# Compressed Liquid Densities of Carbon Dioxide + Ethanol Mixtures at Four Compositions via a Vibrating Tube Densimeter up to 363 K and 25 MPa 

Abel Zúñiga-Moreno and Luis A. Galicia-Luna*<br>Instituto Politecnico Nacional, ESI QI E-Graduados- Lab. de Termodinamica, Edif. Z, Secc. 6, $1^{\text {ER }}$ Piso, UPALM, C.P. 07738, México, D.F. (México)


#### Abstract

PvT properties in a single phase were determined for carbon dioxide + ethanol mixtures at four compositions from 313 to 363 K and up to 25 MPa with an uncertainty less than ( $\pm 0.04 \mathrm{~kg} \cdot \mathrm{~m}^{-3}$ ) using a vibrating tube densimeter. The classical calibration method of the vibrating tube densimeter was used with $\mathrm{N}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$ as the reference fluids.


## Introduction

PvT properties and vapor-liquid, vapor-liquid-liquid, and liquid-liquid equilibria of pure compounds and mixtures at high pressures are required in the development of supercritical fluid extraction processes.

For over 20 years the vibrating tube principle has been widely and successfully applied for the experimental study of PvT properties of various fluids. High precision and applicability of this method for liquid density measurements in a wide temperature/pressure range make it attractive for experimenters and even competitive compared with the classical PvT methods.

This research focused on a systematic study to get experimental vapor-liquid equilibria ${ }^{1-4}$ and PVT data ${ }^{5-7}$ of $\mathrm{CO}_{2}+$ alcohol mixtures for knowledge, development, and application of techniques directed toward supercritical extraction processes. The main objective is to perform systematic studies of PvT and phase equilibria of $\mathrm{CO}_{2}+$ al cohol binary mixtures containing from ethanol to decanol in order to select the best supercritical operating conditions focused on industrial applications such as extraction of carotenes from the cempasuchil flower of Mexico (tagetes erecta) and from the Chile Poblano of Mexico (Capsicum annum).

Galicia-Luna et al. .1,2 reported vapor-liquid equilibrium data of the $\mathrm{CO}_{2}+$ ethanol system at temperatures from 313 to 373 K. Zúñiga-M oreno and Galicia-Luna ${ }^{5,6}$ reported PVT data for ethanol and $\mathrm{CO}_{2}$ from 313 to 363 K and for pressures up to 25 MPa . In this work are presented liquid densities of binary mixtures at four compositions from 313 to 363 K and at pressures up to 25 MPa . The excess volumes for these mixtures and their dependence on composition, temperature, and pressure are reported.

The reliability of the measurements for pure compounds has been checked by comparing the data calculated through the BRWS EoS fitted on data reported by Zúñiga-Moreno and Galicia-Luna ${ }^{5,6}$ (ethanol, ${ }^{5}$ 1-propanol, ${ }^{6}$ 2-propanol, ${ }^{6}$ and 1-pentanol ${ }^{5}$ ) with the data reported by several authors. The experimental results are in good agreement.

[^0]

Figure 1. Feed cell: $B$ and $C$, caps in titanium; EC, equilibrium cell; FV, feeding valve; GC, gas compressor; MR, magnetic rod; PI, Isco pump; PT, pressure transducer; PTPi, platinum probe i; ST, sapphire tube; TD, temperature digital indicator F250; VSE, variable speed engine; VP, vacuum pump.

## Experimental Section

Apparatus and Procedure. The apparatus used in this work is that reported by Zúñiga-M oreno and Galicia-L una. ${ }^{6}$ This apparatus is designed to determine simultaneous VLE and PVT properties of pure and binary mixtures containing $\mathrm{CO}_{2}$ and al cohols.
The measuring cell consists of a vibrating tube (Hastelloy C-276 U-tube) containing $1 \mathrm{~cm}^{3}$ of sample. We use the same experimental procedure described by Galicia-Luna et al. 8 and Zúñiga-Moreno and Galicia-Luna. ${ }^{6}$
The pressure measurements are made directly in the equilibrium cell (see Figure 1) by means of a 25 MPa Sedeme pressure transducer. The pressure transducer is thermoregulated at a specific value and calibrated periodically to ensure the best precision (the gauge output is slightly temperature dependent and could be affected by some shift with time).

The experimental procedure consists of four steps: 1, sensor calibration; 2, cell loading; 3, setting up of the

Table 1. Purity and Origin of Pure Compounds

|  |  | max. water |  |
| :--- | :--- | :---: | :--- |
| compound | certified purity (\%) | content (\%) | supplier |
| ethanol | 99.8 | 0.02 | Merck |
| $\mathrm{CO}_{2}$ | 99.995 |  | Air Products-Infra |
| water | 99.95 (HPLC) |  | Fisher |
| nitrogen | 99.995 |  | Air Products-Infra |

