# Isobaric Vapor-Liquid Equilibrium for the Ternary System o-Xylene + Nonane + Cyclohexanol 

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#### Abstract

Isobaric vapor-liquid equilibria (VLE) were measured for the system o-xylene + nonane + cyclohexanol and for two constituent binaries containing cyclohexanol at the pressures $26.66,53.33$, and 79.99 kPa . The new modified Wilson equation is proposed to better describe vapor-liquid equilibria (VLE) in binary and multicomponent systems. The equation takes into account the linear dependence of the difference of interaction energies $\lambda_{\mathrm{ij}}-\lambda_{\mathrm{ii}}$ on temperature and avoids the use of molar volumes. Correlation of binary isobaric VLE experimental data gave four coefficients that can describe VLE at different pressures and in a large boiling temperature region. It was found that VLE data for the ternary system o-xylene + nonane + cyclohexanol can be predicted by the modified Wilson equation.


## Introduction

Among two-parameter equations (Margules, van Laar, UNIQUAQ, UNIFAC), the Wilson equation ${ }^{1}$ is widely used. In the introduction of the Thermodynamics Data Center (Poland) collection, ${ }^{2}$ it has been confirmed that for al cohol + aliphatic hydrocarbon mixtures the Wilson equation gives the best results.

For description of vapor-liquid equilibria (VLE) binary isobaric experimental data, two Wilson parameters $\Lambda_{i j}$ are valid for an average boiling temperature $T$ interval used:

$$
\begin{equation*}
\Lambda_{\mathrm{ij}}=\frac{\mathrm{V}_{\mathrm{j}}}{V_{\mathrm{i}}} \exp \left[-\frac{\lambda_{\mathrm{ij}}-\lambda_{\mathrm{ij}}}{R T}\right] \tag{1}
\end{equation*}
$$

where $\mathrm{V}_{\mathrm{i}}$ and $\mathrm{V}_{\mathrm{j}}$ are the molar volumes of components i and j .

The other possibility is to calculate the $\lambda_{\mathrm{ij}}-\lambda_{\mathrm{ij}}$ values in the correlation procedure instead of $\Lambda_{\mathrm{ij}}$. In this case, for a binary system, $\lambda_{12}-\lambda_{11}$ and $\lambda_{21}-\lambda_{22}$ are regarded as constant parameters for VLE description.

In our previous paper ${ }^{3}$ we have shown that it is reasonable to consider the dependence of the parameter ( $\lambda_{\mathrm{ij}}-\lambda_{\mathrm{ii}}$ ) on temperature, as proposed earlier. ${ }^{4}$ The next equations for binary systems are given by

$$
\begin{align*}
& \Lambda_{12}=\frac{V_{2}}{V_{1}} \exp \left[-\frac{\left(m_{1}+n_{1} T\right)}{R T}\right]  \tag{2}\\
& \Lambda_{21}=\frac{V_{1}}{V_{2}} \exp \left[-\frac{\left(m_{2}+n_{2} T\right)}{R T}\right] \tag{3}
\end{align*}
$$

where $T$ is an actual boiling temperature measured at a chosen pressure and molar composition.

In an earlier paper, ${ }^{3}$ the VLE calculation, by means of these relationships, was successfully applied to the strongly nonideal system 1-nonyne +1 -propanol at five pressures.

In this article, we present simplified equations for $\Lambda_{\mathrm{ij}}$ instead of eqs 2 and 3 . These equations can describe VLE on the basis of isobaric or isothermal experimental data.
The vapor-liquid equilibrium for the ternary system o-xylene + nonane + cyclohexanol was measured in this
work, and for the obtained data, the new equations were tested. I sobaric VLE data at three pressures (26.66, 53.33, and 79.99 kPa ) are presented for this system and for two binaries containing cyd ohexanol. No VLE data were found for these systems in the literature. The vapor-liquid equilibium for 0 -xylene + nonane has been measured by us earlier. ${ }^{5}$ One set of isobaric data at the pressure 101.32 kPa for the system o-xylene + nonane is available. ${ }^{6}$
Azeotropic parameters were determined for the ternary system and two constituent binaries o-xylene + cyclohexanol and nonane + cyclohexanol. Those of o-xylene + nonane have been reported earlier. ${ }^{5}$

