# Vapor-Liquid Equilibria in the Nitrogen + Carbon Dioxide + Propane System from 240 to $\mathbf{3 3 0}$ K at Pressures to $\mathbf{1 5}$ MPa 

Belgin Yucelen and Arthur J. Kidnay*<br>Department of Chemical Engineering and Petroleum-Refining, Colorado School of Mines, Golden, Col orado 80401


#### Abstract

Vapor-liquid equilibria were measured for the nitrogen, carbon dioxide, and propane ternary system and its constituent binaries over thetemperature range 240 K to 330 K . The binary systems were measured at 240,270 , and 330 K , and the ternary system was studied at 240 K for 2.0 and $13.0 \mathrm{MPa}, 270 \mathrm{~K}$ for 2.0 , 6.0 , and 13.0 MPa , and 330 K and 5 MPa . The Peng-Robinson equation of state was used to model the system.


## Introduction

The design and devel opment of separation processes in the natural gas industry requires accurate knowledge of the vapor-liquid equilibria of multicomponent systems consisting of the alkane hydrocarbons with carbon dioxide and nitrogen. Binary data are required for the development of thermodynamic models that are used for the prediction of phase equilibria in multicomponent mixtures, while ternary data are widely used to test the predictive models (Prausnitz, 1985). This is the tenth in a series of experimental studies designed to provide accurate vapor-liquid equilibria data for the gas processing industry.

## Review of Previous Work

The binary isotherms for systems composed of nitrogen, carbon dioxide, and propane have been studied extensively, but there are no measurements on the ternary system. The literature is summarized in Table 1.

## Experimental Section

The gases used in this study were purchased commercially and used without further purification. The nitrogen, carbon dioxide, and propane had minimum purities of $99.995,99.99$, and $99.95 \mathrm{~mol} \%$, respectively.

Two separate experimental units were used, one for temperatures below ambient and one for temperatures above.

Low-Temperature Apparatus. The equipment and procedure described by Wei et al. (1995) were used, with slight modifications to the low-temperature bath and the analytical procedures. Temperatures were measured to $\pm 0.01 \mathrm{~K}$ with a standard platinum resistance thermometer (IPTS-68), and pressures were measured by four Heise bourdon tube gauges (0-100 psia, 0-500 psia, 0-100 atm, and $0-2500 \mathrm{psia}$ ), accurate to $\pm 0.1 \%$ of the full scale reading.

Vapor and liquid samples were analyzed by a HewlettPackard 5890 series II gas chromatograph equipped with a thermal conductivity detector. A Hewlett Packard 3392 integrator was used for peak area evaluation. The composition of each sample was calculated using the calibration curves determined for each of the components by injecting

[^0]Table 1. Experimental Data for Systems of Nitrogen, Carbon Dioxide, and Propane

| temp/K | ref |
| :---: | :---: |
|  | Nitrogen + Carbon Dioxide |
| $288-303$ | Krichevskii et al., 1962 |
| $218-273$ | Zenner and Dana, 1963 |
| 273 | Muirbrock and Prausnitz, 1965 |
| 273 | Yorizane et al., 1970 |
| $253-288$ | Arai et al., 1971 |
| $250-320$ | Altunin et al., 1974 |
| 270 | Somait and Kidnay, 1978 |
| 220,240 | Al-Sahhaf, 1983 |
| $223-273$ | Dorau et al.,1983 |
| 250,270 | Brown et al., 1989a,b |
| 293 | Xu et al., 1992 |
|  | Carbon Dioxide + Propane |
| $290-366$ | Poettman and Katz, 1945 |
| $278-344$ | Reamer et al., 1951 |
| $233-273$ | Akers et al., 1954 |
| $305-361$ | Roof and Baron, 1967 |
| $232-273$ | Nagahama et al., 1974 |
| 244,266 | Hamam and Lu, 1976 |
| $213-273$ | Acosta et al., 1984 |
| $311-361$ | Niesen and Rainwater, 1990 |
| 230,270 | Webster, 1996 |
|  | Nitrogen + Propane |
| 90 | Vellinger and Pons, 1943 |
| $92-128$ | Chueng and Wang, 1964 |
| $103-353$ | Schindler et al., 1966 |
| $312-365$ | Roof and Baron, 1967 |
| $172-255$ | Cannon et al., 1968 |
| $114-122$ | Poon and Lu, 1974 |
| $230-290$ | Grausø et al., 1977 |
| $183-303$ | Hudziak et al., 1984 |
| $117-127$ | Llave et al., 1985 |

pure gas samples at a series of pressures. All three components exhibited linear relationships between the partial pressure and the peak area. The calibrations were checked by injecting mixtures prepared gravimetrically in this laboratory. The estimated error in the measured mole fractions is $\pm 0.002$.

