- molal concentration of electrolyte i, mol·kg⁻¹ m
- m_τ total molality of mixed electrolyte, mol·kg-
- Ţ total ionic strength of mixed electrolyte, mol·kg⁻¹
- ionic strength fraction of electrolyte i in mixture Y
- Φ molal osmotic coefficient of solution
- number of ions formed by the dissociation of one $\nu_{\rm i}$ molecule of electrolyte i
- f¢ Debye-Hückel term in Pitzer's equations for single electrolytes $[= -0.3290I^{1/2}/(1 + 1.2I^{1/2})]$
- B^{ϕ} ionic-strength-dependent parameter in Pitzer's equations for single electrolytes
- $\beta^{(0)}, \beta^{(1)}$ coefficients of B^{ϕ} term in Pitzer's equations for single electrolytes
- C^{ϕ} constant parameter in Pitzer's equations for single electrolytes
- θ°. θ', mixing parameters for Pitzer's ternary solution Ŵ equations
- $\sigma(\Phi)$ standard deviation of fitting equations for Φ
- ϕ_i^0 osmotic coefficient of pure electrolyte i at the total ionic strength of the mixture for Scatchard's neutral electrolyte equations
- mixing parameters for Scatchard's neutral electrob_{ii} lyte equations
- h. osmolality fraction of electrolyte i in mixture
- mean molal activity coefficient γ_+

Registry No. NaCl, 7647-14-5; MgCl₂, 7786-30-3.

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Osmotic and Activity Coefficients of Aqueous La(NO₃)₃ and Densities and Apparent Molal Volumes of Aqueous Eu(NO₃)₃ at 25 °C

Joseph A. Rard

University of California, Lawrence Livermore National Laboratory, Livermore, California 94550

The osmotic coefficients of aqueous La(NO₃)₃ have been measured from 1.3435 to 8.4591 mol·kg⁻¹ at 25 °C by using the isopiestic method. Some earlier osmotic coefficients for this salt are too high, apparently due to a stock solution concentration error, and have been normalized to the present results. These combined data and other activity data were then used to generate recommended values for the osmotic coefficients, water activities, and mean molal activity coefficients of La(NO₃)₃. The solubility of La(NO₃)₃·6H₂O(cr) was determined to be 4.6147 \pm 0.0056 mol·kg⁻¹ by the isoplestic method; this is in excellent agreement with the IUPAC recommended value of 4.610 \pm 0.005 mol·kg⁻¹. Density data were measured for aqueous Eu(NO₃)₃ from 0.03996 to 1.1014 mol·kg⁻¹ at 25 °C by using pycnometry. These results are in fairly good agreement with published low-concentration densities measured with a magnetic float.

Introduction

Activity and osmotic coefficient data for aqueous electrolyte solutions have numerous applications including solubility, chemical speciation, and reaction thermodynamics calculations. Density data are required for buoyancy calculations, for the interconversion of mass and volumetric concentration scales, and for the calculation of partial molal volumes which are related to the pressure derivatives of solute and solvent activities.

We have published isopiestic data for a total of 40 aqueous rare earth chloride, perchlorate, and nitrate solutions from low concentrations to saturation or supersaturation at 25 °C (1-6). Isopiestic measurements yield water activities, osmotic coefficients, and activity coefficients as a function of molality. For the first three parts of this series (1-3), the stock solution preparations, analyses, and the isopiestic measurements were done at Ames Laboratory (Iowa State University). For the last part (6) all of this was done at Lawrence Livermore National Laboratory (LLNL). However, for six of the rare earth nitrates,

published as parts 4 and 5 of this series (4, 5), the stock solutions were prepared and analyzed at Ames Laboratory but were then rebottled and shipped to LLNL for isopiestic measurements. These six salts are La(NO₃)₃, Pr(NO₃)₃, Nd(NO₃)₃, Dy(NO₃)₃, Ho(NO₃)₃, and Lu(NO₃)₃.

The rare earth nitrate solutions prepared at Ames Laboratory were analyzed there for concentration by mass titration with EDTA and by conversion to the anhydrous sulfate (3). Four of the six stock solutions that were shipped to LLNL were reanalyzed at LLNL by the gravimetric sulfate method. For Nd(NO₃)₃, Ho(NO₃)₃, and Lu(NO₃)₃ the reanalyses agreed well within their experimental precision with the Ames Laboratory values. However, for Dy(NO₃)₃ the concentration reported by Ames Laboratory was somewhat below the concentration measured at LLNL, which indicates that some evaporation of water occurred during the handling or shipping of this stock solution to LLNL. This new concentration analysis was used for reporting data for Dy(NO₃)₃ (5). Unfortunately, for La(NO₃)₃ and Pr(NO₃)₃ the amount of stock solution shipped to LLNL was adequate for the isopiestic measurements but was insufficient for concentration analyses. Therefore, for these two salts, concentration calculations were based solely on the reported stock solution concentrations. Since we ran out of the first La(NO₃)₃ stock solution during the isopiestic measurements, a second one was sent to us by Ames Laboratory and was used for the three lowest concentration points. This second stock solution was reanalyzed at LLNL and the measured concentration agreed with the reported value.