## Experimental Section

Materials. o-Xylene and nonane were of the same purity, greater than 99.5 and 99.8 mass $\%$, respectively, as reported in our earlier work. ${ }^{5}$ Cyclohexanol was dried with fresh ignited CaO and distilled at a subatmospheric pressure in a high-efficiency Teflon rotor-col umn. The final purity of cydohexanol determined by GLC (flame ionization detector, glass tube col umn with Chromaton N-AW-DMCS and $5 \%$ DC550) was greater than 99.5 mass $\%$. In Table 1, the densities measured with a capillary pycnometer, refractive indices measured with a calibrated Abbé refractometer, and boiling temperatures are compared with those given in the literature.
Apparatus and Procedure. The T-x results were obtained by the semi-mi croebulliometer described by us in detail. 5,7 Uncertainties of the boiling temperature were estimated to be less than 0.05 K . The amount of mixtures investigated was less than 1 mL . Uncertainties of mole fraction composition of a liquid mixture (x) were estimated to be less than $5 \times 10^{-4}$.

## Modified Expressions for Wilson Parameters

By setting in eqs 2 and 3

$$
\begin{gather*}
a_{i j}=-\frac{n_{i}}{R}+\ln \frac{V_{j}}{V_{i}}  \tag{4}\\
b_{i j}=-\frac{m_{i}}{R} \tag{5}
\end{gather*}
$$

Table 1. Densities d, Refractive Indices $n_{D}$, and Normal Boiling Points $T_{b}$ of Pure Components

| component | $\mathrm{d} / \mathrm{kg} \cdot \mathrm{m}^{-3}$ |  |  | $\mathrm{n}_{\mathrm{D}}$ |  |  | Tb/K |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | T/K | obs | lit. | T/K | obs | lit. | obs | lit. |
| o-xylene | 293.15 | 880.1 | $880.1^{\text {a }}$ | 293.15 | 1.5054 | $1.50545^{\text {a }}$ | 417.53 | $417.55{ }^{\text {b }}$ |
| nonane | 293.15 | 717.6 | $717.72^{\text {a }}$ | 293.15 | 1.4055 | $1.40542^{\text {a }}$ | 423.97 | $423.95{ }^{\text {b }}$ |
| cyclohexanol | 303.15 | 941.6 | $941.6{ }^{\text {b }}$ | 303.15 | 1.4621 | $1.462 \mathrm{~g}^{\text {b }}$ | 433.89 | $434.25{ }^{\text {b }}$ |

a TRC Thermodynamic Tables. ${ }^{8}$ b Dean. ${ }^{9}$

Table 2. Isobaric Vapor-Liquid Equilibrium Data: Liquid-Phase Mole Fraction $x_{1}$ and Boiling Temperatures T in Binary Systems

|  | $\mathrm{T} / \mathrm{K}$ at pressure $\mathrm{P} / \mathrm{kPa}$ |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{x}_{1}$ | $\mathrm{P}=26.66$ | $\mathrm{P}=53.33$ | $\mathrm{P}=79.99$ |
|  | o-Xylene $(1)+$ Cyclohexanol (2) |  |  |
| 0.000 | 394.86 | 413.79 | 426.16 |
| 0.173 | 384.71 | 405.21 | 418.44 |
| 0.184 | 385.09 | 405.36 | 418.52 |
| 0.260 | 381.67 | 402.44 | 415.91 |
| 0.332 | 379.59 | 400.51 | 414.05 |
| 0.421 | 377.72 | 398.73 | 412.35 |
| 0.508 | 376.37 | 397.40 | 411.05 |
| 0.596 | 375.36 | 396.45 | 410.15 |
| 0.614 | 375.04 | 396.14 | 409.85 |
| 0.697 | 374.28 | 395.38 | 409.13 |
| 0.797 | 373.55 | 394.78 | 408.60 |
| 0.898 | 373.15 | 394.50 | 408.42 |
| 1.000 | 373.40 | 394.86 | 408.82 |
|  | Nonane |  |  |
| 0.000 | 394.86 | 413 |  |
| 0.119 | 384.75 | 404.99 | 426.16 |
| 0.225 | 380.56 | 401.04 | 418.06 |
| 0.317 | 378.75 | 399.18 | 414.27 |
| 0.427 | 377.75 | 398.10 | 412.44 |
| 0.503 | 377.14 | 397.52 | 411.37 |
| 0.600 | 376.54 | 397.04 | 410.82 |
| 0.651 | 376.44 | 396.90 | 410.46 |
| 0.704 | 376.40 | 396.93 | 410.29 |
| 0.749 | 376.37 | 397.05 | 410.39 |
| 0.835 | 376.48 | 397.36 | 410.62 |
| 0.920 | 377.47 | 398.74 | 411.08 |
| 1.000 | 379.88 | 401.28 | 412.70 |
|  |  | 415.26 |  |

