Densities, Excess Molar Volumes, and Excess Molar Enthalpies of (*N*-Methyl-2-pyrrolidinone + Ketone) at T = 298.15 K

Urszula Domańska* and Joanna Łachwa

Warsaw University of Technology, Faculty of Chemistry, Physical Chemistry Division, Noakowskiego 3, 00-664 Warsaw, Poland

Trevor M. Letcher

University of Natal, Department of Chemistry and Applied Chemistry, Durban 4041, South Africa

The densities have been measured at 298.15 K and atmospheric pressure for nine binary mixtures of N-methyl-2-pyrrolidinone with + 2-propanone or + 2-butanone or + 2-pentanone or + 3-pentanone or + cyclopentanone or + 2-hexanone or + 4-methyl-2-pentanone or + 4-heptanone or + 5-nonanone using a vibrating-tube densimeter. The excess molar volumes have been calculated from measured values of densities. The excess molar enthalpies have been measured at 298.15 K and atmospheric pressure for two mixtures of N-methyl-2-pyrrolidinone + 4-heptanone or + 5-nonanone using flow calorimetry. The experimental results have been correlated and compared with the results from the Flory-Benson-Treszczanowicz (FBT) theory and from the extended real associated solution (ERAS) theory. The results are discussed in terms of the intermolecular association.

Introduction

Continuing research into the thermodynamic excess functions and the thermodynamics of phase equilibria of mixtures containing *N*-methyl-2-pyrrolidinone (NMP),¹⁻¹⁹ we present here excess molar volumes and excess molar enthalpies for (NMP + ketone). The compound NMP is a heterocyclic, polar solvent used for the extraction of low molecular weight aromatic compounds from petroleum feedstock.²⁰ The knowledge of the excess molar properties of a solvent in some organic liquids is useful in predicting the solution behavior in other organic liquids.²¹

In this paper we report excess volumes $V_{\rm m}^{\rm E}$ and excess enthalpies $H_{\rm m}^{\rm E}$ of the NMP with some ketones. The Flory– Benson–Treszczanowicz (FBT) theory^{22,23} and the extended real associated solution (ERAS)^{24,25} theory were used to correlate the experimental data. The FBT model has been applied to describe simultaneously $V_{\rm m}^{\rm E}$ and $H_{\rm m}^{\rm E}$ of mixtures containing only one self-associating component (NMP). The cross-association constant in the mixture was assumed to be equal to zero.

Experimental Section

Herein are reported the Chemical Abstracts Service registry numbers and the sources of the chemicals: *N*-methyl-2-pyrrolidinone (872-50-4, Aldrich), 2-propanone (67-64-1, POCH), 2-butanone (78-93-3, Aldrich), 2-pentanone (107-87-9, Aldrich), 3-pentanone (96-22-0, Aldrich), cyclopentanone (120-92-3, PROLABO), 2-hexanone (591-78-6, Aldrich), 4-methyl-2-pentanone (108-10-1, Merck), 4-heptanone (123-19-3, Janssen Chimica, 98%), and 5-nonanone (502-56-7, Janssen Chimica). The chemicals were dried over type 0.4-nm molecular sieves (SERVA, Heidelberg, F.R.G.) and purified by fractional distillation. After the distillation all

 * To whom correspondence should be addressed. E-mail: Ula@ ch.pw.edu.pl.

Table 1. Physical Constants of Pure Compounds at T = 298.15 K: *d*, Density; V_{mol} , Molar Volume; α , Cubic Expansion Coefficient; κ_T , Isothermal Compressibility

