

- (21) LoSurdo, A.; Millero, F. J. *J. Solution Chem.* **1980**, *9*, 163.  
 (22) Spedding, F. H.; Saeger, V. W.; Gray, K. A.; Boneou, P. K.; Brown, M. A.; Dekock, C. W.; Baker, J. L.; Shlers, L. E.; Weber, H. O.; Habenschuss, A. *J. Chem. Eng. Data* **1975**, *20*, 72.  
 (23) Spedding, F. H.; Shlers, L. E.; Brown, M. A.; Derer, J. L.; Swanson, D. L.; Habenschuss, A. *J. Chem. Eng. Data* **1975**, *20*, 82.  
 (24) Söhnel, O.; Novotny, P.; Solc, Z. *J. Chem. Eng. Data* **1984**, *29*, 379.  
 (25) Romankiw, L. A.; Chou, I-Ming *J. Chem. Eng. Data* **1983**, *28*, 300.  
 (26) Gates, J. A.; Wood, R. H. *J. Chem. Eng. Data* **1985**, *30*, 44.  
 (27) Ackerlof, G.; Kegeles, G. *J. Am. Chem. Soc.* **1938**, *60*, 1226.  
 (28) Hershey, J. P.; Damesceno, R.; Millero, F. J. *J. Solution Chem.* **1984**, *13*, 825.  
 (29) Vaslow, F. J. *Phys. Chem.* **1966**, *70*, 2286.  
 (30) Fortier, J. L.; LeDuc, P. A.; Desnoyers, J. E. *J. Solution Chem.* **1974**, *3*, 323.  
 (31) Isono, T. *J. Chem. Eng. Data* **1984**, *29*, 45.  
 (32) Kumar, A. *J. Solution Chem.* **1986**, *15*, 409.  
 (33) Kumar, A. *J. Chem. Eng. Data* **1986**, *31*, 347.  
 (34) Ackerlof, G.; Kegeles, G. *J. Am. Chem. Soc.* **1939**, *61*, 1027.  
 (35) Tham, M. K.; Gubbins, K. E.; Walker, Jr., R. D. *J. Chem. Eng. Data* **1985**, *12*, 525.  
 (36) LoSurdo, A.; Alzola, M.; Millero, F. J. *J. Chem. Thermodyn.* **1982**, *14*, 649.  
 (37) Correia, R. J.; Kestin, J.; Ezzat Khalifa, H. *J. Chem. Eng. Data* **1980**, *25*, 201.  
 (38) Hershey, J. P.; Satolongo, S.; Millero, F. J. *J. Solution Chem.* **1983**, *12*, 233.  
 (39) Correia, R. J.; Kestin, J. *J. Chem. Eng. Data* **1981**, *26*, 43.  
 (40) Fabuss, B. M.; Korosl, A.; Huq, A. K. M. *J. Chem. Eng. Data* **1986**, *11*, 325.  
 (41) Habenschuss, A.; Spedding, F. H. *J. Chem. Eng. Data* **1976**, *21*, 95.  
 (42) Gildseth, W. M.; Habenschuss, A.; Spedding, F. H. *J. Chem. Eng. Data* **1975**, *20*, 292.  
 (43) Wakabayashi, T.; Takaizumi, K. *J. Solution Chem.* **1982**, *11*, 565.  
 (44) Takaizumi, K.; Wakabayashi, T. *J. Solution Chem.* **1980**, *9*, 809.

Received for review February 6, 1986. Revised June 19, 1986. Accepted July 23, 1986.

## Volume Properties of Aqueous Electrolytes. 2. Application of the Pitzer Model in Estimating Apparent Molal Compressibility and Expansibility

Anil Kumar

Institute of Physical Chemistry and Electrochemistry, University of Karlsruhe, D 7500 Karlsruhe, Federal Republic of Germany

The Pitzer model of virial coefficients is applied to the apparent molal compressibility and expansibility of aqueous single electrolyte solutions. Pitzer coefficients for several electrolyte solutions are given in the form of temperature-dependent equations. Also, these coefficients are applied for estimating the above properties in aqueous mixed electrolytes. The Pitzer equations can predict these properties with excellent accuracy.