we obtain

$$
\begin{equation*}
\Lambda_{i j}=\exp \left[a_{i j}+\frac{b_{i j}}{T}\right] \tag{6}
\end{equation*}
$$

and for binary systems

$$
\begin{align*}
& \Lambda_{12}=\exp \left[a_{12}+\frac{b_{12}}{T}\right]  \tag{7}\\
& \Lambda_{21}=\exp \left[a_{21}+\frac{b_{21}}{T}\right] \tag{8}
\end{align*}
$$

As seen from eqs 4 and 5 , the parameters $a_{12}, b_{12}, a_{21}$, and $b_{21}$ simplify calculation procedures, because they include molar volumes $V_{1}$ and $V_{2}$ and the gas constant $R$. The ratio of molar volumes $\mathrm{V}_{\mathrm{j}} N_{\mathrm{i}}$ usually does not depend considerably on temperature, but eqs 7 and 8 take into account its temperature dependence.

Consequently, the Wilson equation with two parameters at a given pressure could be replaced with a four-parameter equation. These parameters describe VLE in a large boiling temperature region for simultaneous use at different chosen pressures in isobaric experiments. This means that actually the number of required parameters decreases. For example, as we have shown, VLE of the system 1-nonyne + 1-propanol system can be described with four parameters

Table 3. Fitted Coefficients of the Modified Wilson Equation (Eqs 7 and 8) and Calculated Absolute Mean Errors ( $\Delta \mathrm{P}$ ) and Standard Deviations ( $\sigma \mathrm{P}$ ) of Pressure for Binary Systems

| system <br> $(1)+(2)$ | $\mathrm{a}_{12}$ | $\mathrm{~b}_{12}$ | $\mathrm{a}_{21}$ | $\mathrm{~b}_{21}$ | $\Delta \mathrm{P} / \%$ | $\mathrm{kPa} /$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| o-xylene + <br> cyclo- | 0.21256 | -129.163 | 0.21256 | -129.163 | 0.294 | 0.22 |
| hexanol <br> nonane + <br> cyclo- <br> hexanol | 0.05676 | -314.903 | 3.58544 | -1774.377 | 0.203 | 0.15 |
| -xylene + <br> nonane | 0.14382 | 41.904 | 0.23169 | -315.517 | 0.094 | 0.08 |

Table 4. Coefficients for the Antoine Vapor Pressure Equation (kPa, K) (Eq 12)

| component | $\mathrm{A}_{\mathrm{i}}$ | $\mathrm{B}_{\mathrm{i}}$ | $\mathrm{C}_{\mathrm{i}}$ | temp region |
| :--- | :---: | :---: | :---: | :---: |
| o-xylene | 14.04369 | 3352.595 | -61.832 | (373 to 418) K |
| nonane | 13.85459 | 3224.816 | -74.824 | (380 to 424) K |
| cyclohexanol | 13.72185 | 2778.058 | -128.7243 | (395 to 426) K |

Table 5. Azeotropic Boiling Temperatures $\mathrm{T}_{\mathrm{az}}$ and Compositions $X_{1}{ }^{\text {az }}$ of Binary Systems versus Pressure $\mathbf{P}$

| P/kPa | o-xylene (1) + cyclohexanol (2) |  | nonane (1) + cyclohexanol (2) |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{T}_{\mathrm{az}} / \mathrm{K}$ | $\mathrm{x}_{1}{ }^{\text {az }}$ | $\mathrm{T}_{\mathrm{az}} / \mathrm{K}$ | $\mathrm{x}_{1}{ }^{\text {az }}$ |
| 26.66 | 373.1 | 0.945 | 376.3 | 0.742 |
| 53.33 | 394.4 | 0.905 | 396.9 | 0.695 |
| 79.99 | 408.3 | 0.875 | 410.2 | 0.665 |

at five pressures in a large temperature range from 324.98 to 424.21 K. ${ }^{3}$

For practical calculation of the parameters $\mathrm{a}_{12}, \mathrm{~b}_{12}, \mathrm{a}_{21}$, and $b_{21}$ in the correlation procedure, different iteration methods can be used. As we have demonstrated, ${ }^{3}$ the Newton iteration method is recommended because analytical expressions of partial derivatives of the first and second order are easy to find. Convergence is rapid, and the set of initial approximations $0,0,0,0$ or $1,0,1,0$ can be used.