We recently reported isopiestic solubility data for several rare earth nitrate solutions at 25 °C (7, 8). Osmotic coefficients for saturated solutions generally agreed to within 0.1–0.3% of interpolated values from the earlier studies (3–6), which is very good agreement and confirms the usual precision and reproducibility of isopiestic measurements (9). A solubility determination for $Pr(NO_3)_3$ ·6H₂O(cr) using a new stock solution analyzed at LLNL agreed with other reported solubilities but the osmotic coefficient was discrepant (8). Subsequent measurements for La(NO₃)₃·6H₂O(cr), reported below, indicate similar problems for La(NO₃)₃.

Many of the earlier La(NO3)3 and Pr(NO3)3 isopiestic equilibrations were done simultaneously with Nd(NO3)3 samples present in other cups in the chamber (4). Several series of equilibrations were made with different samples from the same stock solutions. Since consistent results were obtained for the various equilibrations, simple weighing errors can be eliminated as the source of the problem. The CaCl₂ reference solution for our present redetermination of La(NO₃)₃ and Pr(NO₃)₃ osmotic coefficients is the same as used for the earlier determination (4), so it can be eliminated as the source of the discrepancy. Its concentration has been determined several times (9) and consistent results obtained. Also, ten of the earlier Nd(NO₃)₃ high concentration equilibrations with CaCl₂ standards were done simultaneously with MgCl₂ but without La(NO₃)₃ or Pr(NO₃)₃ samples. Separate measurements for MgCl₂ gave osmotic coefficients that agreed with these values within 0.2% (9, 10). This provides additional evidence that the CaCl₂ reference concentrations reported earlier (4) were accurate.

The only remaining possibility is errors in some of the rare earth nitrate stock solution concentrations in that study (4). As noted above, $Nd(NO_3)_3$ samples were included in most of the equilibrations (4) and its stock solution concentration was independently analyzed both in Ames and at LLNL. Osmotic coefficients for $Nd(NO_3)_3$ have also been determined at the Technical University of Gdańsk by Libuś et al. (11) up to 4.8342 mol·kg⁻¹, and their osmotic coefficients are within 0.12–0.45% of ours. Since osmotic coefficients are reproducible to about 0.2% under favorable conditions and the reference solution osmotic coefficients are uncertain by about an equal amount (9), agreement for the two Nd(NO₃)₃ studies is excellent. Thus, data for Nd(NO₃)₃ can be trusted and only the earlier results for La(NO₃)₃ and Pr(NO₃)₃ seem to be in error.

Discrepancies for La(NO₃)₃ and Pr(NO₃)₃ in the earlier study (4) relative to the new solubility values can be accounted for if their actual stock solution concentrations were higher than determined at Ames Laboratory. This is in the same direction as the difference noted for Dy(NO₃)₃, and the same explanation seems appropriate. That is, some evaporation probably occurred for La(NO₃)₃ and Pr(NO₃)₃ stock solutions prior to their arrival at LLNL. Thus, isopiestic data have been redetermined for La(NO₃)₃ using the second stock solution supplied by Ames Laboratory and are reported here. Although the three lowest concentration points in the earlier study were measured with samples from this second stock solution, no discrepancies were obvious at that time since molality concentration errors are greatly reduced at low concentrations.

Since similar discrepancies occur for Pr(NO₃)₃, isopiestic measurements are in progress at LLNL and will be reported elsewhere.

Spedding et al. (*12*, *13*) have reported densities for solutions of 13 aqueous rare earth nitrates from about 0.0015 to 0.09–0.27 mol·kg⁻¹ at 25 °C by using a magnetically controlled float, and they have extended the data for 11 of these salts to saturation by using pycnometry (*14*). However, density data for Eu(NO₃)₃ extend only from 0.00138 to 0.16994 mol·kg⁻¹ (*13*). Jeżowska-Trzebiatowska et al. (*15*) have reported five density points for Eu(NO₃)₃ from 0.40894 to 0.67400 mol·kg⁻¹ using pycnometry. These two density studies for Eu(NO₃)₃ do not overlap in concentration.

A convenient deviation function for comparing density data is the density of the solution minus that of the solvent, all divided by the molality. For the majority of aqueous electrolytes, this deviation function is a monotonic decreasing function of concentration. The Eu(NO₃)₃ density data of Spedding et al. (*13*) show this typical behavior, whereas the values of Jeżowska-Trzebiatowska et al. (*15*) for this function are not only discrepant but increase rather than decrease with concentration. Thus, new density data are needed for Eu(NO₃)₃, and they are reported in this paper.

Experimental Section

The isopiestic experiments were performed at 25.00 ± 0.005 °C (IPTS-68) using stainless steel isopiestic chambers that have been described in detail elsewhere (β). Isopiestic equilibration times were generally 4–6 days over most of the concentration range, but were increased to 6–12 days for the lower concentrations. All sample weights were converted to masses by using their appropriate densities.

Our Eu(NO₃)₃ stock solution was prepared at LLNL from Analytical Reagent HNO₃ and Eu₂O₃ (supplied by Ames Laboratory), and it was adjusted to its equivalence pH by using dilute HNO₃. This equivalence pH was determined by titration of samples of unadjusted stock solution with the same dilute HNO₃ solution. The La(NO₃)₃ stock solution was prepared by the same method at Ames Laboratory, and it was supplied to us as an analyzed stock solution.

