# Burnett Measurements for the Difluoromethane + Carbon Dioxide System 

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#### Abstract

As part of our ongoing research program on PVTx measurements using the isochoric and Burnett methods for hydrofluorocarbon + hydrocarbon and/or inorganic compound systems, this work reports on the experimental results for the difluoromethane $(\mathrm{R} 32)+$ carbon dioxide $\left(\mathrm{CO}_{2}\right)$ system obtained by the Burnett method. The apparatus was calibrated using helium, and its performance was confirmed by measurements for pure R32. The second and third virial coefficients were derived, and a good consistency was found after comparison with data in the literature. A new experimental procedure for mixture measurements was devel oped, on the basis of the gas chromatographic analysis of the sample collected during expansions. The gas chromatograph was calibrated precisely using samples prepared by the gravimetric method. PVTx measurements were performed for the binary $\mathrm{R} 32+\mathrm{CO}_{2}$ system at $T=(303,313,323,333$, and 343) K. The second and third cross virial coefficients were derived from the experimental results. No experimental data could be found in accessible literature sources on the PVTx for the R $32+\mathrm{CO}_{2}$ system. Results were compared with the prediction obtained using REFPROP 6.01.


## Introduction

Carbon dioxide has received much attention for industrial applications. It is also an attractive compound for research because of its convenient critical temperature and thermal stability, which explains the fairly abundant and accurate literature providing thermophysical data for $\mathrm{CO}_{2}$. ${ }^{1}$ It is neither flammable nor toxic, is inexpensive and is widely available. One of the main disadvantages of this natural fluid is that the plant components need to be designed for much higher pressures; typically 150 bar is the maximum operating pressure.

Difluoromethane is a hydrofluorocarbon used in the refrigeration industry. In particular, it is an important alternative refrigerant as a constituent in several binary or ternary mixtures intended as a substitute for difluorochloromethane (R22), and its thermophysical properties have been studied extensively in the past decade. Themain limit of this refrigerant fluid lies in its flammability. This alternative refrigerant has a zero ODP but a far from negligible GWP, so its combination with a low-GWP and nonflammable compound such as $\mathrm{CO}_{2}$ is particularly promising.

Nevertheless, publications on the PVTx properties of systems containing carbon dioxide as one of their components and a hydrofluorocarbon as the other are rare. Studying the combination of carbon dioxide and difluoromethane thus provides important information for future applications. Moreover, no experimental results have been published to our knowledge on the PVTx properties of this specific binary system.

This work presents and discusses the PVTx resulting from Burnett measurements.

## Experimental Section

Reagents. $\mathrm{CO}_{2}$ and R 32 were supplied by Sol SpA and Ausimont SpA, respectively; the purity was checked by gas

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Figure 1. Schematic view of the experimental apparatus: 1, nitrogen reservoir; 2, vacuum pump (Vacuubrand, mod. RZ2); 3, precision pressure controller (Ruska, mod. 3981); 4, gas lubricated dead weight gauge (Ruska, mod. 2465); 5, vibr. cylinder pressure gauge (Ruska, mod. 6220); 6, digital temperature indicator (Corradi, RP 7000); 7, electronic null indicator (Ruska, mod. 2416); 8, stirrer; 9, heater; 10, cooling coil connected with an auxiliary bath; 11, differential pressure transducer (Ruska, mod. 2413); 12, measurement chamber $\left(\mathrm{V}_{\mathrm{A}}\right)$; 13, expansion chamber $\left(\mathrm{V}_{\mathrm{B}}\right)$; 14, magnetic recirculating pump; 15, Pt resistance thermometer (Tersid, Pt 100); 16, vacuum pump for $\mathrm{V}_{\text {B }}$ (Vacuubrand, mod. RZ2); 17, charging fluid reservoir; 18, Pt resistance thermometer (Hart Scientific, Pt 25); 19, digital pressure indicator (Ruska, mod. 7000); $\mathrm{V}_{1}, \mathrm{~V}_{2}, \mathrm{~V}_{3}, \mathrm{~V}_{4}$, constant volume valves.
chromatographic analysis, using a thermal conductivity detector. It was found to be 99.99\% for the $\mathrm{CO}_{2}$ and 99.98\% for the R32 on an area-response basis.

Apparatus. A diagram of the apparatus is shown in Figure 1. It is the same as the one described elsewhere ${ }^{2-4}$ and used with only minimal modifications. It consists of

