

# Specific Heat Capacity at Constant Volume for Water, Methanol, and Their Mixtures at Temperatures from 300 K to 400 K and Pressures to 20 MPa<sup>†</sup>

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Specific heat capacities at constant volume ( $c_v$ ) of water, methanol, and their mixtures were measured with a new adiabatic calorimeter. Temperatures ranged from 300 K to 400 K, and pressures ranged to 20 MPa. Densities were determined at the initial and final end points during each calorimetric experiment. The calorimeter is a twin-cell type whose sample and reference cells (33 cm<sup>3</sup>) and their shields are heated by electric power. The cells are surrounded by a high vacuum. During the experiment, the heating power was carefully controlled so that the cell temperature increased uniformly. The reference cell was always evacuated and was heated with a constant current. The temperature of the sample cell tracked that of the reference cell temperature by means an automatic control system. Automated sample pressure measurements were made with a crystal quartz transducer. The expanded relative uncertainty for  $c_v$  is estimated to be 1% for liquid-phase measurements, and for density it is about 0.2%.

## Introduction

To develop a reliable equation of state for a fluid, various thermodynamic property measurements of the fluid are required. Among them, isochoric heat capacity measurements provide a very useful check for calculations of the second derivative of the pressure with respect to temperature, which is essential information to develop an accurate equation but is challenging to measure accurately. By use of molecular theory, vibrational and orientational modes of molecules can account for the thermodynamic properties of a substance. When a substance is heated, the increasing vibrational energy stored in molecules makes a strong contribution to the heat capacity. On the other hand, changes of molecular structure with temperature can also affect the magnitude of the heat capacity contribution which is dominated by orientational energy.

Hydrogen bonding of water (H<sub>2</sub>O) is certain to introduce the effect of the molecular energy to the heat capacity. In fact, interactions between water and methanol (CH<sub>3</sub>OH) molecules show anomalous thermodynamic properties due to the presence of strong hydrogen bonding.<sup>1</sup> There has been, even very recently, considerable interest in the physical property behavior of H<sub>2</sub>O + CH<sub>3</sub>OH mixtures in the supercritical and high-density regions; for example, *PVTx* properties,<sup>2–4</sup> excess molar heat capacity, and excess molar enthalpies<sup>5–7</sup> have been reported. However, published information on the isochoric heat capacity of the mixtures is limited to recent work by Abdulgatov et al.,<sup>8</sup> who reported isochoric heat capacities for an equimass H<sub>2</sub>O + CH<sub>3</sub>OH mixture in a range of temperatures from 435 K

to 645 K. To better characterize the H<sub>2</sub>O + CH<sub>3</sub>OH system, additional measurements are needed that cover a wide range of temperatures, pressures, and compositions.

To measure the heat capacity of fluids, various methods have been proposed;<sup>9</sup> however, the high accuracy potential of adiabatic methods makes them the most desirable. In the adiabatic principle, heat exchange between the calorimeter and the surroundings does not occur in the system; thus, the energy applied to the sample cell would be precisely the desired quantity to calculate the heat flow and heat capacity. In actual practice, however, the ideal adiabatic condition is very difficult to realize due to heat leakage by thermal conduction, convection, and thermal radiation. If the heat leakage is considerable, it may be important to evaluate the amount of the heat leakage accurately to correct the measured values. A small heat leak is self-correcting if we use the twin calorimeter method in which there are two identical vessels (cells) in identical surroundings. In one cell is the sample to be measured, and in the other either there is a reference fluid or it may be empty. A novel twin-cell adiabatic calorimeter<sup>10,11</sup> has been developed in the NIST labs; it has been applied to measure H<sub>2</sub>O and H<sub>2</sub>O + NH<sub>3</sub> mixtures.<sup>11,12</sup> In a recent development, a new twin-cell adiabatic calorimeter<sup>13</sup> was built in Japan which traces its roots to the design of the NIST calorimeter but features numerous improvements such as a smaller size and greater simplicity in its design.

In this paper, we report the first measurements with this new calorimeter. Water was chosen for apparatus validation due to its well-established thermodynamic surface. Methanol and methanol + water mixtures were selected to establish the performance of the calorimeter for a mixture system of scientific and industrial interest. We will report heat capacities of H<sub>2</sub>O, CH<sub>3</sub>OH, and their mixtures for liquid samples in a range of temperatures from 280 K to 400 K. In addition, we will report density values that were calculated from the volume of the calorimeter cell and sample mass measurements.

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**Table 1.** Mass Fraction  $w$  and Mole Fraction  $x$  of  $\{x\text{H}_2\text{O} + (1-x)\text{CH}_3\text{OH}\}$  Mixtures Used in This Study

| $w$     | $x$     |
|---------|---------|
| 0.19010 | 0.29452 |
| 0.64858 | 0.76649 |

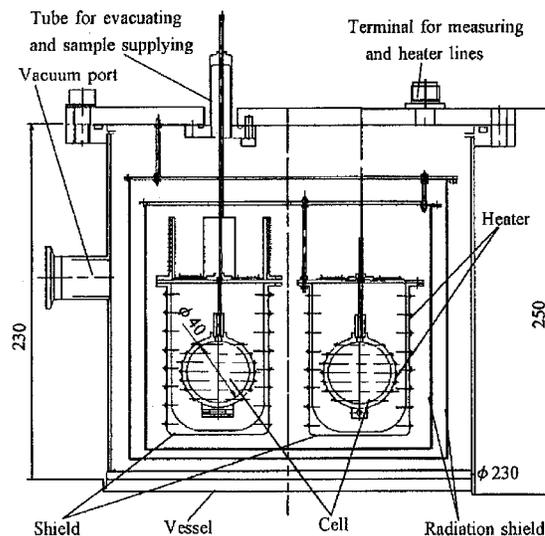
### Experimental Section

**Materials.** High-purity samples of  $\text{H}_2\text{O}$  and  $\text{CH}_3\text{OH}$  were obtained to prepare the mixtures. The  $\text{H}_2\text{O}$  sample was twice-distilled and has a minimum purity of 0.9999 mass fraction and an insulating resistance of  $18 \text{ M}\Omega \cdot \text{cm}$ . For the  $\text{CH}_3\text{OH}$  sample, the commercial supplier claimed a minimum liquid purity of 0.998 mass fraction with 0.001 mass fraction  $\text{H}_2\text{O}$  and 0.0005 mass fraction  $\text{C}_2\text{H}_5\text{OH}$ . Each component was degassed twice and was stored in a lightweight cylinder ( $75 \text{ cm}^3$ ). The sample cylinders were accurately weighed with a 0.1 mg uncertainty.

