# Thermodynamic Properties of the Ternary Mixture Acetone + Methanol + Ethanol at 298.15 K 

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#### Abstract

Speeds of sound, densities, and refractive indices of the ternary mixture acetone + methanol + ethanol have been measured at 298.15 K and atmospheric pressure. The excess molar volumes, changes of refractive indices, and isentropic compressibilities were determined from the experimental data. Several methods for predicting multicomponent derived properties from binary data were tested. The PengRobinson and Soave-Redlich-Kwong equations of state were also applied, with three different mixing rules, to calculate binary interaction parameters and predict ternary excess volumes, satisfactory results being obtained for this mixture.


## 1. Introduction

This paper continues our study of various homogeneous and heterogeneous azeotropic mixtures (I glesias et al., 1996a, 1997, 1998; Orge et al., 1997). The aim of this research is the measurement of physical properties and study of liquid equilibrium of multicomponent mixtures, as well as the application of several predictive models to obtain theoretical predictions. The objective of the application of these techniques is identification of separation agents for binary azeotropic or binary mixtures with close boiling points in modified rectification processes.

This paper reports the measured densities, refractive indices and speeds of sound as well as excess and derived properties of the ternary mixture acetone + methanol + ethanol at 298.15 K and atmospheric pressure. The experimental data were fitted by means of the Cibulka (1982) equation.

The measured values have been al so used to test several empirical predictive methods (Piñeiro et al., 1998), used to estimate multicomponent properties from the corresponding magnitude of the binary mixtures involved.

The equations of state of Peng-Robinson (Peng and Robinson, 1976) and Soave-Redlich-K wong (Soave, 1972) were applied with several combination rules to calculate binary interaction parameters between the chemicals present in the mixture. After that, these parameters were applied for estimating the ternary excess molar volumes, no other multicomponent parameter being necessary. The results obtained agreed very close with the experimentaly determined volumetric data.

## 2. Experimental Section

The chemicals used for the preparation of the mixtures were Lichrosolv Quality and supplied by Merck. Before use, they were degassed by ultrasound technique, dried over molecular sieves type 3A (Aldrich catalog no. 208582 ), and kept in inert argon ( $\mathrm{N}-55$, less than 3 ppm in water)

[^0]Table 1. Comparison of Measured Pure Component Properties Data with Literature Values at 298.15 K

| component | $\rho /\left(\mathrm{g} \cdot \mathrm{cm}^{-3}\right)$ |  | $\mathrm{n}_{\mathrm{D}}$ |  | $\mathrm{u} /\left(\mathrm{m} \cdot \mathrm{s}^{-1}\right)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | exptl | lit. | exptl | lit. ${ }^{\text {b }}$ | exptl | lit. |
| acetone | 0.7844 | 0.784 29a | 1.35580 | 1.35596 | 1161 | 1160.6c |
| methanol | 0.7866 | $0.78664^{\text {b }}$ | 1.32645 | 1.32652 | 1102 | 1102.0 ${ }^{\text {d }}$ |
| ethanol | 0.7850 | $0.78509{ }^{\text {b }}$ | 1.35922 | 1.35941 | 1142 | 1142.4 ${ }^{\text {c }}$ |

${ }^{\text {a }}$ Hnedkovsky and Cibulka (1993). ${ }^{\text {b }}$ TRC Thermodynamic Tables (1994). c Papal oannou Panayiotou (1991). d Arce et al. (1996).
atmosphere. The purity of the chemicals was checked using gas chromatography, obtaining purities better than 99.8 mass \%. The values measured of density, refractive index, and speed of sound for the pure chemicals were compared with those found in open literature, and the results are listed in Table 1. The mixtures were prepared by weight using a Mettler AE-240 balance, with an accuracy of $\pm 10^{-4}$. Densities and speeds of sound of the mixtures were determined by means of an Anton Paar DSA-48 density and sound analyzer, with an accuracy of $\pm 5 \times 10^{-5} \mathrm{~g} \cdot \mathrm{~cm}^{-3}$ for densities and $\pm 1 \mathrm{~m} \times \mathrm{s}^{-1}$ for speeds of sound. Refractive indices were measured using an ABBEMAT-HP Dr. Kernchen automatic refractometer, the accuracy being $\pm 2 \times 10^{-5}$. The refractometer was thermostatyzed with a PolyScience controller bath model 9010, whose temperature stability was $\pm 10^{-2} \mathrm{~K}$. The mole fractions were determined with an accuracy of $\pm 10^{-4}$. The accuracy obtained when measuring excess molar volumes, changes of refractive indices, and isentropic compressibilities were $\pm 5 \times 10^{-3} \mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1}, \pm 10^{-4}$, and $\pm 1 \mathrm{TPa}^{-1}$, respectively. Further details of the experimental procedures used and the mode of operation in our laboratory have already been published (I glesias et al., 1996b).