A sample of the La(NO₃)₃ stock solution was evaporated to dryness and then thermally decomposed to La₂O₃ at 800 °C. Both this La₂O₃ and some of the original Eu₂O₃ were analyzed by direct current arc optical emission spectroscopy (DCAOES), and the Eu₂O₃ by X-ray fluorescence spectroscopy (XRFS), at LLNL to quantitatively determine impurities present. The La₂O₃ contained (in weight percent) 0.001% Mg, \leq 0.001% Ca, and \leq 0.0001% Sr, B, and Cu; other rare earth elements were below their detection limits. DCAOES indicated the Eu₂O₃ contained 0.06% Gd, \leq 0.0001% Ci, 0.0005% each of B and Fe, 0.0004% Mg, and \leq 0.0001% Si; XRFS gave 0.04% Gd

Table I. Isopiestic Molalities of $La(NO_3)_3$ Solutions with $CaCl_2$ Reference Solutions at 25 °C

[CaCl ₂], mol·kg ⁻¹	$[La(NO_3)_3]$, mol·kg ⁻¹	$\Phi(La(NO_3)_3)$
1.4051	1.3435	0.9156
1.6016	1.5554	0.9524
1.7004	1.6644	0.9712
1.7279	1.6945	0.9768
1.8696	1.8529	1.0049
2.0163	2.0191	1.0348
2.1230	2.1417	1.0569
2.2419	2.2796	1.0819
2.3324	2.3867	1.1005
2.4947	2.5783	1.1356
2.5918	2.6978	1.1552
2.7166	2.8489	1.1822
2.8281	2.9845	1.2067
2.9387°	3.1225	1.2301
3.0717°	3.2879	1.2592
3.1782^{a}	3.4205	1.2828
3.2710ª	3.5379	1.3030
3.3848	3.6833	1.3275
3.4890	3.8172	1.3500
3.5743	3.9265	1.3686
3.7035	4.0911	1.3974
3.7724	4.1802	1.4124
3.8353	4.2645	1.4251
3.8877	4.3319	1.4367
3.9472	4.4117	1.4487
4.0781	4.5809	1.4774
4.1049	4.6140^{b}	1.4838
4.1049	4.6150°	1.4834
4.1045	4.6150^{d}	1.4832
4.1839	4.7184	1.5003
4.2508	4.8066	1.5143
4.3896	4.9898	1.5433
4.4662	5.0885	1.5598
4.5947	5.2595	1.5857
4.6658	5.3515	1.6007
4.7605	5.4767	1.6196
4.8586	5.6062	1.6389
4.9602	5.7368	1.6596
5.0288	5.8292	1.6722
5.1102	5.9347	1.6879
5.1753	6.0176	1.7007
5.3014	6.1752	1.7258
5.3850	6.2823	1.7411
5.4729	6.3941	1.7570
5.5958	6.5477	1.7792
5.7715	6.7598	1.8111
5.8497	6.8529	1.8248
5.9036	6.9178	1.8338
6.0485	7.0814	1.8598
6.1948	7.2487	1.8835
6.3340	7.4036	1.9055
6.4778	7.5540	1.9288
6.6571	7.7414	1.9551
0.7583	7.8529	1.9672
0.9453	8.0342	1.9934
7.1354	8.2163	2.0174
7.2482	8.3233	2.0304
7.3986	8.4591	2.0480

^aQuadruplicate CaCl₂ samples used for these determinations. ^bFirst solubility determination, with 4-day equilibration. The La-(NO₃)₃ saturation molality is 4.6140 ± 0.0008 and the CaCl₂ molality 4.1049 ± 0.0007. ^cSecond solubility determination, with 6day equilibration. The La(NO₃)₃ saturation molality is 4.6150 ± 0.0008 and the CaCl₂ molality 4.1049 ± 0.0011. ^dThird solubility determination, with 13-day equilibration. The La(NO₃)₃ saturation molality is 4.6150 ± 0.0008 and the CaCl₂ molality 4.1045 ± 0.0011. ^eSingle La(NO₃)₃ sample; see text for details.

and 0.006% Dy. Other rare earth elements were below their detection limits.

Stock solution concentration analyses were performed by conversion of triplicate samples of the stock solution to the anhydrous sulfate at 500 °C. To avoid coprecipitation of nitrate ions in the rare earth sulfate, nitrate ions were decomposed

Table II. Densities and Apparent Molal Volumes of Aqueous $Eu(NO_3)_3$ at 25 °C

- ,	•.•		
m, mol·kg ⁻¹	c, mol•dm ⁻³	$d, g \cdot cm^{-3}$	$\phi_{\mathbf{v}}, \mathbf{cm}^3 \cdot \mathbf{mol}^{-1}$
0.039 961	0.039 763	1.008 489	50.32
0.062242	0.061 860	1.014756	51.82
0.12197	0.12082	1.031451	53.37
0.20201	0.199 21	1.053479	54.85
0.359 49	0.35128	1.095 89	56.76
0.56124	0.54182	1.14852	58.58
0.72176	0.689 92	1.18907	59.82
0.901 84	0.85234	1.23318	61.11
1.1014	1.0277	1.28040	62.44

prior to the H_2SO_4 addition. This decomposition was done either by doing two evaporations of stock solution samples with excess HCI, or by thermally decomposing the nitrate followed by another evaporation with HCI. The resulting rare earth chlorides/oxychlorides are readily converted to the sulfates by evaporation with excess H_2SO_4 .