	d^{exp}	$d^{\rm lit}$	$V_{ m mol}$	$\alpha \times 10^4$	$\kappa_{\rm T} imes 10^4$
component	g•cm ⁻³	g·cm ⁻³	cm ³ ⋅mol ⁻¹	K ⁻¹	MPa ⁻¹
<i>N</i> -methyl-2- pyrrolidinone	1.02851	1.02804 ^a	96.43 ^a	8.37 ^a	8.42 ^b
2-propanone	0.78510	0.78547 ^c	74.05^{d}	14.6^{d}	13.30^{d}
2-butanone	0.80085	0.79992^{e}	90.16 ^f	13.1^{f}	11.52^{f}
2-pentanone	0.80191	0.80145 ^g	107.47 ^g	10.2^{g}	10.82 ^g
3-pentanone	0.80994	0.80945 ^c	106.41 ^h	12.0^{h}	10.73^{h}
cyclopentanone	0.95712	i	i	i	i
2-hexanone	0.80697	0.80698 ^g	124.12^{g}	11.1^{g}	9.97^{g}
4-methyl-2- pentanone	0.79612	0.79625 ^g	125.79 ^g	11.4 ^g	11.00 ^g
4-heptanone	0.81106	i	140.79	10.5 ^j	9.32^{j}
5-nonanone	0.81739	i	174.02	9.5/	8.38 ^j

^{*a*} From ref 3. ^{*b*} From ref 7. ^{*c*} From ref 27. ^{*d*} From ref 28. ^{*e*} From ref 29. ^{*f*} From ref 30. ^{*g*} From ref 31. ^{*h*} From ref 32. ^{*i*} Not found. ^{*j*} Extrapolated from values of other ketones C_3-C_6 .

compounds were checked by GLC analysis and no significant impurities (less than 0.003 mass %) were found. Analysis using the Karl-Fisher technique showed that the impurity in each of the solvents was less than 0.02 mol %. The density of the compounds were measured as a test of purity.

An Anton Paar DMA 602 vibrating-tube densimeter thermostated at $T = (298.15 \pm 0.01)$ K was used to determine the densities. The densimeter's calibration was performed at atmospheric pressure using doubly distilled and degassed water, specially purified benzene (CHEMIPAN, Poland, 0.999), and dried air. The vibratingtube temperature was measured by an Anton Paar DM 100-30 digital thermometer and was regulated to within better than ± 0.01 K. The temperature was stabilized using a UNIPAN 60 thermostat and 202 temperature control system (UNIPAN, Poland). Mixtures were prepared by

Table 2. Experimental Excess Molar Volumes V_m^E for {x NMP + (1-x) RCOR'} Systems at 298.15 K