The mixtures were prepared in the calorimeter cell by introducing each component through evacuated tubing. During the transfer step, each component was heated above 373 K to enable faster transfer. After both components of the mixture were charged from the cylinders into the calorimeter cell, the cell was cooled below 278 K by a minicooler. The remaining mass in each cylinder was weighed and then the composition of the sample in the cell was calculated from the masses charged to the cell. To ensure complete homogenization, the sample cell temperature was increased until the sample pressure reached the apparatus pressure limit of 20 MPa. This process was carried out twice before the first measurement was begun. Both the mass fraction and mole fraction compositions of the two mixtures prepared for this study are given in Table 1. The expanded uncertainty (coverage factor  $k = 2$ ) of the mass fraction composition is 0.002, after including the uncertainty due to the impurities of the constituents.

**Measurements.** The twin-cell adiabatic calorimeter,<sup>13</sup> shown in Figure 1, was used for these measurements. A type-304 stainless steel spherical cell of  $33 \text{ cm}^3$  capacity was designed for this apparatus. It has a maximum permissible pressure of 60 MPa at 800 K. A pair of these cells was made from stainless steel block by spinning in a lathe within a  $\pm 5 \mu\text{m}$  tolerance to produce hemispheres which then were welded together. On the bottom of each cell was brazed a copper block to accept a platinum resistance thermometer (PRT). Absolute temperatures are measured with the PRT's and are reported on the ITS-90. Sheath heaters, which were specially insulated and are capable of reaching 900 K in a vacuum were prepared for this apparatus. A  $2 \Omega$  heater was wound around each sphere with a pitch of about 8 mm. Small strips were attached to the cell surface to hold the heater wires in place.

A 6.4 mm outer diameter (o.d.) type-316 stainless steel tube was welded into a hole in the top of each sphere. A 1.735 mm inner diameter capillary was welded into the 6.4 mm o.d. tube. Two type-K thermocouples sealed in a stainless steel sheath were put on each cell surface to read the temperature difference between each cell and its associated adiabatic shield, also made from type-304 stainless steel. Each spherical cell was jacketed in a cylindrical adiabatic shield whose temperature was adjusted by a  $3 \Omega$  sheath heater for the sides and a  $0.8 \Omega$  one for the top to keep it in equilibrium with the cell temperature. To control the temperature, two type-K thermocouples were put onto the surface of each adiabatic shield side and one was put onto each shield top. A pressure transducer using a precision quartz-crystal resonator, attached to the charg-

**Figure 1.** Twin-cell adiabatic calorimeter.

ing manifold, provided pressure measurements to 68 MPa. Adiabatic conditions are ensured by each thermal radiation shield and by maintaining a high vacuum (approximately  $1 \times 10^{-4} \text{ Pa}$ ) in the vacuum vessel that surrounds both cell/adiabatic shield assemblies.

Each of the six heaters (cell, shield side, and shield top for each set) in the calorimeter was driven by a direct-current power supply system. Two 4-channel 16-bit A/D converters control it. The entire instrument was connected to a personal computer through an IEEE-488 standard interface bus. The computer carried out several functions of temperature control and data acquisition with the aid of a graphical programming language and a specialized program. The measurement and temperature-control tasks were executed every 30 s during the course of an experiment. Between measurement cycles, the cell temperature rose about 35 mK. The temperature difference between the cells was maintained within  $\pm 3 \text{ mK}$  during a measurement. In addition, the system controlled each temperature difference between the cells and shield sides, and between the cells and shield tops, within  $\pm 10 \text{ mK}$ .

For the heat capacity measurement, a precisely determined electrical energy ( $Q$ ) is applied and the resulting temperature rise ( $\Delta T = T_2 - T_1$ ) is measured. The isochoric specific heat capacity is obtained from

$$c_v = \left( \frac{\partial U}{\partial T} \right)_V \cong \frac{\Delta Q - \Delta Q_0 - \Delta W_{PV}}{m\Delta T} \quad (1)$$

where  $U$  is the internal energy,  $\Delta Q_0$  is the energy difference between the sample cell,  $Q_{0,\text{sam}}$ , and the reference cell,  $Q_{0,\text{ref}}$ , when the cells are empty,  $\Delta Q$  refers to the energy added during an experiment with a sample in the sample cell and a blank (vacuum) in the reference cell,  $W_{PV}$  is the change-of-volume work due to the slight dilation of the cell, and  $m$  is the mass of sample in the sample cell.

To prepare for measurements, the sample cell was charged with the sample and was cooled to a starting temperature below room temperature. Then, measurements were performed by raising the temperature until the upper pressure limit of 20 MPa was reached. At the completion of a run, a portion of the sample in the cell was cryopumped into a lightweight cylinder and was weighed. The next run was started with a lower density. When the runs were completed, the remaining sample in the cell was

**Table 2. Expanded Uncertainties for This Work**

|                            |                       |
|----------------------------|-----------------------|
| temperature                |                       |
| absolute                   | 0.04 K                |
| difference, $\Delta T$     | 0.0011 K              |
| pressure                   | 0.007 MPa             |
| mass                       | 0.0002 g              |
| volume                     | 0.007 cm <sup>3</sup> |
| composition, mass fraction | 0.002                 |
| density                    | 0.2%                  |
| energy                     |                       |
| power                      | 0.02%                 |
| difference                 | 0.25 J                |
| change-of-volume work      | 2%                    |
| specific heat capacity     | 1%                    |

discharged and weighed. The sample mass of each run was determined from the sum of the appropriate mass increments for that run.