High-Temperature Apparatus. The apparatus used by Brown et al. (1989a,b) was rebuilt with modifications in the vapor and liquid sampling lines and the vapor circulation pump. A schematic diagram is represented in Figure 1. The equilibrium cell, vapor pump, and both the liquid and vapor sample valves were inside a Hotpack oven, which


Figure 1. Schematic of high-temperature apparatus.

Table 2. Comparison of the Measured and Literature Vapor Pressures for Carbon Dioxide, Propane, and n-Butane

| temp/K | vapor pressure/MPa |  | dev/MPa |
| :---: | :---: | :---: | :---: |
|  | measured | lit. |  |
| Carbon Dioxide ${ }^{\text {a }}$ |  |  |  |
| 230.00 | 0.8946 | 0.8935 | +0.0011 |
| 240.00 | 1.2841 | 1.2830 | +0.0012 |
| 246.00 | 1.5710 | 1.5698 | +0.0012 |
| 250.00 | 1.7837 | 1.7856 | -0.0019 |
| 254.00 | 2.0243 | 2.0223 | +0.0020 |
| 256.00 | 2.1477 | 2.1489 | -0.0012 |
| 260.00 | 2.4173 | 2.4194 | -0.0021 |
| 266.00 | 2.8723 | 2.8705 | +0.0019 |
| 270.00 | 3.2018 | 3.2034 | -0.0016 |
| Propane ${ }^{\text {b }}$ |  |  |  |
| 240.00 | 0.1508 | 0.1479 | +0.0029 |
| 270.00 | 0.4336 | 0.4304 | +0.0032 |
| 330.00 | 1.9795 | 1.9822 | -0.0027 |
| 343.15 | 2.5848 | 2.5868 | -0.0020 |
| 344.26 | 2.6414 | 2.6417 | -0.0003 |
| n-Butane ${ }^{\text {c }}$ |  |  |  |
| 297.44 | 0.2386 | 0.2390 | -0.0004 |
| 327.57 | 0.5585 | 0.5578 | +0.0007 |
| 336.41 | 0.6933 | 0.6931 | +0.0002 |
| 351.11 | 0.9715 | 0.9702 | +0.0013 |

${ }^{\text {a }}$ Angus et al. (1976). ${ }^{\text {b }}$ Goodwin and Haynes (1982a). ${ }^{\text {c Goodwin }}$ and Haynes (1982b).
provided the temperature controlled environment. The temperature was measured with a platinum resistance thermometer (PRT) calibrated from 230 K to 373 K against the standard thermometer used for the low-temperature measurements. The PRT was placed inside the equilibrium cell in direct contact with the liquid and vapor. The PRT had a precision of $\pm 0.01 \mathrm{~K}$; however, shifts in the oven temperature decreased the accuracy of the temperature measurements to $\pm 0.1 \mathrm{~K}$. Pressures were measured from the liquid line using the Heise gauges of the low-temperature apparatus; the gauges were separated from theliquid by a Ruska differential null indicator.

Table 3. Nitrogen + Carbon Dioxide Binary System

| pressure/ MPa | pressure/ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{X}_{\mathrm{N}_{2}}$ | $\mathrm{YN}_{2}$ |  | $\mathrm{X}_{\mathrm{N}_{2}}$ | $\mathrm{yN}_{2}$ |
| 240 K |  |  |  |  |  |
| 1.285 | 0.0000 | 0.0000 | 3.341 | 0.0325 | 0.7002 |
| 1.696 | 0.0094 |  | 8.07 |  |  |
| 1.707 | 0.0082 | 0.3186 | 10.24 | 0.1705 |  |
| 2.000 |  |  | 10.93 | 0.1830 | 0.6977 |
| 2.647 | 0.0265 |  | 13.00 | 0.2467 | 0.6692 |
| 3.066 | 0.0307 |  |  |  |  |
| 270 K |  |  |  |  |  |
| 3.209 | 0.0000 | 0.0000 | 4.108 | 0.0164 |  |
| 3.567 | 0.0064 | 0.0759 | 5.076 | 0.0358 | 0.2629 |
| 3.688 | 0.0096 |  | 6.986 |  | 0.3728 |
| 3.719 | 0.0088 | 0.1036 | 10.90 | 0.1850 |  |
| 3.871 | 0.0125 |  | 11.97 | 0.2456 | 0.3822 |

A magnetic piston pump circulated the vapor from the top of the cell through a $2.8 \mu \mathrm{~L}$ sample valve and back to the bottom of the cell. The liquid was transferred by a diaphragm pump through a $0.2 \mu \mathrm{~L}$ sample valve and a stainless steel heat exchanger before returning to the cell. The samples were analyzed with the equipment and procedures used for the low-temperature measurements.