Table 1. Experimental Pressures Measured during Burnett Expansions of R32

| P/kPa |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| series 1 | series 2 | series 3 | series 4 | series 5 | series 6a | series ${ }^{\text {a }}$ | series 8 | series 9 |
| $\mathrm{T} / \mathrm{K}=303.15$ | $\mathrm{T} / \mathrm{K}=303.16$ | $\mathrm{T} / \mathrm{K}=313.15$ | $\mathrm{T} / \mathrm{K}=313.16$ | T/K = 323.16 | $\mathrm{T} / \mathrm{K}=323.16$ | T/K = 333.16 | $\mathrm{T} / \mathrm{K}=343.16$ | $\mathrm{T} / \mathrm{K}=343.16$ |
| 1548.2 | 1783.7 | 1730.8 | 2363.1 | 2291.1 | 3110.5 | 2123.3 | 4198.0 | 4365.7 |
| 1119.8 | 1313.8 | 1249.4 | 1786.3 | 1685.3 | 2444.3 | 1526.7 | 3335.6 | 3520.5 |
| 788.6 | 935.6 | 878.4 | 1293.4 | 1200.0 | 1816.3 | 1071.3 | 2503.2 | 2667.7 |
| 545.5 | 652.0 | 607.3 | 911.2 | 835.9 | 1301.9 | 739.7 | 1807.8 | 1940.4 |
| 373.0 | 448.1 | 415.1 | 630.8 | 574.4 | 911.3 | 504.9 | 1273.4 | 1372.7 |
| 253.3 | 305.2 | 281.6 | 431.5 | 390.9 | 628.0 | 342.1 | 881.3 | 953.2 |
| 171.1 | 206.7 | 190.1 | 292.9 | 264.2 | 428.4 | 230.6 | 603.4 | 653.3 |
| 115.2 | 139.4 | 128.0 | 197.9 | 177.9 |  | 155.1 | 409.5 | 444.2 |
|  |  |  | 133.3 |  | 195.8 |  | 276.7 | 300.5 |
|  |  |  |  |  | 131.6 |  | 186.4 | 202.5 |
|  |  |  |  |  |  |  | 125.2 | 136.2 |

a Data obtained with $\mathrm{N}=1.49570$.
Table 2. Second and Third Virial Coefficients for R32a

| series | T/K | $\mathrm{B} / \mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | $\mathrm{C} / \mathrm{cm}^{6} \cdot \mathrm{~mol}^{-2}$ | $\rho(1)^{\mathrm{a}} / \mathrm{mol} \cdot \mathrm{dm}^{-3}$ | abs(dP)/kPa | 100(P - $\mathrm{P}_{\text {calc }}$ ) $\mathrm{P}^{-1 / \%}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 303.15 | -284.3 | 24420 | 0.77270 | 0.1 | -0.01 |
| 2 | 303.16 | -283.5 | 23940 | 0.93677 | 0.0 | 0.01 |
| 3 | 313.15 | -257.5 | 20650 | 1.29402 | 0.1 | -0.01 |
| 4 | 313.16 | -257.4 | 19890 | 0.83116 | 0.1 | -0.02 |
| 5 | 323.16 | -238.7 | 19570 | 1.85209 | 0.2 | -0.06 |
| $6^{\text {b }}$ | 323.16 | -238.3 | 18980 | 1.12925 | 0.2 | -0.04 |
| $7{ }^{\text {b }}$ | 333.16 | -220.8 | 17380 | 0.95137 | 0.2 | -0.05 |
| 8 | 343.16 | -203.2 | 16070 | 2.46554 | 0.4 | 0.04 |
| 9 | 343.16 | -202.3 | 15760 | 2.68047 | 0.6 | 0.06 |

${ }^{\text {a }} \rho(1)$ denotes regressed initial density. ${ }^{\text {b }}$ Data obtained with $\mathrm{N}=1.49570$.
Table 3. Second and Third Virial Coefficients for $\mathrm{CO}_{2}{ }^{\mathbf{a}}$

| series | T/K | $\mathrm{B} / \mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | $\mathrm{C} / \mathrm{cm}^{6} \cdot \mathrm{~mol}^{-2}$ | $\rho(1) / \mathrm{mol} \cdot \mathrm{dm}^{-3}$ | abs(dP)/kPa | 100(P - P calc $^{\text {) }} \mathrm{P}^{-1} / \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 283.14 | -136.2 | 4390 | 2.24627 | 0.3 | -0.30 |
| 2 | 283.14 | -136.6 | 4580 | 2.53439 | 0.2 | -0.07 |
| 3 | 283.14 | -136.4 | 4890 | 2.57016 | 0.1 | -0.03 |
| 4 | 303.15 | -118.9 | 4870 | 3.28011 | 0.1 | -0.09 |
| 5 | 303.15 | -118.1 | 4690 | 3.11860 | 0.2 | -0.04 |
| 6 | 303.15 | -119.2 | 4980 | 3.27410 | 0.0 | -0.02 |
| 7 | 303.15 | -118.9 | 4860 | 3.30130 | 0.0 | -0.02 |
| 8 | 313.15 | -109.8 | 4600 | 2.80884 | 0.1 | -0.01 |
| 9 | 323.16 | -103.6 | 4660 | 2.81253 | 0.2 | -0.03 |
| 10 | 323.16 | -103.7 | 4680 | 2.87813 | 0.2 | -0.09 |
| 11 | 333.63 | -95.0 | 4040 | 2.49594 | 0.2 | -0.09 |
| 12 | 333.63 | -94.5 | 4000 | 2.54126 | 0.2 | -0.25 |
| 13 | 343.15 | -88.7 | 3920 | 2.34421 | 0.1 | 0.02 |
| 14 | 343.15 | -90.2 | 4250 | 2.47549 | 0.1 | 0.03 |
| 15 | 363.15 | -79.6 | 4130 | 2.16473 | 0.1 | 0.00 |
| 16 | 363.15 | -78.4 | 3670 | 2.09960 | 0.2 | 0.01 |
| 17 | 363.15 | -75.9 | 3210 | 2.14779 | 0.4 | -0.03 |

