid; 3, alternating switch for auxiliary liquid; 4, differential temperature and temperature detector; 5, inlet; and 6, outlet of auxiliary liquid.

All substances were stored under a nitrogen atmosphere and protected from light. Table II compares characteristic properties of the substances, viz., the density, the refractive index, and the normal boiling point with published values (9-11).

### **Experimental Results**

### Vapor Pressures of Pure Liquids. Measurement of the va-

Table V. Expe	rimental <i>h</i> <sup>E</sup> –x Da	ta for Mixture	s of Dibutyl Ether	(2) wit	h Three Chloroalkanes
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T/K	<i>x</i> <sub>1</sub>	$h^{\mathrm{E}}/(\mathrm{J}\cdot\mathrm{mol}^{-1})$	T/K	<i>x</i> <sub>1</sub>	$h^{\mathrm{E}}/(\mathrm{J}\cdot\mathrm{mol}^{-1})$	T/K	x1	$h^{\mathrm{E}}/(\mathrm{J}\cdot\mathrm{mol}^{-1})$	T/K	<i>x</i> <sub>1</sub>	$h^{\mathrm{E}}/(\mathrm{J}\cdot\mathrm{mol}^{-1})$
1,1,1	-Trichloro	oethane (1)		0.5626	-70.1		0.5638	509.8		0.2989	27.5
298.15	0.1773	-54.1		0.5935	-68.3		0.6012	511.6		0.3443	28.6
	0.2308	-65.0		0.6241	-66.3		0.6328	512.4		0.3833	29.1
	0.2819	-73.0		0.6549	-63.7		0.6654	507.1		0.4214	29.3
	0.3305	-78.7		0.6842	-61.1		0.6942	497.9		0.4595	29.2
	0.3771	-82.6		0.7133	-57.4		0.7251	482.7		0.4930	28.8
	0.4216	-85.4		0.7409	-53.3		0.7518	465.3		0.5308	28.1
	0.4642	-86.6		0.7686	-49.2		0.7780	444.0		0.5631	27.1
	0.5051	-86.5		<b></b>			0.8006	423.8		0.5968	25.9
	0.6061	-82.2	1,2-	Dichloroe			0.8272	395.5		0.6296	24.7
	0.6527	-77.8		0.1681	202.6		0.8508	365.8		0.6618	23.2
	0.7794	-59.2		0.2237	264.6			4.5		0.6934	21.6
	0.8176	-51.2	288.15	0.2802	323.2		Chloropen			0.7232	19.8
	0.8542	-42.5		0.3355	370.8	288.15	0.1807	13.1		0.7535	17.9
283.15	0.2469	-82.2		0.3860	407.4		0.2243	14.9		0.7838	16.0
	0.2931	-88.7		0.4395	433.4		0.2671	14.9		0.8142	13.9
	0.3349	-93.1		0.4843	450.4		0.2671	16.3	313.15	0.1807	33.5
	0.3770	-95.7		0.5244	463.1		0.3084	17.4		0.2243	38.1
	0.4177	-96.8		0.5638	468.8		0.3526	18.0		0.2671	41.1
	0.4513	-97.6		0.6012	469.7		0.3912	18.3		0.3084	43.2
	0.4992	-96.8		0.6328	468.5		0.4288	18.4		0.3526	44.5
	0.5298	-96.0		0.6654	461.9		0.4664	18.2		0.3912	45.2
	0.5626	-94.9		0.6942	453.1		0.4995	17.9		0.4288	45.4
	0.5935	-93.9		0.7251	440.1		0.5369	17.5		0.4664	45.2
	0.6241	-91.3		0.7511	425.8		0.5695	16.9		0.4995	44.6
	0.6549	-88.1		0.7780	408.1		0.6034	16.1		0.5369	43.7
	0.6989	-82.8		0.8006	388.3		0.6363	15.3		0.5695	42.5
	0.7409	-76.1		0.8272	362.8		0.6684	14.4		0.6034	40.8
	0.7686	-70.9		0.8508	337.7		0.6999	13.4		0.6363	38.9
	0.8077	-62.5		0.1681	216.8		0.7295	12.3		0.6684	37.1
308.15	0.2931	-63.7		0.2237	281.7		0.7604	11.1		0.6999	34.8
	0.3349	-67.9	298.15	0.2802	343.1		0.7908	9.8		0.7295	32.6
	0.3770	-70.4		0.3355	396.0	000.15	0.8212	8.5		0.7604	29.8
	0.4177	-71.8		0.3860	436.7	298.15	0.1663	20.0		0.7908	26.9
	0.4513	-72.4		0.4395	466.4		0.2118	23.2		0.8212	23.7
	0.4992	-71.9		0.4843	486.5		0.2561	25.8			
	0.5298	-71.4		0.5244	501.0						