Table 2. Selected Data of Excess Molar Volumes VE versus $x\left(\mathrm{CO}_{2}\right)$, Mole Fraction of Carbon Dioxide, at Different Pressures of the $\mathbf{C O}_{2}+$ Ethanol Mixtures (see Figure 5)

| $x\left(\mathrm{CO}_{2}\right)$ | $\mathrm{P} / \mathrm{MPa}$ | $\mathrm{V}^{\mathrm{E}} \mathrm{a} / \mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | $\mathrm{x}\left(\mathrm{CO}_{2}\right)$ | $\mathrm{P} / \mathrm{MPa}$ | $\mathrm{V}^{\mathrm{E}} \mathrm{b} / \mathrm{cm}^{3} \mathrm{~mol}^{-1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| This Work |  |  |  |  |  |
| 10.945 | 0.2317 | -8.7079 | 10.945 | 0.2317 | -9.3421 |
| 11.939 | 0.4076 | -13.1307 | 11.099 | 0.4076 | -14.1492 |
| 10.959 | 0.5569 | -15.4711 | 10.959 | 0.5569 | -16.9666 |
| 11.000 | 0.7703 | -18.5684 | 11.000 | 0.7703 | -20.5978 |
| Pholer and Kiran ${ }^{13}$ |  |  |  |  |  |
|  |  |  | 11.050 | 0.9000 | -17.01 |
|  |  |  | 11.000 | 0.8000 | -20.00 |
|  |  |  | 11.000 | 0.7000 | -22.50 |
|  |  |  | 11.000 | 0.5000 | -18.17 |

${ }^{\text {a }}$ Calculated excess molar volumes using the BWRS EoS ${ }^{12}$ for $\mathrm{CO}_{2}$ and ethanol. ${ }^{\text {b }}$ Calculated excess molar volumes using the BWRS EoS ${ }^{12}$ for ethanol and the MBWRS EoS ${ }^{11}$ for $\mathrm{CO}_{2}$.
experimental conditions; and 4, measurements at equilibrium. A detailed procedure regarding the calibrations of the platinum temperature probes and the pressure transducer is given in previous papers by Galicia-Luna et al.,1,6

Both platinum probes (Specitec, France) connected to a digital indicator (Automatic Systems, USA, model F250) were calibrated as described in detail by Zúñiga-Moreno and Galicia-Luna. ${ }^{7}$ The resulting uncertainty is estimated to be less than $\pm 0.03 \mathrm{~K}$. The 25 MPa Sedeme pressure transducer connected to a $61 / 2$ digital multimeter (HP34401A, USA) gives pressures with uncertainties within $\pm 0.008 \mathrm{MPa}$.

Loading of the Feed Cell. A pure liquid, such as water, is first degassed and then distilled under vacuum into the evacuated feed cell.
Loading is more complex for a binary mixture. First the degassed, less volatile component is transferred by lowpressure distillation into the weighed (empty) feed cell. Then a new weighing of the feed cell is performed to determine the exact amount introduced. Afterward, if it is a liquid, the second component is transferred in the same manner into the feed cell. If it is a gas, at feed conditions, it is introduced into the feed cell under pressure. A third weighing yields the mass of the second component and therefore the mixture composition.
Weighing is carried out within $10^{-7} \mathrm{~kg}$ (maximum contents of the feed cell, $12 \mathrm{~cm}^{3}$; mass of the empty cell, $\cong 1 \mathrm{~kg}$ ). A Sartorius (Sartorius, Germany) comparator balance was used (model MCA1200; accuracy, $\pm 10^{-7} \mathrm{~kg}$ ); it is calibrated with a mass of 1 kg class E1 (Sartorius, Germany).

Measurements performed with water and nitrogen are used to calibrate the vibrating tube following the classical method procedure. Reference density values of $\mathrm{H}_{2} \mathrm{O}$ and

Table 3. Densities and Excess Molar Volumes for the Carbon Dioxide (1) + Ethanol (2) Mixture at Six Temperatures and $\mathrm{x}_{1}=0.2317$

