# Densities of Carbon Dioxide + Methanol Mixtures at Temperatures from 313.2 to 323.2 K and at Pressures from $\mathbf{1 0}$ to $\mathbf{2 0} \mathbf{~ M P a}$ 

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#### Abstract

Densities of carbon dioxide (1) + methanol (2) mixtures were measured with a variable-volume static type of apparatus at three temperatures (313.2, 318.2, and 323.2 K ) over a range of pressures (10 to 20 MPa ) for methanol-rich mole fractions ( $\mathrm{x}_{2}>0.257$ ). Molar volumes could be correlated to within about $\pm 0.1 \mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1}$ by combining a Redlich-Kister expression with a Tait type of equation.


## Introduction

The addition of compressed gases to polar liquids leads to an enhancement in the fluid properties such as viscosity, diffusion coefficient, and density and this effect is being studied for new chromatographic applications ${ }^{1}$ and for particle design with gas antisol vent techniques. ${ }^{2}$ Methanol and carbon dioxide are two of the most widely used solvent pairs and, thus, properties of these mixtures are of great interest. Some of the studies that have been made on methanol $-\mathrm{CO}_{2}$ systems include Frank et al. ${ }^{3}$ who measured diffusion coefficients and viscosities, Dai et al., ${ }^{4}$ who measured excess enthalpies, and $Y$ eo et al., ${ }^{5}$ who measured critical properties. Bezanehtak et al. ${ }^{6}$ summarize vaporliquid equilibria of methanol $-\mathrm{CO}_{2}$ systems. Densities at various compositions and temperatures of methanol in the presence of carbon dioxide have been measured by Roškar et al., ${ }^{7}$ Chang et al., ${ }^{8}$ Galicia-Luna et al.,9,10 and Goldfarb et al. ${ }^{11}$ We have begun to measure dielectric spectra of methanol $-\mathrm{CO}_{2}$ mixtures, ${ }^{12}$ and in the data reduction, the mixture density is needed. As a result, we have measured densities of methanol $-\mathrm{CO}_{2}$ mixtures at temperatures from 313.2 K to 323.2 K at pressures from 10 MPa to 20 MPa with emphasis on compositions in the methanol-rich region. In this work, our objective is to report on our methanol$\mathrm{CO}_{2}$ density measurements and to provide a suitable correlating equation for the data.

## Experimental Section

Materials. Anhydrous methanol (99.8\%) and water (HPLC-grade) were obtained from Wako Pure Chemicals (Osaka) and were handled to avoid contamination with air and moisture. Methanol purity was checked with gas chromatography. $\mathrm{CO}_{2}$ (99.99\%) was obtained Nihon Sanso (Sendai) and was dried by passing the gas through a column of silica gel and then filtered with a $0.5-\mu \mathrm{m}$ sintered filter.

Apparatus. The apparatus used for the density measurements was developed in our research on dielectric spectra and uses a vibrating tube densimeter (model DMA 512 P and DMA 60, Anton Paar, Graz). ${ }^{12,13}$ The vibration period of the tube and its contents are proportional to the square root of its mass times an instrument constant that