## Results and Discussion

The accuracy of the temperature and pressure measurements for both experimental units was verified by comparing the measured vapor pressures of the pure components with accepted values from the literature (Table 2).

The results of all the binary and ternary measurements are given in Tables 3-6. The data were modeled with the Peng-Robinson (1976) equation of state, using the standard linear mixing rule for the van der Waals volume b and quadratic mixing rule for the attraction parameter $a$, with one binary interaction coefficient, $\mathrm{k}_{\mathrm{ij}}$. The interaction coefficients (Table 7) were obtained by selecting the $\mathrm{k}_{\mathrm{ij}}$ which minimized the differences between calculated and experimental vapor and liquid mole fractions for the binary isotherms.

Nitrogen + Carbon Dioxide Binary System. Figure 2 compares the data of this study at 270 K with previous

Table 4. Carbon Dioxide + Propane Binary System

| pressure/MPa | $\mathrm{XCO}_{2}$ | $\mathrm{ycO}_{2}$ | pressure/MPa | $\mathrm{XCO}_{2}$ | $\mathrm{ycO}_{2}$ | pressure/MPa | $\mathrm{XCO}_{2}$ | $\mathrm{ycO}_{2}$ | pressure/MPa | $\mathrm{XCO}_{2}$ | $\mathrm{ycO}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 240 K |  |  |  |  |  |  |  |  |  |  |  |
| 0.1508 | 0.0000 | 0.0000 | 0.4640 | 0.1282 | 0.6935 | 0.8370 | 0.3354 | 0.8488 | 1.057 | 0.5700 | 0.8933 |
| 0.2020 | 0.0220 |  | 0.5896 |  | 0.7570 | 0.8811 | 0.3736 | 0.8583 | 1.200 | 0.8206 | 0.9302 |
| 0.3160 | 0.0604 | 0.5424 | 0.7277 |  | 0.8122 | 0.9740 |  | 0.8808 | 1.284 | 1.0000 | 1.0000 |
| 0.4480 | 0.1203 | 0.6787 | 0.7440 | 0.2727 | 0.8184 | 1.017 | 0.5165 | 0.8902 |  |  |  |
| 270 K |  |  |  |  |  |  |  |  |  |  |  |
| 0.4340 | 0.0000 | 0.0000 | 1.014 | 0.1129 |  | 2.022 | 0.4161 | 0.8095 | 2.287 | 0.5326 | 0.8374 |
| 0.6990 | 0.0524 |  | 1.331 |  | 0.6843 | 2.055 |  | 0.8102 | 2.460 |  | 0.8574 |
| 0.9130 | 0.0940 |  | 1.700 | 0.3107 | 0.7658 | 2.249 | 0.5106 | 0.8377 | 3.202 | 1.0000 | 1.0000 |
| 330 K |  |  |  |  |  |  |  |  |  |  |  |
| 1.980 | 0.0000 | 0.0000 | 2.886 | 0.0876 | 0.2640 | 4.439 | 0.2710 |  | 5.438 | 0.3860 |  |
| 2.189 | 0.0197 | 0.0873 | 3.722 | 0.1890 | 0.4000 | 5.000 | 0.3340 | 0.5150 | 5.852 | 0.4430 | 0.5690 |
| 2.479 | 0.0458 | 0.1810 |  |  |  |  |  |  |  |  |  |