| P/MPa | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\mathrm{V}^{\mathrm{E}} / \mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | P/MPa | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\mathrm{V}^{\mathrm{E}} / \mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | P/MPa | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\mathrm{V}^{\mathrm{E}} / \mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{T}=312.95 \mathrm{~K}$ |  |  | $\mathrm{T}=322.91 \mathrm{~K}$ |  |  | $\mathrm{T}=332.79 \mathrm{~K}$ |  |
| 9.968 | 815.33 | -5.4970 | 7.963 | 799.42 | -35.6948 | 7.927 | 784.85 | -42.1712 |
| 10.938 | 816.71 | -4.2472 | 8.956 | 801.31 | -24.9601 | 8.917 | 786.95 | -32.3290 |
| 11.953 | 818.21 | -3.5723 | 9.984 | 803.19 | -15.2871 | 9.984 | 789.13 | -23.6042 |
| 13.028 | 819.70 | -3.1094 | 10.946 | 804.90 | -9.3421 | 10.960 | 791.11 | -17.0393 |
| 13.935 | 820.96 | -2.8264 | 11.992 | 806.73 | -6.4075 | 12.019 | 793.20 | -11.7409 |
| 14.950 | 822.41 | -2.5807 | 12.926 | 808.33 | -5.1434 | 13.061 | 795.19 | -8.5033 |
| 15.995 | 823.82 | -2.3754 | 13.970 | 810.06 | -4.3107 | 13.959 | 796.88 | -6.8147 |
| 16.948 | 825.10 | -2.2203 | 14.937 | 811.57 | -3.7956 | 14.978 | 798.72 | -5.5952 |
| 17.998 | 826.59 | -2.0842 | 15.953 | 813.16 | -3.4013 | 15.918 | 800.38 | -4.8380 |
| 18.905 | 827.74 | -1.9760 | 16.931 | 814.64 | -3.1076 | 16.958 | 802.18 | -4.2390 |
| 19.949 | 829.09 | -1.8673 | 17.953 | 816.18 | -2.8622 | 17.887 | 803.74 | -3.8358 |
| 20.949 | 830.36 | $-1.7770$ | 18.932 | 817.62 | -2.6691 | 18.991 | 805.58 | -3.4625 |
| 21.999 | 831.71 | -1.6948 | 19.994 | 819.12 | -2.4917 | 19.911 | 807.02 | -3.2116 |
| 22.953 | 832.93 | -1.6297 | 20.957 | 820.50 | -2.3565 | 20.990 | 808.75 | -2.9694 |
| 23.939 | 834.40 | -1.5823 | 21.963 | 821.89 | -2.2321 | 21.952 | 810.22 | -2.7867 |
| 25.112 | 835.82 | -1.5138 | 22.889 | 823.15 | -2.1309 | 22.913 | 811.64 | -2.6291 |
|  |  |  | 24.016 | 824.65 | -2.0223 | 24.044 | 813.33 | -2.4706 |
|  |  |  | 25.082 | 826.07 | -1.9325 | 25.119 | 814.91 | -2.3408 |
|  | $\mathrm{T}=342.73 \mathrm{~K}$ |  |  | $\mathrm{T}=352.67 \mathrm{~K}$ |  |  | $\mathrm{T}=362.56 \mathrm{~K}$ |  |
| 7.936 | 767.75 | -46.7830 | 8.929 | 754.25 | -41.2488 | 9.868 | 739.13 | -37.2463 |
| 8.947 | 770.58 | -37.0257 | 9.916 | 757.13 | -33.6036 | 10.920 | 742.63 | -29.0469 |
| 9.955 | 773.25 | -29.1914 | 10.923 | 759.91 | -27.2394 | 12.020 | 745.83 | -24.9037 |
| 10.963 | 775.72 | -22.7541 | 12.014 | 762.68 | -21.6044 | 13.042 | 748.65 | -20.5794 |
| 11.920 | 778.00 | -17.7371 | 12.948 | 765.01 | -17.6539 | 13.933 | 751.04 | -17.4360 |
| 12.997 | 780.47 | -13.3204 | 13.944 | 767.38 | -14.2345 | 14.964 | 753.71 | -14.4181 |
| 13.922 | 782.51 | -10.5457 | 14.985 | 769.79 | -11.4550 | 15.924 | 756.10 | -12.1438 |
| 14.942 | 784.69 | -8.3856 | 15.945 | 771.94 | -9.5104 | 16.981 | 758.65 | -10.1556 |
| 15.914 | 786.71 | -6.9662 | 16.962 | 774.14 | -7.9614 | 17.869 | 760.73 | -8.8261 |
| 16.978 | 788.83 | -5.8726 | 17.930 | 776.17 | -6.8517 | 18.973 | 763.20 | -7.5196 |
| 17.890 | 790.61 | -5.1889 | 19.013 | 778.39 | -5.9105 | 19.968 | 765.40 | -6.5993 |
| 19.020 | 792.73 | -4.5500 | 19.903 | 780.17 | -5.3101 | 20.930 | 767.43 | -5.8842 |
| 19.909 | 794.36 | -4.1585 | 20.985 | 782.26 | -4.7286 | 22.024 | 769.72 | -5.2295 |
| 20.958 | 796.23 | -3.7868 | 21.903 | 784.02 | -4.3305 | 22.930 | 771.57 | -4.7847 |
| 21.922 | 797.91 | -3.5066 | 22.965 | 785.98 | -3.9510 | 24.015 | 773.72 | -4.3417 |
| 23.004 | 799.76 | -3.2450 | 23.904 | 787.70 | -3.6702 | 25.169 | 775.95 | -3.9532 |
| 23.906 | 801.24 | -3.0584 | 25.135 | 789.90 | -3.3647 |  |  |  |
| 25.062 | 803.14 | -2.8564 |  |  |  |  |  |  |

Table 4. Densities and Excess Molar Volumes for the Carbon Dioxide (1) + Ethanol (2) Mixture at Six Temperatures and $\mathrm{x}_{1}=0.4076$