	$V_{\mathrm{m}}^{\mathrm{E}}$	$\delta V^{\rm E}_{ m m} imes 10^{-3}$		$V_{\mathrm{m}}^{\mathrm{E}}$	$\delta V_{ m m}^{ m E} imes 10^{-3}$		$V_{\mathrm{m}}^{\mathrm{E}}$	$\delta V^{\rm E}_{ m m} imes 10^{-3}$	
Х	$\overline{\mathrm{cm}^3\cdot\mathrm{mol}^{-1}}$	cm ³ ⋅mol ⁻¹	Х	$\overline{\mathrm{cm}^3\cdot\mathrm{mol}^{-1}}$	cm ³ ⋅mol ⁻¹	X	$\overline{\mathrm{cm}^3\cdot\mathrm{mol}^{-1}}$	cm ³ ·mol ⁻¹	
x NMP + (1-x) 2-Propanone									
0.0239	-0.097	-5	0.4480	-0.738	-2	0.7108	-0.527	-6	
0.1176	-0.386	-1	0.4882	-0.719	5	0.7730	-0.426	5	
0.1832	-0.532	-1	0.5323	-0.706	-5	0.8804	-0.243	2	
0.2536	-0.636	4	0.5791	-0.661	7	0.9118	-0.186	-1	
0.3553	-0.724	-1	0.6310	-0.623	-5				
			хN	MP + (1-x) 2-B	utanone				
0.0104	-0.034	-6	0.2653	-0.514	-7	0.7898	-0.366	-8	
0.0193	-0.053	0	0.3474	-0.572	3	0.8553	-0.267	-7	
0.0861	-0.222	-5^{-5}	0.4669	-0.599	6	0.8963	-0.190	3	
0.1564	-0.356	-1	0.5740	-0.563	10	0.9896	-0.016	5	
0.2201	-0.455	-2	0.6959	-0.476	-3	0.0000	0.010	0	
			v NI	(1 - x) 2 D	ntanana				
0.0740	0 177	9	0 4194	(1-x) 2-P(1-x) - P(1-x) - P(0 7499	0.400	F	
0.0740	-0.177	-3	0.4124	-0.370	-3	0.7403	-0.400	5	
0.1141	-0.245	9	0.4730	-0.370	0	0.0339	-0.291	0	
0.2034	-0.399	0	0.0382	-0.564	0	0.9067	-0.174	0	
0.2394	-0.452	-8 F	0.6213	-0.528	-6	0.9631	-0.068	4	
0.3338	-0.526	5	0.6799	-0.480	-4				
			x NI	MP + (1-x) 3-Pc	entanone			_	
0.1497	-0.238	6	0.6212	-0.456	6	0.9169	-0.142	-7	
0.2798	-0.401	-4	0.7495	-0.357	0	0.9735	-0.053	-9	
0.4524	-0.497	-3	0.7567	-0.346	3				
0.5322	-0.497	-3	0.8481	-0.235	1				
			x NM	P + (1-x) Cyclo	pentanone				
0.0340	-0.0162	0	0.4752	-0.0993	. 1	0.8281	-0.0474	-1	
0.1086	-0.0470	0	0.5088	-0.0961	2	0.8656	-0.0375	-1	
0.2353	-0.0778	4	0.5643	-0.0890	5	0.9234	-0.0232	-2	
0.2968	-0.0978	-6	0.6922	-0.0718	3	0.9460	-0.0172	$^{-2}$	
0.3628	-0.1012	-3	0.7899	-0.0601	-5	0.9887	-0.0022	1	
			٧N	MP + (1 - v) 2 - H	avanone				
0 1977	-0 299	10	0.5222	-0.465	0	0.8318	-0.250	0	
0.3143	-0.417	-4	0.5916	-0.451	-5	0.8927	-0.171	-1	
0.3615	-0.447	-7	0.6663	-0.402	5	0.9740	-0.049	-5	
0.4813	-0.466	2	0.7560	-0.330	3	0.0710	0.010	Ū	
			v NMD 4	-(1-y) 4 Mothy	2 poptanono				
0.0231	-0.055	9	0 3232	-0.601		0 7175	-0.519	9	
0.0231	-0.228	9	0.3232	-0.662	-1	0.7175	-0.465	2	
0.0852	-0.228	~ _2	0.4361	-0.002	-1	0.7393	-0.403	_~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	
0.1430	-0.330	-5	0.4002	-0.004	1	0.8200	-0.370	-7	
0.2022	-0.445	3	0.5597	-0.043	4				
0.2055	-0.541	-4	0.0340	-0.387	0				
0.4000	0.040	2	X NI	MP + (1-x) 4-H	eptanone	0.0000	0.007	0	
0.1989	-0.246	3	0.5755	-0.378	4	0.8288	-0.225	-3	
0.2961	-0.326	0	0.5789	-0.377	4	0.9001	-0.149	-8	
0.3849	-0.379	-9	0.6117	-0.370	1	0.9233	-0.116	-5	
0.4588	-0.393	-5	0.6772	-0.340	2				
0.5060	-0.389	2	0.7511	-0.286	6				
			хN	MP + (1-x) 5-N	onanone				
0.2348	-0.140	6	0.5276	-0.221	-6	0.7037	-0.182	3	
0.3643	-0.189	4	0.5404	-0.220	-6	0.7795	-0.149	6	
0.4331	-0.207	1	0.5814	-0.216	-4	0.8931	-0.087	1	
0.4729	-0.213	-1	0.6591	-0.200	-2	0.9475	-0.035	11	

mass, the error in mole fraction being estimated as less than 5 \times 10⁻⁵. The method of determining excess molar volumes has been described elsewhere.²⁶ The densities, *d*, of the pure liquids determined here were compared to the literature values in Table 1. The estimated standard uncertainty, *u_i*, in the excess molar volume *V*^E_m is less than ±0.005.