[^0]is determined by measurement of the vibration period for known reference fluids at given conditions of temperature and pressure. The cal ibration procedure is described in the next section. The apparatus consisted of a variable volume ( $\approx 110 \mathrm{~cm}^{3}$ ) static system in which a magnetic pump was used to circulate $\mathrm{CO}_{2}$ and methanol mixtures through the densimeter until equilibrium was reached. The entire apparatus was enclosed in a constant temperature forced convection air bath (model FV-450, Advantec, Tokyo) in which temperature was controlled to within $\pm 0.1 \mathrm{~K}$. Further details are given in ref 13.
Temperature was measured inside the system and outside of the system with a three-wire platinum resistance thermometer (PRT) (model TF-A31, K eyence, Osaka) and a four-wire PRT (model RMB-100SY02, Yamari, Osaka), respectively. Accuracy of the temperature probes was confirmed within the system by comparison with a secondary temperature standard that was NIST traceable to 0.01 K. Temperature gradients in the system were no greater than 0.05 K . Pressure of the system was measured with a digital sensor (model SPX-G, Sokken, Tokyo) to an accuracy of 0.05 MPa . Accuracy of the pressure sensor was confirmed by comparison with a dead weight tester that was accurate to 0.5 kPa . Temperatures and pressures reported are estimated to have reproducibilities of $\pm 0.12 \mathrm{~K}$ and $\pm 0.07$ MPa , respectively, due to gradual temperature and pressure cycling of the system. Composition of the system was determined by trapping the entire system contents in a $125-\mathrm{cm}^{3}$ bomb with liquid nitrogen that was followed by weighing the loaded substances before and after slow depressurization into a second trap filled with water. Compositions reported are estimated to be accurate to 0.005 in mole fraction. Replicate measurements and some analyses are given in the discussion.

Calibration. In this work, air, water, and methanol were used as the reference fluids. Air was used as a reference fluid at atmospheric pressure with properties being determined from the Kyushu University physical property package PROPATH. ${ }^{14}$ Pure water and pure methanol were used as reference fluids at pressures up to 20 MPa with properties being determined from the IAPWS95 formulation of Pru $\beta$ and Wagner ${ }^{15}$ and the IUPAC equation of state of de Reuck and Craven, ${ }^{16}$ respectively. It was noticed that some curvature existed between pure water, pure methanol, and air at atmospheric pressures.

Table 1. Experimental Densities for the $\mathbf{C O}_{2}(1)+$ Methanol (2) System at 313.2 K