### Introduction

The Pitzer equations are proving to be very useful in estimating various thermodynamic properties of aqueous single and mixed electrolytes (1, 2). In our attempts to understand better their utility in predicting volume properties of electrolytic solutions, we (3) recently successfully fitted the apparent molal volumes of several single electrolytes and presented the Pitzer coefficients. We now apply these equations for estimating apparent molal compressibility  $\phi_K$  and expansibility  $\phi_E$  of single electrolytes. The Pitzer coefficients obtained from the single-electrolyte analysis are used for calculating these properties in mixtures.

### Pitzer Equations

The details of the Pitzer equations are given elsewhere (4). For immediate use, the system of Pitzer equations is given below. Since the equations used for  $\phi_K$  and  $\phi_E$  are analogous, we give them for general property  $\phi$ . Apparent molal property of a single electrolyte  $M_{\nu_M}X_{\nu_X}$  as a function of concentration  $m$  (mol kg<sup>-1</sup>) is

$$\phi = \phi^0 + \nu|Z_M Z_X|(A/2b) \ln(1 + bI^{1/2}) + 2\nu_M \nu_X RT [mB_{MX} + m^2(\nu_M \nu_X)^{1/2} C_{MX}] \quad (1)$$

where

$$B_{MX} = \beta_{MX}^{(0)} + 2\beta_{MX}^{(1)}/\alpha^2 I [1 - (1 + \alpha I^{1/2})e^{-\alpha I^{1/2}}] \quad (2)$$

$$C_{MX} = C_{MX}^\phi/2 \quad (3)$$

Note that for  $\phi_K$ , terms  $\beta_{MX}^{(0)}$  and  $\beta_{MX}^{(1)}$  are  $(\partial^2\beta/\partial P^2)$  and  $(\partial^2\beta/\partial P\partial T)$ , respectively. For  $\phi_E$ , they are  $(\partial^2\beta^{(0)}/\partial P\partial T)$  and  $(\partial^2\beta^{(1)}/\partial P\partial T)$ , respectively. Similarly, in eq 3,  $(\partial^2 C^\phi/\partial P^2)_T$  and  $(\partial^2 C^\phi/\partial P\partial T)$  are for  $\phi_K$  and  $\phi_E$ , respectively. Terms  $\beta_{MX}^{(0)}$ ,  $\beta_{MX}^{(1)}$ , and  $C_{MX}^\phi$  are the Pitzer coefficients.  $A$ , the Pitzer-Debye-Hückel slope, can be taken from elsewhere (5-7).  $\phi^0$ , apparent molal compressibility or expansibility at infinite dilution, is equal to the partial molal compressibility or expansibility at infinite dilution.

Any of the Pitzer coefficients may be fitted with the temperature-dependent equation of the form

$$Y = A + BT + CT^2 \quad (4)$$

where  $A$ ,  $B$ , and  $C$  are the coefficients.

Apparent molal property of an ion in mixture,  $\phi_i$ , is given by

$$\phi_i = \phi_i^0 + (Z_i A/2b) \ln(1 + bI^{1/2}) + RT \sum_j B_{ij} m_j + (RT/2|Z_i|^{1/2}) \sum_j C_{ij} m_j^2 |Z_j|^{1/2} + RT \sum_k \theta_{ik} m_k \quad (5)$$

in eq 5, the last term on the right-hand side expresses the mixing term recognizing explicitly the interactions among like-charged ions.  $\theta_{ik}$  is the difference parameter and can be evaluated from the experimental  $\phi$  and  $\phi$  obtained from eq 5 minus last term. One notes that last term has the sum over  $k$  ions with the same charge ions and over  $i$  with the opposite charge ions. The equation for calculating  $\theta_{ik}$  is

$$\theta_{ik} = \frac{\Delta\phi^*(m_1 + m_2)}{RT m_1 m_2 (\nu_i + \nu_k)} \quad (6)$$

where  $m_1$  and  $m_2$  are molalities of the electrolytes whose cations are under consideration for interactions and  $\nu_i$  and  $\nu_k$  are the moles of  $i$  and  $k$  in their respective electrolytes.

The calculated  $\phi_i$  is converted to  $\phi^*$  by using the relation

$$\phi^* = \frac{\sum_j m_j \phi_j}{\sum_j m_j} \quad (7)$$

where  $\phi_j = \sum_i \nu_i \phi_i$ .