## 3. Results and Discussion

The values corresponding to densities, refractive indices, speeds of sound, and isentropic compressibilities (cal culated by means of the Laplace equation $\kappa_{\mathrm{S}}=\rho^{-1} \cdot \mathrm{u}^{-2}$ ), are given in Table2. The excess molar volumes, changes of refractive indices on mixing, and changes of isentropic compressibili-


Figure 1. Curves of constant (a), excess molar volumes, (b) changes of refractive indices on mixing, and (c) changes of isentropic compressibilities for acetone (1) + methanol (2) + ethanol (3) at 298.15 K .
ties were calculated using the following expressions

$$
\begin{gather*}
\mathrm{V}^{\mathrm{E}}=\sum_{\mathrm{i}=1}^{\mathrm{N}} \mathrm{x}_{\mathrm{i}} \mathrm{M}_{\mathrm{i}}\left(\rho^{-1}-\rho_{\mathrm{i}}^{-1}\right)  \tag{1}\\
\delta \mathrm{n}_{\mathrm{D}}=\mathrm{n}_{\mathrm{D}}-\sum_{\mathrm{i}=1}^{\mathrm{N}} \mathrm{x}_{\mathrm{i}} \mathrm{n}_{\mathrm{Di}}  \tag{2}\\
\delta \kappa_{\mathrm{S}}=\kappa_{\mathrm{S}}-\sum_{\mathrm{i}=1}^{\mathrm{N}} \mathrm{x}_{\mathrm{i}} \kappa_{\mathrm{Si}} \tag{3}
\end{gather*}
$$



Figure 2. Curves of (a) $\delta \mathrm{V}_{123}^{\mathrm{E}}=\mathrm{V}^{\mathrm{E}}-\mathrm{V}_{12}^{\mathrm{E}}-\mathrm{V}_{13}^{\mathrm{E}}-\mathrm{V}_{23}^{\mathrm{E}}$, (b) $\delta\left(\delta \mathrm{n}_{\mathrm{D}, 123}\right)=\delta \mathrm{n}_{\mathrm{D}}-\delta \mathrm{n}_{\mathrm{D}, 12}-\delta \mathrm{n}_{\mathrm{D}, 13}-\delta \mathrm{n}_{\mathrm{D}, 23}$, and (c) $\delta(\delta \kappa \mathrm{s}, 123)=\delta \kappa \mathrm{s}$ $-\delta \kappa \mathrm{s}, 12-\delta \kappa \mathrm{s}, 13-\delta \kappa \mathrm{s}, 23$ at 298.15 K for acetone (1) + methanol (2) + ethanol (3).
where $\rho, \mathrm{n}_{\mathrm{D}}$, and $\mathrm{k}_{\mathrm{S}}$ stand for the density, refractive index, and isentropic compressibility of the mixture, and $\rho_{\mathrm{i}}, \mathrm{n}_{\mathrm{Di}}$, and $\mathrm{k}_{\mathrm{si}}$ are the corresponding properties of pure components. N represents the number of components in the mixture. The excess and derived values are also presented in Table 2. These magnitudes were correlated using the Cibulka equation
$\delta \mathbf{Q}_{123}=\delta \mathbf{Q}_{12}+\delta \mathbf{Q}_{13}+\delta \mathbf{Q}_{23}+\mathbf{x}_{1} \cdot \mathbf{x}_{2} \cdot \mathbf{x}_{3} \cdot\left(\mathrm{~B}_{0}+\mathrm{B}_{1} \cdot \mathbf{x}_{1}+\right.$
$\left.\mathbf{B}_{2} \cdot \mathbf{x}_{2}\right)$
where $\delta \mathrm{Q}_{12}, \delta \mathrm{Q}_{13}$, and $\delta \mathrm{Q}_{23}$ represent the binary contribu-