| P | $\mathrm{x}_{2}$ | $\rho$ | $\mathrm{V}_{\text {mix }}$ | $\mathrm{V}_{\text {mix }}(\mathrm{eq} 4)$ | deviation (eq 4) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| MPa |  | $\mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | $\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | \% |
| 10.50 | 0.580 | 845.39 | 43.848 | 43.876 | 0.064 |
| 10.56 | 0.580 | 845.34 | 43.851 | 43.867 | 0.037 |
| 10.57 | 0.580 | 845.41 | 43.847 | 43.866 | 0.043 |
| 10.89 | 0.580 | 846.19 | 43.806 | 43.819 | 0.028 |
| 10.95 | 0.630 | 843.03 | 43.261 | 43.244 | -0.039 |
| 10.96 | 0.630 | 842.87 | 43.269 | 43.242 | -0.062 |
| 10.96 | 0.630 | 842.96 | 43.264 | 43.242 | -0.051 |
| 10.97 | 0.630 | 843.00 | 43.262 | 43.241 | -0.049 |
| 11.01 | 0.580 | 846.43 | 43.794 | 43.801 | 0.017 |
| 11.02 | 0.580 | 846.59 | 43.786 | 43.800 | 0.032 |
| 11.03 | 0.580 | 846.56 | 43.787 | 43.799 | 0.025 |
| 11.08 | 0.720 | 835.34 | 42.370 | 42.364 | -0.014 |
| 11.09 | 0.720 | 835.45 | 42.364 | 42.363 | -0.004 |
| 11.12 | 0.720 | 835.57 | 42.358 | 42.360 | 0.005 |
| 11.14 | 0.810 | 823.90 | 41.651 | 41.687 | 0.087 |
| 11.16 | 0.810 | 824.05 | 41.643 | 41.686 | 0.102 |
| 11.18 | 0.720 | 835.74 | 42.350 | 42.355 | 0.013 |
| 11.18 | 0.810 | 824.13 | 41.639 | 41.684 | 0.108 |
| 11.18 | 0.810 | 824.16 | 41.638 | 41.684 | 0.112 |
| 12.41 | 0.630 | 846.32 | 43.093 | 43.076 | -0.039 |
| 12.41 | 0.630 | 846.28 | 43.095 | 43.076 | -0.043 |
| 12.42 | 0.630 | 846.34 | 43.091 | 43.075 | -0.038 |
| 12.43 | 0.630 | 846.37 | 43.090 | 43.074 | -0.038 |
| 12.90 | 0.810 | 826.27 | 41.531 | 41.567 | 0.086 |
| 12.97 | 0.580 | 851.86 | 43.515 | 43.531 | 0.037 |
| 12.97 | 0.810 | 826.43 | 41.523 | 41.562 | 0.094 |
| 12.99 | 0.810 | 826.51 | 41.519 | 41.561 | 0.100 |
| 13.00 | 0.810 | 826.55 | 41.517 | 41.560 | 0.104 |
| 13.01 | 0.580 | 851.92 | 43.512 | 43.526 | 0.032 |
| 13.02 | 0.580 | 851.93 | 43.511 | 43.524 | 0.030 |
| 13.03 | 0.580 | 852.00 | 43.508 | 43.523 | 0.035 |
| 13.11 | 0.630 | 847.80 | 43.017 | 42.999 | -0.043 |
| 13.11 | 0.630 | 847.80 | 43.017 | 42.999 | -0.043 |
| 13.18 | 0.630 | 848.11 | 43.002 | 42.991 | -0.024 |
| 13.18 | 0.720 | 838.68 | 42.201 | 42.185 | -0.038 |
| 13.26 | 0.630 | 848.28 | 42.993 | 42.983 | -0.025 |
| 13.27 | 0.720 | 838.95 | 42.187 | 42.177 | -0.024 |
| 13.29 | 0.720 | 839.03 | 42.183 | 42.176 | -0.018 |
| 13.29 | 0.720 | 838.99 | 42.186 | 42.176 | -0.023 |
| 14.83 | 0.580 | 856.43 | 43.283 | 43.295 | 0.028 |
| 14.88 | 0.580 | 856.53 | 43.278 | 43.289 | 0.025 |
| 14.88 | 0.810 | 828.55 | 41.417 | 41.437 | 0.048 |
| 14.89 | 0.720 | 841.22 | 42.073 | 42.047 | -0.063 |
| 14.89 | 0.810 | 828.57 | 41.416 | 41.436 | 0.049 |
| 14.89 | 0.810 | 828.58 | 41.415 | 41.436 | 0.051 |
| 14.90 | 0.720 | 841.22 | 42.074 | 42.046 | -0.066 |
| 14.92 | 0.720 | 841.24 | 42.073 | 42.044 | -0.067 |
| 15.02 | 0.580 | 856.89 | 43.259 | 43.272 | 0.028 |
| 15.11 | 0.580 | 857.32 | 43.238 | 43.261 | 0.053 |
| 15.11 | 0.720 | 841.87 | 42.041 | 42.029 | -0.028 |
| 15.26 | 0.630 | 852.20 | 42.795 | 42.773 | -0.051 |
| 15.30 | 0.630 | 852.28 | 42.791 | 42.769 | -0.052 |
| 15.32 | 0.630 | 852.31 | 42.790 | 42.767 | -0.052 |
| 15.34 | 0.630 | 852.35 | 42.788 | 42.765 | -0.052 |
| 15.35 | 0.630 | 852.46 | 42.782 | 42.764 | -0.042 |
| 16.81 | 0.810 | 830.58 | 41.316 | 41.316 | 0.000 |
| 16.87 | 0.810 | 830.72 | 41.309 | 41.312 | 0.008 |
| 16.92 | 0.580 | 861.55 | 43.026 | 43.049 | 0.055 |
| 16.92 | 0.810 | 830.81 | 41.304 | 41.309 | 0.013 |
| 16.94 | 0.580 | 861.61 | 43.022 | 43.047 | 0.058 |
| 16.95 | 0.580 | 861.68 | 43.019 | 43.046 | 0.062 |
| 16.99 | 0.580 | 861.74 | 43.016 | 43.041 | 0.060 |
| 17.05 | 0.720 | 844.50 | 41.910 | 41.881 | -0.070 |
| 17.07 | 0.720 | 844.53 | 41.908 | 41.879 | -0.069 |
| 17.09 | 0.720 | 844.58 | 41.906 | 41.878 | -0.067 |
| 17.10 | 0.720 | 844.64 | 41.903 | 41.877 | -0.062 |
| 17.13 | 0.720 | 844.74 | 41.898 | 41.875 | -0.055 |
| 17.69 | 0.630 | 857.15 | 42.548 | 42.537 | -0.026 |
| 18.03 | 0.630 | 857.72 | 42.520 | 42.506 | -0.033 |
| 18.06 | 0.630 | 857.78 | 42.517 | 42.503 | -0.033 |
| 18.09 | 0.630 | 857.87 | 42.512 | 42.500 | -0.028 |