As noted above, we used the second La(NO₃)₃ stock solution that had been sent by Ames Laboratory; it had been analyzed there for concentration both by mass titration with EDTA and by oxalate precipitation followed by thermal decomposition to the oxide. Our sulfate analysis agreed well with these other analyses, and the mean value of 4.4551 ± 0.0040 mol·kg⁻¹ was used in calculations. Here and elsewhere the uncertainty limits are one standard deviation. Two separate sulfate analyses at LLNL for the Eu(NO₃)₃ stock concentration gave 1.1013 ± 0.0001 and 1.1015 ± 0.0003 mol·kg⁻¹. Assumed molecular masses are 324.92 for La(NO₃)₃, 565.98 for La₂(SO₄)₃, 337.975 for Eu(NO₃)₃, and 592.09 g·mol⁻¹ for Eu₂(SO₄)₃.

CaCl₂ solutions were used as isopiestic reference standards. The concentration of this stock solution was determined by conversion of samples to CaSO₄ and by dehydration; the analyses results are given elsewhere (9). Assumed molecular masses are 110.986 for CaCl₂ and 136.138 g-mol⁻¹ for CaSO₄.

Table I contains the experimental molalities of La(NO₃)₃ in isopiestic equilibrium with a CaCl₂ reference solution. Duplicate samples were used in the majority of these equilibrations; the average molalities for each electrolyte are reported and they are reliable to better than $\pm 0.087\%$, with most molalities being precise to at least $\pm 0.05\%$. For a few equilibrations, four CaCl₂ samples were used.

Crystals of La(NO₃)₃·n H₂O were grown by seeding a slightly supersaturated solution followed by slow evaporation of water in a desiccator. An extra isopiestic cup containing saturated solution and crystals was added to the chamber for solubility determinations. See ref 8 for details. Measured solubilities using 4-, 6-, and 13-day equilibrations were in excellent agreement, so true saturation had been reached. The experimental solubility is $4.6147 \pm 0.0010 \text{ mol·kg}^{-1}$, where the uncertainty limits are statistical only. Including the stock solution concentration uncertainty gives a total uncertainty of $\pm 0.0056 \text{ mol·kg}^{-1}$. Chemical analysis of the solid phase by thermal decomposition at 825 °C gave $n = 6.06 \pm 0.1$; i.e., the hexahydrate was present. Our solubility value is in excellent agreement with the IUPAC recommended value (16) of 4.610 $\pm 0.005 \text{ mol·kg}^{-1}$.

Our isopiestic measurements for $La(NO_3)_3$ extend 3.844 mol·kg⁻¹ into the supersaturated concentration region. A total of 29 supersaturated solution experiments were performed which involved $4^{1}/_{2}$ months of experimentation. Supersaturated La(NO₃)₃ solutions show very little tendency to spontaneously crystallize, and problems occurred in only two of these attempts. In both cases only one La(NO₃)₃ sample went dry while the other sample remained in solution. Since the reference solution molalities were in agreement, these two runs should be reliable and are reported in Table I. In a third experiment, only one La(NO₃)₃ sample was used since the other was left out to be dissolved and reconcentrated.



Figure 1. Differences between experimental densities and least-squares equations for $Eu(NO_{3})_{3}$ solutions in g·cm⁻³ × 10⁵: (\bullet) this research; (\blacktriangle) Spedding et al. (*13*).

Densities of Eu(NO₃)₃ solutions were measured in duplicate at 25.00 \pm 0.005 °C by using a matched pair of 30.87-cm³ single-stem pycnometers. The pycnometer volumes had been calibrated 7–9 times each by using purified water and assuming a water density of 0.997 045 g·cm⁻³ (*17*). Table II contains the Eu(NO₃)₃ densities which are precise to about (2–3) \times 10⁻⁵ g·cm⁻³. These measurements extend only to 1.1014 mol·kg⁻¹ since the amount of stock solution was limited.

Density Results for Aqueous Eu(NO₃)₃

Density data for $Eu(NO_3)_3$ solutions were represented by the least-squares equations

$$d = d^{0} + \sum_{i=2}^{n} B_{i} X_{i}^{i/2}$$
(1)

where X = m in mol·kg⁻¹ or *c* in mol·dm⁻³, and $d^0 = 0.997045$ g-cm⁻³ (17). Table II contains our experimental densities, and Table III contains the least-squares B_i for eq 1. These coefficients were calculated by giving equal weight to our densities and to those of Spedding et al. (13).

Figure 1 shows the differences between the experimental densities and the least-squares fit to eq 1. The data of Spedding et al. (13) are about 4×10^{-5} g·cm⁻³ below ours, which only slightly exceeds our experimental precision of (2–3) × 10⁻⁵ g·cm⁻³. Spedding et al. used a magnetically controlled float, and their densities are slightly more precise than ours. However, the major source of error was their stock solution concentration uncertainty of ±0.1% which exceeds our concentration uncertainty. Thus, these two studies probably agree within experimental error. Densities of Jeżowska-Trzebiatowska et al.

Table IV. La(NO₃)₃ Osmotic Coefficients from Freezing Point Depression Data^a

m, mol·kg ⁻¹	$\Phi_{\rm f}{}^b$	Φ_{c}	m, mol·kg ⁻¹	$\Phi_{\mathrm{f}}{}^{b}$	Φ^c
0.022 311	0.8002	0.7952	0.051 483	0.7670	$0.7639 \\ 0.7511 \\ 0.7420^d$
0.023 699	0.7964	0.7915	0.087 282	0.7514	
0.043 599	0.7734	0.7697	0.177 14	0.7363	

^aBased on the data of Hall and Harkins (20). ^bOsmotic coefficient at the freezing temperature. ^cOsmotic coefficient at 25 °C. ^dThis point given zero weight in the least-squares fits.