The prediction of VLE in multicomponent systems can be realized on the basis of binary parameters. F or example, the values of activity coefficients in ternary systems can be expressed as

$$
\begin{equation*}
\gamma_{\mathrm{i}}=\exp \left[1-\ln \left(\sum_{\mathrm{j}=1}^{3} \mathrm{x}_{\mathrm{j}} \Lambda_{\mathrm{ij}}\right)-\sum_{\mathrm{k}=1}^{3} \frac{\mathrm{x}_{\mathrm{k}} \Lambda_{\mathrm{ki}}}{\sum_{\mathrm{j}=1}^{3} \mathrm{x}_{\mathrm{j}} \Lambda_{\mathrm{kj}}}\right] \tag{9}
\end{equation*}
$$

and the Gibbs energy $\mathrm{G}^{\mathrm{E}}$ as

$$
\begin{equation*}
\mathrm{G}^{\mathrm{E}}=-\mathrm{RT}\left(\sum_{\mathrm{i}=1}^{3} \mathrm{x}_{\mathrm{i}} \ln \sum_{\mathrm{j}=1}^{3} \mathrm{x}_{\mathrm{j}} \Lambda_{\mathrm{ij}}\right) \tag{10}
\end{equation*}
$$

where $x_{i}$ is the mole fraction of component $i$.
For predicting VLE in ternary systems, values of 12 parameters must be previously found for the binaries.

Table 6. Experimental Vapor-Liquid Equilibria Data for the Ternary System o-Xylene (1) + Nonane (2) + Cyclohexanol (3) at Three Pressures and Values Calculated by Using Eqs 7 and 8 of Activity Coefficients $\gamma_{1}, \gamma_{2}$, and $\gamma_{3}$, Vapor Mole Fractions $y_{1}$ and $y_{2}$, Excess Gibbs Energy $G^{E}$, Pressure $P_{\text {calc }}$, Boiling Temperature $T_{\text {calc }}$, and Differences in Pressure $\Delta P$ and Boiling Temperature $\Delta T$