| $\mathrm{P} / \mathrm{MPa}$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\mathrm{V}^{\mathrm{E}} / \mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | P/MPa | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\mathrm{V}^{\mathrm{E}} / \mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | P/MPa | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\mathrm{V}^{\mathrm{E}} / \mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{T}=313.16 \mathrm{~K}$ |  |  | $\mathrm{T}=323.11 \mathrm{~K}$ |  |  | $\mathrm{T}=333.01 \mathrm{~K}$ |  |
| 7.995 | 818.40 | -44.3915 | 10.012 | 803.10 | -25.2875 | 9.945 | 776.16 | -40.0295 |
| 8.977 | 822.64 | -17.5797 | 11.099 | 807.58 | -14.1492 | 10.976 | 781.43 | -28.0018 |
| 9.984 | 826.71 | -8.8111 | 11.939 | 810.93 | -10.2222 | 11.967 | 786.10 | -19.3406 |
| 10.996 | 830.56 | -6.6161 | 12.980 | 814.78 | -7.7748 | 12.974 | 790.58 | -13.7152 |
| 12.002 | 834.17 | -5.5443 | 13.930 | 818.16 | -6.5068 | 13.936 | 794.60 | -10.4991 |
| 12.942 | 837.32 | -4.9072 | 14.966 | 821.63 | -5.6028 | 14.969 | 798.66 | -8.3859 |
| 13.973 | 840.61 | -4.4157 | 15.958 | 824.81 | -4.9916 | 15.930 | 802.32 | -7.1019 |
| 14.925 | 843.44 | -4.0708 | 16.917 | 827.80 | -4.5478 | 16.939 | 805.92 | -6.1535 |
| 16.000 | 846.38 | -3.7590 | 17.939 | 830.86 | -4.1774 | 17.987 | 809.57 | -5.4395 |
| 16.933 | 848.75 | -3.5347 | 18.955 | 833.77 | -3.8822 | 18.911 | 812.66 | -4.9578 |
| 17.974 | 851.31 | -3.3260 | 20.022 | 836.71 | -3.6284 | 19.999 | 816.14 | -4.5090 |
| 18.883 | 853.46 | -3.1724 | 20.923 | 839.10 | -3.4487 | 20.915 | 818.96 | -4.2041 |
| 19.966 | 855.89 | -3.0106 | 21.942 | 841.78 | -3.2771 | 21.960 | 822.06 | -3.9171 |
| 20.937 | 858.04 | -2.8870 | 22.974 | 844.36 | -3.1256 | 22.994 | 825.05 | -3.6820 |
| 21.920 | 860.10 | -2.7739 | 23.937 | 846.77 | -3.0056 | 23.991 | 827.83 | -3.4885 |
| 23.031 | 862.42 | -2.6637 | 25.115 | 849.55 | -2.8767 | 25.125 | 830.95 | -3.3053 |
| 23.936 | 864.28 | -2.5848 |  |  |  |  |  |  |
| 25.084 | 866.57 | -2.4947 |  |  |  |  |  |  |
|  | $\mathrm{T}=342.95 \mathrm{~K}$ |  |  | $\mathrm{T}=352.90 \mathrm{~K}$ |  |  | $\mathrm{T}=362.79 \mathrm{~K}$ |  |
| 11.928 | 754.02 | -28.3867 | 12.390 | 732.52 | -31.9373 | 12.924 | 708.50 | -33.3956 |
| 12.940 | 759.95 | -21.2617 | 12.954 | 736.16 | -28.0624 | 13.938 | 716.40 | -27.4081 |
| 13.881 | 765.04 | -16.3537 | 13.960 | 742.22 | -22.2370 | 14.911 | 722.77 | -22.6424 |
| 14.911 | 770.22 | -12.6261 | 14.969 | 747.89 | -17.6889 | 15.937 | 729.04 | -18.5912 |
| 15.894 | 774.82 | -10.1776 | 16.005 | 753.36 | -14.1906 | 16.919 | 734.51 | -15.4996 |
| 17.005 | 779.83 | -8.3035 | 16.970 | 758.03 | -11.7648 | 17.972 | 739.85 | -12.9041 |
| 17.875 | 783.53 | -7.2523 | 17.999 | 762.69 | -9.8358 | 18.923 | 744.55 | -11.0835 |
| 18.973 | 787.96 | -6.2623 | 19.007 | 767.12 | -8.4285 | 20.082 | 749.77 | -9.3475 |
| 19.920 | 791.59 | -5.6144 | 20.055 | 771.50 | -7.3165 | 20.970 | 753.67 | -8.3114 |
| 20.978 | 795.52 | -5.0495 | 20.900 | 774.79 | -6.6010 | 22.060 | 758.18 | -7.2841 |
| 21.916 | 798.82 | -4.6484 | 21.942 | 778.67 | -5.8891 | 22.864 | 761.38 | -6.6650 |
| 22.976 | 802.42 | -4.2770 | 22.874 | 782.08 | -5.3786 | 24.021 | 765.78 | -5.9278 |
| 23.999 | 805.86 | -3.9897 | 24.009 | 786.04 | -4.8672 | 25.098 | 769.73 | -5.3750 |
| 25.204 | 809.69 | -3.7059 | 25.098 | 789.71 | -4.4698 |  |  |  |

$\mathrm{N}_{2}$ are obtained from the equations of state (E oS's) of Harr et al. ${ }^{9}$ and Span et al., ${ }^{10}$ respectively.

The square of the vibration period, $\tau^{2}(\mathrm{P}, \mathrm{T})$, of the U-tube is represented in the classical method, as a first approximation, by eq 1 , where $\rho_{\mathrm{i}}(\mathrm{P}, \mathrm{T})$ is the density of the fluid i :

$$
\begin{equation*}
\rho_{\mathrm{F}}(\mathrm{P}, \mathrm{~T})=\rho_{\mathrm{H}_{2} \mathrm{O}}(\mathrm{P}, \mathrm{~T})+\frac{1}{\mathrm{~A}}(\mathrm{P}, \mathrm{~T})\left[\tau_{\mathrm{F}}^{2}(\mathrm{P}, \mathrm{~T})-\tau_{\mathrm{H}_{2} \mathrm{O}}{ }^{2}(\mathrm{P}, \mathrm{~T})\right] \tag{1}
\end{equation*}
$$

with

$$
\begin{equation*}
\frac{1}{\mathrm{~A}}=\frac{\rho_{\mathrm{H}_{2} \mathrm{O}}-\rho_{\mathrm{N}_{2}}}{\tau_{\mathrm{H}_{2} \mathrm{O}}{ }^{2}-\tau_{\mathrm{N}_{2}}{ }^{2}} \tag{2}
\end{equation*}
$$

Taking into account all uncertainties and the dispersions on vibrating periods, a cumulative uncertainty has been estimated to be $\pm 0.05 \%$ for the densities in the liquid region.

## Results

The purity and origin of chemicals used in this work are given in Table 1. Chemicals were used without any purification except for a careful degassing of water and ethanol. The main objectives of the determinations of the densities of pure compounds were to test the capabilities and limitations of this apparatus and confirm its capability to determine densities with an accuracy better than 0.04 $\mathrm{kg} \cdot \mathrm{m}^{-3}$. For mixtures the liquid densities have the same accuracy, with the same equations (eqs 1 and 2 ) being used.