**Table I. Pitzer Coefficients for  $\phi_K$  of Aqueous Single Electrolytes at 25 °C**

electrolytes	$(\partial^2\beta^{(0)})/\partial P^2 \times 10^8$	$(\partial^2\beta^{(0)})/\partial P^2 \times 10^8$	$(\partial^2C^\phi)/\partial P^2 \times 10^9$	$\sigma(\phi_K) \times 10^4, \text{cm}^3 \text{mol}^{-1} \text{bar}^{-1}$
KCl (20) <sup>a</sup>	4.5	1.34	-1.93	0.05
KBr (21)	4.0	0.825	-0.968	0.04
NaBr (20)	8.4	0.930	-0.894	0.08
RbCl (20)	6.1	1.30	-1.79	0.10
CsCl (20)	9.3	1.08	-1.12	0.10
CsBr (20)	4.7	1.45	-2.99	0.09
CsI (20)	2.2	1.19	-4.02	0.05
MnSO <sub>4</sub> (22)	1.1	15.17	-133.7	0.18
CoSO <sub>4</sub> (22)	1.0	17.07	-164.7	0.10
NiSO <sub>4</sub> (22)	0.9	17.82	-181.0	0.10
ZnSO <sub>4</sub> (22)	1.0	16.98	-166.2	0.09
CdSO <sub>4</sub> (22)	0.8	17.19	-194.1	0.09
LaCl <sub>3</sub> (23)	0.8	7.51	-46.36	0.16

<sup>a</sup> Number in parentheses indicates the reference source of data.

### General Equations

Experimental sound velocities  $u$  from the literature can be converted into adiabatic compressibility  $\beta$  as

$$\beta = 1/u^2d \quad (8)$$

$\beta$  is then used to estimate the apparent molal compressibility  $\phi_K$  as

$$\phi_K = \frac{1000(\beta d_0 - \beta_0 d)}{m d d_0} + \frac{\beta M}{d} \quad (9)$$

where  $\beta_0$  and  $d_0$  are the adiabatic compressibility and the density of pure water, taken from elsewhere (8, 9).

Mean apparent molal compressibility of the mixture  $\phi_K^*$  can be calculated from

$$\phi_K^* = \frac{1000(\beta^* d_0 - \beta_0 d^*)}{\sum_j m_j d^* d_0} + \frac{\sum_j \beta_j M_j}{\sum_j m_j d^*} \quad (10)$$

The experimental  $\phi_E$  and  $\phi_E^*$  can be obtained from the slope of  $\phi_V$  or  $\phi_V^*$ , the apparent molal volume of a single or mixed aqueous electrolytes. This is discussed in detail in our earlier work (4).

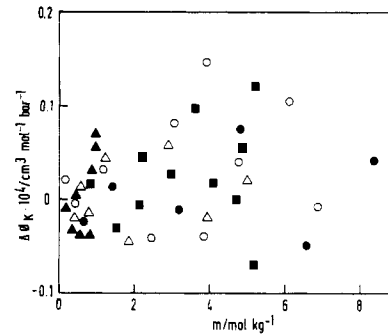
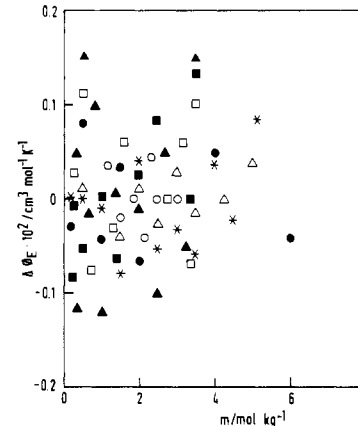
### Results and Discussion

**Single Electrolytes.** We used the literature data on apparent molal compressibility and expansibility of single-electrolyte solutions in order to generate the Pitzer coefficients using eq 1 to 3. Following our earlier work (3) and that of Rogers and