Table 5. Nitrogen + Propane Binary System

| pressure/MPa | $\mathrm{X}_{\mathrm{N}_{2}}$ | $\mathrm{y}_{\mathrm{N}_{2}}$ | pressure/MPa | $\mathrm{X}_{\mathrm{N}_{2}}$ | $\mathrm{y}_{\mathrm{N}_{2}}$ | pressure/MPa | $\mathrm{XN}_{2}$ | $\mathrm{y}_{\mathrm{N}_{2}}$ | pressure/MPa | $\mathrm{x}_{\mathrm{N}_{2}}$ | $\mathrm{y}_{\mathrm{N}_{2}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 240 K |  |  |  |  |  |  |  |  |  |  |  |
| 0.1508 | 0.0000 | 0.0000 | 2.768 | 0.0537 | 0.9291 | 9.315 | 0.1793 | 0.9462 | 14.00 | 0.2721 | 0.9313 |
| 1.191 | 0.0200 | 0.8652 | 4.823 | 0.0942 | 0.9434 | 12.21 |  | 0.9386 | 15.08 | 0.2845 | 0.9252 |
| 2.069 | 0.0378 | 0.9125 | 7.094 | 0.1385 | 0.9486 | 12.84 | 0.2447 | 0.9375 |  |  |  |
| 270 K |  |  |  |  |  |  |  |  |  |  |  |
| 0.4336 | 0.0000 | 0.0000 | 4.277 | 0.0785 | 0.8485 | 6.577 | 0.1240 |  | 13.70 | 0.2837 | 0.8655 |
| 2.006 | 0.0305 | 0.7482 | 4.433 | 0.0820 | 0.8504 | 7.988 | 0.1590 | 0.8920 | 14.98 | 0.3168 | 0.8628 |
| 2.279 | 0.0376 | 0.7785 | 5.023 | 0.0920 |  | 10.16 |  | 0.8817 |  |  |  |
| 3.547 | 0.0651 | 0.8350 | 5.249 | 0.0976 | 0.8673 | 11.49 | 0.2369 | 0.8806 |  |  |  |
| 330 K |  |  |  |  |  |  |  |  |  |  |  |
| 1.981 | 0.0000 | 0.0000 | 3.975 | 0.0471 | 0.3721 | 5.711 | 0.0985 | 0.4705 | 9.808 | 0.2180 | 0.5530 |
| 2.979 | 0.0248 | 0.2325 | 4.845 | 0.0774 | 0.4219 | 6.468 | 0.1192 | 0.4981 | 12.50 | 0.3180 | 0.5460 |
| 3.518 | 0.0390 | 0.3085 | 4.995 | 0.0798 | 0.4302 | 7.919 | 0.1600 | 0.5339 |  |  |  |