The densities of the $\mathrm{CO}_{2}+$ ethanol liquid system at each composition have been determined at six temperatures from 313 to 363 K (see Tables $2-7$ ). The excess volumes
for these mixtures and their variation with composition, temperature, and pressure are reported in these tables. The data for $\mathrm{CO}_{2}$ reported by Zúñiga-M oreno and Galicia-Luna ${ }^{6}$ are correlated in the whol e reported range of pressures and temperatures using the BWRS equation of state. ${ }^{11}$ The detailed description of the method used here is presented by Zúñiga-M oreno and Galicia-Luna. ${ }^{7}$ F or ethanol data are taken the BWRS parameters reported by Zúñiga-M oreno and Galicia-Luna ${ }^{7}$ (see Table 7).
Density data in the liquid region were correlated using a least-squares optimization procedure with the following objective function:

$$
\begin{equation*}
\mathrm{S}=\sum_{\mathrm{i}}\left[\frac{\left(\rho_{\mathrm{i}, \exp }-\rho_{\mathrm{i}, \text { cal }}\right)}{\rho_{\mathrm{i}, \exp }}\right]^{2} \tag{3}
\end{equation*}
$$

The adjusted parameters for the BWRS EoS are reported in Table 7. The units for pressure, temperature, and density are bar, kelvin, and cubic centimeter per mole.

Previous papers ${ }^{5,7}$ had as a main focus the elimination of experimental determinations of the vibrating period of $\mathrm{N}_{2}$ without lost precision in measurements. In this paper the vibrating period of the tube under vacuum is used as a reference point and $\mathrm{H}_{2} \mathrm{O}$ is used as a referencefluid. The density $\rho_{\mathrm{F}}$ is given by

$$
\begin{equation*}
\rho_{\mathrm{F}}(\mathrm{P}, \mathrm{~T})=\rho_{\mathrm{H}_{2} \mathrm{O}}(\mathrm{P}, \mathrm{~T})\left(\frac{\tau_{\mathrm{F}}^{2}(\mathrm{P}, \mathrm{~T})-\tau_{\mathrm{vac}}{ }^{2}(\mathrm{~T})}{\tau_{\mathrm{H}_{2} \mathrm{O}}^{2}(\mathrm{P}, \mathrm{~T})-\tau_{\mathrm{vac}}{ }^{2}(\mathrm{~T})}\right) \tag{4}
\end{equation*}
$$

The vibrating period of the tube under vacuum was measured at all reported measurement temperatures. The corresponding results were correlated as a function of

Table 5. Densities and Excess Molar Volumes for the Carbon Dioxide (1) + Ethanol (2) Mixture at Six Temperatures and $\mathrm{x}_{1}=0.5569$

| P/MPa | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\mathrm{VE} / \mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | P/MPa | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\mathrm{VE}^{\mathrm{E}} / \mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | P/MPa | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | V / $/ \mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{T}=313.16 \mathrm{~K}$ |  |  | $\mathrm{T}=323.10 \mathrm{~K}$ |  |  | $\mathrm{T}=333.00 \mathrm{~K}$ |  |
| 8.326 | 787.05 | -44.9931 | 9.189 | 743.74 | -47.5606 | 10.425 | 673.55 | -37.2347 |
| 8.898 | 793.08 | -23.2671 | 9.979 | 756.00 | -30.8967 | 10.919 | 711.42 | -33.0105 |
| 9.940 | 802.75 | -9.4960 | 10.959 | 768.21 | -16.9666 | 11.927 | 728.88 | -21.8319 |
| 10.930 | 811.03 | -6.6710 | 11.958 | 778.51 | -10.6260 | 12.983 | 742.84 | -14.4143 |
| 11.997 | 819.02 | -5.3056 | 12.928 | 787.29 | -7.8191 | 13.912 | 753.25 | -10.6417 |
| 12.916 | 825.42 | -4.6233 | 13.999 | 795.85 | -6.1587 | 14.947 | 763.35 | -8.1337 |
| 13.925 | 831.74 | -4.1115 | 14.916 | 802.61 | -5.2913 | 15.904 | 771.74 | -6.6878 |
| 14.962 | 837.81 | -3.7431 | 15.933 | 809.44 | -4.6219 | 16.913 | 779.80 | -5.6651 |
| 15.896 | 842.99 | -3.5009 | 16.899 | 815.50 | -4.1734 | 17.930 | 787.09 | -4.9338 |
| 17.053 | 848.86 | -3.2648 | 17.934 | 821.50 | -3.8102 | 18.902 | 793.63 | -4.4266 |
| 17.921 | 853.13 | -3.1302 | 18.894 | 826.83 | -3.5563 | 20.003 | 800.53 | -3.9946 |
| 18.910 | 857.68 | -3.0017 | 19.981 | 832.38 | -3.3213 | 20.934 | 806.05 | -3.7146 |
| 19.857 | 861.87 | -2.9028 | 20.897 | 836.93 | -3.1709 | 21.956 | 811.69 | -3.4640 |
| 20.929 | 866.42 | -2.8121 | 21.933 | 841.71 | -3.0225 | 22.914 | 816.78 | -3.2797 |
| 21.900 | 870.35 | -2.7438 | 22.903 | 846.12 | -2.9162 | 23.982 | 822.05 | -3.1046 |
| 22.928 | 874.43 | -2.6864 | 23.972 | 850.62 | -2.8109 | 25.170 | 827.79 | -2.9586 |
| 23.939 | 878.22 | -2.6369 | 25.046 | 855.08 | -2.7293 |  |  |  |
| 25.061 | 882.26 | -2.5905 |  |  |  |  |  |  |
|  | $\mathrm{T}=342.94 \mathrm{~K}$ |  |  | $\mathrm{T}=352.89 \mathrm{~K}$ |  |  | $\mathrm{T}=362.78 \mathrm{~K}$ |  |
| 11.513 | 615.56 | -30.5690 | 12.917 |  |  | 14.013 | 602.84 | -25.8713 |
| 11.906 | 659.59 | -30.6649 | 13.913 | 642.24 | -21.6117 | 14.951 | 622.61 | -21.3388 |
| 12.919 | 680.85 | -22.3535 | 14.939 | 662.62 | -16.7797 | 15.878 | 640.32 | -17.6887 |
| 13.934 | 698.56 | -16.2948 | 15.953 | 681.04 | -13.3153 | 16.953 | 657.48 | -14.2334 |
| 14.972 | 712.97 | -12.0346 | 16.907 | 694.70 | -10.8119 | 17.969 | 671.47 | -11.6968 |
| 15.909 | 724.57 | -9.4969 | 17.926 | 706.76 | -8.7870 | 18.933 | 683.15 | -9.8156 |
| 16.964 | 735.95 | -7.5577 | 18.889 | 717.11 | -7.3989 | 19.998 | 694.89 | -8.2352 |
| 17.969 | 746.02 | -6.3297 | 19.890 | 727.28 | -6.3603 | 20.943 | 704.14 | -7.1293 |
| 18.915 | 754.44 | -5.4904 | 20.933 | 736.68 | -5.5302 | 21.964 | 713.45 | -6.2034 |
| 19.909 | 762.55 | -4.8343 | 21.889 | 744.05 | -4.9029 | 22.952 | 721.81 | -5.5021 |
| 20.948 | 770.13 | -4.3048 | 22.983 | 752.43 | -4.3860 | 23.969 | 729.64 | -4.9120 |
| 21.921 | 776.93 | -3.9367 | 23.966 | 759.39 | -4.0181 | 25.132 | 738.13 | -4.3880 |
| 22.938 | 783.47 | -3.6239 | 25.089 | 766.69 | -3.6736 |  |  |  |
| 23.974 | 789.90 | -3.3852 |  |  |  |  |  |  |
| 25.064 | 796.30 | -3.1861 |  |  |  |  |  |  |