Ether (2) with Three Chloroalkanes									
T/K	<i>x</i> <sub>1</sub>	$v^{\mathrm{E}}/(\mathrm{cm}^{3}\cdot\mathrm{mol}^{-1})$							
	1-Chloropentan	ie (1)							
298.15	0.1741	-0.0586							
	0.2114	-0.0640							
	0.3910	-0.0874							
	0.4076	-0.0882							
	0.5141	-0.0930							
	0.5766	0.0895							
	0.6516	-0.0830							
	0.7091	-0.0740							
	0.7999	-0.0554							
	0.8527	-0.0419							
1	1,2-Dichloroetha	ne (1)							
298.15	0.1972	0.0822							
	0.4989	0.1977							
	0.6100	0.2217							
	0.6710	0.2197							
	0.7083	0.2107							
	0.7550	0.1946							
	0.8514	0.1581							
1,	1,1-Trichloroeth	ane (1)							
298.15	0.0154	-0.023							
	0.0494	-0.060							
	0.0971	-0.100							
	0.1632	-0.220							
	0.2389	-0.278							
	0.4235	-0.368							
	0.6555	-0.325							
	0.8102	-0.247							
	0.9226	-0.112							
	0.9688	-0.045							

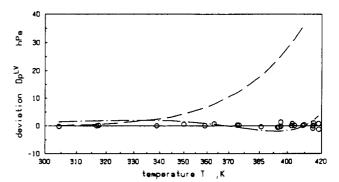
Table VI. Experimental  $v^{E}$ -x Data for Mixtures of Dibutyl

por pressure as a function of temperature serves several purposes: (1) it provides a sensitive test for the purity of the substance if reliable published data are available for comparison; (2) after interpolation of the experimental points by a suitable formula such as the Antoine equation

$$\ln (p^{LV}/kPa) = A - B/(T/K - C)$$
(1)

deviations between measured and calculated points provide an indication of the quality and reliability of the equipment; and (3) the pure-component vapor pressures must be known for reduction of binary data.

Table III lists, for all liquids, coefficients of the Antoine equation and integrated deviation in relative pressure between Antoine equations of this work and of literature (8, 10, 12-15). Figure 3 shows the deviations Dp between experimental pressure and calculated vapor pressures for dibutyl ether, using Antoine equation with coefficients fitted to the experimental data of this work and with coefficients reported in literature. The scatter of the experimental points gives a measure for the reproducibility of the data (vapor pressures were measured twice, once with increasing and once with decreasing temperature). There is a satisfactory agreement between our data and those of Riddick et al. (8).



**Figure 3.** Deviations of the experimental vapor pressures (O) and values calculated from the Antoine equation of this work and from Antoine equations reported in literature: (--) Cydlinski (1) and (--) Riddick (17).

**Vapor**-Liquid Equilibria. Temperature, pressure, and the mole fractions of liquid and vapor were measured in the equilibrium apparatus. Table IV presents all experimental data as well as the relative volatility  $\alpha_{12}$ . Figures 4–6 show experimental bubble and dew points. For comparison, they also show the isotherms calculated from the Uniquac equation after adjustment of binary interaction parameters to the same set of binary data.

**Excess Enthalples.** In the calorimeter, the heat of mixing (excess enthalpy) was determined for defined mixing ratios given by the volumetric flow rates of the two coupled Picker pumps. The composition of the mixture was checked by re-fractometry. Results are shown in Table V and in Figures 4–6.

**Excess Volumes.** Mixtures of two components were prepared gravimetrically by using a scale with an inaccuracy of  $\pm 0.2$  mg. The density of a pure liquid was determined (see Table II) after the instrument had been calibrated by the reference substances, i.e., distilled water and *n*-nonane (product of Fluka AG (CH) with a purity of better than 99.8%, GC). The densities of the mixtures were determined by differential measurements with one of the pure components as a reference. The differential method also reduced inaccuracies caused by temperature fluctuations in the circulating thermostat liquid. Experimental results are presented in Table VI.