two pressure vessels, the measurement chamber, $\mathrm{V}_{\mathrm{A}}$, and the expansion chamber, $\mathrm{V}_{\mathrm{B}}$, with a volume of approximately (70 and 35) $\mathrm{cm}^{3}$, respectively, and some auxiliary systems for filling and mixing the compounds in the Burnett vessels and for controlling and measuring the pressure and temperature. The spherical shape of the vessels simplifies the evaluation of the distortion coefficients as a function of temperature and pressure. Moreover, the ratio of outer and inner diameters of both spheres is the same. The relative volume change with pressure is consequently identical for the two vessels. The vessels are made of I nvar, because of its excellent corrosion resistance and low thermal expansion coefficient. The constant volume valves have been redesigned to ensure thermal compensation of the packing and val ve body. The four-valve arrangement enables the vessels $\mathrm{V}_{\mathrm{A}}$ and $\mathrm{V}_{\mathrm{B}}$ to be filled or emptied separately and, in addition to the expansion experiment, allows for the compounds in the Burnett vessels to be mixed using a magnetic recirculating pump.

The packing surfaces of valves $\mathrm{V}_{1}$ and $\mathrm{V}_{4}$ are exposed to the expansion volume $\mathrm{V}_{\mathrm{B}}$, and those of valves $\mathrm{V}_{2}$ and $\mathrm{V}_{3}$ are exposed in the opposite direction of the volumes $\mathrm{V}_{\mathrm{A}}$ and $\mathrm{V}_{\mathrm{B}}$. Thus, the principal volume $\mathrm{V}_{\mathrm{A}}$ and its fixtures are allmetal, to prevent contact between the sample gas in vessel $\mathrm{V}_{\mathrm{A}}$ and the Teflon packing throughout the lengthy Burnett experiment, except for the time it takes to reach thermal equilibrium after expansion.

The measurement vessel is connected to a diaphragmtype differential pressure transducer (Ruska Model 2413), which is coupled to an electronic null indicator (Ruska Model 2416).

The pressure is regulated by a precision pressure controller (Ruska Model 3981), while a digital pressure indicator (Ruska Model 7000) is used to measure pressures. Nitrogen is used to balance the sample gas pressure, and the nitrogen circuit consists of a reservoir, expansion vessels, and pressure regulating systems.
The vessels are immersed in a thermostatic bath filled with about 45 L of an ethylene glycol and water mixture.


Figure 2. Deviations between the second virial coefficients calculated according to the Tsonopoul os method ${ }^{12}$ and the experimental second virial coefficients for R32 against temperature: - , present work; O, ref $7 ; \diamond$, ref $8 ; \square$, ref $9 ; \nabla$, ref $10 ; \Delta$, ref 11 .


Figure 3. Deviations between the third virial coefficients calculated according to eq 3 and the experimental third virial coefficients for R32 against temperature: ■, present work; $\diamond$, ref 8 ; $\nabla$, ref 10 .

The temperature of the bath is kept constant by means of a system with a PID device, piloted by a computer to which the temperature measurement system is also connected. The temperature control and acquisition system relies on two platinum resistance thermometers calibrated according to ITS 90 at the I stituto M etrologico G. Col onnetti (IMGC), of Turin. In particular, for temperature measurements, a Hart Scientific Pt $25 \Omega$ resistance thermometer (mod. Hart 5680) is used, while for control purposes a Tersid Pt 100 $\Omega$ resistance thermometer is used. Both the thermometers are connected to a digital temperature indicator (Corradi, RP 7000).

The Burnett constant, N , defined as the ratio of the volume of cell A and the sum of the volumes of cells A and $B$ at zero pressure, was determined by means of gaseous helium measurements (since its thermodynamic properties are well established). After taking measurements at several isotherms, the constant was found to be $\mathrm{N}=1.49485 \pm 0.0001$; after servicing the setup, we found the Burnett constant to be $N=1.49570 \pm 0.0001$ and $\mathrm{N}=1.49691 \pm 0.0001$. These results are marked with a footnote in Tables 1, 2, and 4. The Burnett constant found reproduces the pressures of helium with absolute average deviations, AAD $=0.418 \mathrm{kPa}$ or $\mathrm{AAD}=0.142$, in percent.

Table 4. Experimental Pressures Measured during Burnett Expansions and Regressed Compressibility Factors of the R32 (1) + CO $\mathbf{O}_{2}$ (2) System