Table 2. Densities, Refractive Indices, Speeds of Sound, Isentropic Compressibilities, Excess Molar Volumes, Changes of Refractive Indices on Mixing, and Changes of Isentropic Compressibilities on Mixing, for Acetone (1) + Methanol (2) + Ethanol (3) at 298.15 K

| $\mathrm{x}_{1}$ | $\mathrm{X}_{2}$ | $\rho /\left(\mathrm{g} \cdot \mathrm{cm}^{-3}\right)$ | $\mathrm{n}_{\mathrm{D}}$ | $\mathrm{u} /\left(\mathrm{m} \cdot \mathrm{s}^{-1}\right)$ | $\kappa_{\mathrm{S}} /\left(\mathrm{TPa}^{-1}\right)$ | V / $/\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right.$ ) | $\delta \mathrm{n}_{\mathrm{D}}$ | $\delta \kappa_{\mathrm{S}} /\left(\mathrm{TPa}^{-1}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0312 | 0.0854 | 0.7856 | 1.35724 | 1143 | 975 | -0.039 | 0.0009 | 6 |
| 0.0319 | 0.2371 | 0.7859 | 1.35359 | 1138 | 982 | -0.045 | 0.0022 | -10 |
| 0.0228 | 0.3871 | 0.7859 | 1.34939 | 1133 | 992 | -0.029 | 0.0029 | -11 |
| 0.0241 | 0.5152 | 0.7861 | 1.34522 | 1128 | 1000 | -0.028 | 0.0030 | -11 |
| 0.0230 | 0.6371 | 0.7864 | 1.34141 | 1123 | 1008 | -0.033 | 0.0031 | -12 |
| 0.0220 | 0.7477 | 0.7865 | 1.33745 | 1118 | 1018 | -0.026 | 0.0028 | -10 |
| 0.0230 | 0.8520 | 0.7868 | 1.33341 | 1113 | 1026 | -0.031 | 0.0022 | -9 |
| 0.0211 | 0.9460 | 0.7870 | 1.32930 | 1108 | 1035 | -0.030 | 0.0012 | -7 |
| 0.0906 | 0.0845 | 0.7858 | 1.35730 | 1145 | 970 | -0.058 | 0.0012 | -9 |
| 0.1069 | 0.2373 | 0.7863 | 1.35366 | 1142 | 975 | -0.079 | 0.0026 | -14 |
| 0.0984 | 0.3848 | 0.7867 | 1.34981 | 1138 | 982 | -0.089 | 0.0035 | -18 |
| 0.0941 | 0.5162 | 0.7870 | 1.34597 | 1133 | 990 | -0.092 | 0.0040 | -19 |
| 0.0898 | 0.6389 | 0.7874 | 1.34194 | 1128 | 997 | -0.100 | 0.0040 | -21 |
| 0.0854 | 0.7523 | 0.7878 | 1.33808 | 1124 | 1005 | -0.108 | 0.0038 | -21 |
| 0.0820 | 0.8514 | 0.7881 | 1.33429 | 1119 | 1013 | -0.110 | 0.0033 | -21 |
| 0.1711 | 0.0854 | 0.7860 | 1.35718 | 1148 | 965 | -0.079 | 0.0013 | -11 |
| 0.1644 | 0.2400 | 0.7867 | 1.35367 | 1145 | 970 | -0.112 | 0.0029 | -17 |
| 0.1482 | 0.3971 | 0.7871 | 1.34966 | 1140 | 978 | -0.119 | 0.0040 | -21 |
| 0.1464 | 0.5270 | 0.7876 | 1.34590 | 1136 | 984 | -0.135 | 0.0045 | -25 |
| 0.1401 | 0.6533 | 0.7882 | 1.34185 | 1131 | 991 | -0.153 | 0.0045 | -27 |
| 0.1323 | 0.7674 | 0.7886 | 1.33801 | 1127 | 998 | -0.158 | 0.0044 | -27 |
| 0.1449 | 0.8115 | 0.7891 | 1.33641 | 1126 | 999 | -0.182 | 0.0043 | -30 |
| 0.2132 | 0.3978 | 0.7875 | 1.34962 | 1143 | 973 | -0.153 | 0.0042 | -25 |
| 0.2042 | 0.5315 | 0.7882 | 1.34615 | 1139 | 978 | -0.180 | 0.0050 | -29 |
| 0.1942 | 0.6647 | 0.7889 | 1.34210 | 1135 | 985 | -0.202 | 0.0053 | -32 |
| 0.1845 | 0.7785 | 0.7895 | 1.33830 | 1131 | 991 | -0.217 | 0.0052 | -34 |