(15) are too high by 0.7-1.8% and were rejected.

Apparent molal volumes for $Eu(NO_3)_3$ were calculated by use of the equation

$$\phi_{\rm v} = \frac{10^3(d^0 - d)}{md^0 d} + \frac{M_2}{d} \tag{2}$$

where M_2 is the molecular mass of Eu(NO₃)₃. These values are also given in Table II. The density differences of 4×10^{-5} g·cm⁻³ between us and Spedding et al. (*13*) affect ϕ_v by 1.2 cm³·mol⁻¹ at 0.04 mol·kg⁻¹, but change ϕ_v by only 0.03 cm³·mol⁻¹ at 1.1 mol·kg⁻¹.

Activity Results for Aqueous La(NO₃)₃

Osmotic coefficients, $\Phi,$ of La(NO_3)_3 were calculated by using the equation for isopiestic equilibrium

$$\Phi = \frac{\nu^* m^* \Phi^*}{\nu m} \tag{3}$$

where *m* is the molality of La(NO₃)₃, $\nu = 4$ is the number of ions formed by the dissociation of one molecule of La(NO₃)₃, and the corresponding quantities for CaCl₂ reference solutions in equilibrium with the La(NO₃)₃ solutions are denoted with asterisks ($\nu^* = 3$). CaCl₂ Φ^* values were taken from a published equation (*18*). Table I contains the isopiestic equilibrium molalities and La(NO₃)₃ Φ values.

Other activity data have been reported for aqueous $La(NO_3)_3$. Two freezing point depression studies were made for $La(NO_3)_3$ early this century (19, 20), and they can be converted to osmotic coefficients by using available heat capacity (21) and enthalpy of dilution data (22). The four points of Noyes and Johnston (19) are of low precision and are scattered, so they were rejected. Freezing point data of Hall and Harkins (20) were converted to osmotic coefficients at 25 °C, and these derived values are given in Table IV. Yakimov and Guzhavina's eight vapor pressure points (23) were rejected because of considerable scatter; osmotic coefficients calculated from them are about right at 1.17 mol·kg⁻¹ but are 3–10% high at other concentrations.

Kirgintsev and Luk'yanov (24) reported isopiestic data for seven La(NO₃)₃ compositions from 1.450 to 2.922 mol·kg⁻¹ using NaCl as the isopiestic reference solution. Osmotic coefficients were recalculated from these data by using eq 3 and Hamer and Wu's (25) NaCl Φ^* equation. Their point at 1.978 mol·kg⁻¹ is discrepant from their other values, but their other six points are in fair agreement with the values in Table I ($\simeq 0.5\%$ lower). It was concluded previously (4) that their data are unreliable since the sulfate method of analysis is unreliable without precautions to destory nitrate ions. In fact, they actually used oxalate precipitation followed by ignition to La2O3. This method is less prone to coprecipitation problems, so our earlier criticism (4) of that part of their study (24) was unwarranted. However, they also used evaporation of samples followed by thermal decomposition, which has been shown to give high apparent concentrations (and low Φ values) owing to incomplete decomposition of the oxynitrate (6).

In addition to these other studies, there is our earlier isopiestic data relative to KCI and $CaCl_2$ reference solutions (4).

Table V. Isopiestic Molalities from Rard, Miller, andSpedding (4) Normalized to Table I Data

[reference], mol·kg ⁻¹	$[La(NO_3)_3], mol \cdot kg^{-1}$	$\Phi(La(NO_3)_3)$
	KCl Reference	
0.20504	0.12481^{a}	0.7491
0.21249	0.12990^{a}	0.7454
0.50176	0.29628^{a}	0.7614
0.67018	0.39041	0.7701
0.68341	0.39762	0.7710
0.81030	0.46634	0.7791
1.0147	0.57326	0.7942
1,1909	0.00000	0.8070
1.5736	0.85124	0.8353
1.7837	0.95067	0.8511
1.9755	1.0401	0.8650
2.2806	1.1789	0.8872
2.3641	1.2152	0.8941
	CaCl. Reference	
1.2564	1,1886	0.8876
1.2733	1.2052	0.8914
1.2947	1.2282	0.8947
1.3186	1.2548	0.8979
1.4587	1.4031	0.9239
1.5903	1.5467	0.9480
1.6822	1.6489	0.9650
1.7515	1.7267	0.9780
1.8250	1.8090	0.9925
1.9094	1.9040	1.0096
1.9724	1.9773	1.0215
2.0519	2.0671	1.0385
2.1390	2.1603	1.0581
2.2200	2.2001	1.0756
2.3751	2.0001	1 1042
2.4518	2.5374	1.1219
2.5367	2.6353	1.1417
2.6053	2.7215	1.1550
2.7061	2.8409	1.1780
2.8198	2.9802	1.2025
2.8982	3.0733	1.2210
2.9329	3.1194	1.2273
2.9706	3.1625	1.2369
3.0413	3.2511	1.2521
3.1104	3.3419	1.2097
3 2634	3 5396	1.2002
3.3399	3.6276	1.2557
3.4201	3.7281	1.3353
3.5365	3.8787	1.3601
3.5962	3.9549	1.3733
3.6563	4.0337	1.3859
3.7271	4.1252	1.4013
3.7693	4.1745	1.4123
3.8288	4.2526	1.4248
3.8399 2.0010	4.2634	1.4258
3.9218	4.3700	1.4401
4.0030	4.4010	1.4030
4.1572	4.6797	1 4958
4.2724	4.8281	1.5211
4.3374	4.9181	1.5333
4.3962	4.9935	1.5462
4.5083	5.1414	1.5693
4.5367	5.1792	1.5750
4.6688	5.3560	1.6011
4.7452	5.4558	1.6168
4.8233	5.5595	1.6320
4.9102 5.0228	0.0002 5.9156	1.6502
5.0236	5.8780	1.0732
5.1577	5.9954	1.6972
5.2457	6.1044	1.7152
5.3125	6.1876	1.7283
5.3978	6.2910	1.7456
5.4884	6.4116	1.7604
5.5404	6.4779	1.7695
5.5888	6.5356	1.7789