Table 6. Nitrogen + Carbon Dioxide + Propane Ternary System

| pressure/MPa | $\mathrm{X}_{\mathrm{N}_{2}}$ | $\mathrm{XCO}_{2}$ | $\mathrm{XC}_{\mathrm{C}_{3} \mathrm{H}_{8}}$ | $\mathrm{y}_{\mathrm{N}_{2}}$ | $\mathrm{ycO}_{2}$ | $\mathrm{yc}_{3} \mathrm{H}_{8}$ | pressure/MPa | $\mathrm{X}_{\mathrm{N}_{2}}$ | $\mathrm{XCO}_{2}$ | $\mathrm{XC}_{\mathrm{C}_{3} \mathrm{H}_{8}}$ | $\mathrm{y}_{\mathrm{N}_{2}}$ | $\mathrm{ycO}_{2}$ | $\mathrm{yc}_{3} \mathrm{H}_{8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 240 K and 2.0 MPa |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2.000 | 0.0294 | 0.0048 | 0.9658 | 0.8953 | 0.0094 | 0.0951 | 2.000 | 0.0238 | 0.5375 | 0.4387 | 0.4325 | 0.4968 | 0.0707 |
| 2.000 | 0.0284 | 0.3539 | 0.6177 | 0.5205 | 0.4037 | 0.0758 | 2.000 | 0.0211 | 0.6317 | 0.3472 | 0.4030 | 0.5374 | 0.0596 |
| 2.000 |  |  |  | 0.3896 | 0.5545 | 0.0560 | 2.000 | 0.0175 | 0.7413 | 0.2412 | 0.3507 | 0.6092 | 0.0401 |
| 2.000 |  |  |  | 0.4746 | 0.4543 | 0.0712 | 2.000 | 0.0266 | 0.9238 | 0.0496 | 0.8216 | 0.0859 | 0.0925 |
| 2.000 | 0.0265 | 0.4229 | 0.5506 | 0.4849 | 0.4424 | 0.0727 | 2.000 | 0.0130 | 0.9870 | 0.0000 | 0.3186 | 0.6814 | 0.0000 |
| 240 K and 13.0 MPa |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 13.00 | 0.2500 | 0.0000 | 0.7500 | 0.9370 | 0.0000 | 0.0630 | 13.00 | 0.3114 | 0.2817 | 0.4069 | 0.7649 | 0.1598 | 0.0753 |
| 12.99 |  |  |  | 0.8490 | 0.0729 | 0.0781 | 13.00 | 0.2612 | 0.6986 | 0.0403 | 0.9006 | 0.0263 | 0.0731 |
| 13.00 |  |  |  | 0.8013 | 0.1240 | 0.0747 | 13.00 | 0.2531 | 0.7450 | 0.0019 | 0.6679 | 0.3316 | 0.0005 |
| 13.00 |  |  |  | 0.7878 | 0.1366 | 0.0756 | 13.00 | 0.2467 | 0.7533 | 0.0000 | 0.6692 | 0.3308 | 0.0000 |
| 12.99 | 0.3014 | 0.2485 | 0.4501 | 0.7810 | 0.1444 | 0.7460 |  |  |  |  |  |  |  |
| 270 K and 2.0 MPa |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2.006 | 0.0305 | 0.0000 | 0.9695 | 0.7320 | 0.0000 | 0.2680 | 2.000 | 0.0069 | 0.3019 | 0.6862 | 0.1179 | 0.6772 | 0.2049 |
| 2.000 | 0.0286 | 0.0182 | 0.9532 | 0.6812 | 0.0676 | 0.2512 | 2.000 | 0.0038 | 0.3621 | 0.6341 | 0.0613 | 0.7381 | 0.2006 |
| 2.000 | 0.0204 | 0.1234 | 0.8562 | 0.4046 | 0.3373 | 0.2581 | 2.000 | 0.0008 | 0.3956 | 0.6037 | 0.0062 | 0.8055 | 0.1883 |
| 2.000 | 0.0141 | 0.2087 | 0.7790 | 0.2607 | 0.4994 | 0.2399 | 2.000 | 0.0000 | 0.8170 | 0.1830 | 0.0000 | 0.4150 | 0.5850 |
| 2.000 | 0.0096 | 0.2774 | 0.7130 | 0.1669 | 0.6133 | 0.2198 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 6.00 | 0.1133 | 0.0079 | 0.8787 | 0.8533 | 0.0106 | 0.1363 | 6.01 | 0.0933 | 0.5475 | 0.3592 | 0.4606 | 0.4493 | 0.0900 |
| 6.01 | 0.0974 | 0.2085 | 0.6921 | 0.6595 | 0.2197 | 0.1208 | 6.01 | 0.0904 | 0.5770 | 0.3326 | 0.4463 | 0.4667 | 0.0871 |
| 5.99 | 0.1012 | 0.3038 | 0.5950 | 0.5894 | 0.2935 | 0.1171 | 6.00 | 0.0682 | 0.8435 | 0.0882 | 0.3543 | 0.6107 | 0.0351 |
| 6.00 | 0.1031 | 0.3069 | 0.5901 | 0.5966 | 0.2945 | 0.1088 | 6.00 | 0.0530 | 0.9470 | 0.0000 | 0.3250 | 0.6750 | 0.0000 |
| 6.00 | 0.0937 | 0.4002 | 0.5061 | 0.5270 | 0.3675 | 0.1055 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 13.00 | 0.2646 | 0.0000 | 0.7354 | 0.8612 | 0.0000 | 0.1388 | 13.00 | 0.2990 | 0.2990 | 0.4020 | 0.6657 | 0.1828 | 0.1515 |
| 13.00 | 0.2663 | 0.0217 | 0.7120 | 0.8386 | 0.0192 | 0.1423 | 13.00 |  |  |  | 0.6312 | 0.2166 | 0.1522 |
| 13.00 |  |  |  | 0.7839 | 0.0727 | 0.1434 | 12.99 |  |  |  | 0.6060 | 0.2400 | 0.1541 |
| 13.00 | 0.2854 | 0.2046 | 0.5100 |  |  |  |  |  |  |  |  |  |  |
| 330 K and 5.0 MPa |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 5.00 | 0.0000 | 0.3340 | 0.6660 | 0.0000 | 0.5150 | 0.4850 | 5.00 | 0.0357 | 0.1479 | 0.8164 | 0.1650 | 0.2967 | 0.5383 |
| 5.00 | 0.0090 | 0.2989 | 0.6921 |  |  |  | 5.00 | 0.0450 | 0.1297 | 0.8253 | 0.2273 | 0.2428 | 0.5299 |
| 5.00 | 0.0149 | 0.2681 | 0.7170 |  |  |  | 5.00 |  |  |  | 0.2634 | 0.1977 | 0.5389 |
| 5.00 | 0.0204 | 0.2258 | 0.7538 | 0.0300 | 0.4460 | 0.5240 | 5.00 | 0.0712 | 0.0367 | 0.8921 | 0.3713 | 0.0715 | 0.5572 |
| 4.99 | 0.0229 | 0.2216 | 0.7555 | 0.0400 | 0.4236 | 0.5364 | 5.01 | 0.0792 | 0.0000 | 0.9208 | 0.4339 | 0.0000 | 0.5661 |