| T/K $=303.15$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Series } 1^{\mathrm{a}} \\ \mathrm{x}_{1}=0.1667 \end{gathered}$ |  | $\begin{gathered} \text { Series 2 } \\ \mathrm{x}_{1}=0.3192 \end{gathered}$ |  | $\begin{gathered} \text { Series 3 } \\ x_{1}=0.4576 \end{gathered}$ |  | $\begin{gathered} \text { Series 4 } \\ x_{1}=0.6462 \end{gathered}$ |  |
| P/kPa | z | P/kPa | z | P/kPa | z | P/kPa | z |
| 4639.0 | 0.6841 | 4077.7 | 0.6786 | 3004.2 | 0.7486 | 2353.4 | 0.7697 |
| 3532.1 | 0.7797 | 3120.0 | 0.7762 | 2220.2 | 0.8270 | 1722.4 | 0.8420 |
| 2568.4 | 0.8487 | 2275.8 | 0.8463 | 1584.8 | 0.8824 | 1221.6 | 0.8927 |
| 1813.5 | 0.8970 | 1611.5 | 0.8958 | 1105.5 | 0.9202 | 849.0 | 0.9274 |
| 1256.8 | 0.9305 | 1118.7 | 0.9295 | 760.2 | 0.9459 | 582.7 | 0.9515 |
| 860.2 | 0.9534 | 766.9 | 0.9526 | 518.3 | 0.9639 | 396.5 | 0.9678 |
| 583.9 | 0.9687 | 520.4 | 0.9663 | 351.1 | 0.9762 | 267.4 | 0.9758 |
| 394.0 | 0.9784 | 351.8 | 0.9766 | 236.7 | 0.9836 | 180.2 | 0.9832 |
| 265.0 | 0.9851 | 237.2 | 0.9841 | 159.1 | 0.9883 |  |  |
|  |  | 159.4 | 0.9888 |  |  |  |  |
| T/K $=313.15$ |  |  |  |  |  |  |  |
| $\begin{gathered} \text { Series } 5 \\ x_{1}=0.3220 \end{gathered}$ |  | $\begin{gathered} \text { Series } 6 \\ x_{1}=0.4628 \end{gathered}$ |  | $\begin{gathered} \text { Series } 7 \\ x_{1}=0.6312 \end{gathered}$ |  | $\begin{gathered} \text { Series } 8 \\ x_{1}=0.8029 \end{gathered}$ |  |
| P/kPa | z | P/kPa | z | P/kPa | z | P/kPa | z |
| 4222.1 | 0.7154 | 3251.3 | 0.7618 | 2367.6 | 0.8042 | 2294.3 | 0.7708 |
| 3163.9 | 0.8013 | 2387.2 | 0.8361 | 1705.9 | 0.8662 | 1676.8 | 0.8421 |
| 2280.5 | 0.8634 | 1696.6 | 0.8883 | 1197.7 | 0.9091 | 1187.9 | 0.8918 |
| 1602.3 | 0.9068 | 1181.5 | 0.9247 | 827.5 | 0.9390 | 825.8 | 0.9268 |
| 1107.7 | 0.9371 | 811.0 | 0.9488 | 565.2 | 0.9587 | 566.8 | 0.9508 |
| 757.4 | 0.9577 | 552.2 | 0.9657 | 383.4 | 0.9720 | 385.7 | 0.9673 |
| 513.9 | 0.9714 | 373.6 | 0.9767 | 259.0 | 0.9816 | 261.0 | 0.9784 |
| 347.1 | 0.9808 | 251.9 | 0.9843 | 174.1 | 0.9866 | 175.9 | 0.9859 |
| 233.7 | 0.9872 | 169.3 | 0.9890 |  |  |  |  |
| 157.0 | 0.9914 |  |  |  |  |  |  |


| $\mathrm{T} / \mathrm{K}=323.15$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Series } 9 \\ x_{1}=0.3108 \end{gathered}$ |  | $\begin{gathered} \text { Series } 10 \\ x_{1}=0.3487 \end{gathered}$ |  | $\begin{gathered} \text { Series } 11 \\ x_{1}=0.5709 \end{gathered}$ |  | $\begin{gathered} \text { Series } 12 \\ x_{1}=0.5866 \end{gathered}$ |  |
| P/kPa | z | P/kPa | z | P/kPa | z | P/kPa | z |
| 5124.0 | 0.6908 | 3833.7 | 0.7764 | 3270.9 | 0.7641 | 3409.1 | 0.7473 |
| 3880.7 | 0.7820 | 2791.2 | 0.8450 | 2394.7 | 0.8363 | 2514.8 | 0.8241 |
| 2818.6 | 0.8491 | 1975.1 | 0.8938 | 1700.5 | 0.8877 | 1794.7 | 0.8791 |
| 1991.5 | 0.8968 | 1371.6 | 0.9278 | 1183.7 | 0.9237 | 1253.3 | 0.9177 |
| 1381.6 | 0.9299 | 940.7 | 0.9513 | 813.1 | 0.9484 | 862.8 | 0.9444 |
| 947.0 | 0.9529 | 639.9 | 0.9673 | 553.6 | 0.9654 | 588.3 | 0.9626 |
| 643.9 | 0.9685 | 432.9 | 0.9781 | 374.8 | 0.9769 | 398.7 | 0.9751 |
| 435.5 | 0.9791 | 291.8 | 0.9855 | 252.7 | 0.9846 | 269.0 | 0.9834 |
| 293.5 | 0.9864 | 196.1 | 0.9904 | 169.9 | 0.9898 | 180.9 | 0.9888 |
| 197.3 | 0.9915 | 131.6 | 0.9935 |  |  | 121.5 | 0.9928 |
| 132.3 | 0.9934 |  |  |  |  |  |  |