^a These three points only were not adjusted; see text for details.

Table VI. Coefficients and Powers for $La(NO_3)_3$ Osmotic Coefficient Polynomial^a

i	ri	A_i	
1	0.75	0.568 8551	
2	1.00	22.39564	
3	1.25	-53.57635	
4	1.50	57.93019	
5	1.75	-33.22622	
6	2.00	9.830907	
7	2.25	-1.184351	
$\sigma(\Phi)$	0.00141		

^a These parameters apply to 8.4591 mol·kg⁻¹.

We concluded above that these reference molalities were reliable; only the La(NO_3)₃ stock solution molality was incorrect. It should therefore be possible to "normalize" the earlier concentration scale to our present data in their overlap region, to generate a corrected set of isopiestic molalities from that earlier study (4).

The isopiestic reference solution used for the isopiestic measurements in Table I was $CaCl_2$, and samples from the very same $CaCl_2$ stock solution were used in the earlier study (4) for $La(NO_3)_3$ nominal concentrations of 1.1836–6.4739 mol·kg⁻¹. Thus, the new $La(NO_3)_3$ to $CaCl_2$ isopiestic molality ratio *R* can be used to adjust the earlier $La(NO_3)_3$ molalities from their isopiestic $CaCl_2$ concentrations.

A large expanded-scale plot of the isopiestic molality ratio R $= m/m^*$ was made for all of the data in Table I. For certain selected molalities of CaCl₂ obtained in the earlier study (4), the R values were graphically interpolated and then used to calculate what the La(NO3)3 molality should have been for that equilibration. From this adjusted La(NO₃)₃ molality, the final weights of La(NO3)3 solution for the two samples used for that particular equilibration, and the weights of stock solution added initially to these isopiestic cups, we back-calculated what the correct number of moles of La(NO3)3 and the weight of water were per gram of stock solution for the earlier study. This was done for seven approximately equally spaced CaCl₂ concentrations from the earlier study: 2.5367 (1.0036), 3.0413 (1.0061), 3.5365 (1.0068), 4.0050 (1.0084), 4.5367 (1.0087), 5.0238 (1.0099), and 5.5888 (1.0108) mol·kg⁻¹. The numbers in parentheses are the ratios of the corrected to the uncorrected $La(NO_3)_3$ molality for that particular $CaCl_2$ reference molality. These La(NO₃)₃ molality ratios are uncertain between about 0.0005 and 0.0023 based on uncertainties in the R values (which have been graphically smoothed at one stage during the calculations). This normalization was done at relatively high concentrations since the larger differences there give greater precision to the final results. The back-calculated La(NO₃)₃ stock solution concentration was nearly independent of the selected equilibrium CaCl₂ molalities and highly consistent, and the average value was used to recalculate the La(NO₃)₃ molalities. This shows that the earlier study has nearly the same concentration dependence for Φ as the present study.

Table V contains the normalized isopiestic results from the earlier study (4). Only the three lowest $La(NO_3)_3$ molalities in this table were not adjusted, since they were done with samples from the same stock solution used in the current study. Molality changes for $La(NO_3)_3$ are 1% at about 6 mol·kg⁻¹ but decrease to about 0.3% at low concentrations; this variation is just that due to changes in molality with changes in the weight fraction of water present. The uncertainty in the adjusted molalities due to the normalization is fairly small. For example, this uncertainty in the highest $La(NO_3)_3$ molality in Table V is only 0.19% and it is 0.08% at 1.1886 mol·kg⁻¹.

Osmotic coefficients for $La(NO_3)_3$ were then represented by the least-squares equation

$$\Phi = 1 - (A/3)m^{1/2} + \sum_{i} A_{i} m^{r_{i}}$$
 (4)



Figure 2. Differences between experimental osmotic coefficients and the least-squares eq 4 for La(NO₃)₃ solutions: (**●**) this research; corrected data of Rard et al. (4) from Table V: (\diamond) KCl standard and (O) CaCl₂ standard; (**A**) freezing point depression data (20) from Table IV; (**□**) isopiestic data of Kirgintsev and Luk'yanov (24).

where A = 8.6430 is the Debye-Hückel limiting slope for a 3-1 electrolyte. Unit weights were given to our isopiestic data in Table I and to the freezing point depression results in Table IV, and weights of 0.5 were given to the normalized isopiestic data in Table V and to six of Kirgintsev and Luk'yanov's (24) points. Other data (19, 23) were rejected as inaccurate.