Since all measurements were at super-atmospheric conditions and at methanol-rich mole fractions, methanol and


Figure 1. Pressure-volume diagram for the $\mathrm{CO}_{2}(1)+$ methanol (2) system at 313.2 K ; lines calculated from eq 4.


Figure 2. Pressure-volume diagram for the $\mathrm{CO}_{2}(1)+$ methanol (2) system at 318.2 K ; lines calculated from eq 4.
water were used mainly in regressing the constants for the calibration equations at a given temperature. The form of the calibration equations were

$$
\begin{equation*}
\rho=\mathrm{AT}^{2}+\mathrm{BT}+\mathrm{C}+\mathrm{DT}^{2} \mathrm{P} \tag{1}
\end{equation*}
$$

where $\rho\left(\mathrm{kg} \cdot \mathrm{m}^{-3}\right)$ is the density, T is the period ( s ), P is the absolute pressure (MPa), and A, B, C, and D are fitted parameters in consistent units. At each temperature, 60 to 70 points were used to determine the constants in eq 1, and in all fits, maximum deviations were less than 0.05\% with many deviations being less than $0.01 \%$. For all temperatures, the $95 \%$ confidence interval of the density residuals contained zero.

## Results and Discussion

Tables 1-3 show the experimental data at $313.2 \mathrm{~K}, 318.2$ K, and 323.2 K, respectively. The correlated values and the residuals are discussed in the next section. From the data, it can be seen that all densities in the range of 750 to 870 $\mathrm{kg} \cdot \mathrm{m}^{-3}$, which is intermediate to those of pure methanol and pure water at the same temperature and pressure. The methanol and $\mathrm{CO}_{2}$ system exhibits a maximum in density versus composition for a given temperature and pressure ${ }^{17}$ and thus pressure-molar volume plots show the trend of the data more clearly. A maximum in density for the 2-propanol and $\mathrm{CO}_{2}$ system has also been noted by Yaginuma et al. ${ }^{18}$ Figures $1-3$ show all data plotted in $\mathrm{P}-\mathrm{V}$ coordinates at given mole fractions of methanol. From the

Table 2. Experimental Densities for the $\mathbf{C O}_{2}(1)+$ Methanol (2) System at 318.2 K