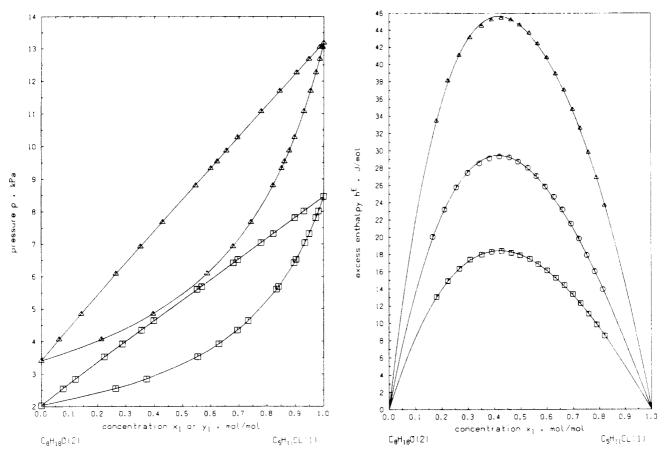
# **Data Reduction**

**Consistency Test of VLE Data.** In the test proposed by van Ness and Fredenslund (16), p-x data for one isotherm are used to fit the coefficients of a Legendre polynomial for  $g^{E}$  by minimizing the sum of the squares of the deviations between experimental pressure and calculated pressure. The degree of the polynomial should be considerably smaller than the number of experimental points. The standard deviation and a Dp vs. *x* plot provide an indication of the accuracy of the experimental method and of the reproducibility of the experimental data.

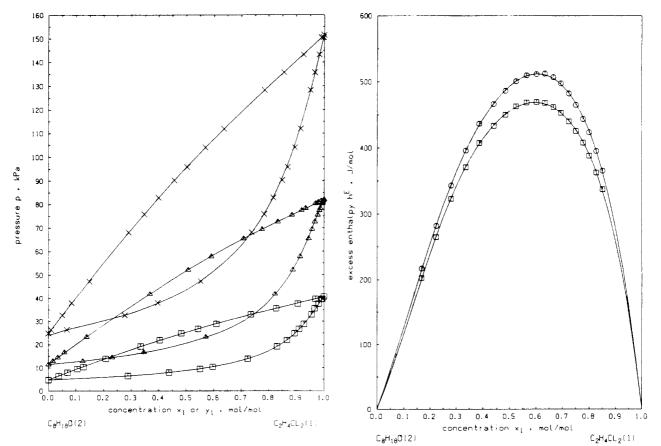
Table VII. Results of the Consistency Test: Standard Deviations between Calculated and Observed Pressure SIG(Dp) and Average Absolute Deviation between Calculated and Observed Vapor Concentration AA(Dy) for Binary Mixtures of Dibutyl Ether with Three Chloroalkanes (the Degree of Legendre Polynomials is 3)

	T/K	$n^b$	estd exptl δp/kPA	ideal	gas	virial eq <sup>a</sup>		
components				$rac{\mathrm{SIG}(\mathrm{Dp})/}{\mathbf{kPa}}$	$AA(D_y)$	SIG(Dp)/ kPA	$AA(D_y)$	
C <sub>5</sub> H <sub>11</sub> Cl	313.15	14	0.05	0.01	0.0012	0.01	0.0009	
•	323.15	15	0.06	0.01	0.0005	0.01	0.0008	
$C_2H_4Cl_2$	330.00	15	0.12	0.10	0.0018	0.10	0.0020	
	350.00	16	0.21	0.10	0.0013	0.10	0.0024	
	370.00	16	0.33	0.11	0.0015	0.11	0.0027	
$C_2H_3Cl_3$	323.15	19	0.13	0.10	0.0013	0.10	0.0025	
2 0 0	343.15	21	0.23	0.71	0.0032	0.72	0.0044	

<sup>a</sup> Second virial coefficients according to Hayden-O'Connell (17). <sup>b</sup> Number of experimental points.