| $\mathrm{T} / \mathrm{K}=333.15$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Series } 13 \\ x_{1}=0.3222 \end{gathered}$ |  | $\begin{gathered} \text { Series } 14 \\ x_{1}=0.4489 \end{gathered}$ |  | $\begin{gathered} \text { Series } 15 \\ x_{1}=0.5791 \end{gathered}$ |  | $\begin{gathered} \text { Series } 16 \\ \mathrm{x}_{1}=0.7372 \end{gathered}$ |  |
| P/kPa | z | P/kPa | z | P/kPa | z | P/kPa | z |
| 2456.6 | 0.8842 | 4388.0 | 0.7457 | 3522.3 | 0.7739 | 2877.4 | 0.7889 |
| 1711.9 | 0.9210 | 3235.9 | 0.8220 | 2566.3 | 0.8429 | 2082.6 | 0.8535 |
| 1177.0 | 0.9466 | 2310.2 | 0.8772 | 1817.2 | 0.8922 | 1468.4 | 0.8996 |
| 801.8 | 0.9640 | 1614.2 | 0.9162 | 1262.6 | 0.9266 | 1017.3 | 0.9317 |
| 543.0 | 0.9759 | 1111.7 | 0.9433 | 866.3 | 0.9504 | 696.8 | 0.9539 |
| 366.0 | 0.9834 | 758.4 | 0.9619 | 589.5 | 0.9667 | 473.6 | 0.9691 |
| 246.2 | 0.9889 | 514.1 | 0.9747 | 398.8 | 0.9777 | 320.2 | 0.9795 |
| 165.3 | 0.9925 | 346.9 | 0.9833 | 268.9 | 0.9854 | 215.7 | 0.9864 |
|  |  | 233.5 | 0.9891 | 180.8 | 0.9906 | 145.0 | 0.9912 |
|  |  | 156.8 | 0.9930 | 121.4 | 0.9942 |  |  |

$\mathrm{T} / \mathrm{K}=343.15$

| $\begin{gathered} \text { Series 17 } \\ x_{1}=0.3210 \end{gathered}$ |  | $\begin{gathered} \text { Series } 18 \\ x_{1}=0.4956 \end{gathered}$ |  | $\begin{gathered} \text { Series } 19 \\ x_{1}=0.6856 \end{gathered}$ |  | $\begin{gathered} \text { Series 20 } \\ x_{1}=0.7132 \end{gathered}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| P/kPa | z | P/kPa | z | P/kPa | z | P/kPa | z |
| 4093.8 | 0.8229 | 3340.7 | 0.8293 | 2253.8 | 0.8664 | 3160.6 | 0.799 |
| 2922.3 | 0.8781 | 2377.3 | 0.8822 | 1580.8 | 0.9084 | 2276.6 | 0.8607 |
| 2041.3 | 0.9169 | 1657.7 | 0.9195 | 1091.6 | 0.9377 | 1600.4 | 0.9045 |
| 1405.5 | 0.9437 | 1140.2 | 0.9454 | 745.9 | 0.9579 | 1106.7 | 0.9350 |
| 958.4 | 0.9619 | 777.0 | 0.9631 | 506.2 | 0.9716 | 757.0 | 0.9560 |
| 649.6 | 0.9746 | 526.4 | 0.9753 | 341.9 | 0.9810 | 514.1 | 0.9705 |
| 438.1 | 0.9827 | 355.1 | 0.9835 | 230.2 | 0.9873 | 347.5 | 0.9805 |
| 295.0 | 0.9889 | 238.9 | 0.9892 | 154.7 | 0.9917 | 234.1 | 0.9874 |
| 198.2 | 0.9931 | 160.4 | 0.9930 |  |  | 157.3 | 0.992 |
| 132.9 | 0.9959 | 107.6 | 0.9952 |  |  |  |  |

[^1]Table 5. Experimental and Calculated Second and Third Virial Coefficients for the R32 (1) $+\mathbf{C O}_{\mathbf{2}}$ (2) System

| T/K | $\mathrm{x}_{1}$ | $\frac{\mathrm{Bm}_{\mathrm{m}}^{\mathrm{exp}}}{\mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1}}$ | $\frac{\mathrm{Bm}_{\mathrm{m}}^{\text {calc }}}{\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}}$ | $\frac{\mathrm{dB}_{\mathrm{m}}}{\mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1}}$ | $\frac{\mathrm{Cm}_{\mathrm{m}}^{\exp }}{\mathrm{cm}^{6} \cdot \mathrm{~mol}^{-2}}$ | $\frac{\mathrm{Cm}_{\mathrm{m}}^{\text {calc }}}{\mathrm{cm}^{6} \cdot \mathrm{~mol}^{-2}}$ | $\frac{\mathrm{dC}_{\mathrm{m}}}{\mathrm{~cm}^{6} \cdot \mathrm{~mol}^{-2}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 303.15 | 0.1667 | -133.0 | -133.3 | 0.3 | 5790 | 5850 | -60 |
|  | 0.3192 | -151.5 | -151.1 | -0.3 | 6990 | 6940 | 50 |
|  | 0.4576 | -171.3 | -171.1 | -0.2 | 8430 | 8420 | 10 |
|  | 0.6462 | -204.0 | -204.1 | 0.0 | 11680 | 11710 | -30 |
| 313.15 | 0.3220 | -142.1 | -141.6 | -0.5 | 7280 | 6370 | 910 |
|  | 0.4628 | -157.8 | -160.1 | 2.3 | 7620 | 8210 | -590 |
|  | 0.6312 | -184.5 | -186.2 | 1.6 | 10060 | 11190 | -1130 |
|  | 0.8029 | -219.1 | -216.9 | -2.2 | 16350 | 15010 | 1340 |
| 323.15 | 0.3108 | -130.3 | -131.2 | 0.9 | 6620 | 6710 | -90 |
|  | 0.3487 | -135.0 | -135.5 | 0.4 | 7280 | 7180 | 100 |
|  | 0.5709 | -165.0 | -164.2 | -0.8 | 10640 | 10620 | 20 |
|  | 0.5866 | -167.3 | -166.5 | -0.8 | 10870 | 10900 | -30 |
| 333.15 | 0.3222 | -122.0 | -123.2 | 1.2 | 6520 | 6170 | 350 |
|  | 0.4489 | -136.6 | -137.5 | 0.9 | 7940 | 8110 | -170 |
|  | 0.5791 | -153.9 | -154.0 | 0.2 | 9900 | 10420 | -520 |
|  | 0.7362 | -178.5 | -176.6 | -1.9 | 13790 | 13320 | 470 |
| 343.15 | 0.3210 | -110.5 | -110.8 | 0.3 | 5130 | 5500 | -370 |
|  | 0.4956 | -132.5 | -128.4 | -4.2 | 8250 | 8010 | 240 |
|  | 0.6856 | -157.6 | -152.3 | -5.3 | 12160 | 11260 | 900 |
|  | 0.7927 | -161.4 | -168.0 | 6.5 | 12020 | 13070 | -1050 |