A Thermometric 2277 thermal activity monitor in flow mode, driven by two LKB peristaltic pumps, was used to determine H_m^E at T = 298.15 K. The temperature was accurate to within ± 0.01 K and was monitored by a calibrated quartz thermometer fixed in the cell compartment. The experimental procedure has been detailed previously.³³ The estimated error in the excess enthalpy H_m^E and mole fraction *x* is less than $\pm 2\%$ and $\pm 0.1\%$, respectively. The accuracy of the method was verified with a test on (hexane + cyclohexane). 34 The experimental results agreed with the literature data to within ± 5 J (2%) in the worst case.

Excess Molar Functions

The $V_{\rm m}^{\rm E}$ values are given in Table 2 and $H_{\rm m}^{\rm E}$ values are given in Table 3, together with the deviations $\delta V_{\rm m}^{\rm E}$ and $\delta H_{\rm m}^{\rm E}$, respectively, calculated from the smoothing equation

$$\delta Z_{\rm m}^{\rm E} = Z_{\rm m}^{\rm E} - x(1-x) \sum_{r=0}^{r=3} X_r (2x-1)^r \tag{1}$$

where *x* is the mole fraction of the NMP and Z_m^E is either $V_m^E/(\text{cm}^3 \cdot \text{mol}^{-1})$ or $H_m^E/(J \cdot \text{mol}^{-1})$. The values of the pa-

Table 3. Experimental Excess Molar Entalpies H_m^E for {x NMP + (1-x) RCOR'} Systems at 298.15 K

	$H_{ m m}^{ m E}$	$\delta H_{\rm m}^{\rm E}$		$H_{ m m}^{ m E}$	$\delta H_{\rm m}^{\rm E}$		$H_{ m m}^{ m E}$	$\delta H_{\rm m}^{\rm E}$
X	$\overline{\mathbf{J}\boldsymbol{\cdot}\mathbf{mol}^{-1}}$	$\overline{\mathbf{J}\boldsymbol{\cdot}\mathbf{mol}^{-1}}$	X	$\overline{\mathbf{J}\boldsymbol{\cdot}\mathbf{mol}^{-1}}$	$\overline{\mathbf{J}\boldsymbol{\cdot}\mathbf{mol}^{-1}}$	X	$\overline{\mathbf{J}\boldsymbol{\cdot}\mathbf{mol}^{-1}}$	$\overline{\mathbf{J}\boldsymbol{\cdot}\mathbf{mol}^{-1}}$
			x NM	P + (1 - x) 4-Hep	otanone			
0.3064	184.0	-1.7	0.4912	225.2	-1.1	0.6728	176.7	-8.8
0.3568	205.4	0.7	0.5865	213.9	-0.5	0.7144	168.9	0.5
0.4217	223.1	2.5	0.6192	206.5	1.1	0.8727	74.4	0.3
			x NM	P + (1-x) 5-Nor	nanone			
0.2365	179.0	3.0	0.4086	306.3	-3.9	0.7544	358.3	5.4
0.2638	202.3	3.5	0.4906	356.5	-1.2	0.8089	309.8	0.2
0.3400	262.0	1.6	0.6545	386.1	-4.1			
0.3719	281.4	-3.1	0.7027	379.9	1.3			

Table 4. Coefficients, X_r , for Eq 1 and Standard Deviation, σ , Calculated According to Eq 2, A_r , for the Excess Molar Volume and B_r for the Excess Molar Enthalpy for {x NMP + (1-x) RCOR'} Systems at 298.15 K