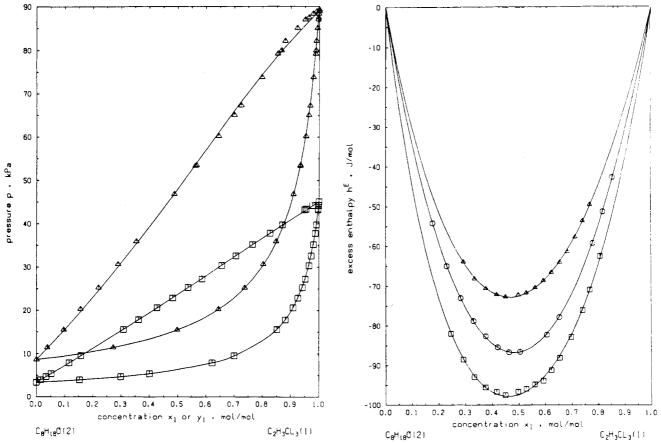


**Figure 4.** Experimental and calculated VLE and  $h^{E}$  for the system  $C_{6}H_{11}CI-C_{8}H_{18}O$ . (Left) Experimental p-x, y data; T = 313.15 K ( $\Box$ ) and T = 323.15 K ( $\Delta$ ); lines, Uniquac equation. (Right) Experimental  $h^{E}-x$  data; T = 288.15 K ( $\Box$ ), T = 298.15 K (O); and T = 313.15 K ( $\Delta$ ); lines, Redlich-Kister polynomials.



**Figure 5.** Experimental and calculated VLE and  $h^{E}$  for the system  $C_{2}H_{4}Cl_{2}-C_{8}H_{18}O$ . (Left) Experimental p-x, y data;  $T = 330.0 \text{ K} (\Box)$ ,  $T = 350.0 \text{ K} (\Delta)$ , and T = 370.0 K (X); lines, Uniquac equation. (Right) Experimental  $h^{E}-x$  data;  $T = 288.15 \text{ K} (\Box)$  and T = 298.15 K (O); lines, Redlich-Kister polynomials.

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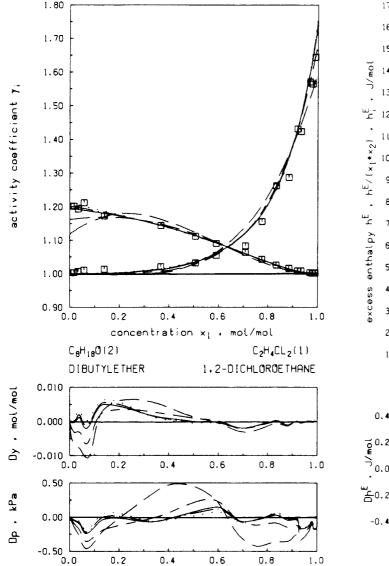


**Figure 6.** Experimental and calculated VLE and  $h^{E}$  for the system  $C_{2}H_{3}Cl_{3}-C_{8}H_{18}O$ . (Left) Experimental p-x, y data; T = 323.15 K ( $\Box$ ) and T = 343.15 K ( $\Delta$ ); lines, Uniquac equation. (Right) Experimental  $h^{E}-x$  data; T = 283.15 K ( $\Box$ ), T = 298.15 K (O), and T = 308.15 K ( $\Delta$ ); lines, Redlich-Kister polynomials.

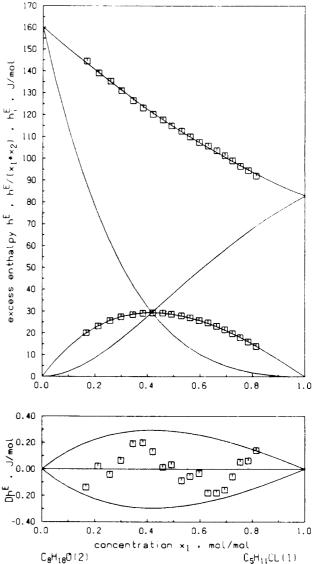
Table VIII. (A) Results of the Parameter Estimation Using the Algorithm of Prausnitz et al. (19), AP, and Kemeny et al. (21), KM, and (B) Comparison of Different Optimization Procedures and Objective Functions