Least-squares coefficients for the best fit to eq 4 and the standard deviation of the fit $\sigma(\Phi)$ are given in Table VI. Table VII contains calculated values of Φ , a_1 , and γ_{\pm} . Here a_1 is the water activity of the solution, and γ_{\pm} is the mean molal activity coefficient calculated from

$$\ln \gamma_{\pm} = -Am^{1/2} + \sum_{i} A_{i} \left(\frac{r_{i} + 1}{r_{i}} \right) m^{r_{i}}$$
 (5)

Figure 2 shows the difference between the various experimental Φ values for La(NO₃)₃ and their corresponding values calculated by using the least-squares parameters in Table VI. These various sets of data are obviously now in excellent agreement.

The normalized data of Rard et al. (4), Table V, agree with our new Φ values within 0.0–0.2% over most of their overlapping concentration range, but slightly systematic differences of 0.3–0.5% do occur from 1.65 to 2.9 mol·kg⁻¹ for the earlier study using CaCl₂ reference standard data. Our new Φ values are more precise and are probably more accurate than the earlier data in this concentration region. However, their KCl standard data connect up smoothly with our redetermined data of Table I.

The experimental Φ data up to 1.5 mol·kg⁻¹ were also represented by Pitzer's equation (*26*) using $A^{\phi} = 0.3920$. Following Pitzer et al. (*26*), we set $3\beta^{(1)}/2 = 7.700$ and used their recommended weighting scheme. Least-squares calculations then give $3\beta^{(0)}/2 = 0.7374$, $(3^{3/2}/2)C^{\phi} = -0.1989$ and $\sigma(\Phi) = 0.0069$. These parameters have changed slightly from those reported earlier (*4*). Higher concentration results were not included because of excessive cycling of this equation around the Φ data.

The isopiestic molality ratio of $La(NO_3)_3$ to $CaCl_2$, *R*, is greater than unity above 1.995 mol·kg⁻¹, whereas we expect it to be less than unity for dissociated salts of these valence types. Since $CaCl_2$ is a strong electrolyte, this implies that $La(NO_3)_3$ has considerable amounts of complex formation present at moderate and high concentrations.

Table VII.	Osmotic C	Coefficients,	Water A	ctivities, and
Activity Co	efficients	of La(NO ₃) ₃	at Even	Molalities

clivity Coefficient	S OF LAUNO	3/3 at Even Mu	lanues	
m, mol·kg ⁻¹	Φ	a_1	γ_{\pm}	
0.01	0.8328	0.999400	0.5500	-
0.05	0.7642	0.997250	0.3699	
0.1	0.7496	0.994613	0.3077	
0.2	0.7507	0.98924	0.2588	
0.3	0.7602	0.98370	0.2366	
0.4	0.7720	0.97799	0.2238	
0.5	0.7848	0.97212	0.2157	
0.6	0.7983	0.96608	0.2105	
0.7	0.8123	0.95985	0.2071	
0.8	0.8270	0.95344	0.2052	
0.9	0.8421	0.94685	0.2043	
1.0	0.8577	0.94007	0.2042	
1.2	0.8900	0.92593	0.2061	
1.4	0.9235	0.91104	0.2101	
1.5	0.9407	0.90332	0.2127	
1.6	0.9580	0.8954	0.2157	
1.8	0.9932	0.8791	0.2228	
2.0	1.0288	0.8622	0.2312	
2.2	1.0647	0.8447	0.2407	
2.4	1.1007	0.8267	0.2513	
2.5	1.1187	0.8175	0.2570	
2.6	1.1366	0.8082	0.2630	
2.8	1.1725	0.7893	0.2757	
3.0	1.2081	0.7702	0.2894	
3.2	1.2434	0.7507	0.3043	
3.4	1.2785	0.7311	0.3201	
3.5	1.2958	0.7212	0.3285	
3.6	1.3131	0.7113	0.3371	
3.8	1.3475	0.6914	0.3551	
4.0	1.3814	0.6715	0.3743	
4.2	1.4149	0.6517	0.3947	
4.4	1.4481	0.6318	0.4162	
4.5	1.4645	0.6219	0.4275	
4.6	1.4808	0.6121	0.4391	
4.8	1.5132	0.5925	0.4632	
5.0	1.5452	0.5731	0.4887	
5.2	1.5768	0.5539	0.5156	
5.4	1.6080	0.5349	0.5440	
5.5	1.6235	0.5255	0.5588	
5.6	1.6389	0.5161	0.5739	
5.8	1.6695	0.4977	0.6055	
6.0	1.6998	0.4795	0.6388	
6.2	1.7297	0.4617	0.6738	
6.4	1.7594	0.4442	0.7107	
6.5	1.7741	0.4356	0.7299	
6.6	1.7888	0.4271	0.7495	
6.8	1.8179	0.4103	0.7904	
7.0	1.8468	0.3939	0.8334	
7.2	1.8754	0.3779	0.8787	
7.4	1.9038	0.3623	0.9263	
7.5	1.9179	0.3547	0.9510	
7.6	1.9320	0.3471	0.9764	
7.8	1.9599	0.3323	1.0290	
8.0	1.9877	0.3179	1.0844	
8.2	2.0152	0.3040	1.1425	
8.4	2.0425	0.2904	1.2036	
8.4591	2.0505	0.2865	1.2223	