**Table II. Temperature Dependence of Pitzer Coefficients for  $\phi_K$  of Aqueous Single Electrolytes ( $F = (\partial^2\beta^{(0)}/\partial P^2)$ ,  $S = (\partial^2C^\phi/\partial P^2)$ )**

electrolyte, temp range, °C, $m_{max}, \text{mol kg}^{-1}$	term	$10^8 A$	$10^{10} B$	$10^{12} C$	$10^4 \sigma(\phi_K), \text{cm}^3 \text{mol}^{-1} \text{K}^{-1}$
HCl (24), <sup>a</sup> 0-45, 1.0	F	9.29	-3.37	1.22	0.03
	S	-9.91	6.87	-1.29	
NaOH (24), 0-45, 1.0	F	-105.1	754	-13.0	0.03
	S	73.33	-51.1	8.75	
Na <sub>2</sub> SO <sub>4</sub> (25), 0-50, 1.5	F	29.3	-7.77		0.18
	S	-8.39	2.16		
MgSO <sub>4</sub> (25), 0-50, 2.2	F	225.1	-135.1	21.6	0.19
	S	-128.2	82.3	-13.5	
MgCl <sub>2</sub> (25), 0-50, 5.2	F	10.96	3.08		0.09
	S	-1.434	0.410		
NaHCO <sub>3</sub> (26), 0-50, 1.0	F	14.4	-3.15		0.09
	S	73.4	-53.7	9.39	
Na <sub>2</sub> CO <sub>3</sub> (26), 0-50, 1.0	F	230.4	-140.0	22.0	0.18
	S	-113.1	68.9	-10.9	

<sup>a</sup> Number in parentheses indicates the reference source of data.

**Figure 1.**  $\Delta\phi_K$  (experimental  $\phi_K$  - calculated  $\phi_K$ ) against  $m$ . ●, NaBr, 25 °C, ref 20; ○, CsCl, 25 °C, ref 20; △, RbCl, 25 °C, ref 20; ▲, Na<sub>2</sub>CO<sub>3</sub>, 45 °C, ref 26; ■, MgCl<sub>2</sub>, 35 °C, ref 31.**Figure 2.**  $\Delta\phi_E$  (experimental  $\phi_E$  - calculated  $\phi_E$ ) against  $m$ . ●, NaBr, 50 °C, ref 29; ○, HCl, 40 °C, ref 27; △, KCl, 35 °C, ref 11; ▲, PrCl<sub>3</sub>, 75 °C, ref 34; □, NdCl<sub>3</sub>, 25 °C, ref 34; ■, LaCl<sub>3</sub>, 50 °C, ref 34; \*, MgCl<sub>2</sub>, 25 °C, ref 31.

Pitzer (6), we fitted the entire array of the data without  $\beta_{MX}^{(1)}$  term for both the properties with good degree of accuracy. Table I lists the Pitzer coefficients for  $\phi_K$  of the single electrolytes at 25 °C together with the standard deviation ( $\sigma$ ). Similarly, Table II lists the temperature dependence of the Pitzer coefficients as calculated by eq 4 for  $\phi_K$  of those electrolyte solutions for which  $\phi_K$  were known at more than three temperatures. Both the tables include the molality range used in the fits and source of experimental data. Figure 1 shows the difference ( $\Delta$ ) between the experimental and the predicted  $\phi_K$  as a function of molality. The fits were random throughout and the average standard deviation of the is  $0.9 \times 10^{-4} \text{cm}^3 \text{mol}^{-1} \text{bar}^{-1}$  with slightly higher  $\sigma$  for sulfates. Carpio et al. (10) have recently measured the adiabatic compressibilities of aqueous

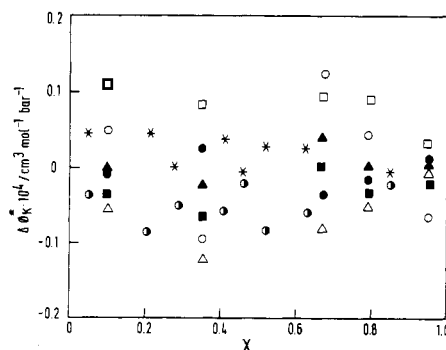
**Table III. Temperature Dependence of Pitzer Coefficients for  $\phi_E$  of Aqueous Single Electrolytes ( $F = (\partial^2\beta^{(0)}/\partial P\partial T)$ ,  $S = (\partial^2C^\phi/\partial P\partial T)$ )**