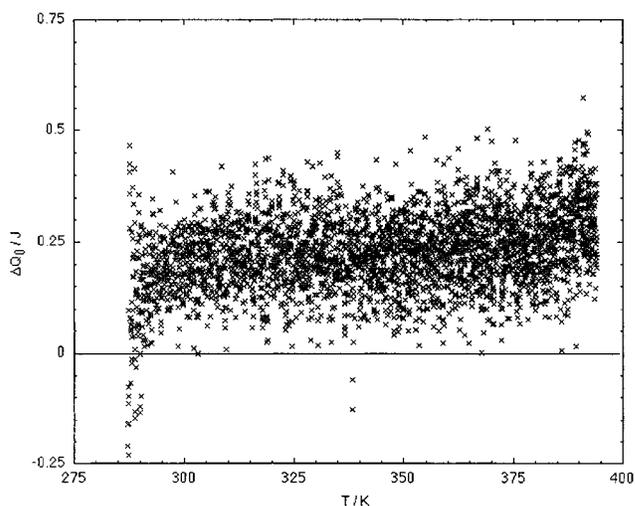
**Uncertainties.** In the following discussion, a definition is used for the expanded uncertainty that is two times the standards uncertainty (a coverage factor  $k = 2$ ). The estimated uncertainty of the absolute temperature measurement based on ITS-90 is  $\pm 40$  mK, even though the stability of the PRT readings was  $\pm 2.5$  mK. It was obtained by considering the temperature distribution on the cell ( $\pm 10$  mK to 20 mK) and the systematic accuracy of the instruments ( $\pm 4$  mK). The temperature distribution on the cell was measured with the two thermocouples placed on the top and bottom sides of each cell. The uncertainty of the temperature rise at the experimental ramp rate of  $+70$  mK $\cdot$ min<sup>-1</sup> is  $\pm 1.1$  mK obtained from the 0.8 mK standard uncertainty of the experimental temperatures from the temperature ramp curve. The uncertainty of the pressure measurement is  $\pm 7$  kPa, on the basis of the pressure transducer's specifications. However, the uncertainty deteriorates exponentially at pressures below 10% of the full scale of 68 MPa. To improve the uncertainty, another pressure transducer with a lower full scale will be prepared for lower pressure measurements. The uncertainty of the change-of-volume work, which was calculated<sup>14</sup> with eq 2 below, may be determined from experimental *PVT* data because the derivative of the pressure with respect to temperature could be estimated from the measured temperature rise and pressure difference.

$$W_{PV} = \left( T_2 \left( \frac{\partial P}{\partial T} \right)_{V_2} - \frac{1}{2} \Delta P \right) \Delta V \quad (2)$$

From the fluctuation of the experimental data, the estimated uncertainty of the change-of-volume work is  $\pm 2\%$ , which leads to an uncertainty in specific heat capacity of  $\pm 0.08\%$ .

The energy applied to the cells is the product of the constant power and the time interval to heat from  $T_1$  to  $T_2$ . The measurements of the electrical quantities are exceptionally accurate and have an estimated uncertainty of  $\pm 0.02\%$ . A function of temperature was fitted to the energy difference  $\Delta Q_0$  applied to the empty cells; its fluctuation is less than  $\pm 2.5$  J $\cdot$ K<sup>-1</sup>, which propagates an added uncertainty of  $\pm 0.5\%$  to the specific heat capacity. By combining the various sources of experimental uncertainty, the expanded uncertainty of the specific heat capacity is estimated to be  $\pm 1\%$ . The expanded uncertainties and the resulting combined uncertainties are shown in Table 2.

**Blank Tests.** The empty calorimeter energy function was determined from heating the evacuated cells. Heating experiments covering a temperature range from 280 K to 400 K were repeated before each series. The energy data in unit of joules are shown in Figure 2. An equation for

**Figure 2.** Measured  $\Delta Q_0$  as a function of temperature.

the temperature was fit to the data; most data agreed with eq 3 within  $\pm 0.25$  J.

$$\Delta Q_0 = [(8.6260 \times 10^{-4}) \text{ J}\cdot\text{K}^{-1}]T - 0.070299 \text{ J} \quad (3)$$

### Heat Capacity and Density Results

The isochoric specific heat capacity data  $c_v$  of each run is shown in Table 3. Each density  $\rho$  was calculated from the measured sample mass and the calibrated cell volume at the measured temperature and pressure. As shown in eq 4, the calibrated cell volume  $V_{\text{cell}}$  in cubic centimeters is obtained from the coefficient of thermal expansion of stainless steel and a coefficient related to the pressure-dependence of the volume derived from the experimental data.

$$V_{\text{cell}} = \{0.00153 \text{ cm}^3\cdot\text{K}^{-1}(T - 273.15 \text{ K}) + 33.132 \text{ cm}^3\} (1 + (4.40 \times 10^{-5} \text{ MPa}^{-1})P) \quad (4)$$

The coefficient of thermal expansion of type-304 stainless steel was obtained from a handbook<sup>15</sup> and has a claimed uncertainty of  $10^{-5}$  cm<sup>3</sup> $\cdot$ K<sup>-1</sup>. The coefficient of pressure dilation of the sample cell was determined from the slope of the experimental isochore of water with an uncertainty of  $4 \times 10^{-6}$  MPa<sup>-1</sup>. The reliability of the coefficient was confirmed with a numerical stress analysis for the cell. The uncertainty of the cell volume is estimated to be 0.007 cm<sup>3</sup>.