Figure 2. Nitrogen + carbon dioxide at 270 K .


Figure 3. Carbon dioxide + propane at 270 K .
Table 7. Binary Interaction Parameters ( $\mathrm{k}_{\mathrm{ij}}$ ) for the Peng-Robinson Equation of State

| temp/K | $\mathrm{k}_{\mathrm{ij}}$ | AAD |
| :---: | :---: | :---: |
| Nitrogen + Carbon Dioxide |  |  |
| 240.00 | -0.029 | 0.0043 |
| 270.00 | -0.024 | 0.0045 |
| Carbon Dioxide + Propane |  |  |
| 240.00 | 0.126 | 0.0044 |
| 270.00 | 0.120 | 0.0050 |
| 330.00 | 0.124 | 0.0061 |
|  |  |  |
|  | Nitrogen + Propane |  |
| 240.00 | 0.069 | 0.0043 |
| 270.00 | 0.054 | 0.0079 |
| 330.00 | 0.089 | 0.0024 |



Figure 4. Nitrogen + propane at 270 K .


Figure 5. Nitrogen + carbon dioxide + propane at 270 K and 2.0 MPa .
work, and shows the results of calculations using the Peng-Robinson (PR) equation with $\mathrm{k}_{\mathrm{ij}}$ from Table 7. The PR equation is not capable of accurately modeling the critical region for this system, a result that is commonly observed.
Carbon Dioxide + Propane Binary System. The results at 270 K are shown in Figure 3. The data at 240 K and 270 K are below the critical temperature of carbon dioxide( 304.21 K ), while the 330 K isotherm is considerably above. The PR equation is quite satisfactory in modeling at all temperatures, although the critical region at 330 K is not well-defined experimentally. Limited measurements were also made at 344.26 K to compare with the earlier work of Reamer et al. (1951). The agreement was excellent.

Nitrogen + Propane Binary System. The data at 270 $K$ are shown in Figure 4, together with the PR predictions. The measurements were made to pressures of 15 MPa , which was the maximum limit for the pressure gauges used. For all isotherms the fits from the PR equation of


Figure 6. Nitrogen + carbon dioxide + propane at 270 K and 6.0 MPa.


Figure 7. Nitrogen + carbon dioxide + propane at 270 K and 13.0 MPa.
state were good for both the vapor and the liquid phases, but again the critical region at 330 k is not well-defined experimentally.

Nitrogen + Carbon Dioxide + Propane Ternary System. The ternary data and the PR predictions at 270 K for $2.0,6.0$, and 13.0 MPa , at 240 K for 2.0 and 13.0 MPa , and at 330 K for 5.0 MPa are shown in Figures 5-9. The binary end points were checked by comparing them with the previously generated binary curves at each pressure and were found to be within $\pm 0.002$ mole fraction of the previous points.

At 270 K and 13.0 MPa the ternary system has a critical point since the system pressure was above the critical pressure of the nitrogen + carbon dioxide binary system. For all other conditions two binary end points exist. The accuracy of the predictions for the ternary system depends on the goodness of the fit of the binary systems which form the boundaries of the ternary system. At low pressures the PR equation models the data very well; this is reflected in the quality of the ternary predictions. At 13.0 MPa, the PR fits to the binary data were particularly poor for the liquid phase at 240 K and for the vapor phase at 270 K ,


Figure 8. Nitrogen + carbon dioxide + propane at 240 K and 2.0 MPa.


Figure 9. Nitrogen + carbon dioxide + propane at 240 K and 13.0 MPa .
and as a result the ternary predictions were also poor in these regions. Peng-Robinson predictions for 13.0 MPa and 270 K using $\mathrm{k}_{\mathrm{ij}}$ values of 0.0 are shown in Figure 7, demonstrating the importance of the interaction coefficients.