electrolyte, temp range, °C, $m_{max}$ , mol kg <sup>-1</sup>	term	10 <sup>5</sup> A	10 <sup>5</sup> B	10 <sup>5</sup> C	10 <sup>2</sup> $\partial(\phi_E)$ , cm <sup>3</sup> mol <sup>-1</sup> K <sup>-1</sup>
HCl (24, 27, 28), <sup>a</sup> 0-75, 3.0	F	-4.79	29.49	-0.453	0.01
	S	1.190	-7.34	0.113	
HBr (27), 25-75 3.0	S	0.443	-2.77	0.043	0.02
	F	-1.41	8.69	-0.135	
HI (27), 25-75, 3.0	F	-1.41	8.69	-0.135	0.02
	S	0.9330	-1.99	0.031	
HClO <sub>4</sub> (27), 25-75, 3.0	F	-14.46	89.52	-1.39	0.03
	S	14.06	-90.80	1.47	
NaBr (29), 15-55, 8.0	F	-2.05	12.23	-0.184	0.07
	S	0.151	-0.867	0.012	
NaNO <sub>3</sub> (29), 15-55, 8.0	S	0.151	-0.867	-0.012	0.10
	F	-3.99	24.17	-0.367	
NaOH (24, 30), 0-70, 25.0	S	0.585	-35.59	0.054	0.08
	F	5.23	-10.34	1.35	
Na <sub>2</sub> SO <sub>4</sub> (31), 0-50, 1.5	F	-0.368	3.44	-0.080	0.01
	S	-0.024	0.378	-0.011	
KBr (29), 15-55, 4.0	F	-6.19	38.75	-0.608	0.07
	S	1.76	-11.24	0.18	
KNO <sub>3</sub> (29), 15-55, 4.0	F	-8.12	51.99	-0.835	0.05
	S	3.87	-25.10	0.409	
MgCl <sub>2</sub> (11, 29, 31), 0-55, 5.2	F	-0.144	-0.605	-0.033	0.15
	S	-0.049	0.126		
SrCl <sub>2</sub> (29), 15-55, 2.5	F	-13.7	87.2	-0.014	0.17
	S	3.88	-24.8	0.397	
BaCl <sub>2</sub> (29), 15-55, 1.5	F	-16.1	101.0	-1.59	0.15
	S	8.059	-50.16	0.784	
MgSO <sub>4</sub> (31), 0-508, 2.2	F	-1.51	9.11	-0.141	0.08
	S	-0.481	1.92	-0.001	
Cd(NO <sub>3</sub> ) <sub>2</sub> (29, 32), 15-85, 13.0	F	-6.63	41.4	-0.649	0.08
	S	1.02	-6.36	0.099	
SmCl <sub>3</sub> (33), 0-80, 3.5	F	-2.18	12.8	-0.190	0.15
	S	0.327	-1.95	0.029	
GdCl <sub>3</sub> (33), 0-80, 3.5	F	-2.25	13.9	-0.208	0.19
	S	0.285	-1.66	0.025	
DyCl <sub>3</sub> (33), 0-80, 3.5	F	-2.35	13.7	-0.202	0.15
	S	0.404	-2.39	0.036	
ErCl <sub>3</sub> (33), 0-80, 3.5	F	-2.80	16.5	-0.245	0.17
	S	0.287	-1.68	0.025	
YbCl <sub>3</sub> (33), 0-80, 3.5	F	-2.47	14.4	-0.212	0.15
	S	0.349	-2.05	0.036	
LaCl <sub>3</sub> (34), 15-80, 3.5	F	-1.87	10.8	-0.157	0.15
	S	0.421	-2.52	0.038	
PrCl <sub>3</sub> (34), 0-80, 3.9	F	-2.28	13.3	-0.197	0.19
	S	0.308	-1.84	0.028	
NdCl <sub>3</sub> (34), 0-80, 3.9	F	-2.24	13.5	-0.199	0.15
	S	0.674	-4.06	0.061	

<sup>a</sup> Number in parentheses indicates the reference source of data.

Ca(NO<sub>3</sub>)<sub>2</sub>, ZnCl<sub>2</sub>, and Zn(NO<sub>3</sub>)<sub>2</sub> solutions. On analyzing their data with the Pitzer equations, we obtained large systematic deviations. This may apparently be due to the structural changes occurring in the solutions. The similar behavior was observed by us (3) during the  $\phi_v$  fit. We do not give the Pitzer coefficients for these solutions as they may not have physical significance. The Pitzer coefficients of aqueous CaCl<sub>2</sub> and problems associated with the fit are discussed elsewhere (4).