| 0.3119 | 0.0901 | 0.7862 | 1.35690 | 1151 | 960 | -0.105 | 0.0017 | -13 |
| 0.2905 | 0.2523 | 0.7871 | 1.35343 | 1148 | 964 | -0.152 | 0.0035 | -21 |
| 0.2792 | 0.4062 | 0.7880 | 1.34988 | 1145 | 968 | -0.194 | 0.0049 | -28 |
| 0.2673 | 0.5429 | 0.7888 | 1.34611 | 1142 | 972 | -0.226 | 0.0056 | -34 |
| 0.2552 | 0.6686 | 0.7895 | 1.34242 | 1138 | 978 | -0.248 | 0.0060 | -38 |
| 0.3272 | 0.6397 | 0.7900 | 1.34369 | 1143 | 969 | -0.296 | 0.0066 | -42 |
| 0.3386 | 0.5058 | 0.7889 | 1.34733 | 1145 | 966 | -0.248 | 0.0058 | -35 |
| 0.3631 | 0.3501 | 0.7879 | 1.35102 | 1149 | 962 | -0.205 | 0.0045 | -28 |
| 0.3916 | 0.0867 | 0.7862 | 1.35671 | 1152 | 958 | -0.111 | 0.0017 | -13 |
| 0.3716 | 0.2552 | 0.7873 | 1.35322 | 1150 | 960 | -0.175 | 0.0036 | -22 |
| 0.4710 | 0.0827 | 0.7861 | 1.35655 | 1154 | 955 | -0.110 | 0.0016 | -12 |
| 0.4388 | 0.2663 | 0.7874 | 1.35306 | 1152 | 957 | -0.188 | 0.0041 | -24 |
| 0.4245 | 0.4137 | 0.7886 | 1.34967 | 1150 | 959 | -0.253 | 0.0055 | -33 |
| 0.4048 | 0.5592 | 0.7898 | 1.34590 | 1147 | 962 | -0.310 | 0.0064 | -41 |
| 0.5489 | 0.0827 | 0.7860 | 1.35637 | 1156 | 953 | -0.108 | 0.0017 | -12 |
| 0.5218 | 0.2612 | 0.7875 | 1.35290 | 1154 | 953 | -0.205 | 0.0040 | -26 |
| 0.4881 | 0.4216 | 0.7889 | 1.34967 | 1152 | 955 | -0.282 | 0.0059 | -36 |
| 0.6283 | 0.0983 | 0.7860 | 1.35577 | 1157 | 950 | -0.112 | 0.0019 | -14 |
| 0.5919 | 0.2662 | 0.7876 | 1.35270 | 1156 | 950 | -0.219 | 0.0042 | -27 |
| 0.5764 | 0.3701 | 0.7886 | 1.35059 | 1155 | 950 | -0.280 | 0.0055 | -35 |
| 0.7089 | 0.0956 | 0.7859 | 1.35570 | 1159 | 947 | -0.110 | 0.0020 | -14 |
| 0.6795 | 0.2756 | 0.7877 | 1.35250 | 1159 | 945 | -0.235 | 0.0046 | -30 |
| 0.8035 | 0.0864 | 0.7856 | 1.35545 | 1161 | 945 | -0.091 | 0.0018 | -13 |
| 0.1113 | 0.0548 | 0.7858 | 1.35798 | 1147 | 968 | -0.062 | 0.0009 | -9 |
| 0.2422 | 0.0630 | 0.7860 | 1.35758 | 1150 | 962 | -0.086 | 0.0013 | -11 |
| 0.0334 | 0.1480 | 0.7856 | 1.35572 | 1141 | 978 | -0.033 | 0.0015 | -7 |
| 0.1337 | 0.1378 | 0.7861 | 1.35601 | 1146 | 969 | -0.078 | 0.0018 | -13 |
| 0.2651 | 0.1642 | 0.7865 | 1.35538 | 1149 | 963 | -0.115 | 0.0024 | -16 |
| 0.4071 | 0.1716 | 0.7867 | 1.35497 | 1152 | 958 | -0.142 | 0.0028 | -18 |
| 0.4840 | 0.1805 | 0.7868 | 1.35464 | 1154 | 955 | -0.156 | 0.0030 | -19 |
| 0.6456 | 0.1811 | 0.7868 | 1.35426 | 1158 | 948 | -0.171 | 0.0032 | -21 |
| 0.0335 | 0.2335 | 0.7857 | 1.35350 | 1138 | 982 | -0.032 | 0.0020 | -9 |
| 0.0337 | 0.3093 | 0.7858 | 1.35152 | 1136 | 986 | -0.031 | 0.0025 | -10 |
| 0.1362 | 0.2948 | 0.7866 | 1.35222 | 1142 | 975 | -0.096 | 0.0031 | -17 |
| 0.2612 | 0.3285 | 0.7874 | 1.35155 | 1146 | 967 | -0.161 | 0.0040 | -24 |
| 0.4706 | 0.3532 | 0.7882 | 1.35105 | 1152 | 956 | -0.239 | 0.0050 | -31 |