Table 6. Smoothed Second and Third Virial Coefficents for the R32 (1) + CO2 (2) System


## Experimental Procedure, Gas Chromatographic Calibration and Experimental Uncertainties

Experimental Procedure. To measure the system components, the classical Burnett experimental procedure was followed. Initially, the first vessel was filled with the sample and its temperature and pressure were measured. Then, after evacuating the second vessel, the expansion valve was opened. Once the pressures between the vessels had equalized, the second vessel was isolated and evacuated again. This procedure was repeated until low pressures were achieved.

In the mixture-charging procedure, the two vessels were separately filled with different compounds. Then the fluids were mixed together with the aid of the magnetic pump while the expansion valve was kept open. During the first expansion, a sample of the mixture was collected and used for gas chromatographic analysis of the mixture's composition.

Gas Chromatographic Calibration. The mixtures for the calibration were prepared in stainless steel bottles of about $250 \mathrm{~cm}^{3}$ capacity; the mass of charged components, depending on the composition, was varied from 8 to 15 g and was weighed with an analytical balance to $\pm 0.1 \mathrm{mg}$. On that basis, the molar fraction of the sample was found. Next, the prepared samples were connected on-line to the gas chromatograph, and after the sample was preheated to about 323 K (for the sample homogenization), a series of gas chromatographic analyses was performed. The reproducibility of the gas chromatograph for each sample was within $0.1 \%$. The results of the analysis for the series of samples covering a wide range of composition were next regressed to find the relation between ratio of area and composition in molar fraction. A third-degree polynomial expression, obtained by forcing it also to the points corresponding to pure compounds, gives us the unknown composition when its peak area ratio is measured. The
composition of the mixtures was found from the gas chromatographic analysis performed for the same gas chromatograph parameters and applying the expression found. F or the analysis, the samples collected from the first Burnett expansions were used. Further details of the method are given in ref 5 .

Experimental Uncertainties. The uncertainty in the temperature measurements is due to the thermometer and any instability of the bath. The stability of the bath was found to be better than $\pm 0.015 \mathrm{~K}$, and the uncertainty of the thermometer was found to be better than $\pm 0.010 \mathrm{~K}$ in our temperature range. The total uncertainty in the temperature measurements was thus lower than $\pm 0.03 \mathrm{~K}$.

The uncertainty in the pressure measurements is due to the transducer and null indicator system, and to the pressure gauges. The digital pressure indicator (Ruska, mod. 7000 ) has an uncertainty of $\pm 0.003 \%$ of the full scale. The total uncertainty in the pressure measurement is also influenced by temperature fluctuations due to bath instability and was found to be lower than $\pm 1 \mathrm{kPa}$.
The uncertainty of the mixture's composition was found to be always lower than $0.5 \%$ in mole fraction, based on the calibration with samples prepared gravimetrically and on the reproducibility of the gas chromatograph (Carlo Erba Mega Series 5380 with a thermal conductivity detector).

## Results for $\mathbf{R} 32$ and $\mathbf{C O}_{2}$

For R32, 81 experimental points along 5 isotherms (9 sets in all) were collected in the temperature range from 303 K to 343 K and for pressures from 125 kPa up to 4370 kPa . For $\mathrm{CO}_{2}, 234$ experimental points along 7 isotherms (17 sets altogether) were collected in the temperature range from 283 K to 363 K and in the pressure range from 11 kPa to 5700 kPa . The experimental data for R32 are shown in Table 1 while the experimental data for $\mathrm{CO}_{2}$ are reported elsewhere. ${ }^{6}$


Figure 4. Second virial coefficients for the R 32 (1) $+\mathrm{CO}_{2}$ (2) system against the mole fraction at the following temperatures, T: $0,303.15 ; \square, 313.15 ; \Delta, 323.15 ; \nabla, 333.15 ; \diamond, 343.15 \mathrm{~K}$. The lines represent the correlated values.

The experimental PVT measurements were used to derive the second, $B$, and third, $C$, virial coefficients of the virial equation

$$
\begin{equation*}
P=\frac{R T}{V}\left(1+\frac{B}{V}+\frac{C}{V^{2}}\right) \tag{1}
\end{equation*}
$$

In the regression, each run was treated separately and $(\mathrm{dP})^{2}$ was used as an objective function applying the Burnett constant from the helium calibration. The pressure distortion of the Burnett cells was considered, as explained elsewhere. ${ }^{2-4}$

Defining the average absolute deviation in pressure as

$$
\begin{equation*}
\mathrm{AAD}=\sum_{\mathrm{i}=1}^{\mathrm{N}} \mathrm{abs}(\mathrm{dP}) / \mathrm{N} \tag{2}
\end{equation*}
$$

the $A A D=0.239 \mathrm{kPa}$ for R 32 and $A A D=0.163 \mathrm{kPa}$ for $\mathrm{CO}_{2}{ }^{6}$ were found, well within the estimated experimental uncertainty.