We list the temperature dependence of the Pitzer coefficients for  $\phi_E$  in Table III along with the standard deviation of the fit. Figure 2 depicts the difference ( $\Delta$ ) between experimental and predicted  $\phi_E$  as a function of molality. The average standard deviation of the fit for  $\phi_E$  is  $0.10 \times 10^{-2}$  cm<sup>3</sup> mol<sup>-1</sup> K<sup>-1</sup>.  $\phi_E$  of aqueous KCl (11) did not vary with temperature (5-45 °C). For KCl, the Pitzer coefficients ( $\partial^2\beta/\partial P\partial T$ ) and ( $\partial^2C^\phi/\partial P\partial T$ ) are  $1.34 \times 10^{-8}$  and  $-1.93 \times 10^{-9}$ , respectively. All the three tables do not include the work on aqueous NaCl as Rogers and Pitzer (6) have discussed them in detail. During the single-electrolyte fitting, first the attempts were made to treat  $\phi^0$  unknown and evaluate it through the least-squares method as other Pitzer coefficients. Since  $\phi^0$  thus obtained was in ex-



**Figure 3.**  $\Delta\phi_{\kappa}^*$  (experimental - calculated) against  $X$  (mole fraction of second component) without and with  $\theta_{ik}$ . NaCl-MgCl<sub>2</sub>: ○ without, ● with, ref 35. Na<sub>2</sub>SO<sub>4</sub>-MgCl<sub>2</sub>: △ without, ▲ with, ref 35. MgSO<sub>4</sub>-MgCl<sub>2</sub>: □ without, ■ with, ref 35. KCl-KBr: ○ without, \* with, ref 36.

**Table IV. Analysis of Mixture Data on Apparent Molal Compressibilities by Pitzer Equation**

system	temp, °C	std dev $\sigma \times 10^4$ , cm <sup>3</sup> mol <sup>-1</sup> bar <sup>-1</sup>	
		without $\theta_{ik}$	with $\theta_{ik}$
NaCl-MgCl <sub>2</sub> (35) <sup>a</sup>	30	0.60	0.19
Na <sub>2</sub> SO <sub>4</sub> -MgCl <sub>2</sub> (35)	30	0.58	0.24
MgSO <sub>4</sub> -MgCl <sub>2</sub> (35)	30	0.64	0.21
KCl-KBr (36)	25	0.25	0.09

<sup>a</sup> Number in parentheses indicates the reference source of data.

**Table V. Values of  $\theta_{ik}$  Used in Mixture Calculations in Eq 5 (Treated Independent of Ionic Strength)**

$\theta_{ik}$	values
Na <sup>+</sup> -Mg <sup>2+</sup>	$-1.33 \times 10^{-9}$
SO <sub>4</sub> <sup>2-</sup> -Cl <sup>-</sup>	$4.32 \times 10^{-9}$
Cl <sup>-</sup> -Br <sup>-</sup>	$1.35 \times 10^{-9}$

cellent agreement with the literature data (given in the original papers of the experimental data), we directly used those values and evaluated the Pitzer coefficients for each electrolyte solution.

**Mixed Electrolytes.** The experimental data on mixtures for compressibility are not too many in the literature. A few data (12-16) are found in Russian literature, but they could not be analyzed due to the want of an easy access and lack of full information on experimental data. We have therefore tested the Pitzer equations only for accurate and accessible data. Equations 5-7 were used to calculate  $\phi_{\kappa}^*$  without and with the mixing parameters  $\theta_{ik}$ . Table IV lists these systems together with the standard deviations of the fit. Also listed are the standard deviations of the fit with the use of  $\theta_{ik}$ . Figure 3 shows the effect of  $\theta_{ik}$  on the fit for  $\phi_{\kappa}^*$  for few systems. As is apparent, the use of  $\theta_{ik}$  brings a remarkable improvement in the fit of  $\phi_{\kappa}^*$  and removes the systematic deviation. Table V lists the values of  $\theta_{ik}$ . The magnitude of ternary interaction term similar to that derived for  $\phi_v$  (17) was very small and hence was neglected. The Pitzer analysis for  $\phi_{\kappa}^*$  of aqueous NaCl-CaCl<sub>2</sub> system from 278.15 to 308.15 K and  $I = 0.3$  to 20 mol kg<sup>-1</sup> is given in our earlier work (4, 18).