tion fitted with the Redlich-Kister expression for every binary mixture. The parameters of binary contributions were gathered in a previous work (Iglesias et al., 1997). $\mathrm{B}_{\mathrm{i}}, \mathrm{i}=0,1,2$, are the ternary fitting parameters that have been calculated applying the nonlinear algorithm due to Marquardt (Marquardt, 1963), and they are displayed in Table 3, as well as the root-mean-square deviations calculated according to the expression

$$
\begin{equation*}
\sigma=\left(\sum_{i}^{\mathrm{n}_{\mathrm{DAT}}} \frac{\left(\mathrm{z}_{\exp }-\mathrm{z}_{\mathrm{cal}}\right)^{2}}{\mathrm{n}_{\mathrm{DAT}}}\right)^{1 / 2} \tag{5}
\end{equation*}
$$

where $\mathrm{z}_{\mathrm{exp}}$ is the experimental value, $\mathrm{z}_{\text {cal }}$ is the calculated

Table 3. Parameters $B_{i}$ of the Cibulka Equation and Root-Mean-Square Deviations $\sigma$

|  | Acetone (1) + Methanol (2) + Ethanol (3) |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{VE}_{\mathrm{E}}\left(\mathrm{cm}^{3 .}\right.$ | $\mathrm{B}_{0}=-1.1325$ | $\mathrm{~B}_{1}=1.6475$ | $\mathrm{~B}_{2}=1.6184$ | $\sigma=0.0076$ |
| $\left.\mathrm{~mol}^{-1}\right)$ |  |  |  |  |
| $\delta \mathrm{n}_{\mathrm{D}}$ | $\mathrm{B}_{0}=0.0027$ | $\mathrm{~B}_{1}=-0.0137$ | $\mathrm{~B}_{2}=-0.0022$ | $\sigma=0.0001$ |
| $\delta \kappa_{\mathrm{S}} /\left(\mathrm{TPa}^{-1}\right)$ | $\mathrm{B}_{0}=-167.5$ | $\mathrm{~B}_{1}=398.1$ | $\mathrm{~B}_{2}=46.9$ | $\sigma=0.4$ |

value, and $n_{\text {DAT }}$ is the number of experimental data points. Parts a, b, and c of Figure 1 show, respectively, the computed isol ines corresponding to ternary derived properties. Figure la shows a contractive trend through the whole composition range, where a minimum value is reached in approximately equimolar binary composition of