					В					
	1: 1-Chloro					RM	IS	parar	neters	
temp, K	313.1		323.15	T/K	model	$\overline{D_p/\mathbf{k}\mathbf{P}\mathbf{a}}$	$D_y$	$X_{12}$	X21	$method^b$
eq 20	Uniq	uac, AP	Van Laar, AP			<u>F'</u>	<u>,</u>			
parameter <sup>a</sup>	-865.	10	0.0489		System:	1,2-Dichloroethane–Dibutyl Ether				
$X_{12}$	-865. 1103.		0.0337	330	Uniquac	0.118	0.0021	457.92	31.42	KM
X <sub>21</sub>	1.065		1.050			0.103	0.0020	350.63	128.11	BA
$\gamma_1$	1.005		1.034			0.099	0.0022	209.16	268.69	AP
$\gamma_2^{\infty}$ SIG(Dp)/kH			0.009		Margules-3	0.123	0.0031	0.3061	0.1405	KM
SIG(Dp)/ KI	0.001		0.0007			0.108	0.0024	0.3195	0.1383	BA
51G(DP)	0.001	4	0.0007			0.099	0.0033		0.1557	AP
System	2: 1,2-Dichlo	roethane–D	butyl Ether	350	Uniquac	0.101	0.0014	610.15	-98.70	KM
temp, K	330.0	350.0	370.0			0.120	0.0021	420.04	74.49	BA
eq 20	NRTL, KM	Van Laar	AP Uniquac, AP			0.101	0.0014	605.26	-98.19	AP
parameter <sup>a</sup>			-		Margules-3	0.387	0.0039	0.3124		KM
$X_{12}$	3988.24	0.1913	-5.75			0.361	0.0029	0.3060		BA
$X_{21}$	-2041.01	0.5700	481.13		<b></b> .	0.297	0.0037	0.2915	0.1822	AP
$\gamma_1$ "	1.217	1.211	1.196	370	Uniquac	0.105	0.0019	2.69	472.21	KM
$\gamma_2$	1.699	1.768	1.485			0.106	0.0019	6.62	467.99	BA
SIG(Dp)/kPa	0.084	0.083	0.105			0.359	0.0013	285.34	191.21	KM(b)
SIG(Dy)	0.0023	0.0018	0.0019			0.105	0.0019	-5.75	481.13	AP
Sustan 2	. 111 Treich	anaathana	Dibutul Ether		Margules-3	0.227	0.0021	0.2485	0.0964	KM
	323.		Dibutyl Ether 343.15			0.231	0.0022	0.2532	0.0920	BA
temp, K eq 20		juac, AP	Wilson, AP			0.598	0.0023	0.2727	0.1260	KM(b)
parameter <sup>a</sup>	Unio	quae, Ar	wilson, Ar			0.203	0.0022	0.2482	0.1085	AP
$X_{12}$	842.	50	-1708.26							
$X_{21}^{12}$	-692		5174.26							
$\gamma_1^{2}$	0.91		0.846							
$\gamma_2^{\prime 1}$	0.92		1.463							
SIG(Dp)/k			0.693							
SIG(Dy)	0.00		0.0051							

<sup>a</sup> Uniquac, NRTL, and Wilson parameters in J-mol<sup>-1</sup>; Third NRTL parameter  $\alpha = 0.3$ . <sup>b</sup> Methods: KM, maximum likelihood procedure with objective function SSQ (Dp/p + ln  $\gamma_1/\gamma_2$ ); KM(b), minimizing the SSQ (Dp/p + ln  $\gamma_1/\gamma_2$ ); BA, minimizing the SSQ (Dp/p); AP, maximum likelihood procedure minimizing the weighted SSQ (Dp + DT + Dx + Dy).



**Figure 7.** Activity coefficients  $\gamma_i$  vs. composition for the system  $C_2H_4CI_2-C_8H_{18}O$  at T = 350.0 K. Experimental points and values calculated by several  $g^E$  models as well as deviations in pressure and vapor composition: (--) Margules, (···) Van Laar, (-·-) Wilson, (---) NRTL, (--) Uniquac.



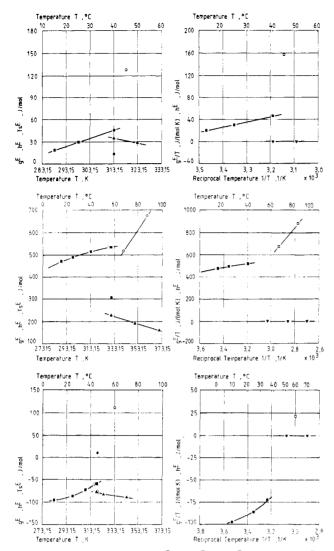
**Figure 8.**  $h^{\text{E}}$ ,  $h^{\text{E}}/(x_1x_2)$ , and  $h_1^{\text{E}}/h_2^{\text{E}}$  vs. composition for the system  $C_5H_{11}CI-C_8H_{18}O$  as well as the deviations  $Dh^{\text{E}}$  of the correlation with Redikoh-Kister polynomial. Points: experimental data; lines: calculated by Redikoh-Kister equation. The lens-shaped curve indicates 1% deviation.