A portion of the sample mass resides in the noxious volume that consists of the combined volumes of the connecting tubing, the charging valve orifices, and the pressure transducer. In total, the noxious volume is approximately 3% of the cell volume; as much as 0.8 g of sample could reside in the noxious volume at the maximum density of the measurements. The amount of sample mass in the noxious volume was calculated from an assumed temperature profile of this volume and from densities calculated with an equation of state<sup>16</sup> or correlations based on measured *PVTx* information from this apparatus. To estimate the temperature profile, the volume was divided into five sections: four along the 1.735 mm inner diameter capillary and one for the rest of the noxious volume. At one end, the temperature was measured with a thermometer located inside the pressure transducer. The other was assumed to be at the calorimeter cell temperature. It was assumed that the expanded uncertainty of the noxious volume is about 0.08 cm<sup>3</sup>. Although the uncertainty of the

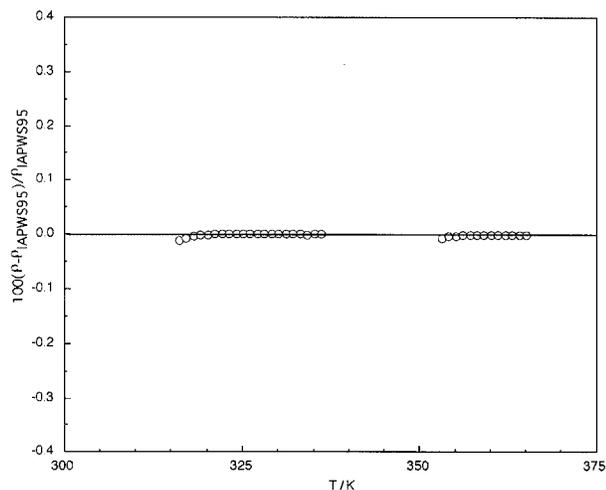
**Table 3. Experimental Densities and Heat Capacities for H<sub>2</sub>O, CH<sub>3</sub>OH, 0.29452 H<sub>2</sub>O + 0.70548 CH<sub>3</sub>OH, and 0.76649 H<sub>2</sub>O + 0.23351 CH<sub>3</sub>OH**