| P | $\mathrm{X}_{2}$ | $\rho$ | $\mathrm{V}_{\text {mix }}$ | $\mathrm{V}_{\text {mix }}(\mathrm{eq} \mathrm{4)}$ | deviation (eq 4) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| MPa |  | $\mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | $\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | \% |
| 8.0 | 0.552 | 822.37 | 45.477 | 45.440 | -0.080 |
| 9.0 | 0.834 | 814.10 | 41.799 | 41.744 | -0.132 |
| 10.0 | 0.552 | 833.71 | 44.859 | 44.897 | 0.085 |
| 10.0 | 0.694 | 833.84 | 42.813 | 42.846 | 0.077 |
| 11.0 | 0.552 | 837.04 | 44.680 | 44.657 | -0.052 |
| 11.0 | 0.694 | 837.25 | 42.639 | 42.721 | 0.192 |
| 11.0 | 0.834 | 817.35 | 41.633 | 41.573 | -0.144 |
| 15.0 | 0.552 | 851.62 | 43.915 | 43.847 | -0.154 |
| 15.0 | 0.694 | 846.17 | 42.190 | 42.266 | 0.182 |
| 15.0 | 0.834 | 823.35 | 41.330 | 41.259 | -0.172 |
| 20.0 | 0.552 | 868.44 | 43.064 | 43.063 | -0.003 |
| 20.0 | 0.694 | 855.99 | 41.705 | 41.781 | 0.182 |
| 20.0 | 0.834 | 830.59 | 40.969 | 40.908 | -0.150 |

Table 3. Experimental Densities for the $\mathbf{C O}_{2}(1)+$ Methanol (2) System at 323.2 K

| P | $\mathrm{X}_{2}$ | $\rho$ | $\mathrm{V}_{\text {mix }}$ | $V_{\text {mix }}(\mathrm{eq} 4)$ | deviation (eq 4) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| MPa |  | $\mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | $\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | \% |
| 11.00 | 0.257 | 748.05 | 54.721 | 54.579 | -0.260 |
| 11.51 | 0.257 | 759.51 | 53.896 | 53.894 | -0.002 |
| 12.61 | 0.257 | 776.47 | 52.718 | 52.738 | 0.037 |
| 13.20 | 0.257 | 784.57 | 52.174 | 52.236 | 0.120 |
| 14.17 | 0.257 | 794.05 | 51.551 | 51.533 | -0.035 |
| 14.74 | 0.257 | 800.56 | 51.132 | 51.173 | 0.081 |
| 15.51 | 0.257 | 806.00 | 50.787 | 50.736 | -0.101 |
| 15.96 | 0.257 | 810.05 | 50.533 | 50.501 | -0.063 |
| 16.57 | 0.257 | 814.88 | 50.233 | 50.205 | -0.057 |
| 17.16 | 0.257 | 819.23 | 49.966 | 49.938 | -0.056 |
| 17.78 | 0.257 | 823.58 | 49.703 | 49.677 | -0.052 |
| 18.25 | 0.257 | 826.84 | 49.507 | 49.490 | -0.034 |
| 11.20 | 0.288 | 769.29 | 52.728 | 52.695 | -0.063 |
| 11.90 | 0.288 | 777.90 | 52.145 | 52.139 | -0.012 |
| 12.10 | 0.331 | 795.59 | 50.338 | 50.324 | -0.029 |
| 12.65 | 0.331 | 800.73 | 50.015 | 50.065 | 0.101 |
| 13.40 | 0.331 | 806.56 | 49.653 | 49.741 | 0.176 |
| 14.65 | 0.331 | 814.48 | 49.171 | 49.258 | 0.178 |
| 15.78 | 0.331 | 821.89 | 48.727 | 48.872 | 0.297 |
| 16.95 | 0.331 | 829.12 | 48.303 | 48.512 | 0.433 |
| 15.31 | 0.380 | 824.71 | 47.850 | 47.741 | -0.226 |
| 18.14 | 0.380 | 839.56 | 47.003 | 47.060 | 0.122 |
| 10.57 | 0.486 | 817.09 | 46.743 | 46.654 | -0.191 |
| 11.00 | 0.486 | 819.64 | 46.598 | 46.551 | -0.101 |
| 11.15 | 0.486 | 819.63 | 46.598 | 46.515 | -0.178 |
| 12.07 | 0.486 | 823.23 | 46.395 | 46.307 | -0.188 |
| 12.09 | 0.486 | 825.25 | 46.281 | 46.303 | 0.046 |
| 13.12 | 0.486 | 827.25 | 46.169 | 46.085 | -0.183 |
| 11.00 | 0.570 | 823.34 | 45.168 | 45.237 | 0.153 |
| 13.00 | 0.570 | 828.19 | 44.903 | 44.902 | -0.003 |
| 15.00 | 0.570 | 833.26 | 44.630 | 44.598 | -0.071 |
| 17.00 | 0.570 | 837.79 | 44.389 | 44.322 | -0.151 |
| 20.00 | 0.570 | 844.14 | 44.055 | 43.947 | -0.244 |
| 13.00 | 0.700 | 821.39 | 43.381 | 43.499 | 0.271 |
| 15.00 | 0.700 | 825.14 | 43.184 | 43.274 | 0.209 |
| 17.00 | 0.700 | 829.15 | 42.974 | 43.064 | 0.209 |
| 20.00 | 0.700 | 834.91 | 42.678 | 42.775 | 0.226 |
| 10.50 | 0.880 | 796.86 | 42.013 | 42.086 | 0.174 |
| 11.00 | 0.880 | 796.83 | 42.014 | 42.041 | 0.064 |
| 13.00 | 0.880 | 800.29 | 41.833 | 41.868 | 0.086 |
| 15.00 | 0.880 | 802.69 | 41.708 | 41.705 | -0.006 |
| 17.00 | 0.880 | 805.35 | 41.570 | 41.550 | -0.047 |
| 20.00 | 0.880 | 808.84 | 41.391 | 41.333 | -0.140 |
| 10.70 | 0.940 | 785.76 | 41.693 | 41.674 | -0.045 |
| 11.00 | 0.940 | 786.19 | 41.670 | 41.649 | -0.049 |
| 13.00 | 0.940 | 788.61 | 41.542 | 41.492 | -0.121 |
| 15.00 | 0.940 | 790.77 | 41.428 | 41.342 | -0.209 |
| 17.00 | 0.940 | 793.16 | 41.304 | 41.200 | -0.252 |
| 20.00 | 0.940 | 796.43 | 41.134 | 40.998 | -0.329 |