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Glossary

d	density	of	solution,	g•cm ^{−3}	
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- d⁰ density of pure water, g·cm⁻³
- ϕ_v apparent molal volume of solute, cm³·mol⁻¹
- Φ molal osmotic coefficient
- ν number of ions formed by the dissociation of one molecule of solute
- m molal concentration of solute, mol·kg⁻¹
- c molar concentration of solute, mol·dm⁻³

*	symbols with asterisks refer to isoplestic reference solution	(7) (8)	Rard, C Rard, C
B.	least-squares coefficients of eq.1	(9) (10)	Rard, .
_, 	least-squares coefficients of eq.4 and 5	(,	issue.
		(11)	Libuś, 2
r	powers of eq 4 and 5		11, 11
Α	Debye-Hückel constant for 3-1 electrolytes	(12)	Speddi
M ₁	molecular mass of water, g·mol ⁻¹	(13)	2440-2 Speddi
M	molecular mass of solute, g·mol-1	(13)	78.11
A(0) A(1)	narameters for Pitzer's equations	(14)	Speddi
ρ , ρ ,	parameters for ritzers equations		McDow
- C+			1087-1
A^{φ}	Debye-Hückel constant (1-1 charge type) for Pit-	(15)	Jeżows
	zer's Φ equation	(16)	Siekier
σ	standard deviation of fitting equations	(10)	num ar
~	mean molal activity coefficient		ity Data
Υ±		(17)	Kell, G.
a ₁	water activity	(18)	Rard, J
Φ_{f}	osmotic coefficient at the freezing temperature of	(10)	1977, .
	the solution	(19)	Noyes,
R	isoniestic molality ratio of La(NO ₂), to CaCl	(20)	Sneddi
		(21)	24.29
Registry	No. La(NO ₃) ₃ , 10099-59-9; Eu(NO ₃) ₃ , 10138-01-9.	(22)	Speddi

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Viscosities of Gaseous R13B1, R142b, and R152a

Mitsuo Takahashi, Chiaki Yokoyama, and Shinji Takahashi*

Chemical Research Institute of Non-Aqueous Solutions, Tohoku University, Sendai, 980 Japan

The viscosities of gaseous bromitrifluoromethane (R13B1), 1-chloro-1,1-difluoroethane (R142b), and 1,1-difluoroethane (R152a) were measured with an oscillating disk viscometer of the Maxwell type at 273.15-448.15 K up to 10 MPa for R13B1 and at 298.15-423.15 K up to 5 MPa for R142b and R152a. Two empirical equations were obtained; one is for the viscosity at atmospheric pressure as a function of temperature, and the other is for the viscosity in the whole range of the present measurement as a function of temperature and density. The intermolecular force constants of Stockmayer 12-6-3 potential were determined from the temperature dependence of the viscosity at atmospheric pressure as follows: $\epsilon/k = 235$ K, $\sigma = 0.506$ nm, and δ = 0.058 for R13B1; ϵ/k = 362 K, σ = 0.499 nm, and δ = 0.36 for R142b; ϵ/k = 312 K, σ = 0.463 nm, and δ = 0.62 for R152a.

Many halogenated hydrocarbons are commonly used as refrigerants and expected to be used as working fluids of turbines. However, the experimental data of gas viscosity needed for the design of related equipments are scarce and the reliability of the literature data is uncertain because of the large discrepancies among them. Therefore, the measurement of the gas viscosities of halogenated hydrocarbons under pressure is being continued by the present authors, and the viscosity data for chlorodifluoromethane (R22), dichlorodifluoromethane (R12),

Table I. Physical Properties of Refrigerants

	R13B1	R142b	R152a
chem formula	CBrF ₃	CClF ₂ CH ₃	CHF ₂ CH ₂
mol wt ^a	148.910	100.496	66.050
$T_{\rm b}^{\ a} {\rm K}$	215.4	263.4	248.2
T_{c}^{a} K	340.2	410.2	386.6
P _c ^b MPa	3.97	4.12	4.50
$\rho_{\rm c},^{\rm b}$ kg·m ⁻³	760	435	365
dipole moment, ^c D	0.7	2.1	2.3

^a T_{b} , boiling point at atmospheric pressure; T_{c} , critical temperature; P_{c} , critical pressure; ρ_{c} , critical density. ^b Makita, T. Viscosity and Thermal Conductivity; Baifukan: Tokyo, 1975; p 224 and 225. °Reid, R. C.; Prausnitz, J. M.; Sherwood, T. K. The Properties of Gases and Liquids; McGraw Hill: New York, 1977; p 630 and 636.

chlorotrifluoromethane (R13), 1,2,2-trichloro-1,1,2-trifluoroethane (R113), 1,2-dichloro-1,1,2,2-tetrafluoroethane (R114), and chloropentafluoroethane (R115) were reported previously (1-4). The viscosities of gaseous bromotrifluoromethane (R13B1), 1-chloro-1,1-difluoroethane (R142b), and 1,1-difluoroethane (R152a) are described in the present paper.

The viscosity of gaseous R13B1 has been measured by Tsui (5), Reed et al. (6), Wilbers (7), Karbanov et al. (8), and Kletskii et al. (9). Figure 1 shows the temperatures and pressures at which the literature data were obtained. The present measurement covers the area with oblique lines. The point C.P. denotes the critical point. No experimental data for the viscosities of R142b and R152a could be found in the literature.

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