Table IX. Coefficients of Eq 3, Standard Deviations, and Maximum Deviations for the  $h^E$  Measurements of Dibutyl Ether (2) with Three Chloroalkanes

component	$T/\mathrm{K}$	$A_1$	$A_2$	$A_3$	$A_4$	$rac{\mathrm{SIG}(\mathrm{Dh}^{\mathrm{E}})/{(\mathrm{J}\cdot\mathrm{mol}^{-1})}$	$rac{\mathrm{Dh^{E}}_{\mathrm{max}}}{\mathrm{(J \cdot mol^{-1})}}$
$C_5H_{11}Cl$	288.15	71.9	-22.9	3. <b>9</b>		0.06	0.11
	298.15	114.7	-38.2	6.8		0.12	0.18
	313.15	178.5	-48.6	39.1		0.19	0.35
$C_2H_4Cl_2$	288.15	1825	546	394	674	1.35	3.19
	298.15	1975	<b>69</b> 0	423	554	1.63	2.91
$C_2H_3Cl_3$	283.15	-389.8	42.8	-115.7		0.53	0.81
	298.15	-346.6	20.6	-25.1		0.21	0.37
	308.15	-289.1	34.4	-29.3		0.26	0.51

Table X. Coefficients of Eq 3, Standard Deviations and Maximum Deviations for the  $v^E$  Measurements of Dibutyl Ether (2) with Three Chloroalkanes

component	$T/\mathrm{K}$	$A_1$	$A_2$	$A_3$	$\frac{\mathrm{SIG}(\mathrm{Dv}^{\mathbf{E}})}{(\mathrm{cm}^3\cdot\mathrm{mol}^{-1})}$	$\mathrm{Dv^E}/(\mathrm{cm^3 \cdot mol^{-1}})$
C <sub>5</sub> H <sub>11</sub> Cl	298.15	-0.3680	0.0316	-0.0032	0.0018	0.0025
$C_2H_4Cl_2$	298.15	0.7968	0.5182	0.1015	0.0048	0.0066
$C_2H_3Cl_3$	298.15	-1.5244	-0.0798	0.0787	0.0165	0.0241



**Figure 9.** (a, top) Experimental  $h^{E}(\blacksquare)$ ,  $g^{E}(\blacktriangle)$ ,  $g^{E/T}(\triangledown)$ , and  $Ts^{E} = h^{E} - g^{E}(\spadesuit)$ . Comparison with calculated caloric properties  $Ts^{E} = -T(\partial g^{E}/dT)_{p,x}(\bigcirc)$  and  $h^{E} = (\partial (g^{E}/T)/\partial (1/T))_{p,x})(\square)$  for the system  $C_{5}H_{11}CI-C_{8}H_{18}O$ . (b, middle) The same as Figure 9a for the system  $C_{2}H_{4}CI_{2}-C_{8}H_{18}O$  (points in parentheses indicate extrapolated values). (c, bottom) The same as Figure 9a for the system  $C_{2}H_{3}CI_{3}-C_{8}H_{18}O$  (points in parentheses indicate extrapolated values).

The test was performed for ideal and for real gas behavior, although the real gas corrections were small. The truncated virial equation of state was used with second virial coefficients from Hayden and O'Connell (17). The Poynting correction is calculated assuming  $v_{0l}^{L}$  to be independent of pressure. The liquid molar volume is calculated by the correlation of Hankinson et al. (18). The consistency can be checked by calculating vapor composition  $y^+$  for each T, p, x point and by comparing  $y^+$  with the experimental y. The absolute average deviation AA(Dy) and the Dy vs. x plot are indications of the consistency and most likely of the correctness of the data (see Table VII).

As the deviations AA(Dy) of the isotherms are approximately as large as the uncertainties of the experimental results, the T,p,x,y sets can be considered consistent. (The consistency was better for the assumption of ideal gas conditions.)