Table 4. Root-Mean-Square Deviations of the Experimental Results from the Predicted Results for Different Empirical Equations

|  | $\sigma\left(\mathrm{V}^{\mathrm{E}} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)\right)$ | $\sigma\left(\delta \mathrm{n}_{\mathrm{D}}\right)$ | $\sigma\left(\delta \kappa_{\mathrm{s}} /\left(\mathrm{TPa}^{-1}\right)\right)$ |
| :---: | :---: | :---: | :---: |
| K ohler | 0.005 | 0.0001 | 1 |
| J acob-Fitzner | 0.005 | 0.0001 | 1 |
| Colinet | 0.005 | 0.0001 | 1 |
| K nobeloch | 0.037 | 0.0008 | 5 |
| Tsao-Smitha | 0.012 | 0.0006 | 3 |
| Tsao-Smith ${ }^{\text {b }}$ | 0.010 | 0.0001 | 1 |
| Tsao-Smith ${ }^{\text {c }}$ | 0.041 | 0.0010 | 6 |
| Scatchard ${ }^{\text {a }}$ | 0.011 | 0.0002 | 2 |
| Scatchard ${ }^{\text {b }}$ | 0.007 | 0.0001 | 2 |
| Scatchard ${ }^{\text {c }}$ | 0.009 | 0.0001 | 1 |
| Toopa | 0.011 | 0.0002 | 2 |
| Toop ${ }^{\text {b }}$ | 0.007 | 0.0001 | 1 |
| Toop ${ }^{\text {c }}$ | 0.008 | 0.0001 | 1 |
| Mathieson-Tynne ${ }^{\text {a }}$ | 0.248 | 0.0030 | 31 |
| Mathieson-Tynne ${ }^{\text {b }}$ | 0.147 | 0.0048 | 23 |
| Mathieson-Tynne ${ }^{\text {c }}$ | 0.013 | 0.0015 | 10 |
| Hillerta | 0.014 | 0.0015 | 5 |
| Hillert ${ }^{\text {b }}$ | 0.031 | 0.0001 | 3 |
| Hillertc | 0.139 | 0.0028 | 19 |

${ }^{\text {a }}$ Ethanol is the asymmetric component in the equation. ${ }^{\mathrm{b}}$ Methanol is the asymmetric component in the equation. ${ }^{\text {c Acetone is }}$ the asymmetric component in the equation.
acetone + methanol owing to the hydrogen bonds between methanol and acetone molecules. In decreasing ethanol composition mixtures, lower values of excess molar volumes and an increasing trend toward pure methanol or acetone could be observed. The changes of refractive indices on mixing show positive values (Figure 1b), in agreement with this trend shown, a maximum appearing. The changes of isentropic compressibilities show a similar trend to excess molar volumes (Figure 1c).

The empirical predictive methods for derived properties of K ohler, J acob and Fitzner, Colinet, K nobel och, Tsao and Smith, Scatchard, Toop, Mathieson-Tynne, and Hillert (Piñeiro et al., 1998) calculate multicomponent properties by means of different additive binary contributions. Table 4 shows root-mean-square deviations computed using eq 5. The derived properties of multicomponent mixtures may be estimated using the corresponding binary data as follows

$$
\begin{equation*}
\delta \mathrm{Q}_{\mathrm{ij}}=\sum_{\mathrm{i}<\mathrm{j}}\left(\mathrm{x}_{\mathrm{i}} \mathrm{x}_{\mathrm{j}} / \mathrm{x}_{\mathrm{i}}^{\prime} \mathrm{X}_{\mathrm{j}}^{\prime}\right) \delta \mathrm{Q}_{\mathrm{ij}}\left(\mathrm{x}_{\mathrm{i}}^{\prime}, \mathrm{x}_{\mathrm{j}}^{\prime}\right) \tag{6}
\end{equation*}
$$