| $T_1^a$   | $P^b$  | $\rho^c$ | $c_v^d$ | $T_1^a$ | $P^b$  | $\rho^c$ | $c_v^d$ | $T_1^a$ | $P^b$  | $\rho^c$ | $c_v^d$ | $T_1^a$ | $P^b$  | $\rho^c$ | $c_v^d$ |
|---|--------|----------|---------|---------|--------|----------|---------|---------|--------|----------|---------|---------|--------|----------|---------|
| H <sub>2</sub> O                                      |        |          |         |         |        |          |         |         |        |          |         |         |        |          |         |
| 316.177   | 2.200  | 991.82   | 4.078   | 325.180 | 9.219  | 991.05   | 4.011   | 334.168 | 17.709 | 990.22   | 3.916   | 358.173 | 9.925  | 972.97   | 3.824   |
| 317.164   | 2.825  | 991.74   | 4.003   | 326.154 | 10.082 | 990.96   | 4.009   | 335.175 | 18.722 | 990.12   | 3.910   | 359.155 | 11.117 | 972.87   | 3.828   |
| 318.161   | 3.524  | 991.66   | 4.073   | 327.164 | 10.996 | 990.87   | 3.992   | 336.181 | 19.741 | 990.03   | 3.879   | 360.165 | 12.353 | 972.76   | 3.811   |
| 319.171   | 4.267  | 991.57   | 4.041   | 328.162 | 11.911 | 990.78   | 3.983   | 337.173 | 4.082  | 973.48   | 3.864   | 361.171 | 13.589 | 972.66   | 3.830   |
| 320.186   | 5.053  | 991.49   | 4.035   | 329.153 | 12.840 | 990.69   | 3.951   | 338.153 | 5.181  | 973.39   | 3.861   | 362.170 | 14.830 | 972.55   | 3.805   |
| 321.181   | 5.841  | 991.40   | 3.992   | 330.180 | 13.812 | 990.59   | 3.969   | 339.153 | 6.334  | 973.28   | 3.842   | 363.155 | 16.068 | 972.45   | 3.769   |
| 322.163   | 6.647  | 991.32   | 4.002   | 331.169 | 14.759 | 990.50   | 3.939   | 339.176 | 7.530  | 973.18   | 3.827   | 364.175 | 17.342 | 972.34   | 3.828   |
| 323.186   | 7.498  | 991.23   | 4.020   | 332.151 | 15.714 | 990.41   | 3.957   | 339.159 | 8.699  | 973.08   | 3.856   | 365.158 | 18.588 | 972.24   | 3.787   |
| 324.170   | 8.337  | 991.14   | 3.991   | 333.169 | 16.711 | 990.31   | 3.916   |         |        |          |         |         |        |          |         |
| CH <sub>3</sub> OH                                    |        |          |         |         |        |          |         |         |        |          |         |         |        |          |         |
| 285.153   | 0.943  | 798.54   |         | 306.154 | 18.754 | 796.95   | 2.213   | 333.171 | 0.347  | 752.94   | 2.380   | 353.161 | 15.373 | 751.53   | 2.514   |
| 286.172   | 1.924  | 798.45   |         | 307.151 | 19.571 | 796.88   | 2.234   | 334.177 | 1.091  | 752.87   | 2.391   | 354.171 | 16.139 | 751.46   | 2.508   |
| 287.179   | 2.830  | 798.37   |         | 313.150 | 4.643  | 776.83   |         | 335.159 | 1.821  | 752.79   | 2.423   | 355.178 | 16.901 | 751.39   | 2.510   |
| 288.163   | 3.711  | 798.29   |         | 314.150 | 5.502  | 776.75   |         | 336.170 | 2.581  | 752.71   | 2.416   | 356.154 | 17.635 | 751.33   | 2.487   |
| 289.177   | 4.610  | 798.21   |         | 315.178 | 6.366  | 776.68   |         | 337.180 | 3.336  | 752.64   | 2.406   | 357.151 | 18.387 | 751.26   | 2.502   |
| 290.195   | 5.492  | 798.13   |         | 316.184 | 7.216  | 776.60   |         | 338.180 | 4.088  | 752.57   | 2.408   | 358.170 | 19.160 | 751.19   | 2.525   |
| 291.150   | 6.321  | 798.06   |         | 317.185 | 8.063  | 776.52   |         | 339.174 | 4.835  | 752.50   | 2.417   | 359.154 | 19.910 | 751.13   | 2.500   |
| 292.158   | 7.186  | 797.98   |         | 318.183 | 8.908  | 776.45   | 2.281   | 340.167 | 5.580  | 752.43   | 2.427   | 378.155 | 1.119  | 705.94   | 2.690   |
| 293.161   | 8.032  | 797.91   |         | 319.172 | 9.743  | 776.37   | 2.302   | 341.154 | 6.321  | 752.36   | 2.442   | 379.153 | 1.625  | 705.89   | 2.715   |
| 294.162   | 8.866  | 797.84   | 2.139   | 320.157 | 10.571 | 776.30   | 2.312   | 342.169 | 7.085  | 752.29   | 2.460   | 380.171 | 2.178  | 705.83   | 2.713   |
| 295.158   | 9.693  | 797.76   | 2.134   | 321.174 | 11.420 | 776.22   | 2.325   | 343.182 | 7.849  | 752.22   | 2.450   | 381.158 | 2.810  | 705.77   | 2.692   |
| 296.150   | 10.510 | 797.69   | 2.148   | 322.151 | 12.233 | 776.15   | 2.308   | 344.155 | 8.584  | 752.15   | 2.455   | 382.161 | 3.460  | 705.71   | 2.691   |
| 297.185   | 11.364 | 797.61   | 2.167   | 323.157 | 13.066 | 776.08   | 2.297   | 345.157 | 9.338  | 752.08   | 2.437   | 383.153 | 4.106  | 705.65   | 2.707   |
| 298.182   | 12.170 | 797.54   | 2.154   | 324.161 | 13.893 | 776.00   | 2.317   | 346.181 | 10.108 | 752.01   | 2.449   | 384.165 | 4.765  | 705.58   | 2.714   |
| 299.208   | 13.013 | 797.47   | 2.186   | 325.160 | 14.719 | 775.93   | 2.333   | 347.164 | 10.847 | 751.94   | 2.458   | 385.153 | 5.407  | 705.52   | 2.734   |
| 300.189   | 13.833 | 797.40   | 2.200   | 326.159 | 15.543 | 775.86   | 2.318   | 348.176 | 11.609 | 751.87   | 2.482   | 386.162 | 6.068  | 705.46   | 2.741   |
| 301.167   | 14.645 | 797.32   | 2.199   | 327.173 | 16.382 | 775.78   | 2.312   | 349.156 | 12.349 | 751.81   | 2.463   | 387.165 | 6.725  | 705.40   | 2.717   |
| 302.182   | 15.483 | 797.25   | 2.203   | 328.165 | 17.206 | 775.71   | 2.318   | 350.160 | 13.103 | 751.74   | 2.482   | 388.153 | 7.367  | 705.34   | 2.709   |
| 303.188   | 16.310 | 797.17   | 2.205   | 329.179 | 18.039 | 775.63   | 2.329   | 351.157 | 13.855 | 751.67   | 2.475   | 389.165 | 8.031  | 705.28   | 2.718   |
| 304.155   | 17.109 | 797.10   | 2.196   | 330.184 | 18.868 | 775.56   | 2.323   | 352.172 | 14.623 | 751.60   | 2.507   | 390.159 | 8.690  | 705.22   | 2.733   |
| 305.153   | 17.931 | 797.02   | 2.223   | 331.154 | 19.669 | 775.49   |         |         |        |          |         |         |        |          |         |
| 0.29452 H <sub>2</sub> O + 0.70548 CH <sub>3</sub> OH |        |          |         |         |        |          |         |         |        |          |         |         |        |          |         |