## Literature Cited

Acosta, J. C.; Hevia, E.; Leipziger, S. Dew and Bubble Point Measurements for Carbon Dioxide-Propane Mixtures. J. Chem. Eng. Data 1984, 29, 304-308.
Akers, W. W.; Kelley, R. E.; Lipscomb, T. G. Carbon Dioxide-Propane System. Ind. Eng. Chem. 1954, 46, 2535-2536.
Al-Sahhaf, T. A. Liquid-Vapor Equilibria for the $\mathrm{N}_{2}+\mathrm{CO}_{2}+\mathrm{CH}_{4}$ System. Ind. Eng. Chem. Fundam. 1983, 22, 372-380.
Altunin, V. V.; Gvozdkov, A. V.; Sosinovskii, V. K. Liquid-Vapor Phase Equilibrium of Binary Systems with Carbon Dioxide. Tr. Mosk. Energ. Inst. 1974, 177, 28-32.
Angus, S.; Armstrong, B.; de Reuck, K. M. International Thermodynamic Tables of Fluid StateCarbon Dioxide; Pergamon Press: New York, 1976.
Arai, Y.; Kaminishi, G.; Saito, S. The Experimental Determination of the P-V-T-X Relations for the Carbon Dioxide-Nitrogen System and the Carbon Dioxide-M ethane System. J. Chem. Eng. J pn. 1971, 4, 113-122.
Brown, T. S.; Niesen, V. G.; Sloan E. D.; Kidnay, A. J. Vapor-Liquid Equilibria for the Binary Systems of Nitrogen, Carbon Dioxide and n-Butane at Temperatures from 220 to 344 K . Fluid Phase Equilib. 1989b, 53, 7-14.

Brown, T. S.; Sloan, E. D.; Kidnay, A. J. Vapor-Liquid Equilibria in the Nitrogen + Carbon Dioxide + Ethane System. Fluid Phase Equilib. 1989b, 51, 299-313.
Cannon, W. A.; Robson, J. H.; English, W. D. Liquid Propellant Gas Absorption Study; Douglas Missile and Space Systems Division Astropower Laboratory, Report DAC-60510-F 2, 1968.
Chueng, H.; Wang, D. I. J. Solubility of Volatile Gases in Hydrocarbon Solvents at Cryogenic Temperatures. Ind. Eng. Chem. Fundam. 1964, 3, 355-361.
Dorau,W.; Kremer, H. W.; K napp, H. An Apparatus for the Investigation of Low-Temperature, High-Pressure, Vapor-Liquid and Vapor-Liquid-Liquid Equilibria. Fluid Phase Equilib. 1983, 11, 83-89.
Goodwin, R. D.; Haynes, W. M. Thermopysical Properties of Propane from 85 to 700 K at Pressures to 70 MPa Monograph 170; National Bureau of Standards (U.S.); U.S. GPO: Washington, DC, 1982a.
Goodwin, R. D.; Haynes, W. M. Thermopysical Properties of Normal Butane from 135 to 700 K atPressures to 70 MPa Monograph 169; National Bureau of Standards (U.S.); GPO: Washington, DC, 1982b.
Grausø, L.; Fredenslund, A.; Mollerup, J. Vapor-Liquid Equilibrium Data for the Natural Gas Systems, $\mathrm{C}_{2} \mathrm{H}_{6}+\mathrm{N}_{2}, \mathrm{C}_{2} \mathrm{H}_{4}+\mathrm{N}_{2}, \mathrm{C}_{3} \mathrm{H}_{8}+\mathrm{N}_{2}$ and $\mathrm{C}_{3} \mathrm{H}_{6}+\mathrm{N}_{2}$. Fluid Phase Equilib. 1977, 1, 13-26.
Hamam, S. E.; Lu, B. C. Y. Isothermal Vapor-Liquid Equilibrium in the Binary System Propane-Carbon Dioxide. J. Chem. Eng. Data 1976, 21, 200-204.
Hudziak, J. A.; K ahvand, H.; Yassale, M.; Leipziger, S. Dew Point Measurements for Nitrogen-Propane and Nitrogen-Butane Mixtures. J. Chem. Eng. Data 1984, 29, 296-300.
Krichevskii, I. R.; Khazanova, N. E.; Lesnevskaya, L. S.; Sandalova, L. Y. Liquid-Gas Equilibrium in the Nitrogen-Carbon Dioxide System Under Elevated Pressures. Khim. Promst. (M oscow) 1962, 38, 169-171.
Llave, F. M.; Luksk, D.; Kohn, J. P. Three Phase Liquid-Liquid-Vapor Equilibria in the Binary Systems Nitrogen + Ethane and Nitrogen + Propane. J. Chem. Eng. Data 1985, 30, 485-491.
Muirbrook, N. K.; Prausnitz, J. M. Multicomponent Vapor-Liquid Equilibria at High Pressures. Part I. Experimental Study of the Nitrogen-Oxygen-Carbon Dioxide System at $0^{\circ} \mathrm{C}$. AIChE J. 1965, 11, 1092-1096.
Nagahama, K.; Konishi, H.; Hoshino, D.; Hirata, M. Binary VaporLiquid Equilibriums of Carbon Dioxide-Light Hydrocarbons at Low Temperature. J. Chem. Eng. J pn. 1974, 7, 323-328.
Niesen, V. G.; Rainwater, J. C. Critical Locus (Vapor + Liquid) Equilibria and Coexisting Densities (Carbon Dioxide + Propane) at Temperatures from 311 K to 361 K . J. Chem. Thermodyb. 1990, 22, 777-795.