Only one isotherm (343.15 K) of the system 1,1,1-trichloroethane-dibutyl ether shows a noticeable deviation Dy. We observed by GC during the experiments an increasing amount of lighter impurities which could not be identified (probably due to chemical decomposition of the chloro compound).

Models for the Excess Glbbs Energy. Based on the experimental data and additional information about the thermophysical properties, it is possible to determine the activity coefficients for each experimental point with

$$\gamma_{i}(T,p,x_{i}) = \varphi_{i}^{V} p y_{i} / (x_{i} \varphi_{0i} p_{0i}^{LV} \exp[(v_{0i}^{L} / RT)(p - p_{0i}^{LV})])$$
(2)

From the consistency test, it can be concluded that the vapor phase behaves ideally. Therefore, vapor-phase nonidealities are not considered.

An isothermal data set can be used to fit adjustable binary coefficients in so-called  $g^{E}$  models. Values of the coefficients and the SIG(Dp) and AA(Dy) are affected not only by the equation of state used for the vapor phase but also by the type of objective function used in the minimization procedure, by the minimizing algorithm itself, and by the choice of the subset chosen from the total set of experimental points.

It might help those who specialize in data reduction to learn about the results of parameter fitting. Therefore, a brief summary will be presented, without the intention to judge about the physical or chemical "truth" of the  $g^{E}$  models.

Table VIII, section B, gives a comparison of different optimization procedures for the system  $C_2H_4Cl_2-C_8H_{18}O$ . For the systems investigated it can be concluded, first, that for specified *T* and *x*, the *p* and *y* can be represented slightly better with the Uniquac model (with respect to the deviation RMS Dp and RMS Dy) than with the Margules equation independent of the fitting procedures; second, that for Uniquac the method suggested by Prausnitz and Anderson (*19*) yields the best set of parameters; third that the simplest procedure for minimizing the relative deviation in pressure (Dp/*p*) is as satisfactory as the more complicated and time-consuming procedures.

All experimental data sets were used to fit binary parameters for five popular  $g^{E}$  models (20) with the methods of Prausnitz (19) and Kemeny et al. (21). Table VIII, section A, gives the results of the parameter estimation for the model, which represents the data best.

In our experience there is no "favorite" model that could correlate the experimental data essentially better than the other models. As a typical example, Figure 7 gives the results for the C<sub>2</sub>H<sub>4</sub>Cl<sub>2</sub>-C<sub>8</sub>H<sub>18</sub>O system at 350 K, showing the activity coefficients calculated from the experimental data and values from several  $g^{\rm E}$  models, as well as deviations in pressure and vapor concentration.

**Redilch**–Kister Polynomial for  $h^{E}$ . Experimental  $h^{E}-x$  data are usually correlated by a polynomial proposed by Redilch and Kister.

$$h^{\rm E} = x_1 x_2 \sum (x_1 - x_2)^{k-1} A_k \qquad k = 1, ..., m$$
 (3)

The degree m - 1 and the number of adjustable coefficients m depend on the complexity of the mixture. Table IX lists the coefficients of the isotherms for three binary systems. Figure 8 shows  $h^{E}$ , partial molar excess enthalpies, and  $h^{E}/(x_1 \cdot x_2)$  calculated with the polynomial as well as experimental points. In addition, the deviations of single experimental points from the polynomial are plotted.

**Data Reduction of**  $v^{E}$ . Experimental values for the excess volumes were correlated by Redlich–Kister polynomials (eq 3). Table X gives coefficients of the correlation as well as standard and maximum deviations. In the C<sub>2</sub>H<sub>3</sub>-Cl<sub>3</sub>-C<sub>8</sub>H<sub>16</sub>O system the accuracy of the experiments was lowered by the high relative volatility and by the large difference in density of pure components.

