# Physical Properties of the Ternary System 1-Butanol + Methanol + 2-Methoxy-2-methylpropane at 298.15 K: Measurement and Prediction 

Alberto Arce,* Eva Rodil, and Ana Soto<br>Department of Chemical Engineering, University of Santiago de Compostela, E-15706 Santiago, Spain


#### Abstract

Densities, refractive indices, speeds of sound, excess molar volumes ( $\mathrm{V}^{\mathrm{E}}$ ), and deviations in molar refractions ( $\Delta \mathrm{R}$ ) and isentropic compressibilities ( $\Delta \kappa_{\mathrm{s}}$ ) were determined for the system 1-butanol + methanol + 2-methoxy-2-methylpropane at 298.15 K and atmospheric pressure. The values of $\mathrm{V}^{\mathrm{E}}, \Delta \mathrm{R}$, and $\Delta \kappa_{\mathrm{s}}$ were satisfactorily correlated by the Redlich-Kister polynomial. These values were also predicted using several empirical equations from the values of their constituent binary subsystems, and the best results were obtained with the Kohler and the Radojkovic equations.


## Introduction

There is considerable interest in the thermodynamic properties of mixtures of ethers and alcohols, particularly in the industrial use of 2-methoxy-2-methylpropane (MTBE) as an oxygenated antiknock agent for gasol ines. In previous papers (Arce et al., 1997, 1998, 1999) we have undertaken a systematic study of the density, speed of sound, excess volume, and isentropic compressibility of binary and ternary mixtures containing ethers and alcohols. These properties are sensitive to different kinds of association in the liquid mixtures and have often been used to investigate the molecular packing, molecular motion, and various types of intramolecular interactions and their strength, influenced by the size and chemical nature of component molecules. In addition, it is interesting because the determination of two physical properties can be used for compositional analysis of ternary mixtures.

In this work we will investigate the ternary system 1-butanol + methanol + MTBE, taking into account that 1-butanol may be used as an entrainer in the separation, by extractive distillation, of the mixture methanol + MTBE. We consider several phenomena such as the hydrogen bonding and polar characteristics of both the entrainer and the components of the mixture as well as the difference between the boiling points for the recovery of the entrainer. The physical properties measured at 298.15 K were densities, refractive indices, and sound velocities. The calculated properties were excess molar volumes and deviations in molar refraction and isentropic compressibility from the mole fraction or volume fraction average, respectively, of these properties of the pure components. No comparable data in the surveyed literature for this ternary system have been found.

We will also evaluate several empirical equations allowing the prediction of the properties of the ternary system from the corresponding properties of the constituent binary subsystems. If this approach works, an enormous experimental effort would be saved.

Table 1. Densities $\rho$, Refractive Indices $n_{D}$ and Speeds of Sound $u$ of the Pure Components at 298.15 K and Atmospheric Pressure

| component | $\rho /\left(\mathrm{g} \cdot \mathrm{cm}^{-3}\right)$ |  | $\mathrm{n}_{\text {D }}$ |  | $\mathrm{u} /\left(\mathrm{m} \cdot \mathrm{s}^{-1}\right)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | exptl | lit. | exptl | lit. | expt | lit. |
| 1-butanol | 0.8060 | $0.80575^{\text {a }}$ | 1.3975 | $1.39741^{\text {a }}$ | 1241 | $1240^{6}$ |
| methanol | 0.7866 | $0.78637^{\text {a }}$ | 1.3264 | $1.32652^{\text {a }}$ | 1102 | $1102^{\text {b }}$ |
| MTBE | 0.7356 | $0.73528^{\text {c }}$ | 1.3666 | $1.36630{ }^{\text {c }}$ | 1037 | d |

${ }^{\text {a }}$ Riddick et al. (1986). ${ }^{\text {b }}$ Aminabhavi (1993). ${ }^{\text {c }}$ Daubert and Danner (1989). d Not Found.

Table 2. Densities $\rho$, Speeds of Sound u, Isentropic Compressibilities $K_{5}$, Refractive Indices $\mathrm{n}_{\mathrm{D}}$, Excess Molar Volumes $V^{E}$, and Deviations $\Delta \kappa_{s}$ and $\Delta R$ for Mixtures of 1-Butanol (1) + Methanol (2) at 298.15 K and Atmospheric Pressure