In this case, for each ternary mixture the mole fractions $x^{\prime}$ may be obtained in a triangular Gibbs diagram, projecting the considered ternary composition point on the binary axis. The possible combinations of symmetric and asymmetric geometric choice yield the expressions of the referred
methods. Asymmetry can be regarded as the different individual contribution of one of the binary mixtures involved, caused by a polar or strong associative behavior in the multicomponent mixture. In Table 4 the deviations show that symmetric equations, except for K nobeloch, provide the best predictions for the set of magnitudes taken into consideration for this mixture. Low deviations are obtained by these methods owing to the scarce ternary contribution to derived magnitudes (Figure 2).
In what is referred to the equations of state, the facts of its high simplicity, low data requirements, and wide versatility in estimating different physical properties of both pure substances and multicomponent mixtures has attracted the general interest. The accuracy of the results obtained depend to a great extent on the combination of equations and mixing rules. A considerable number of equations of state are currently available, and most of them are adequate to obtain acceptable results, combined with simple rules, if some binary parameters are calculated from experimental data from the enclosed binary mixtures in the multicomponent system. In this case, the Soave-Redlich-K wong (SRK) and the Peng-Robinson (PR), equations were selected and applied with combining rules where the $a$ and $b$ factors in the mixture are dependent on one or two fitting parameters. These equations can be expressed by the general equation

$$
\begin{equation*}
\mathrm{P}=\frac{\mathrm{RT}}{\mathrm{~V}-\mathrm{b}}-\frac{\mathrm{a}}{\left(\mathrm{~V}+\delta_{1} \mathrm{~b}\right)\left(\mathrm{V}+\delta_{2} \mathrm{~b}\right)} \tag{7}
\end{equation*}
$$

where $\delta_{1}$ and $\delta_{2}$ are parameters with the following values: $\delta_{1}=1, \delta_{2}=0$ for SRK and $\delta_{1}=1+\sqrt{ } 2, \delta_{2}=1-\sqrt{ } 2$ for PR equations. For a binary mixture at constant $P$ and $T$, the excess molar volume can be expressed according to

$$
\begin{equation*}
\mathrm{V}^{\mathrm{E}}=\Delta \mathrm{V}=\mathrm{V}_{\mathrm{m}}-\sum_{\mathrm{i}=1}^{\mathrm{n}} \mathrm{x}_{\mathrm{i}} \mathrm{~V}_{\mathrm{i}}=\sum_{\mathrm{i}=1}^{\mathrm{n}} \mathrm{x}_{\mathrm{i}}\left(\overline{\mathrm{~V}}_{\mathrm{i}}-\mathrm{V}_{\mathrm{i}}\right) \tag{8}
\end{equation*}
$$

where $\overline{\mathrm{V}}_{\mathrm{i}}$ is the partial molar volume defined by

$$
\begin{equation*}
\bar{V}_{i}=-\left(\frac{\partial P}{\partial n_{i}}\right)_{T, V, n}\left(\frac{\partial P}{\partial V_{m}}\right)^{-1}{ }_{T, n} \tag{9}
\end{equation*}
$$

and can be calculated from the selected equation of state, attending to the i component and mixture molar volume dependence.
Three different combining rules were tested with these equations, showing different dependences of $a$ and $b$