					$\sigma imes 10^3$
system		A_0	A_1	A_2	cm ³ ⋅mol ⁻¹
NMP +					
2-propanone		-2.876	0.904	-0.244	5
2-butanone		-2.404	0.423		6
2-pentanone		-2.291	0.287		5
3-pentanone		-1.990	0.059	0.235	6
cyclopentanone		-0.395	0.109		3
2-hexanone		-1.871	0.127		5
4-methyl-2-pentar	none	-2.659	0.200		5
4-heptanone		-1.564			5
5-nonanone		-0.857	-0.080		6
					σ
system	B_0		B_1	B_2	J•mol ^{−1}
NMP +					
4-heptanone	904	.4 –	56.8	-351.5	2.4
5-nonanone	1448	.0 8	98.3		3.5

rameters X_r refer to volumes (A_r) or enthalpies (B_r) and have been determined using a method of least-squares. The parameters are given in Table 4 for V_m^E and H_m^E together with the standard deviations σ

$$\sigma = \{\sum_{i=1}^{n} (Z_{m,expt}^{E} - Z_{m,calc}^{E})_{i}^{2} / (n-k)\}^{1/2}$$
(2)

where n is the number of experimental points and k is the number of coefficients.

The $V_{\rm m}^{\rm E}$ is negative for all the mixtures over the entire composition range. This could be due to the packing effect and the association between NMP and the ketone. The minimum of $V_{\rm m}^{\rm E}$ occurs over the mole fraction range 0.4 < x < 0.5. The excess molar volume data increases in the following order: 2-propanone < 4-methyl-pentanone < 2-butanone < 2-pentanone < 3-pentanone < 2-hexanone < 4-heptanone < 5-nonanone < cyclopentanone. The largest negative $V_{\rm m}^{\rm E}$ results were observed for the (NMP + 2-propanone). The minimum of the experimental curve is skewed toward the low concentrations of NMP. The $V_{\rm m}^{\rm E}$ (min) value was $-0.736 \, {\rm cm}^3 \cdot {\rm mol}^{-1}$ for x = 0.4239. The $V_{\rm m}^{\rm E}$ (at x = 0.5) data increases with increasing the normal ketone chain length (see Figure 1).

The comparison of the excess molar volumes for the mixtures of NMP with three different isomers of pentanone (see Figure 2) has shown that the better packing effect and the association effects A–B are stronger for a nonsymmetrical chain ketone (2-pentanone) compared with those of a symmetrical chain (3-pentanone). The $V_{\rm m}^{\rm E}$ (0.5) value was $-0.573 \,{\rm cm^3 \cdot mol^{-1}}$ and $-0.498 \,{\rm cm^3 \cdot mol^{-1}}$ for 2-pentanone)



Figure 1. Excess molar volume V_m^E for a binary mixture of *x* NMP + (1-x) (\bigcirc) 2-propanone, or (\blacktriangle) 2-butanone, or (\square) 4-heptanone, or (\bigcirc) 5-nonanone at 298.15 K. Solid lines are calculated by the Redlich-Kister equation.

tanone and 3-pentanone, respectively. The smallest $V_{\rm m}^{\rm E}$ results were observed for the (NMP + cyclopentanone) system. The minimum of the $V_{\rm m}^{\rm E}$ curve was -0.101 cm³·mol⁻¹ for x = 0.4348. This reflects a small deviation from additivity in the mixture containing two cyclic compounds.

A similar effect is observed during the comparison between a branched chain ketone and the straight chain ketone (see Figure 3). The $V_m^{\rm E}$ (min) value was -0.468 cm³·mol⁻¹ (for x = 0.50) and -0.666 cm³·mol⁻¹ for (x = 0.4823) for 2-hexanone and 4-methyl-2-pentanone, respectively. More negative excess molar volume, observed for a branched chain ketone, would seem to indicate that a more organized packing effect and stronger co-association A–B is present in mixtures containing a branched chain ketone.