figures, it can be seen that the methanol liquid $\mathrm{P}-\mathrm{V}$ lines had very steep slopes for methanol mole fractions of about 0.5 or higher. However, as the $\mathrm{CO}_{2}$ mole fraction increased, the $\mathrm{P}-\mathrm{V}$ lines exhibited greater curvature.


Figure 3. Pressure-volume diagram for the $\mathrm{CO}_{2}(1)+$ methanol (2) system at 323.2 K ; white circles, this work; filled circles, Galicia-Luna et al.;9,10 lines calculated from eq 4; dashed lines calculated from eq 4 at compositions of ref 9 .


Figure 4. Excess molar volumes for the $\mathrm{CO}_{2}$ (1) + methanol (2) system at 313.2 K ; lines calculated from eq 4.

The precision of the data can be estimated from replicate measurements made at 313.2 K . From Table 1 and Figure 1, maximum variabilities of $0.1 \mathrm{~kg} \cdot \mathrm{~m}^{-3}$ were observed by comparing density measurements made at the same pressures or pressures within about 0.01 MPa . In general, the variations in the density were much less than $0.1 \mathrm{~kg} \cdot \mathrm{~m}^{-3}$. Due to errors in the mole fraction determination and temperature and pressure cyding in the system, however, accuracy in density is estimated to be no higher than about $0.5 \mathrm{~kg} \cdot \mathrm{~m}^{-3}$ with the higher errors occurring for the higher $\mathrm{CO}_{2}$ mole fractions.

Some measurements were performed at specific pressures of nominally 11, 13, 15, 17, and 20 MPa to allow analysis of the excess molar volumes. Pure component molar volumes were obtained from the equations of Span and Wagner ${ }^{19}$ for pure $\mathrm{CO}_{2}$ and IUPAC relations of de Reuck and Craven ${ }^{16}$ for pure methanol. Results are shown plotted in Figures 4-6 along with correlation equation results. The excess volumes can be seen to be negative over the composition region measured. Development of the correlation equations is discussed next.