Table 5. Computed Binary Interaction Parameters by the Applied Mixing Rules on the Equations of State SRK and PR, and Root-Mean-Square Deviations of the Ternary Prediction Results

| mixture | Soave-Redlich-K wong |  |  | Peng-Robinson |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | R1 | R2 | R3 | R1 | R2 | R3 |
| acetone + methanol | $\begin{aligned} & 4.938 \times 10^{-2} \\ & (0.02) \end{aligned}$ | $1.753 \times 10^{-2}$ | 1.917 | $-5.764 \times 10^{-2}$ | $2.610 \times 10^{-2}$ | 1.934 |
|  |  | $-2.258 \times 10^{-2}$ | $-6.373 \times 10^{-3}$ | (0.02) | $-1.969 \times 10^{-2}$ | $-6.351 \times 10^{-3}$ |
|  |  | (0.009) | $-2.258 \times 10^{-2}$ |  | (0.009) | $-1.970 \times 10^{-2}$ |
|  |  |  | (0.01) |  |  | (0.009) |
| acetone + ethanol | $\begin{aligned} & 1.758 \times 10^{-2} \\ & (0.01) \end{aligned}$ | $3.224 \times 10^{-2}$ | $2.571 \times 10^{-2}$ | $1.436 \times 10^{-2}$ | $3.827 \times 10^{-2}$ | $2.327 \times 10^{-2}$ |
|  |  | $-7.221 \times 10^{-3}$ | $2.187 \times 10^{-5}$ | (0.01) | $-5.578 \times 10^{-3}$ | $5.032 \times 10^{-5}$ |
|  |  | (0.006) | $-7.221 \times 10^{-3}$ |  | (0.007) | $-5.578 \times 10^{-3}$ |
|  |  |  | (0.007) |  |  | (0.007) |
| methanol + ethanol | $\underset{(0.007)}{-1.013} \times 10^{-2}$ | $5.317 \times 10^{-2}$ | $1.776 \times 10^{-1}$ |  |  |  |
|  |  | $2.693 \times 10^{-3}$ | $-4.174 \times 10^{-4}$ | $-1.065 \times 10^{-2}$ | $6.145 \times 10^{-2}$ | $1.182 \times 10^{-1}$ |
|  |  | (0.004) | $2.693 \times 10^{-3}$ | (0.007) | $3.922 \times 10^{-3}$ | $-1.904 \times 10^{-4}$ |
|  |  |  | (0.004) |  | (0.004) | $3.922 \times 10^{-3}$ |
|  |  |  |  |  |  | (0.004) |
| acetone + methanol + ethanol | (0.01) | (0.007) | (0.007) | (0.01) | (0.007) | (0.007) |

parameters. A general equations could be expresed as

$$
\begin{gather*}
a=\sum_{i=1}^{n} \sum_{j=1}^{n} x_{i} x_{j}\left(1-k_{i j}-l_{i j} T\right)\left(a_{i} a_{j}\right)^{1 / 2}  \tag{10}\\
b=\sum_{i=1}^{n} \sum_{j=1}^{n} x_{i} x_{j}\left(1-m_{i j}\right)\left(b_{i} b_{j}\right)^{1 / 2} \tag{11}
\end{gather*}
$$

where for mixing rule $R 1 I_{i j}=m_{i j}=0$, for mixing rule R 2 $\mathrm{I}_{\mathrm{ij}}=0$, and for mixing rule $R 3 \mathrm{k}_{\mathrm{ij}}, \mathrm{I}_{\mathrm{ij}}, \mathrm{m}_{\mathrm{ij}} \neq 0$ these parameters being a constant value over the whole composition range for every binary mixture. The Marquardt algorithm was applied to calculate the parameters $\mathrm{K}_{\mathrm{ij}}, \mathrm{I}_{\mathrm{ij}}$, and $m_{i j}$ in the cases mentioned above, using the experimentaly measured binary excess volumes, in combination with a Newton-Raphson method to solve the equation of state. Once these binary parameters were computed, the ternary excess values were predicted and compared with the experimental results. The parameters are given in Table 5, together with the root-mean-square deviations from the experimental data. The results displayed show that the predictions achieve a good accuracy, especially those calculated with mixing rules R2 and R3, and more precise than that usually offered by other theoretical methods when polar mixtures are invol ved. The equations of state reveal its usefulness as a predictive tool for excess volumes, as they have been validated in many other thermophysical magnitudes.

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