The two, measured $H_{\rm m}^{\rm E}$ curves are positive. The $H_{\rm m}^{\rm E}$ (max) increases with increasing ketone chain length (see Figure 4), an order similar to the $V_{\rm m}^{\rm E}$ values. The $H_{\rm m}^{\rm E}$ (0.5) value was 226.1 J·mol⁻¹ and 362.0 J·mol⁻¹ for 4-heptanone and 5-nonanone, respectively. For 5-nonanone the maximum is shifted toward higher concentration of the NMP. This skewness reflects the dominance of self-association of the NMP at low concentration of a long-chain ketone in the mixture. No $H_{\rm m}^{\rm E}$ data were found in the literature on mixtures containing short-chain ketones. No measure-



Figure 2. Excess molar volume V_m^E for a binary mixture of *x* NMP + (1-x) (**•**) 2-pentanone, or (**•**) 3-pentanone, or (**•**) cyclopentanone at 298.15 K. Solid lines are calculated by the Redlich–Kister equation.



Figure 3. Excess molar volume V_m^E for a binary mixture of *x* NMP + (1-x) (\bigcirc) 2-hexanone, or (\bigcirc) 4-methyl-2-pentanone at 298.15 K. Solid lines are calculated by the Redlich-Kister equation.

ments were done on these mixtures in this work, as the ketones react with the tubing of the peristaltic pumps because they react with the tubing of the calorimeter.

The overall magnitude of $H_{\rm m}^{\rm E}({\rm max})$ is a result of the positive effect due to the breakdown of the weak NMP self-association and weak ketone–ketone molecules interaction. These results indicate that the cross-association is weaker than the self-association.

Flory-Benson-Treszczanowicz Model

The FBT model has been applied first to the excess volumes of binary systems formed by mixing a polar substance base with an alkane or cycloalkane.^{24,25} The



Table 5. Characteristic Parameters of Pure Components: V^* , T^* , p^* and Reduce Volume \tilde{v} from the FBT Model at 298.15 K

	<i>V</i> *	<i>T</i> *	n*	
			P	
component	cm³∙mol ^{−1}	K	J∙cm ⁻³	\tilde{V}
NMP	79.5	5796	436	1.213
2-propanone	55.5	4335	583	1.335
2-butanone	68.9	4555	580	1.308
2-pentanone	85.9	5175	440	1.252
3-pentanone	82.7	4754	553	1.287
2-ĥeksanone	97.7	4946	535	1.270
4-methyl-2-pentanone	98.6	4879	503	1.276
4-heptanone	111.9	5094	532	1.258
5-nonanone	140.6	5383	518	1.237

Table 6. Exchange Interaction Coefficient X_{AB} for the Equation of State Contribution and Summary of Calculations for Mixtures of NMP with a Ketone at the Equimolar Concentration Using the FBT Model

	$V_{\rm m}^{\rm E}({\rm exp})$	$H_{\rm m}^{\rm E}({\rm exp})$	X_{AB}	$V_{\rm m}^{\rm E}$ (calc)	$H_{\rm m}^{\rm E}$ (calc)
system	cm ³ ⋅mol ⁻¹	J•mol ^{−1}	J∙cm ^{−3}	cm ³ ⋅mol ⁻¹	J•mol ^{−1}
NMP +					
2-propanone	-0.719		-68.9	-0.719	-466.8
2-butanone	-0.601		-60.0	-0.601	-251.4
2-pentanone	-0.573		-35.3	-0.573	351.3
3-pentanone	-0.498		-46.2	-0.498	87.5
2-hexanone	-0.468		-40.4	-0.468	276.3
4-methyl-2- pentanone	-0.665		-45.6	-0.665	159.6
4-heptanone	-0.391	226.1	-24.7	-0.246	689.2
5-nonanone	-0.214	362.0	-10.5	-0.076	1148.9

excess volumes are described as sums of two contributions. One arises from self-association of the NMP base and is evaluated according to the Mecke–Kempter continuous association model.³⁵ The other comprises equation of state and interaction effects, which are treated according to the Flory theory. The chemical contribution arises from self-association of NMP. The value of $\Delta v_{\rm A}^* = -0.2 \text{ cm}^3 \cdot \text{mol}^{-1}$, $K_{298.15} = 0.58$, and the enthalpy of hydrogen bonding $\Delta H_{\rm A}^* = -23.6$ for NMP were developed earlier.⁷ The value of $\Delta v_{\rm B}^* = 0$, $K_{\rm B} = 0$, and $\Delta H_{\rm B}^* = 0$ for each of the six ketones