Table 6. Densities and Excess Molar Volumes for the Carbon Dioxide (1) + Ethanol (2) Mixture at Two Temperatures and $\mathrm{x}_{1}=0.7703$

| P/MPa | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3} \mathrm{~V} / \mathrm{Vm}^{3} \cdot \mathrm{~mol}^{-1}$ | $\mathrm{P} / \mathrm{MPa}$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3} \mathrm{~V} / \mathrm{Vm}^{3} \cdot \mathrm{~mol}^{-1}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~T}=313.16 \mathrm{~K}$ |  |  | $\mathrm{~T}=323.12 \mathrm{~K}$ |  |  |
| 11.033 | 797.49 | -7.2089 | 11.000 | 735.72 | -20.5978 |
| 12.000 | 806.31 | -5.5240 | 12.000 | 751.30 | -12.3188 |
| 13.000 | 815.04 | -4.4956 | 14.001 | 775.83 | -6.5808 |
| 14.001 | 822.80 | -3.7907 | 16.000 | 794.88 | -4.4794 |
| 16.000 | 836.92 | -2.9126 | 18.000 | 810.88 | -3.4085 |
| 18.000 | 849.25 | -2.3771 | 20.000 | 824.49 | -2.4476 |
| 20.000 | 860.16 | -2.0122 | 22.000 | 836.35 | -2.2940 |
| 22.004 | 870.16 | -1.7562 |  |  |  |
| 24.000 | 879.50 | -1.5788 |  |  |  |

Table 7. BWRS EoS Adjusted Parameters for Carbon Dioxide and Ethanol Pure Compounds

| parameter | $\mathrm{CO}_{2}$ | ethanol |
| :---: | ---: | ---: |
| $\mathrm{B}_{0}$ | $1.5853794 \times 10^{2}$ | $3.7496518 \times 10^{2}$ |
| $\mathrm{~A}_{0}$ | $9.565003 \times 10^{6}$ | $2.1436851 \times 10^{7}$ |
| $\mathrm{C}_{0}$ | $-9.8659274 \times 10^{11}$ | $-7.5497182 \times 10^{11}$ |
| $\mathrm{D}_{0}$ | $-3.3284313 \times 10^{14}$ | $-1.8105870 \times 10^{14}$ |
| $\mathrm{E}_{0}$ | $-3.5802836 \times 10^{16}$ | $-1.1269142 \times 10^{16}$ |
| b | $2.9336722 \times 10^{3}$ | $-8.8171575 \times 10^{1}$ |
| a | $-1.9972992 \times 10^{5}$ | $-5.8413063 \times 10^{6}$ |
| d | $7.9080832 \times 10^{7}$ | $5.7176131 \times 107$ |
| c | $-5.2968867 \times 10^{12}$ | $-3.2076228 \times 10^{12}$ |
| $\alpha$ | $3.1690487 \times 10^{7}$ | $-1.6988398 \times 10^{7}$ |
| u | $5.7381586 \times 10^{4}$ | $3.3266263 \times 10^{2}$ |

temperature using a simple polynomial function:

$$
\begin{equation*}
\tau_{\mathrm{vac}}{ }^{2}(\mathrm{~T})=\mathrm{a}+\mathrm{bT}+\mathrm{cT}^{2} \tag{5}
\end{equation*}
$$

To check the stability of the vibrating period of the tube under vacuum over a period of time (eight months), it was
measured at 313 K as reference before and after measurement campaigns of liquid densities of several al cohols, $\mathrm{CO}_{2}$, and their mixtures from 313 to 363 K and at pressures up to 25 MPa . After this, it was found that the periods could fluctuate within $\pm 5 \times 10^{-6} \mathrm{~ms}$ for the tube under vacuum and pure fluids and within $\pm 1 \times 10^{-5} \mathrm{~ms}$ for mixtures. It was found that the values issued from the nonclassical method overestimate the liquid densities, increasing two times the uncertainty in the full scale of the preceding results, ${ }^{5}$ and the final uncertainty in this case is $\pm 0.12 \%$ in densities. This is valid only in the range of densities reported in this work.