We are not aware of any experimental data on  $\phi_E^*$  except those of Kumar and Atkinson (4) and Krumgalz and Millero (19). The Pitzer analysis of Kumar and Atkinson data is given elsewhere (4). We only computed the  $\phi_E^*$  data on aqueous brines, i.e., NaCl-KCl-CaCl<sub>2</sub>-MgCl<sub>2</sub>, using the density of Krumgalz and Millero (19) in the ionic strength range 8.3-9.6 mol kg<sup>-1</sup> and temperature range 20-40 °C. The Pitzer coefficients from Table III, when used in eq 5-7 yield the prediction of  $\phi_E^*$  with a standard deviation of  $0.48 \times 10^{-2}$  cm<sup>3</sup> mol<sup>-1</sup> K<sup>-1</sup>. No mixing parameters were needed for the fit.

In part 1 and this study, we attempted to demonstrate the

utility of the Pitzer model in estimating the volume properties of aqueous single and mixed electrolyte solutions. The Pitzer equations can fit the volume properties of 1-1 electrolytes up to 9.3 *m* (for NaOH 24 *m*), 2-2 electrolytes up to 2.2 *m*, 2-1 electrolytes up to 7.4 *m* and 1-3 electrolytes up to 3.9 *m* with excellent accuracy. The results prove that this model is a powerful tool for predicting these properties. A preliminary study of these results indicates the possibilities of correlations between the structure of electrolyte solutions and the Pitzer coefficients. The discussion on such correlation is beyond the scope of this paper and will be dealt in a separate article. Also, modified sets of Pitzer equations accounting structural changes in electrolyte solutions like ZnCl<sub>2</sub> and Zn(NO<sub>3</sub>)<sub>2</sub> will be presented.

### Acknowledgment

My stay in West Germany is sponsored through a Humboldt scholarship from the Alexander von Humboldt Foundation, Bonn, West Germany.

### Glossary

<i>A</i>	Pitzer-Debye-Hückel slope
<i>b</i>	1.2, (kg/mol) <sup>1/2</sup>
<i>d</i>	density in solution, g cm <sup>-3</sup>
<i>I</i>	ionic strength = $\frac{1}{2} \sum_i m_i Z_i^2$
<i>M</i>	molecular weight of an electrolyte
<i>m</i>	molality, mol kg <sup>-1</sup>
<i>R</i>	gas constant = 83.1441 cm <sup>3</sup> mol <sup>-1</sup> bar <sup>-1</sup> K <sup>-1</sup>
<i>T</i>	temperature in kelvin
<i>u</i>	sound velocity
<i>Z</i>	charge on ion

### Greek Letters

$\beta_{MX}$ , $\beta_{MX}^2$ , $C_{MX}^0$	Pitzer coefficients
$\phi$	apparent molal property at finite concentration
$\nu$	stoichiometric factor in an electrolyte, $\nu = \nu_M + \nu_X$
$\alpha$	2.0, (kg/mol) <sup>1/2</sup>
$\beta$	adiabatic compressibility, bar <sup>-1</sup>