The second and third virial coefficients for R32 and for $\mathrm{CO}_{2}$ are shown in Tables 2 and 3, together with the pressure deviations from the fit that proved to be randomly distributed. A systematic deviation in pressure is not evident for both compounds, enabling us to say that the adsorption does not affect the results.

In Figures 2 and 3, the second and third virial coefficients for R32 are plotted and compared with values in the literature. ${ }^{7-11}$ In Figure 2, the derived second virial coefficients were compared with the values calculated by means of the Tsonopoulos correlating method, ${ }^{12}$ while, in Figure 3, the third virial coefficients were compared with the ones calculated with the empirical expression

$$
\begin{equation*}
\mathrm{C}=\mathrm{A}_{1}+\mathrm{A}_{2}\left(\mathrm{~T}_{\mathrm{r}}-1\right)+\mathrm{A}_{3}\left(\mathrm{~T}_{\mathrm{r}}-1\right)^{2} \tag{3}
\end{equation*}
$$

where $A_{1}=14$ 565.3408; $A_{2}=-49881.8850 ;$ and $A_{3}=$ 105331.4976.

For R32, there is a good consistency with most of the literature data for the second virial coefficient (refs 7, 8, 10, and 11), while the data in ref 9 are systematically lower. For the third virial coefficients, the results (obtained in a different temperature region) clearly follow a common temperature trend with data in the literature, ${ }^{8,10}$ even if quite big deviations from the trend are evident while comparing data from various sources. F or comparison, we


Figure 5. Third virial coefficients for the R32 (1) $+\mathrm{CO}_{2}(2)$ system against the mole fraction at the following temperatures, $\mathrm{T}: \mathrm{O}$, 303.15; ■, 313.15; $\Delta, 323.15 ; \nabla, 333.15 ; \diamond, 343.15 \mathrm{~K}$.


Figure 6. Deviations in pressure produced by the REFPROP $6.01^{15}$ at the following temperatures, T: O, 303.15; $\square, 313.15 ; \Delta$, $323.15 ; \nabla$, 333.15 ; 厄, 343.15 K .
only considered literature sources in which original data were reported.

For $\mathrm{CO}_{2}$, all the comparisons with the literature are reported elsewhere; ${ }^{6}$ hence, we only report a brief summary of the results here. For the second virial coefficient, the present experimental results are consistent with the literature sources. ${ }^{1}$ Also, the Tsonopoulos correlating method ${ }^{13}$ represents the experimental data well. For the third virial coefficients, the experimental data in the literature are randomly scattered within $25 \%$ around values resulting from the Orbey and Vera correlation; ${ }^{14}$ our results lay well within that limit.

## Results for the Mixtures

For the $\mathrm{R} 32+\mathrm{CO}_{2}$ system, 185 experimental points along 20 sets and 5 isotherms were collected within the temperature range from 303 to 343 K and the pressure range from 110 kPa to 5100 kPa . The experimental findings, together with the compressibility factor values, are given in Table 4. The virial coefficients for the mixtures were found by applying the same procedure as that for the pure compounds. The values of the second and third virial coefficients (Table 5), along with the virial coefficients for the pure compounds (smoothed as a function of reduced temperature), were used to derive cross virial coefficients. The results are shown in Table 6. The second cross virial coefficients were calculated from the expression

$$
\begin{equation*}
B_{m}=\sum_{i=1}^{n} \sum_{j=1}^{n} B_{i j} x_{i} x_{j} \tag{4}
\end{equation*}
$$

for each experimental datum point. Next, the $B_{12}$ values found for each temperature were averaged; the averaged $B_{12}$ values, given in Table 6, were used to calculate the deviations of $B_{m}$ from the experimental values shown in Table 5. The third cross virial coefficients were calculated from the defining equation

$$
\begin{equation*}
C_{m}=\sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{k=1}^{n} C_{i j k} x_{i} x_{j} x_{k} \tag{5}
\end{equation*}
$$

Bearing in mind that two-third cross virial coefficients (namely $\mathrm{C}_{112}$ and $\mathrm{C}_{122}$ ) represent third virial coefficients for each mixture's composition, their values could not be calculated directly for each datum point, so they were calculated as average values by combining data for each temperature. The averaged values of the third cross virial coefficients are included in Table 6. Using these values, the third virial coefficients for the mixtures were recalculated for each point. The results, together with the deviations, are also included in Table 5. The greatest random error in $B_{m}$ was found at $T=343.15 \mathrm{~K}$ with $A A D=4.08$ $\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$, while at $\mathrm{T}=(303.15,313.15,323.15$, and 333.15) K the average absolute deviation was found to be AAD $=0.91 \mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1}$. This is presumably due to a possible slightly poorer thermal stability at higher temperatures while a (water + ethylene glycol) mixture is used as the bath fluid. The overall AAD for $B_{m}$ was evaluated at 2.5 $\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$, while the AAD for $\mathrm{C}_{\mathrm{m}}$ was $399 \mathrm{~cm}^{6} \cdot \mathrm{~mol}^{-2}$, corresponding to an average deviation of around $10 \%$. These values are acceptable if compared with numerous experimental data, obtained in reduced temperature ranges below or close to 1, reported in the compilation. ${ }^{14}$ The second and third virial coefficients for the system being plotted against the mole fraction in Figures 4 and 5, respectively, show positive and negative deviations from ideality, defined here as