| experimental data |  |  | calculated values |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| İquid mole fraction |  | boiling temp | activity coefficient |  |  | vapor mole fraction |  | $\frac{\text { Gibbs energy }}{\mathrm{G}^{\mathrm{E}} / J \cdot \mathrm{~mol}^{-1}}$ | $\frac{\text { pressure }}{\mathrm{P}_{\text {cald } / \mathrm{KPa}}}$ | $\Delta \mathrm{P} / \mathrm{kPa}$ | $\frac{\text { boiling temp }}{\mathrm{T}_{\text {cald }} / \mathrm{K}}$ | $\Delta \mathrm{T} / \mathrm{K}$ |
| $\mathrm{X}_{1}$ | $\mathrm{X}_{2}$ | $\mathrm{T}_{\text {exp }} / \mathrm{K}$ | $\gamma_{1}$ | $\gamma_{2}$ | $\gamma_{3}$ | $\mathrm{y}_{1}$ | $\mathrm{y}_{2}$ |  |  |  |  |  |
| $\mathrm{P}=79.99 \mathrm{kPa}$ |  |  |  |  |  |  |  |  |  |  |  |  |
| 0.254 | 0.254 | 410.00 | 1.185 | 1.508 | 1.245 | 0.311 | 0.330 | 255.5 | 79.95 | -0.04 | 410.02 | 0.02 |
| 0.409 | 0.408 | 408.53 | 1.059 | 1.134 | 1.876 | 0.429 | 0.381 | 189.5 | 80.15 | 0.16 | 408.46 | -0.07 |
| 0.186 | 0.185 | 411.85 | 1.289 | 1.790 | 1.112 | 0.261 | 0.301 | 226.1 | 80.06 | 0.07 | 411.82 | -0.03 |
| 0.563 | 0.281 | 408.13 | 1.036 | 1.174 | 1.864 | 0.572 | 0.269 | 162.2 | 80.05 | 0.06 | 408.11 | -0.02 |
| 0.409 | 0.204 | 409.05 | 1.122 | 1.427 | 1.342 | 0.462 | 0.244 | 233.3 | 79.95 | -0.04 | 409.07 | 0.02 |
| 0.197 | 0.099 | 413.73 | 1.367 | 2.072 | 1.063 | 0.307 | 0.196 | 176.7 | 80.19 | 0.20 | 413.65 | -0.08 |
| 0.330 | 0.165 | 410.31 | 1.196 | 1.620 | 1.201 | 0.410 | 0.232 | 231.1 | 80.16 | 0.17 | 410.24 | -0.07 |
| 0.484 | 0.344 | 408.66 | 1.047 | 1.153 | 1.858 | 0.499 | 0.325 | 177.7 | 80.91 | 0.92 | 408.27 | -0.39 |
| 0.712 | 0.192 | 408.16 | 1.016 | 1.191 | 2.001 | 0.709 | 0.187 | 111.7 | 80.18 | 0.19 | 408.08 | -0.08 |
| 0.208 | 0.528 | 409.34 | 1.099 | 1.141 | 1.745 | 0.231 | 0.507 | 236.3 | 80.35 | 0.36 | 409.19 | -0.15 |
| 0.400 | 0.400 | 408.45 | 1.062 | 1.147 | 1.821 | 0.420 | 0.378 | 198.5 | 79.98 | -0.01 | 408.46 | 0.01 |
| 0.571 | 0.286 | 408.21 | 1.034 | 1.164 | 1.909 | 0.579 | 0.272 | 154.9 | 80.20 | 0.21 | 408.12 | -0.09 |
| 0.250 | 0.500 | 408.91 | 1.090 | 1.142 | 1.761 | 0.274 | 0.478 | 229.3 | 79.81 | -0.18 | 408.99 | 0.08 |
| 0.334 | 0.333 | 409.00 | 1.101 | 1.277 | 1.486 | 0.368 | 0.354 | 245.4 | 80.39 | 0.40 | 408.84 | -0.16 |
| 0.572 | 0.142 | 408.40 | 1.070 | 1.376 | 1.469 | 0.606 | 0.161 | 194.3 | 79.84 | -0.15 | 408.46 | 0.06 |
| 0.287 | 0.142 | 410.78 | 1.248 | 1.755 | 1.144 | 0.382 | 0.222 | 220.1 | 79.20 | -0.79 | 411.10 | 0.32 |
| 0.200 | 0.400 | 409.33 | 1.140 | 1.302 | 1.419 | 0.232 | 0.442 | 271.5 | 79.63 | -0.36 | 409.48 | 0.15 |
| 0.630 | 0.185 | 408.06 | 1.035 | 1.253 | 1.715 | 0.638 | 0.189 | 163.0 | 80.01 | 0.02 | 408.05 | -0.01 |
| 0.774 | 0.113 | 408.16 | 1.014 | 1.258 | 1.881 | 0.768 | 0.116 | 107.9 | 80.22 | 0.23 | 408.06 | -0.10 |
| $\mathrm{P}=53.33 \mathrm{kPa}$ |  |  |  |  |  |  |  |  |  |  |  |  |
| 0.254 | 0.254 | 396.45 | 1.219 | 1.569 | 1.267 | 0.325 | 0.344 | 280.9 | 53.32 | -0.01 | 396.45 | 0.00 |
| 0.409 | 0.408 | 394.76 | 1.068 | 1.148 | 2.006 | 0.435 | 0.382 | 210.6 | 53.40 | 0.07 | 394.72 | -0.04 |
| 0.186 | 0.185 | 398.38 | 1.338 | 1.886 | 1.129 | 0.276 | 0.318 | 247.7 | 53.47 | 0.14 | 398.30 | -0.08 |
| 0.563 | 0.281 | 394.31 | 1.043 | 1.191 | 2.003 | 0.577 | 0.270 | 181.0 | 53.34 | 0.01 | 394.31 | -0.00 |
| 0.409 | 0.204 | 395.42 | 1.144 | 1.475 | 1.378 | 0.476 | 0.251 | 258.6 | 53.33 | 0.00 | 395.42 | 0.00 |
| 0.197 | 0.099 | 400.21 | 1.426 | 2.205 | 1.068 | 0.329 | 0.211 | 194.4 | 53.46 | 0.13 | 400.13 | -0.08 |