Correlation. Data correlation was somewhat more difficult than at first anticipated. Forms of the Tait equation can be fitted to the experimental data at a given composition but do not allow interpolation at other compositions. The excess volumes at a given temperature and pressure can be fit with Redlich-Kister expansions or remarkably well with van-Laar-type expressions but do not allow interpolation at other pressures. Since our objective

Table 4. Parameter Values for Eq 4 and Their Standard Deviation

| parameter | 313.2 K |  | 318.2 K |  | 323.2 K |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | values | standard deviation | values | standard deviation | values | standard deviation |
| $\mathrm{P}_{0}$ (MPa) | 11 |  | 11 |  | 11 |  |
| C | 0.07 |  | 0.07 |  | 0.07 |  |
| $\mathrm{A}_{1}\left(\mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | -11.92293 | 0.095 | -19.22192 | 0.585 | -63.90117 | 1.249 |
| $\mathrm{A}_{2}\left(\mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | 0 |  | 0 |  | -48.13704 | 1.527 |
| $\mathrm{A}_{3}\left(\mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | 0 |  | 0 |  | -25.21391 | 1.189 |
| $\mathrm{V}_{1}\left(\mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | 54.71537 | 0.062 | 59.56155 | 0.349 | 83.07311 | 0.612 |
| $\mathrm{V}_{2}\left(\mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | 40.90840 | 0.002 | 41.18354 | 0.025 | 41.46474 | 0.012 |
| $\mathrm{B}_{1}$ (MPa) | -41.32487 | 0.939 | -39.67061 | 4.277 | -21.30546 | 0.378 |
| $\mathrm{B}_{2}$ (MPa) | 47.59646 | 0.496 | 36.72802 | 3.267 | 28.94383 | 1.082 |



Figure 5. Excess molar volumes for the $\mathrm{CO}_{2}$ (1) + methanol (2) system at 318.2 K ; lines calculated from eq 4 .


Figure 6. Excess molar volumes for the $\mathrm{CO}_{2}$ (1) + methanol (2) system at 323.2 K ; lines calculated from eq 4 ; white circles, this work; filled circles, Galicia-Luna et al., 9,10 dashed lines calculated from eq 4 at the pressures of ref 9 .
in this section was to provide a correlation for interpolation, not extrapolation, of the data, we combined the RedlichKister expansion with theTait form of equation to give the set of empirical correlating equations,

$$
\begin{equation*}
B=x_{1} B_{1}+x_{2} B_{2} \tag{2}
\end{equation*}
$$

$\mathrm{V}_{0}=\mathrm{x}_{1} \mathrm{~V}_{1}+\mathrm{x}_{2} \mathrm{~V}_{2}+$

$$
\begin{align*}
& x_{1} x_{2}\left(A_{1}+A_{2}\left(x_{1}-x_{2}\right)+A_{3}\left(x_{1}-x_{2}\right)^{2}\right)  \tag{3}\\
V_{\text {mix }}= & V_{0}\left(1-c \ln \left((B+P) /\left(B+P_{0}\right)\right)\right) \tag{4}
\end{align*}
$$