**Consistency of VLE and**  $h^{E}$  **Data.** If VLE and  $h^{E}$  measurements are performed at the same temperature,  $Ts^{E}$  can be determined. As vapor-liquid equilibria were investigated at several temperatures,  $g^{E}$  is known as a function of temperature. If  $h^{E}$  is also measured in the same temperature range, general thermodynamic relations can be used to compare the results of VLE and  $h^{E}$  experiments:

$$-T(\partial g^{\mathsf{E}}/\partial T)_{\mathsf{p},\mathsf{x}} = Ts^{\mathsf{E}} = h^{\mathsf{E}} - g^{\mathsf{E}}$$
(4)

$$(\partial (g^{\mathsf{E}}/T)/\partial (1/T))_{p,x} = h^{\mathsf{E}}$$
(5)

The experiments in the calorimeter should preferably be performed at low vapor pressures of the solution; the dynamic VLE experiments are more accurate at higher vapor pressures. The experiments of phase equilibria and the caloric measurements are therefore not always made at exactly the same temperature. The results are graphically shown in Figure 9a-c at equimolar composition. In the  $g^{E}$  vs. T plot, the experimental  $Ts^{E} = h^{E} - g^{E}$  is compared with  $Ts^{E}$  calculated from the slope of the  $g^{E}$  vs. T curve. In the  $g^{E}/T$  vs. 1/T plot the experimental  $h^{E}$  is compared with  $h^{E}$  calculated from the slope of the  $g^{E}/T$ vs. 1/7 curve. The diagrams show that the temperature dependence of  $g^{E}$  or  $g^{E/T}$  based on VLE data is not of sufficient accuracy to allow prediction of h<sup>E</sup> or Ts<sup>E</sup>. As

$$h^{\mathsf{E}} = (\partial (g^{\mathsf{E}}/T)/\partial (1/T))_{p,x} = -T^2 (\partial (g^{\mathsf{E}}/T)/\partial T)_{p,x} \quad (6)$$

small inaccuracies in  $(q^{E}/T)$  are exaggerated by the large factor  $(T^{2}).$ 

**Conclusions.** In addition to VLE,  $h^{E}$  and sometimes  $v^{E}$ measurements are necessary to obtain the complete information required for the design of industrial separation processes. If  $g^{E}$  is determined from VLE measurements, and if the change of  $g^{E}$  with temperature is calculated from two or three isothermal VLE experiments and if  $h^{E}$  is calculated with eq 6, the resulting value of  $h^{E}$  can be very inaccurate, especially if  $h^{E}$ is relatively small ( $h^{E} < 500 \text{ J/mol}$ ).

It can be concluded, therefore, that it is not satisfactory to find the temperature dependence of parameters in  $g^{E}$  models by evaluating VLE experiments only. Independent calorimetric experiments are required to give accurate information about the effect of temperature on activity coefficients.

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### Glossary

A, B, C A <sub>k</sub>	Antoine constants $k^{\text{th}}$ coefficient of polynomial
d	density, g/cm <sup>3</sup>
g	molar Gibbs energy, J/mol
h	molar enthalpy, J/mol
h <sub>i</sub>	partial molar enthalpy, J/mol
m	number of adjustable parameters
n	number of experimental points
NBP	normal boiling temperature, K
<b>n</b> <sub>D</sub>	refractive index
p	pressure, hPa, kPa
S	molar entropy, J/(mol K)
т	temperature, K
t	degree of polynomial
V	molar volume, cm <sup>3</sup> /mol
V	volume flow, cm <sup>3</sup> /s
X	parameter of g <sup>E</sup> model
x	composition of liquid, mol/mol
у	composition of vapor, mol/mol
Z	measurable quantity

- δ experimental uncertainty
- fugacity coefficient Ø
- $\gamma$ activity coefficient

# Subscripts

i, j component i, j

٥i pure component i (reference-state value)

## Superscripts

Е	excess quantity
L	liquid
V	vapor
+	calculated quantity

# Other

relative volatility,  $(y_1/x_1)/(y_2/x_2)$  $\alpha_{12}$ Dz deviation,  $z - z^{*}$ AA(Dz) absolute average deviation,  $(1/n)\sum_{i}^{n} |z - z^{+}|_{i}$ SIG(Dz) standard deviation,  $\{[1/(n - m)]\sum_{i}^{n} (z - z^{+})_{i}^{2}\}^{0.5}$ RMS(Dz) root mean square deviation,  $[(1/n)\sum_{i}^{n} (z - z^{+})_{i}^{2}]^{0.5}$ 

Registry No. C<sub>8</sub>H<sub>18</sub>O, 142-96-1; C<sub>2</sub>H<sub>4</sub>Cl<sub>2</sub>, 107-06-2; C<sub>2</sub>H<sub>3</sub>Cl<sub>3</sub>, 71-55-6; C5H11CI, 543-59-9.

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