| 0.330 | 0.165 | 396.69 | 1.230 | 1.693 | 1.219 | 0.428 | 0.242 | 255.3 | 53.45 | 0.12 | 396.62 | -0.07 |
| 0.484 | 0.344 | 394.78 | 1.055 | 1.169 | 1.991 | 0.505 | 0.326 | 198.1 | 53.82 | 0.49 | 394.50 | -0.28 |
| 0.712 | 0.192 | 394.25 | 1.019 | 1.209 | 2.190 | 0.711 | 0.186 | 125.2 | 53.43 | 0.10 | 394.19 | -0.06 |
| 0.208 | 0.528 | 395.77 | 1.115 | 1.159 | 1.835 | 0.237 | 0.514 | 261.0 | 53.65 | 0.32 | 395.58 | -0.19 |
| 0.400 | 0.400 | 394.71 | 1.072 | 1.163 | 1.939 | 0.427 | 0.380 | 220.5 | 53.29 | -0.04 | 394.73 | 0.02 |
| 0.571 | 0.286 | 394.40 | 1.040 | 1.180 | 2.060 | 0.584 | 0.272 | 172.9 | 53.49 | 0.16 | 394.31 | -0.09 |
| 0.250 | 0.500 | 395.27 | 1.106 | 1.159 | 1.856 | 0.281 | 0.483 | 253.6 | 53.18 | -0.15 | 395.35 | 0.08 |
| 0.334 | 0.333 | 395.41 | 1.121 | 1.309 | 1.539 | 0.378 | 0.362 | 271.3 | 53.66 | 0.33 | 395.22 | -0.19 |
| 0.572 | 0.142 | 394.68 | 1.084 | 1.417 | 1.529 | 0.618 | 0.164 | 217.2 | 53.23 | 0.10 | 394.74 | 0.06 |
| 0.287 | 0.142 | 397.23 | 1.289 | 1.845 | 1.156 | 0.401 | 0.234 | 242.7 | 52.84 | -0.49 | 397.51 | 0.28 |
| 0.200 | 0.400 | 395.81 | 1.166 | 1.339 | 1.458 | 0.241 | 0.455 | 298.4 | 53.08 | -0.25 | 395.95 | 0.14 |
| 0.630 | 0.185 | 394.26 | 1.042 | 1.278 | 1.824 | 0.645 | 0.190 | 182.6 | 53.33 | 0.00 | 394.26 | 0.00 |
| 0.774 | 0.113 | 394.26 | 1.017 | 1.283 | 2.043 | 0.771 | 0.116 | 121.7 | 53.45 | 0.12 | 394.18 | -0.08 |
| $\mathrm{P}=26.66 \mathrm{kPa}$ |  |  |  |  |  |  |  |  |  |  |  |  |
| 0.254 | 0.254 | 375.66 | 1.276 | 1.666 | 1.297 | 0.351 | $0.365$ | 319.4 | 26.62 | -0.04 | 375.70 | 0.04 |
| 0.409 | 0.408 | 373.68 | 1.086 | 1.172 | 2.218 | 0.450 | 0.385 | 244.1 | 26.58 | -0.08 | 373.76 | 0.08 |
| 0.186 | 0.185 | 377.61 | 1.420 | 2.040 | 1.141 | 0.304 | 0.348 | 280.2 | 26.71 | 0.05 | 377.57 | -0.04 |
| 0.563 | 0.281 | 373.19 | 1.055 | 1.220 | 2.235 | 0.591 | 0.271 | 211.1 | 26.61 | -0.05 | 373.25 | 0.06 |
| 0.409 | 0.204 | 374.51 | 1.183 | 1.555 | 1.431 | 0.504 | 0.263 | 297.5 | 26.62 | -0.04 | 374.55 | 0.04 |
| 0.197 | 0.099 | 379.34 | 1.523 | 2.423 | 1.075 | 0.367 | 0.236 | 221.0 | 26.62 | -0.04 | 379.38 | 0.04 |
| 0.330 | 0.165 | 375.83 | 1.288 | 1.811 | 1.245 | 0.461 | 0.259 | 292.0 | 26.72 | 0.06 | 375.77 | -0.06 |
| 0.484 | 0.344 | 373.54 | 1.070 | 1.195 | 2.210 | 0.519 | 0.328 | 230.4 | 26.71 | 0.05 | 373.49 | -0.05 |
| 0.712 | 0.192 | 372.99 | 1.025 | 1.238 | 2.523 | 0.719 | 0.186 | 147.1 | 26.67 | 0.01 | 372.98 | -0.01 |
| 0.208 | 0.528 | 374.95 | 1.145 | 1.190 | 1.973 | 0.250 | 0.526 | 299.4 | 26.75 | 0.09 | 374.86 | -0.09 |
| 0.400 | 0.400 | 373.70 | 1.091 | 1.189 | 2.126 | 0.443 | 0.384 | 255.1 | 26.55 | -0.11 | 373.81 | 0.11 |
| 0.571 | 0.286 | 373.21 | 1.051 | 1.206 | 2.314 | 0.596 | 0.273 | 201.8 | 26.65 | -0.01 | 373.22 | 0.01 |
| 0.250 | 0.500 | 374.41 | 1.133 | 1.189 | 2.004 | 0.295 | 0.493 | 291.4 | 26.49 | -0.17 | 374.58 | 0.17 |
| 0.334 | 0.333 | 374.59 | 1.155 | 1.362 | 1.618 | 0.399 | 0.374 | 311.1 | 26.82 | 0.16 | 374.43 | -0.16 |
| 0.572 | 0.142 | 373.63 | 1.108 | 1.484 | 1.621 | 0.642 | 0.170 | 253.0 | 26.54 | -0.12 | 373.75 | 0.12 |
| 0.287 | 0.142 | 376.23 | 1.359 | 1.992 | 1.173 | 0.437 | 0.253 | 277.0 | 26.23 | -0.43 | 376.66 | 0.43 |
| 0.200 | 0.400 | 375.09 | 1.212 | 1.399 | 1.516 | 0.259 | 0.477 | 339.2 | 26.46 | -0.20 | 375.30 | 0.21 |
| 0.630 | 0.185 | 373.15 | 1.055 | 1.320 | 2.003 | 0.660 | 0.193 | 213.7 | 26.61 | -0.05 | 373.20 | 0.05 |
| 0.774 | 0.113 | 372.98 | 1.022 | 1.324 | 2.323 | 0.780 | 0.117 | 144.1 | 26.67 | 0.01 | 372.98 | 0.00 |