| 282.525   | 4.316  | 879.57   |         | 304.188 | 10.295 | 864.36   | 2.481   | 341.168 | 12.965 | 832.86   | 2.625   | 365.170 | 15.942 | 817.23   | 2.697   |
| 283.170   | 4.351  | 879.55   |         | 305.158 | 11.322 | 864.27   | 2.480   | 342.159 | 13.920 | 832.78   | 2.637   | 366.160 | 16.856 | 817.15   | 2.705   |
| 284.161   | 5.379  | 879.46   |         | 306.164 | 12.384 | 864.17   | 2.485   | 343.179 | 14.907 | 832.69   | 2.636   | 367.169 | 17.815 | 817.07   | 2.706   |
| 285.189   | 6.499  | 879.36   |         | 307.164 | 13.436 | 864.08   | 2.502   | 344.182 | 15.888 | 832.61   | 2.641   | 368.175 | 18.760 | 816.99   | 2.709   |
| 286.255   | 7.660  | 879.26   | 2.415   | 308.163 | 14.491 | 863.99   | 2.511   | 345.154 | 16.838 | 832.53   | 2.644   | 369.165 | 19.697 | 816.91   | 2.708   |
| 287.176   | 8.703  | 879.17   | 2.419   | 309.154 | 15.542 | 863.90   | 2.516   | 346.151 | 17.808 | 832.44   | 2.646   | 369.530 | 4.434  | 804.05   |         |
| 288.159   | 9.812  | 879.08   | 2.418   | 310.175 | 16.624 | 863.81   | 2.526   | 347.178 | 18.812 | 832.36   | 2.648   | 370.161 | 5.002  | 804.00   | 2.715   |
| 289.153   | 10.921 | 878.98   |         | 311.155 | 17.659 | 863.72   | 2.532   | 348.165 | 19.778 | 832.28   | 2.654   | 371.177 | 5.892  | 803.93   | 2.720   |
| 290.166   | 12.046 | 878.89   | 2.426   | 312.168 | 18.736 | 863.63   | 2.536   | 350.155 | 2.025  | 818.41   | 2.657   | 372.169 | 6.712  | 803.86   | 2.718   |
| 291.179   | 13.197 | 878.79   |         | 313.179 | 19.802 | 863.54   | 2.545   | 351.157 | 2.924  | 818.34   | 2.665   | 373.179 | 7.623  | 803.78   | 2.728   |
| 292.185   | 14.306 | 878.70   | 2.416   | 314.186 | 20.870 | 863.44   | 2.544   | 352.158 | 3.849  | 818.26   | 2.659   | 374.150 | 8.498  | 803.71   | 2.704   |
| 293.152   | 15.385 | 878.61   | 2.407   | 329.468 | 1.666  | 833.84   |         | 353.155 | 4.760  | 818.18   | 2.669   | 375.154 | 9.395  | 803.64   | 2.714   |
| 294.157   | 16.496 | 878.52   | 2.418   | 330.161 | 2.334  | 833.78   |         | 354.181 | 5.708  | 818.10   | 2.672   | 376.154 | 10.286 | 803.56   | 2.748   |
| 295.163   | 17.612 | 878.42   | 2.436   | 331.174 | 3.311  | 833.70   | 2.574   | 355.167 | 6.617  | 818.03   | 2.679   | 377.152 | 11.189 | 803.48   | 2.713   |
| 296.159   | 18.718 | 878.33   | 2.441   | 332.171 | 4.272  | 833.61   | 2.592   | 356.177 | 7.553  | 817.95   | 2.678   | 378.176 | 12.125 | 803.40   | 2.754   |
| 297.154   | 19.821 | 878.24   | 2.452   | 333.162 | 5.223  | 833.53   | 2.593   | 357.160 | 8.460  | 817.86   | 2.677   | 379.168 | 13.016 | 803.33   | 2.738   |
| 297.240   | 3.216  | 864.97   |         | 334.175 | 6.207  | 833.45   | 2.594   | 358.169 | 9.399  | 817.79   | 2.674   | 380.154 | 13.907 | 803.26   | 2.756   |
| 298.179   | 3.976  | 864.90   |         | 335.167 | 7.159  | 833.36   | 2.599   | 359.171 | 10.336 | 817.71   | 2.685   | 381.163 | 14.817 | 803.18   | 2.733   |
| 299.171   | 4.938  | 864.81   |         | 336.183 | 8.144  | 833.28   | 2.605   | 360.168 | 11.273 | 817.63   | 2.687   | 382.160 | 15.721 | 803.10   | 2.773   |
| 300.165   | 6.006  | 864.73   |         | 337.163 | 9.087  | 833.20   | 2.614   | 361.179 | 12.220 | 817.55   | 2.690   | 383.176 | 16.647 | 803.02   | 2.765   |
| 301.156   | 7.062  | 864.64   |         | 338.176 | 10.067 | 833.11   | 2.616   | 362.151 | 13.126 | 817.47   | 2.693   | 384.162 | 17.527 | 802.95   | 2.778   |
| 302.178   | 8.150  | 864.54   | 2.456   | 339.180 | 11.042 | 833.03   | 2.627   | 363.155 | 14.061 | 817.39   | 2.694   | 385.157 | 18.415 | 802.87   | 2.750   |
| 303.167   | 9.207  | 864.45   |         | 340.178 | 12.010 | 832.94   | 2.628   | 364.150 | 14.987 | 817.31   | 2.692   | 386.153 | 19.313 | 802.79   | 2.766   |
| 0.76649 H <sub>2</sub> O + 0.23351 CH <sub>3</sub> OH |        |          |         |         |        |          |         |         |        |          |         |         |        |          |         |
| 340.172   | 8.877  | 919.80   | 3.362   | 362.181 | 4.870  | 898.89   | 3.117   | 373.174 | 20.020 | 897.80   | 2.966   | 383.177 | 14.046 | 885.95   | 2.859   |
| 341.200   | 9.787  | 919.65   | 3.354   | 363.151 | 6.228  | 898.78   | 3.117   | 374.156 | 21.386 | 897.72   | 2.940   | 384.158 | 15.427 | 885.85   | 2.815   |
| 342.160   | 10.906 | 919.50   | 3.318   | 364.153 | 7.604  | 898.67   | 3.078   | 375.240 | 3.712  | 886.72   |         | 385.156 | 16.791 | 885.76   | 2.861   |
| 343.158   | 12.127 | 919.36   | 3.306   | 365.172 | 8.999  | 898.57   | 3.092   | 376.169 | 5.063  | 886.62   |         | 386.155 | 18.167 | 885.67   | 2.855   |
| 344.157   | 13.371 | 919.23   | 3.281   | 366.156 | 10.350 | 898.47   | 3.064   | 377.176 | 6.426  | 886.52   | 2.940   | 387.160 | 19.550 | 885.57   | 2.851   |
| 345.152   | 14.612 | 919.12   | 3.236   | 367.162 | 11.730 | 898.36   | 3.079   | 378.171 | 7.587  | 886.41   | 2.938   | 388.159 | 20.921 | 885.48   | 2.822   |
| 346.165   | 15.877 | 919.01   | 3.262   | 368.159 | 13.104 | 898.27   | 3.073   | 379.160 | 8.913  | 886.30   | 2.923   | 390.220 | 2.165  | 872.39   | 2.729   |
| 347.169   | 17.148 | 918.90   | 3.247   | 369.154 | 14.476 | 898.17   | 3.038   | 380.169 | 10.274 | 886.20   | 2.926   | 391.153 | 3.360  | 872.30   | 2.710   |
| 348.163   | 18.402 | 918.80   | 3.215   | 370.171 | 15.878 | 898.07   | 2.992   | 381.164 | 11.621 | 886.10   | 2.862   | 392.164 | 4.795  | 872.19   | 2.668   |
| 349.154   | 19.651 | 918.70   | 3.209   | 371.176 | 17.264 | 897.98   | 2.996   | 382.168 | 12.992 | 886.00   | 2.880   | 393.177 | 6.175  | 872.08   | 2.662   |
| 350.177   | 20.928 | 918.61   | 3.197   | 372.178 | 18.644 | 897.89   | 2.995   |         |        |          |         |         |        |          |         |