Table 7. Adjusted Binary ERAS Model Parameters Characterizing Mixture Properties: Enthalpy ΔH_{AB} , Volume	
ΔV_{AB}^* , and Constant of Cross-Association K _{AB} , Exchange Interaction Coefficient X _{AB} for the Equation of State	
Contribution, and Summary of Calculations for Mixtures of NMP with Ketone at the Equimolar Concentration	

		ΔH_{AB}^{*}	ΔV_{AB}^{*}	X _{AB}	$V_{\rm m}^{\rm E}$ (calc)	$H_{\rm m}^{\rm E}({\rm calc})$
system	K_{AB}	kJ∙mol ⁻¹	cm³∙mol ^{−1}	J∙cm ^{−3}	cm³∙mol ^{−1}	J•mol ^{−1}
NMP +						
2-propanone	1.0	-17.9	-7.4	7.5	-0.720	-252.1
2-butanone	1.0	-17.9	-7.0	7.0	-0.598	-83.8
2-pentanone	1.0	-17.9	-4.9	6.9	-0.577	0.4
3-pentanone	1.0	-17.9	-6.1	6.8	-0.502	44.3
2-hexanone	1.0	-17.9	-5.7	6.0	-0.469	180.9
4-methyl-2-pentanone	1.0	-17.9	-6.8	7.0	-0.672	249.4
4-heptanone	1.0	-17.9	-4.8	3.0	-0.388	222.8
5-nonanone	1.0	-17.9	-3.0	1.0	-0.220	359.1

were assumed to be equal to zero, which means no selfassociation compounds were shown.

The physical contribution was evaluated using the Flory formula $^{36-38} \,$

$$V_{\rm phys}^E = (x_1 V_1^* + x_2 V_2^*) [\tilde{v} - (\phi_1 \tilde{v}_1 + \phi_2 \tilde{v}_2)]$$
(3)

where \tilde{v} , \tilde{v}_1 , and \tilde{v}_2 are the reduced volumes of the mixture and the pure components. Application of the Flory theory requires equation of state parameters for the pure components. Values for the present systems are summarized in Tables 1 and 5.

A comparison of the predicted and the experimental excess properties for (NMP + 4-heptanone or + 5-nonanone) mixtures shows that the FBT model is not able to describe the excess functions for the straight-chain symmetrical ketone (see Figures 5 and 6). For these systems, V_m^E and H_m^E values, calculated by FBT, are however of the same sign as the experimental values. A comparison between the predicted and experimental values for x = 0.5 for two ketones is presented in Table 6, together with predicted $H_{\rm m}^{\rm E}$ for the systems not measured here. For cyclopentanone mixtures, no FBT calculations were possible because the pure component parameters, cubic expansion coefficient, and isothermal compressibility were not known. Finally, it should be noted that estimates of excess molar volumes and enthalpies, based on the interchange energy parameters, obtained from the present analysis of excess molar volumes, generally exhibit relatively large deviations from the experimental results due to the importance of contributions from other structural effects, such as interstitial accommodation and conformational changes.

ERAS Model

The ERAS model^{23,24} combines the real associated solution model with a free volume contribution using Flory's equation of state.^{36–38} A special property of the ERAS theory is its ability to predict simultaneously $H_{\rm m}^{\rm E}$, $V_{\rm m}^{\rm E}$, and $G_{\rm m}^{\rm E}$ of mixtures with self- and cross-associations. Experimental data of the excess properties for NMP + alcohol mixtures are described almost quantitatively by adjusting a few interaction parameters such as van der Waals interaction parameters, association constants, bonding enthalpies, and bonding volumes.^{7,15}