Peng, D. Y.; Robinson, D. B. A New Two Constant Equation of State. Ind. Eng. Chem. Fundam. 1976, 15, 59-64.
Poettman, F. H.; Katz, D. L. Phase Behavior of Binary Carbon Dioxide-Paraffin Systems. Ind. Eng. Chem. 1945, 37, 847-853.
Poon, D. P. L.; Lu, B. C.-Y. Phase Equilibria for Systems Containing Nitrogen, Methane and Propane. In Advances in Cryogenic Engineering; Timmerhaus, K. D., Ed.; Plenum Press: New York, 1974; Vol. 19, pp 292-299.
Prausnitz, J. M. Equations of State from van der Waals Theory: The Legacy of Otto Redlich. Fluid Phase Equilib. 1985, 24, 63-76.
Reamer, H. H.; Sage, B. H.; Lacey, W. N. Phase Equilibria in Hydrocarbon Systems: Volumetric Phase Behavior of the PropaneCarbon Dioxide System. Ind. Eng. Chem. 1951, 43, 2515-2520.
Roof, J. G.; Baron, J. D. Critical Loci of Binary Mixtures of Propane with Methane, Carbon Dioxide, and Nitrogen. J. Chem. Eng. Data 1967, 12, 292-293.
Schindler, D. L.; Swift, G. W.; Kurata, F. M ore Low Temperature V-L Design Data. Hydrocarbon Process. 1966, 45 (11), 205-210.
Somait, F. A.; Kidnay, A. J. Liquid-Vapor Equilibria at 270.00 K for Systems Containing Nitrogen, Methane, and Carbon Dioxide. J. Chem. Eng. Data 1978, 23, 301-305.
Vellinger, E.; Pons, E. On the Solubility of Nitrogen in Methane and Propane Liquids. C. R. Hebd. Seances Acad. Sci. 1943, 217, 689691.

Webster, L. A. Experimental and Calculated Vapor-Liquid Equilibria for the Methane + Propane + Carbon Dioxide System. M.S. Thesis, Chemical Engineering Department, Colorado School of Mines, 1996.
Wei, M.; Brown, T. S.; Kidnay, A. J.; Sloan, E. D. Vapor-Liquid Equilibria for the Ternary System Methane + Ethane + Carbon Dioxide at 230 K and Its Constituent Binaries at Temperatures from 207 to 270 K. J. Chem. Eng. Data 1995, 40, 726-731.
Xu, N.; Dong, J.; Wang, Y.; Shi, J. High Pressure Vapor-Liquid Equilibria at 293 K For Systems Containing Nitrogen, Methane and Carbon Dioxide. Fluid Phase Equilibria. 1992, 81, 175-186.
Yorizane, M.; Yoshimura, S.; Masuoka, H. Vapor-Liquid Equilibrium at High Pressures. $\mathrm{N}_{2}-\mathrm{CO}_{2}, \mathrm{H}_{2}-\mathrm{CO}_{2}$ Systems. Kagaku Kogaku 1970, 34, 953-957.
Zenner, G. H.; Dana, L. I. Liquid-Vapor Equilibrium Composition for Carbon Dioxide-Oxygen-Nitrogen Mixtures. Chem Eng. Progr. Symp. Ser. 1963, 59, 36-41.

Received for review December 30, 1998. Accepted May 14, 1999.
J E 980321E


[^0]:    * To whom correspondence should be addressed.