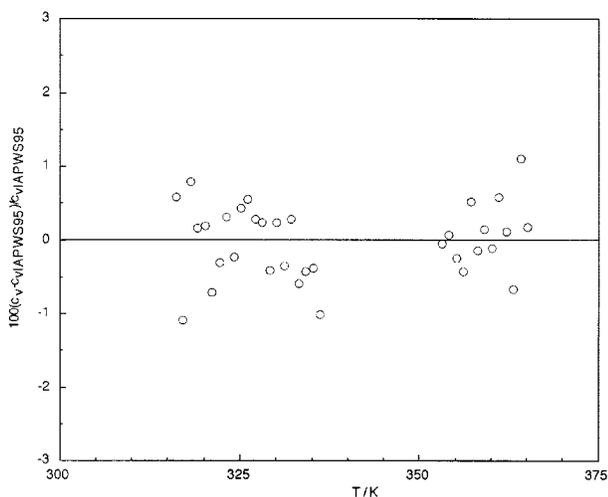
<sup>a</sup> In K. <sup>b</sup> In MPa. <sup>c</sup> In kg·m<sup>-3</sup>. <sup>d</sup> In J·g<sup>-1</sup>·K<sup>-1</sup>.

temperature profile would be very large compared to that for the volume, the effect is not as large on the results.

For example, if the actual temperature of a volume is 30 K higher than the assumed temperature profile, the density



**Figure 3.** Deviations of measured densities for H<sub>2</sub>O from calculations with IAPWS-95.<sup>16</sup>

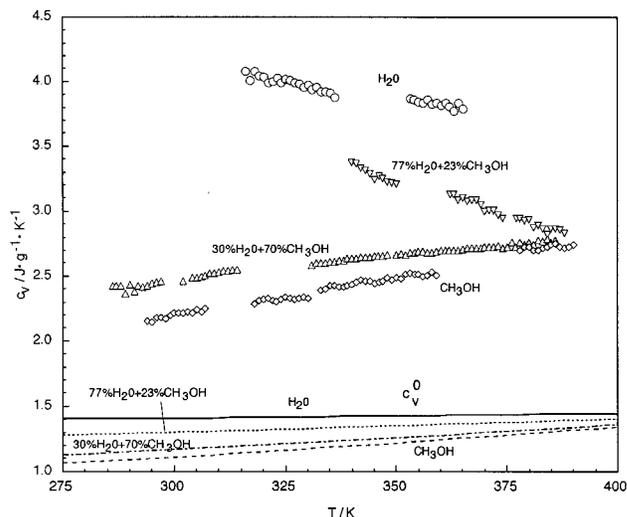


**Figure 4.** Deviations of measured  $c_v$  for H<sub>2</sub>O from calculations with IAPWS-95.<sup>16</sup>

decreases about 1%, leading to an  $\sim 8$  mg error of the sample mass. This amount can be compared with the 0.2 mg expanded uncertainty of the mass measurement, based on the balance's specifications. Thus, the estimated expanded relative uncertainty for the density measurement is 0.2%.

Figure 3 shows the deviations of experimental densities of H<sub>2</sub>O from those calculated with the IAPWS-95 formulation.<sup>16</sup> Deviations from this international reference equation of state were not greater than 0.01%. The uncertainty of the noxious volume of 2% propagates to a 0.03% uncertainty in the density values for this apparatus. To improve the accuracy of the density measurement, a more precise measurement of the noxious volume would be needed. Also, unphysical behavior at the lowest pressures was observed, due to less reliable pressure measurements at pressures below 10% of the full-scale range (68 MPa) of the pressure transducer. To improve this situation, a second pressure transducer with a lower full-scale range would be needed.

Figure 4 shows a comparison of the calculated  $c_v$  of H<sub>2</sub>O with the IAPWS-95 formulation. The plot shows that deviations of  $c_v$  are within  $\pm 1\%$ . While 1% is a reasonable deviation, we would expect deviations to improve if this series were repeated, since the series depicted in Figure 4 had occasional problems with temperature excursions of



**Figure 5.** Measurements of  $c_v$  for H<sub>2</sub>O, CH<sub>3</sub>OH, 0.29452 H<sub>2</sub>O + 0.70548 CH<sub>3</sub>OH, and 0.76649 H<sub>2</sub>O + 0.23351 CH<sub>3</sub>OH as a function of temperature; ideal gas  $c_v^0$  curves are shown for comparisons.

the adiabatic shields. Future results are expected to be more accurate because of optimization of the control. The measured data of H<sub>2</sub>O were also compared with IAPWS-IF97,<sup>17</sup> but the differences were negligible, as expected. It was found that densities and heat capacities calculated with IAPWS-95 differ by less than 0.0015% and 0.076%, respectively, from those calculated with IAPWS-IF97.

For CH<sub>3</sub>OH, an equation of state<sup>18</sup> has been formulated and published under IUPAC auspices. The measured results for CH<sub>3</sub>OH were compared with the equation of state. The measured densities differed from the calculation within  $\pm 0.1\%$ . However, the measured heat capacities deviated by between +1.8% and +4.5% from the equation of state. This is considerably more than the uncertainty of the measurements. The main reason for the discrepancy seems to be that the equation was formulated without any experimental information for heat capacity in the liquid region.