The version of the ERAS model, related to mixtures consisting of one associating component (NMP) and intermolecular association NMP–ketone, has been used to describe the experimental $V_{\rm m}^{\rm E}$ and $H_{\rm m}^{\rm E}$ data for the mixtures (NMP + ketone). Application of the ERAS theory to the mixtures containing a weakly self-associating component together with a cross-association, that is, (NMP + ketone), was described previously for the mixtures of (1-



Figure 5. Excess molar functions, $V_m^E(a)$ and $H_m^E(b)$, for a binary mixture of *x* NMP + (1-*x*) 4-heptanone at 298.15 K. (\bigcirc) Experimental results; (-) calculated data from FBT model; (- - -) calculated data from ERAS model.

alkanol + 1-alkene or 1-alkyne).³⁹ The equations obtained for the thermodynamic excess functions are split into two additive terms, which arise from the hydrogen-bonding effects (the so-called "chemical" contribution) and from nonpolar van der Waals interactions, which accounts for the free volume effects between unlike molecules (the "physical" contribution).

The parameters required for the calculation of the excess properties of NMP-ketone mixtures are evaluated in the



Figure 6. Excess molar functions, $V_m^E(a)$ and $H_m^E(b)$, for a binary mixture of *x* NMP + (1-x) 5-nonanone at 298.15 K. (\bigcirc) Experimental results; (-) calculated data from FBT model; (- -) calculated data from ERAS model.

following way. The value of Δv_A^* , K_A , and the enthalpy of hydrogen bonding ΔH_A^* for NMP are the same as in FBT calculations. Thermal expansion coefficients α and isothermal compressibilities κ_T of the pure substances were used from literature sources and are given in Table 1. The K_A values at other temperatures can be easily calculated by the relationship³⁹

$$K_{\rm A}(T) = K_{\rm A,298.15K} \exp\left\{\frac{\Delta H_{\rm A}^*}{R} \left(\frac{1}{T} - \frac{1}{298.15}\right)\right\}$$
(4)

The characteristic parameters V^* and p^* , obtained from the experimental data, are very similar to those obtained from the FBT model. The unknown parameters, the volume changes being a result of the A–B interaction, Δv_{AB}^* , the cross-association constant, K_{AB} , and enthalpy, ΔH_{AB}^* , and binary interaction coefficient, X_{AB} , have been obtained from a simultaneous adjustment to experimental data of H_m^E and V_m^E at x = 0.5 for two ketones: 4-heptanone and 7-nonanone. All binary ERAS model parameters and the results of prediction for the equimolar compositions using the ERAS model are presented in Table 7. $V_{\rm m}^{\rm E}$ and $H_{\rm m}^{\rm E}$ curves, calculated by the ERAS model for (NMP + 4-heptanone or 7-nonanone) mixtures, show good agreement with the experimental data at the equimolar concentration. The characteristic skewing of all $V_{\rm m}^{\rm E}$ curves toward low NMP concentration is well described by this model (see Figures 5 and 6). For all systems the $V_{\rm m}^{\rm E}$ and $H_{\rm m}^{\rm E}$ curves, as calculated by the ERAS model, are better represented than those by the FBT model. Some deviations in the symmetry of the predicted curves are, however, observed.

Conclusions

All the excess molar volumes reported in this work are large and negative, as was observed for the mixtures of NMP with ethers.¹⁷ The deviations of $V_{\rm m}^{\rm E}$ from ideality are about 30% of those observed for ethers. These negative effects are most likely to be due to packing effect changes in the "molar free volume" of NMP and ketone in the mixing process. From the experimental and calculated values of $V_{\rm m}^{\rm E}$ and $H_{\rm m}^{\rm E}$ one may expect much stronger A–B interactions between NMP and short-chain ketone molecules.

Better organized packing effect and stronger co-association A-B are observed for unsymmetrical and branched chain ketones.

A comparison of the calculated and the experimental excess properties for (NMP + ketone) mixtures shows that the ERAS model is better than the FBT model in describing excess properties for the mixtures discussed in this work (see Table 7), especially for the mixtures containing the longer chain ketones.

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