## Results and Discussion

In Table 2, the liquid-phase mole fraction $x_{1}$ and boiling temperature measurements at the pressures 26.66, 53.33, and 79.99 kPa for binary systems are presented. Table 3 presents the correlation results of $T-x$ data for the systems o-xylene + cyclohexanol, nonane + cyclohexanol, and earlier investigation ${ }^{5}$ of o-xylene + nonane, together with
coefficients of the modified Wilson equation (eqs 7 and 8). The standard deviation is expressed as

$$
\begin{equation*}
\sigma \mathrm{P}=\left[\left\{\sum\left(\mathrm{P}_{\text {calc }}-\mathrm{P}_{\text {exp }}\right)^{2}\right\} /(\mathrm{N}-\mathrm{n})\right]^{1 / 2} \tag{11}
\end{equation*}
$$

where N is the number of experiments and n is the number of coefficients $(\mathrm{n}=4)$ found.

The vapor pressures of pure components were cal culated by the Antoine equation

$$
\begin{equation*}
\ln \left(P_{i}^{\circ} / k P a\right)=A_{i}-\frac{B_{i}}{T / K+C_{i}} \tag{12}
\end{equation*}
$$

where $A_{i}, B_{i}$, and $C_{i}$ and the used temperature regions are reported in Table 4. For o-xylene and nonane the coefficients of the Antoine equation have been published earlier; ${ }^{5}$ for the calculation of coefficients for cycl ohexanol, the experimental data of this work were used. Calculated vapor pressures are in good agreement with literature data. ${ }^{9}$

Each binary system exhibits a minimum boiling azeotrope. The azeotropic points have been determined from the function

$$
\begin{equation*}
\alpha_{12}=\frac{y_{1} / y_{2}}{x_{1} / x_{2}} \tag{13}
\end{equation*}
$$

where $y_{i}$ is the mole fraction of component $i$ in the vapor phase, calculated by the modified Wilson equation and solving for $\alpha_{12}=1$. Azeotropic compositions $x^{a z}$, boiling temperatures $\mathrm{T}_{\mathrm{az}}$, and pressures are presented in Table 5. The azeotropic data for o-xylene + cyclohexanol at 101.33 kPa are given in the literature, ${ }^{10}$ and those at 101.32, 13.33, and 1.33 kPa were reported by Garber et al. ${ }^{11}$

In Table 6 the isobaric VLE data for the ternary system are compared with correlation results obtained by the modified Wilson equation. We have considered ideal behavior for the vapor phase; the error in the calculation of vapor composition can be estimated to be less than 0.002 . Calculations were made using the values of coefficients for three constituent binaries given in Table 3. The mean absolute relative error for all three pressures was equal to $0.32 \%$. Calculation of VLE for the ternary system in the boiling temperature region ( 373 to 414 K ) leads to nearly perfect agreement with experimental data, as seen from differences between experimental and calculated values of pressure and temperature.