### Superscripts

0	property at infinite dilution
*	mean property in mixture

### Subscripts

E	expansibility
i	ion
J	an electrolyte
K	compressibility

M	cation
X	anion
0	property in pure water

### Literature Cited

- (1) Pitzer, K. S. *J. Phys. Chem.* **1973**, *77*, 268.
- (2) Pitzer, K. S.; Kim, J. *J. Am. Chem. Soc.* **1974**, *96*, 5701.
- (3) Kumar, A. *J. Chem. Eng. Data*, preceding paper in this issue.
- (4) Kumar, A.; Atkinson, G. *J. Phys. Chem.* **1983**, *87*, 5504.
- (5) Bradley, D. J.; Pitzer, K. S. *J. Phys. Chem.* **1979**, *83*, 1599.
- (6) Rogers, P. S. Z.; Pitzer, K. S. *J. Phys. Chem. Ref. Data* **1982**, *11*, 15.
- (7) Ananthaswamy, J.; Atkinson, G. *J. Chem. Eng. Data* **1984**, *29*, 81.
- (8) Del Grosso, V. A.; Mader, C. W. *J. Acoust. Soc. Am.* **1972**, *52*, 961.
- (9) Haar, L.; Gallagher, J. S.; Kell, G. S. *NBS/NRC Steam Tables*; Hemisphere: New York, 1984.
- (10) Carpio, R.; Mehicic, M.; Borsay, F.; Petrovic, C.; Yeager, E. *J. Phys. Chem.* **1982**, *86*, 4980.
- (11) Romankiw, L.; Chou-Ming, I. *J. Chem. Data* **1983**, *28*, 300.
- (12) Kanatova, R. F.; Kudryavtsev, B. B. *Primen. Ul'traakust. Issled. Veshchestva* **1960**, *11*, 181.
- (13) Chimitdorzhiev, D. B. *Uch. Zap.—Buryat. Gos. Pedagog. Inst.* **1967**, *28*, 79.
- (14) Devdariani, A. K.; Kolobov, N. P.; Marenina, K. N. *Russ. J. Phys. Chem. (Engl. Transl.)* **1973**, *47*, 653.
- (15) Kuznetsov, V. V.; Trostin, V. N.; Khrenova, L. A. *Izv. Vyssh. Uchebn. Zaved. Khim. Khim. Tekhnol.* **1983**, *26*, 1505.
- (16) Janenas, V.; Abrosimov, V. K. *Izv. Vyssh. Uchebn. Zaved. Khim. Khim. Tekhnol.* **1983**, *26*, 698.
- (17) Kumar, A. *J. Am. Eng. Data* **1986**, *31*, 19.
- (18) Kumar, A.; Atkinson, G.; Howell, R. D. *J. Solution Chem.* **1982**, *11*, 857.
- (19) Krumgalz, B. S.; Millero, F. J. *Mar. Chem.* **1982**, *11*, 477.
- (20) Gucker, F. T.; Stubble, D.; Hill, D. J. *J. Chem. Thermodyn.* **1975**, *7*, 865.
- (21) Weissler, A. *J. Acoust. Soc. Am.* **1951**, *23*, 219.
- (22) Lo Surdo, A.; Millero, F. J. *J. Solution Chem.* **1980**, *9*, 163.
- (23) Chen, C.-T.; Millero, F. J. *J. Solution Chem.* **1977**, *6*, 589.
- (24) Hershey, J. P.; Damesceno, R.; Millero, F. J. *J. Solution Chem.* **1984**, *13*, 825.
- (25) Millero, F. J.; Ricco, J.; Schreiber, D. R. *J. Solution Chem.* **1982**, *11*, 671.
- (26) Hershey, J. P.; Satolongo, S.; Millero, F. J. *J. Solution Chem.* **1983**, *12*, 233.
- (27) Harrington, T. M.; Pathybridge, A. D.; Roffey, M. G. *J. Chem. Eng. Data* **1985**, *30*, 264.
- (28) Akerlöf, G.; Kegeles, G. *J. Am. Chem. Soc.* **1938**, *60*, 1226.
- (29) Isono, T. *J. Chem. Eng. Data* **1984**, *29*, 45.
- (30) Akerlöf, G.; Kegeles, G. *J. Am. Chem. Soc.* **1939**, *61*, 1027.
- (31) Lo Surdo, A.; Alzola, M.; Millero, F. J. *J. Chem. Thermodyn.* **1982**, *14*, 649.
- (32) Söhnel, O.; Novotny, P.; Solc, Z. *J. Chem. Eng. Data* **1984**, *29*, 379.
- (33) Habenschuss, A.; Spedding, F. H. *J. Chem. Eng. Data* **1976**, *21*, 95.
- (34) Gildseth, W. M.; Habenschuss, A.; Spedding, F. H. *J. Chem. Eng. Data* **1975**, *20*, 292.
- (35) Shikheeva, L. V.; Savina, L. I. *Russ. J. Phys. Chem. (Engl. Transl.)* **1982**, *56*, 1356.
- (36) Vilcu, R.; Simion, A. *Rev. Roum. Chem.* **1976**, *21*, 3.

Received for review February 28, 1986. Revised July 7, 1986. Accepted August 18, 1986.