Pöhler and K iran ${ }^{13}$ have reported volumetric properties and excess volumes for $\mathrm{CO}_{2}+$ ethanol mixtures at four compositions, temperatures from 323 to 423 K , and pressures up to 70 MPa with the following estimated uncertainties: $\pm 0.5 \mathrm{~K} ; \pm 0.03 \mathrm{MPa} ; \pm 1.2 \%$ for densities.
In Figure 2 are plotted the densities of ethanol at 320 K up to 200 MPa from ref 14 , those at 322.70 K up to 25 MPa from ref 5, and the data reported at 323.0 K by Pöhler and Kiran. ${ }^{13}$ Zúñiga-Moreno and Galicia-Luna ${ }^{5}$ found good agreement for all isotherms between their data and those published by Takiguchi and Uematsu; ${ }^{14}$ the maximum relative deviation in densities is $\pm 0.2 \%$. In Figure 3 are presented the liquid densities of binary mixtures of carbon dioxide (1) and ethanol (2), reported in this work, at 323.12 $K$ and $x_{1}=0.7703$, and those published by Pöhler and Kiran, ${ }^{17}$ at 323.0 and $x_{1}=0.8$. The two sets of data agree well.

As shown in Figure 4, binary mixtures of $\mathrm{CO}_{2}+$ ethanol are more compressible than pure ethanol. Similar trends were found with those reported by Pöhler and Kiran; ${ }^{13}$ that is, the density of the mixture becomes more than that of


Figure 2. Liquid densities for ethanol: $\bigcirc$, Zuñiga-Moreno and Galicia-Luna, ${ }^{5}$ at 322.70 K ; $\nabla$, Pöhler and Kiran, ${ }^{13}$ at 323.0 K ; $\square$, Takiguchi and Uematsu, ${ }^{14}$ at 320.00 K .


Figure 3. Liquid densities of the binary mixtures of carbon dioxide (1) and ethanol (2) at 323 K : O , this work, at 323.12 K and $x_{1}=0.7703 ; \bullet$, Pöhler and Kiran, ${ }^{13}$ at 323.0 and $x_{1}=0.8$.


Figure 4. Pressure dependence of density for the binary mixtures of carbon dioxide (1) and ethanol (2) at 323 K (see Tables 4-7): literature data for pure ethanol at 323 K are from Zuñiga-M oreno and Galicia-Luna; ${ }^{5} \bullet, x_{1}=0.2317 ; O, x_{1}=0.4076 ; \nabla, x_{1}=0.5569 ;$ $\nabla, x_{1}=0.7703 ;$ ■, $x_{1}=0.0$.
pure ethanol, and each mixture shows a density crossover at a typical pressure.

The temperatures were selected taking into account the industrial applications of $\mathrm{CO}_{2}$, and of binary mixtures containing $\mathrm{CO}_{2}$ and alcohols, as a supercritical fluid for extracting components of natural products of Mexico.


Figure 5. Excess molar volumes $V^{E}$ versus $x$ and $x_{1}$ for carbon dioxide at 11 MPa and 323 K : $\bullet$, calculated molar volumes with the BWRS EoS ${ }^{12}$ for $\mathrm{CO}_{2}$ and ethanol (method A , this work); O , calculated molar volumes with the BWRS EoS ${ }^{12}$ for ethanol and the MBWRS EoS ${ }^{11}$ for $\mathrm{CO}_{2}$ (method B, this work); $\mathbf{\nabla}$, calculated molar volumes with the BWRS EoS ${ }^{12}$ for ethanol and the MBWRS $\mathrm{EoS}^{11}$ for $\mathrm{CO}_{2}$ (method B, Pholer and Kiran data).

Excess Volume. The excess molar volumes for the mixtures were determined using the following equation:

$$
\begin{equation*}
\mathrm{V}^{\mathrm{E}}=\mathrm{V}^{\mathrm{mix}}-\left(\mathrm{x}_{1} \mathrm{~V}_{1}+\mathrm{x}_{2} \mathrm{~V}_{2}\right) \tag{6}
\end{equation*}
$$

where $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$ represent the pure component volumes and $x_{1}$ and $x_{2}$ are the mole fractions of carbon dioxide and ethanol, respectively. The pure component molar volumes were cal culated with the BWRS equation of state reported by Starling ${ }^{12}$ using the parameters presented insideTable 7. In addition, molar volumes for $\mathrm{CO}_{2}$ were cal culated with the 32-term modified Benedict-Webb-Rubin (MBWRS-32) EoS proposed by Ely et al. ${ }^{11}$

To have a real comparison of the excess molar volumes data reported in this work with those published by Pholer and Kiran, ${ }^{13}$ and since they do not publish their calculated method, in this work the excess molar volumes were calculated using the two E oS mentioned above. The excess volume of mixtures presented in Table 2 in the third column (method A) for $\mathrm{CO}_{2}(1)+$ ethanol (2) at the sel ected temperature of 323 K were calculated using the BWRS equation of state reported by Starling ${ }^{12}$ using the parameters of Table 7. F urthermore, in the same table in column 6 are presented the calculated values of the excess molar volumes using the BWRS EoS ${ }^{12}$ for ethanol and the MBWRS-32 $\mathrm{EoS}^{11}$ for $\mathrm{CO}_{2}$ (method B).