Figure 5 depicts the  $c_v$  data of H<sub>2</sub>O, CH<sub>3</sub>OH, and their mixtures. Ideal heat capacities  $c_v^0$ , which were calculated with published correlations<sup>16,18</sup> and ideal mixing rules, are superimposed on this figure. The figure shows a remarkable composition-dependent behavior of the thermodynamic surface for the H<sub>2</sub>O + CH<sub>3</sub>OH binary system. While the ideal gas curves, the methanol-rich mixture curve, and the pure methanol curve increase slowly with temperature, the water-rich mixture curve and pure water curve decrease with temperature. One could readily guess that a mixture composition exists, between those measured, for which the liquid heat capacities are nearly independent of temperature in this region. Finally, the measurements reported in this work are of adequate accuracy for model tests, but were measured primarily for the purpose of performance tests of the new apparatus. Later measurements will incorporate improved temperature control of the shields and are expected to have lower uncertainty.

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## Literature Cited

- (1) D'Arrigo, G.; Paparelli, A. Anomalous Ultrasonic Absorption in Alkoxyethanols Aqueous Solutions near their Critical and Melting Points. *J. Chem. Phys.* **1989**, *91*, 2587–2593.
- (2) Kubota, H.; Tanaka, Y.; Makita, T. Volumetric Behavior of Pure Alcohol and their Water Mixtures under High Pressures. *Int. J. Thermophys.* **1987**, *8*, 47–70.
- (3) Osada, O.; Sato, M.; Uematsu, M. Thermodynamic Properties of  $\{x\text{CH}_3\text{OH}+(1-x)\text{H}_2\text{O}\}$  with  $x = (1.000 \text{ and } 0.4993)$  in the Temperature Range from 320 K to 420 K at Pressures up to 200 MPa. *J. Chem. Thermodyn.* **1999**, *31*, 451–464.
- (4) Xiao, C.; Bianchi, H.; Tremaine, P. R. Excess Molar Volume and Densities of (Methanol+Water) at Temperatures between 323 and 573 K and at Pressures of 7 MPa and 13.5 MPa. *J. Chem. Thermodyn.* **1997**, *29*, 261–286.
- (5) Lama, R. F.; Lu, B. C.-Y. Excess Thermodynamic Properties of Aqueous Alcohol Solutions. *J. Chem. Eng. Data* **1965**, *10*, 216–219.
- (6) Benson, G. C.; D'Arcy, P. J. Excess Isobaric Heat Capacities of Water–*n*-Alcohol Mixtures. *J. Chem. Eng. Data* **1982**, *27*, 439–442.
- (7) Simonson, J. M.; Bradley, D. J.; Busey, R. H. Excess Molar Enthalpies and the Thermodynamics of (Methanol+Water) to 573 K and 40 MPa. *J. Chem. Thermodyn.* **1987**, *19*, 479–492.
- (8) Abdulagatov, I. M.; Dvoryanchikov, V. I.; Aliev, M. M.; Kamalov, A. N. Isochoric Heat Capacity of a 0.5 Water and 0.5 Methanol Mixture at Subcritical and Supercritical Conditions. *Steam, Water, and Hydrothermal Systems: Physics and Chemistry Meeting the Needs of Industry, Proceedings of the 13th International Conference on the Properties of Water and Steam*; Tremaine, P. R., Hill, P. G., Irish, D. E., Balakrishnan, P. V., Eds.; NRC Press: Ottawa, 2000; pp 157–164.
- (9) Hemminger, W.; Hohne, G. *Calorimetry—Fundamentals and Practice*; Verlag Chemie: Weinheim, 1984.
- (10) Magee, J. W. High-Temperature Adiabatic Calorimeter for Constant-Volume Heat Capacity Measurements of Compressed Gases and Liquids. *Proceedings of the 9th Symposium on Energy and Engineering Sciences*; Argonne National Laboratory, NTIS: Springfield, VA, 1991; pp 318–322.
- (11) Magee, J. W.; Blanco, J. C.; Deal, R. J. High-Temperature Adiabatic Calorimeter for Constant-Volume Heat Capacity of Compressed Gases and Liquids. *J. Res. Natl. Inst. Stand. Technol.* **1998**, *103*, 63–75.
- (12) Magee, J. W.; Kagawa, N. Specific Heat Capacity at Constant Volume for  $\{x\text{NH}_3+(1-x)\text{H}_2\text{O}\}$  at Temperatures from 300 to 520 K and Pressures to 20 MPa. *J. Chem. Eng. Data* **1999**, *43*, 1082–1090.
- (13) Kuroki, T.; Kagawa, N.; Araoka, K.; Endo, H.; Tsuruno, S. Specific Heat Capacity Measurement of Fluids with an Adiabatic Calorimeter. *Proceedings of the 20th Japanese Symposium on Thermophysical Properties*, Tokyo, Japanese Society of Thermophysical Properties: Atsugi, Kanagawa, 1999; pp 456–460.
- (14) Goodwin, R. D.; Weber, L. A. Specific Heats  $C_v$  of Fluid Oxygen from the Triple Point to 300 K at Pressures to 350 Atmospheres. *J. Res. Natl. Bur. Stand. (U.S.)* **1969**, *73A*, 15–24.
- (15) *JSME Data Book: Heat Transfer*, 4th ed.; JSME: Tokyo, 1994.
- (16) Wagner, W.; Pruß, A. New International Formulation for the Thermodynamic Properties of Ordinary Water Substance for General and Scientific Use. *J. Phys. Chem. Ref. Data* (to be submitted).
- (17) Wagner, W.; Cooper, J. R.; Dittmann, A.; Kijima, J.; Kretschmar, H.-J.; Kruse, A.; Mares, R.; Oguchi, K.; Sato, H.; Stocker, I.; Sifner, O.; Takaishi, Y.; Tanishita, I.; Trubenbach, J.; Willkommen, Th. The IAPWS Industrial Formulation 1997 for the Thermodynamic Properties of Water and Steam. *ASME J. Eng. Gas Turbines Power* **2000**, *122*, 150–182 (see also *IAPWS Release on the IAPWS Industrial Formulation 1997 for the Thermodynamic Properties of Water and Steam*, 1997; pp 1–48.)
- (18) de Reuck, K. M.; Craven, R. J. B. *Methanol—International Thermodynamic Tables of the Fluid State—12*; Blackwell: Oxford, 1993.

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