where $x_{1}$ and $x_{2}$ are the mole fractions of carbon dioxide and methanol, respectively, and $\mathrm{V}_{\text {mix }}$ is the mixture molar volume. The $\mathrm{V}_{1}, \mathrm{~V}_{2}, \mathrm{~B}_{1}, \mathrm{~B}_{2}, \mathrm{~A}_{1}, \mathrm{~A}_{2}$, and $\mathrm{A}_{3}$ are empirical parameters determined by a least-squares fit of the $\mathrm{P}-\mathrm{V}$
data at a given temperature. The $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$ should not be confused with the pure component molar volumes at the given temperature and pressure since eq 4 can only be applied over a limited composition range. The c and $\mathrm{P}_{0}$ in eq 4 could have been used as fitting parameters, but in this work, we assigned values of c to be a constant independent of temperature and the reference pressure, $\mathrm{P}_{0}$, to be 11 MPa , according to initial evaluations and parameter sensitivities. It should be noted that eq 4 cannot beextrapolated to the saturation region or to $\mathrm{CO}_{2}$-rich mole fractions due to its functional form and choice of reference state, $\mathrm{P}_{0}$ and $\mathrm{V}_{0}$.
Fitted values for eq 4 are summarized in Table 4 and calculated deviations for each point are shown in Tables $1-3$ with the average percent deviation of the correlation from the data for all data points being $0.08 \%$. Percent deviations of the model versus the data are shown for each point in the tables. Parameter standard deviations were calculated and are given in Table 4 and can be used to calculate the $95 \%$ confidence interval of the parameters (not shown). Standard deviations of the A and V parameters were smaller compared with those of the B parameters and indicated a lower range of variability. Values of the covariance matrix indicated low correlation between the parameters. The $\chi^{2}$ values (correlation coefficients) were 0.00984 ( 0.999968 ), 0.0363 ( 0.99988 ), and 0.3179 ( 0.99989 ) for the $318.2 \mathrm{~K}, 318.2 \mathrm{~K}$, and 323.2 K data, respectively. Higher variability for the 323.2 K data set was probably due to the wider range of carbon dioxide mole fractions studied.

Comparison with Other Data. Several other researchers have reported densities of carbon dioxide + methanol mixtures as noted in the Introduction. Brunner et al. ${ }^{20}$ measured densities al ong the $\mathrm{CO}_{2}+$ methanol saturation curve with a static apparatus to a nominal precision of 2.5 digits whereas in this work densities in the compressed regions were measured and therefore these data cannot be directly compared. Roškar et al. ${ }^{7}$ reported $\mathrm{CO}_{2}+$ methanol molar volumes at $308.2 \mathrm{~K}, 323.2 \mathrm{~K}$, and 338.2 K with a static apparatus to a nominal precision of 2.5 digits. However, the region of measurement of Roškar et al. ${ }^{7}$ extends into the two-phase region of Brunner et al., ${ }^{20}$ indicating some inconsistency in the compositions reported, specifically, $x_{2}=0.571$ and $x_{2}=0.781$. The data of Goldfarb et al. ${ }^{11}$ are mainly in the region of $\mathrm{CO}_{2}$-rich mole fractions, where we have not made measurements and show excess volumes that are positive. The data set that we chose for comparison are the high-precision measurements of Gali-cia-Luna et al., who used a vibrating tube method. 9,10 The data applicable to our region of measurement are plotted in Figures 3-6 and calculations made with eq 4 at the compositions reported by those authors are shown by the dashed lines. Good agreement ( $0.25 \%$ ) between the molar volumes of this work and those of the literature can be seen at the methanol mole fraction of 0.6476 but only fair
agreement ( $0.8 \%$ ) is apparent in the methanol mole fraction of 0.9039 and for one point at high $\mathrm{CO}_{2}$ mole fractions at 12.5 MPa. The data are also compared in Figure 6, where experimental data and cal culated excess mol ar volumes are shown. Good agreement can be seen between the two data sets.

## Conclusions

We have reported density data for methanol $+\mathrm{CO}_{2}$ mixtures, where methanol is in its expanded liquid state. The data should find use in the analyses of dielectric spectra data as well as in other fields related to liquid chromatography and gas antisolvent crystallization. A simple correlation equation was devel oped for interpolating within the conditions of measurement. Extreme caution should be used when extrapolating values, specifically, extrapolation tolower pressures or to higher carbon dioxide mole fractions. Extrapolation of the correlating equation to higher pressures, on the other hand, can probably provide acceptable results.

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