The estimated uncertainty of the excess volumes for this system is not higher than $\pm 2.5 \%$. As shown in Figure 5 and in Table 2, the excess volumes of the $\mathrm{CO}_{2}+$ ethanol mixtures reported in this work at 323 K and those published by Pholer and Kiran ${ }^{13}$ agree well.

## Conclusions

Experimental determinations of densities were carried out at temperatures from 313 to 363 K and pressures up to 25 MPa for the carbon dioxide + ethanol mixtures at four compositions with an uncertainty lower than $\pm 0.05 \%$, using a vibrating tube densimeter DTV.

Excess volumes are reported for the carbon dioxide + ethanol mixtures at four compositions; the corresponding uncertainties do not exceed $\pm 2.5 \%$.

## Literature Cited

(1) Galicia-Luna, L. A.; Ortega-Rodríguez, A.; Richon, D. A new apparatus for fast determination of vapor-liquid equilibria of mixtures at high pressures. J. Chem. Eng. Data 2000, 45, 265271.
(2) Mendoza de Ia Cruz, J. L.; Galicia-Luna, L. A. High-Pressure Vapor Liquid Equilibria for the $\mathrm{CO}_{2}+$ Ethanol and $\mathrm{CO}_{2}+1-$ Propanol system from 322.36 to 391.96 K. ELDATA: Int. Electron. J. Phys.-Chem. Data 1999, 5, 157-164.
(3) Silva-Oliver, G.; Galicia-Luna, L. A. VLE near Critical Point and Critical Points of the $\mathrm{CO}_{2}+1$-butanol and $\mathrm{CO}_{2}+2$-butanol systems at temperatures from 324 to 432 K. Fluid Phase Equilib. 2001 182, 145-156.
(4) Silva-Oliver, G.; Galicia-Luna, L. A.; Sandler, S. I. VLE near Critical Point and Critical Points for the $\mathrm{CO}_{2}+1$-Pentanol and $\mathrm{CO}_{2}+2$-Pentanol Systems at Temperatures from 314 to 412 K and Pressures up to 18 MPa. Accepted for publication in Fluid Phase Equilib.
(5) Zúñiga-Moreno, A.; Galicia-Luna, L. A. Compressed liquid densities of ethanol and pentan-1-ol via a vibrating tube densimeter from 310 to 363 K and pressures up to 25 MPa . Accepted for publication in ELDATA: Int. Electron. J. Phys.-Chem. Data.
(6) Zúñiga-M oreno, A.; Galicia-Luna, L. A. Compressed liquid densities of Methanol and carbon dioxide via a vibrating tube densimeter from 310 to 363 K and pressures up to 25 MPa . Accepted for publication in ELDATA: Int. Electron. J. Phys.-Chem. Data.
(7) Zúñiga-Moreno, A.; Galicia-Luna, L. A. Densities of 1-Propanol and 2-Propanol via a vibrating tube densimeter from 310 to 363 K and pressures up to 25 MPa . J. Chem. Eng. Data, in press.
(8) Galicia-Luna, L. A.; Richon, D.; Renon, H. New Loading Technique for a vibrating Tube Densimeter and Measurements of Liquid Densities up to 39.5 MPa for Binary and Ternary Mixtures of the Carbon Dioxide-Methanol-Propane System. J. Chem Eng. Data 1994, 39 (3), 424-431.
(9) Haar, L.; Gallager, J . S.; Kell, G. S. A. A Thermodynamic surface for water: The formulation and computer programs. Natl. Bur. Stand., [Tech. Rep.] 1981.
(10) Span, R.; Lemmon, E. W.; J acobsen, R. T.; Wagner, W. A reference quality equation of state for nitrogen. Int. J. Thermophys. 1998, 19, 1121-1132.
(11) Ely, J. F.; Haynes, W. M.; Bain, B. C. Isochoric ( $\mathrm{p}, \mathrm{V}_{\mathrm{m}}, \mathrm{T}$ ) measurements on $\mathrm{CO}_{2}$ and on $\left(0.982 \mathrm{CO}_{2}+0.018 \mathrm{~N}_{2}\right)$ from 250 to 330 K at pressures to 35 MPa . J. Chem. Thermodyn. 1989, 21, 879-894.
(12) Starling, R. B.; Han, M. S. Thermo data refined for LPG: Mixtures. Hydrocarbon Process. 1972, May, 129-132.
(13) Pöhler, H.; Kiran, E. Volumetric properties of carbon dioxide + ethanol at high pressures. J. Chem. Eng. Data 1997, 42, 384388.
(14) Takiguchi, Y.; Uematsu, M. Densities for liquid ethanol in the temperature range from 310 K to 480 K at pressures up to 200 MPa. J. Chem. Thermodyn. 1996, 28, 7-16.

Received for review J anuary 17, 2001. Accepted October 24, 2001. The authors are grateful to CONACYT (Project 26432-A) and IPN for their financial support.

J E010012F


[^0]:    * To whom correspondence should be addressed. Mailing address: Prof. Luis A. Galicia-Luna, IPN-ESIQIE-Lab. de Termodinámica, APDO. Postal 75-099, Col. Lindavista, C. P. 07301, México, D. F. (México). E-mail: Iagalicia@dsi.com.mx. Telephone: (52) 5729-6000, ext 55133. Fax: (52) 5586-2728.