$$
\begin{gather*}
\mathrm{B}_{12}=\left(\mathrm{B}_{11}+\mathrm{B}_{22}\right) / 2  \tag{6}\\
\mathrm{C}_{112}=\left(2 \mathrm{C}_{111}+\mathrm{C}_{222}\right) / 3  \tag{7}\\
\mathrm{C}_{122}=\left(\mathrm{C}_{111}+2 \mathrm{C}_{222}\right) / 3 \tag{8}
\end{gather*}
$$

Because of the total lack of data in the literature on the superheated vapor region for this system, the experimental findings were compared with the prediction obtained with the REFPROP $6.01^{15}$ software. The calculations were performed at the highest experimental pressures of each run, adopting regressed values for $\rho(1), \mathrm{B}_{\mathrm{m}}$, and $\mathrm{C}_{\mathrm{m}}$. The differences in pressure are given in Figure 6, showing a consistency within 1\%; the figures were systematically below those resulting from our experiment.

## Conclusions

This work reports on experimental results for the R32 $+\mathrm{CO}_{2}$ system obtained with the Burnett method. The
performance of the apparatus was checked by means of measurements for R32 and $\mathrm{CO}_{2}$, and a good consistency was observed between the virial coefficients obtained and those reported in the literature. The $\mathrm{R} 32+\mathrm{CO}_{2}$ system was studied over five isotherms, and second and third cross virial coefficients were derived. Over the entire temperature range, the second virial coefficients showed positive (while the third virial coefficients showed negative) deviations from ideality. Our results proved consistent with the prediction obtained using REFPROP 6.01.

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## Literature Cited

(1) Angus, S.; Armstrong, B.; de Reuck, K. M. International Thermodynamic Tables of the Fluid State, vol. 3, Carbon Dioxide; Pergamon Press: Oxford, 1976.
(2) Glowka, S. A Burnett Apparatus for Accurate Determination of the Volumetric Properties of Gases. Naucznaja apparatura 1988, 3, 79-84.
(3) Glowka, S. Determination of Volumetric Properties of Ammonia Between 298 and 473 K and Carbon Dioxide Between 304 and 423 K Using the Burnett Method. Polym. J. Chem. 1990, 64, 699709.
(4) Glowka, S. Volumetric Properties of Ammonia + Argon, + Helium, + Methane, and + Nitrogen Mixtures Between 298 and 423 by the Burnett- Isochoric Method. Fluid Phase Equilib. 1992, 78, 285-296.
(5) Bobbo, S.; Stryjek, R.; Elvassore, N.; Bertucco, A. A Recirculation Apparatus for Vapor-Liquid Equilibrium Measurements of Refrigerants Binary Mixtures of R600a, R134a and R236fa. Fluid Phase Equilib. 1998, 150-151, 343-352.
(6) Di Nicola, G.; Giuliani, G.; Polonara, F.; Stryjek, R. PVTx Measurements for the R125+CO2 System by the Burnett Method. Fluid Phase Equilib. 2002, 199, 163-176.
(7) BignelI, C. M.; Dunlop, P. J. Second Virial Coefficients for Fluoromethanes and their Binary Mixtures with Helium and Argon. J. Chem. Eng. Data 1993, 38, 139-140.
(8) Defibaugh, D. R.; Morrison, G.; Weber, L. A. Thermodynamic Properties of Difluoromethane. J. Chem. Eng. Data 1994, 39, 333-340.
(9) Quian, Z. Y.; Nishimura, A.; Sato, H.; Watanabe, K. Compressibility Factors and Virial Coefficients of Difluoromethane (HFC32) Determined by Burnett Method. J SME Int. J . 1993, 36, 665670.
(10) Sato, T.; Sato, H.; Watanabe, K. PVT Property M easurements for Difluoromethane (HFC-32). J . Chem. Eng. Data 1994, 39, 851854.
(11) Zhang, H. L.; Sato, H.; Watanabe, K. Second Virial Coefficients for R-32, R-125, R-134a, R-143a, R-152a and their Binary Mixtures. Proceedings of the 19 ${ }^{\text {th }}$ International Congress of Refrigeration, The Hague, The Netherlands, 1995; Vol. IVa, pp 622-629.
(12) Tsonopoulos, C. An empirical correlation of second virial coefficients. AICHE J. 1974, 20, 263-272.
(13) Orbey, H.; Vera, J. H. Correlation for the third virial coefficient using $\mathrm{T}_{\mathrm{c}}, \mathrm{P}_{\mathrm{c}}$ and $\omega$ as parameters. AICHE J. 1983, 29, 107-113.
(14) Dymond, J. H.; Smith, E. B. The Virial Coefficients of Gases; Clarendon Press: Oxford, 1969.
(15) McLinden, M. O.; Klein, S. A.; Lemmon, E. W.; Peskin, A. P. NIST Thermodynamic and transport properties of refrigerants and refrigerant mixtures (REFPROP), version 6.01; Boulder, CO, 1998.

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