The ternary system exhibits a minimum boiling azeotrope whose composition at three pressures was determined by the minimization of the function

$$
\begin{equation*}
\left(\alpha_{\mathrm{ij}}-1\right)+\left(\alpha_{\mathrm{ik}}-1\right) \Longrightarrow \min \tag{14}
\end{equation*}
$$

The parameters of the ternary azeotrope o-xylene + nonane + cyclohexanol obtained at three pressures are given in Table 7.

Table 7. Azeotropic Boiling Temperatures $T_{a z}$ and Compositions $x_{i}{ }^{\text {az }}$ of the Ternary System o-Xylene (1) + Nonane (2) + Cyclohexanol (3) versus Pressure $P$

| $\mathrm{P} / \mathrm{kPa}$ | $\mathrm{T}_{\mathrm{az}} / \mathrm{K}$ | $\mathrm{x}_{1}{ }^{\text {az }}$ | $\mathrm{x}_{2}{ }^{\mathrm{az}}$ |
| :---: | :---: | :---: | :---: |
| 26.66 | 372.94 | 0.765 | 0.142 |
| 53.33 | 394.15 | 0.715 | 0.163 |
| 79.99 | 408.01 | 0.685 | 0.175 |

As seen from data obtained for the ternary system, the modified Wilson equation gives a good correlation in a large boiling temperature range, simultaneously taking into account all experiments carried out at different pressures. Evidently, a better agreement will be achieved also between VLE and excess enthalpy data, usually obtained at different temperatures. ${ }^{12}$

## Literature Cited

(1) Wilson, G. M. Vapor-Liquid Equilibrium. XI. New Expression for Excess Free Energy of Mixing. J. Am. Chem. Soc. 1964, 86, 127-130.
(2) Góral, M.; Maczyński, A.; Bok, A.; Oracz, P.; Skrzecz, A. VaporLiquid Equilibria. Volume 4. Alcohols + Nonaliphatic Hydrocarbons; Thermodynamics Data Center: Warsaw, Poland, 1998.
(3) Siimer, E.; Grintchak, M.; Kuus, M.; Kudryavtseva, L. Use of the Modified Wilson Equation for Description of Vapor-Liquid Equilibrium in the System 1-N onyne-1-Propanol. Thermochim. Acta 1989, 140, 49-58.
(4) Nagata, I. Calculation of Vapor-Liquid Equilibrium Data in Binary and Ternary Systems Using the Wilson Equation. Kagaku Kogaku 1969, 33, 263-267.
(5) Kirss, H.; Siimer, E.; Kuus, M.; Kudryavtseva, L. I sobaric VaporLiquid Equilibria in the System o-Xylene + Amyl Acetate + Nonane. J. Chem. Eng. Data 2001, 46, 147-150.
(6) Kukharenok, I. S.; Stepanova, E. J .; Kharisov, M. A. Study of Vapor-Liquid Equilibrium for o-Xylene + n-N onane System. Zh. Prikl. Khim. 1986, 59, 716-717.
(7) Mihkelson, V.; Kirss, H.; Kudryavtseva, L.; Eisen, O. Vapor-Liquid Equilibrium T-x Measurements by a Semi-Micro Method. Fluid Phase Equilib. 1977/78, 1, 201-209.
(8) TRC Databases for Chemistry and Engineering. Thermodynamic Tables. Version 1996-2S; Thermodynamic Research Center, Texas A \& M University System: College Station, TX, 1996.
(9) Dean, J. A. Lange's Handbook of Chemistry, 14th ed.; McGraw Hill: New York, 1992.
(10) Lecat. Ann. Soc. Sci. Bruxelles, Ser. 2 1928, 48B, 54.
(11) Garber, Yu. N.; Aleinikova, L. I.; Shashkov, Yu. I. Azeotropes of Some I somers with Near Boiling Temperatures. Zh. Prikl. Khim. 1972, 45, 572-574.
(12) Siimer, E.; Kirss, H.; Kuus, M.; Kudryavtseva, L. Excess Enthalpies for the Systems o-Xylene + Cyclohexanol + Nonane at 298.15 and 318.15 K and 3-M ethylphenol + 1-Hexanol + Heptane at 298.15 K and for Constituent Binaries. J. Chem. Eng. Data 1997, 42, 619-622.

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