|  | $\rho /(\mathrm{g} \cdot$ <br> $\left.\mathrm{cm}^{-3}\right)$ | $\mathrm{u} /(\mathrm{m} \cdot$ <br> $\left.\mathrm{s}^{-1}\right)$ | $\kappa_{s} /(\mathrm{T}$ <br> $\left.\mathrm{Pa}^{-1}\right)$ | $\mathrm{n}_{\mathrm{D}}$ | $\mathrm{V}^{\mathrm{E}} /$ <br> $\left(\mathrm{cm}^{3} \mathrm{~mol}^{-1}\right)$ | $\Delta \kappa_{s} /(\mathrm{T}$ <br> $\left.\mathrm{Pa}^{-1}\right)$ | $\Delta \mathrm{R} /$ <br> $\left(\mathrm{cm}^{3}\right.$. <br> $\left.\mathrm{mol}^{-1}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | ---: |
| 0.0657 | 0.7888 | 1117 | 1017 | 1.3357 | 0.0272 | 3 | 0.0002 |
| 0.1073 | 0.7900 | 1125 | 999 | 1.3410 | 0.0409 | 5 | 0.0007 |
| 0.1618 | 0.7916 | 1136 | 978 | 1.3473 | 0.0549 | 5 | 0.0015 |
| 0.2075 | 0.7928 | 1145 | 962 | 1.3520 | 0.0635 | 5 | 0.0023 |
| 0.2575 | 0.7941 | 1154 | 946 | 1.3568 | 0.0699 | 5 | 0.0030 |
| 0.3269 | 0.7957 | 1166 | 925 | 1.3627 | 0.0743 | 4 | 0.0036 |
| 0.3659 | 0.7966 | 1172 | 914 | 1.3658 | 0.0747 | 4 | 0.0036 |
| 0.3852 | 0.7970 | 1175 | 909 | 1.3672 | 0.0743 | 4 | 0.0036 |
| 0.4413 | 0.7981 | 1183 | 895 | 1.3712 | 0.0718 | 3 | 0.0030 |
| 0.5008 | 0.7993 | 1191 | 881 | 1.3750 | 0.0667 | 2 | 0.0020 |
| 0.5317 | 0.7998 | 1196 | 875 | 1.3768 | 0.0633 | 2 | 0.0012 |
| 0.6050 | 0.8010 | 1204 | 860 | 1.3809 | 0.0537 | 1 | -0.0010 |
| 0.635 | 0.8018 | 1210 | 852 | 1.3834 | 0.0464 | 1 | -0.0025 |
| 0.6876 | 0.8023 | 1214 | 846 | 1.3850 | 0.0410 | 0 | -0.0036 |
| 0.7385 | 0.8030 | 1219 | 838 | 1.3874 | 0.0329 | 0 | -0.0051 |
| 0.7926 | 0.8037 | 1224 | 830 | 1.3897 | 0.0244 | 0 | -0.0063 |
| 0.8284 | 0.8042 | 1227 | 825 | 1.3911 | 0.0190 | 0 | -0.0066 |
| 0.8746 | 0.8047 | 1231 | 820 | 1.3930 | 0.0126 | 0 | -0.0064 |
| 0.9244 | 0.8053 | 1235 | 814 | 1.3948 | 0.0066 | 0 | -0.0050 |

## Experimental Section

Methanol was supplied by Merck (Madrid, Spain) with nominal purity > 99.8 mass \%. MTBE and 1-butanol were supplied by Aldrich (Madrid, Spain) and had nominal purities $>99.8$ and $>99.9$ mass $\%$. The water contents of

Table 3. Densities $\rho$, Speeds of Sound $\mathbf{u}$, Isentropic Compressibilities $\kappa_{\mathrm{s}}$, Refractive Indices $\mathbf{n}_{\mathrm{D}}$, Excess Molar Volumes $\mathbf{V}^{\mathrm{E}}$, and Deviations $\Delta \kappa_{s}$ and $\Delta \mathrm{R}$ for Mixtures of 1-Butanol (1) + Methanol (2) + MTBE (3) at 298.15 K and Atmospheric Pressure

| $\mathrm{x}_{1}$ | $\mathrm{x}_{2}$ | $\rho /\left(\mathrm{g} \cdot \mathrm{cm}^{-3}\right)$ | $\mathrm{u} /\left(\mathrm{m} \cdot \mathrm{s}^{-1}\right)$ | $\kappa_{5} /$ ( Pa ${ }^{-1}$ ) | $\mathrm{n}_{\mathrm{D}}$ | $\mathrm{V}^{\mathrm{E}} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | $\Delta \kappa_{s}\left(T \mathrm{~Pa}^{-1}\right)$ | $\Delta \mathrm{R} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0963 | 0.9037 | 0.7896 | 1123 | 1004 | 1.3395 | 0.0375 | 4 | 0.0005 |
| 0.0862 | 0.8085 | 0.7810 | 1116 | 1029 | 1.3475 | -0.2472 | -33 | -0.0106 |
| 0.0774 | 0.7260 | 0.7744 | 1108 | 1052 | 1.3524 | -0.4239 | -50 | -0.0181 |
| 0.0703 | 0.6598 | 0.7696 | 1101 | 1073 | 1.3554 | -0.5266 | -57 | -0.0227 |
| 0.0597 | 0.5607 | 0.7631 | 1090 | 1102 | 1.3589 | -0.6249 | -60 | -0.0272 |
| 0.0506 | 0.4752 | 0.7581 | 1082 | 1126 | 1.3612 | -0.6619 | -60 | -0.0289 |
| 0.0422 | 0.3960 | 0.7538 | 1075 | 1147 | 1.3628 | -0.6589 | -56 | -0.0286 |
| 0.0339 | 0.3183 | 0.7500 | 1068 | 1168 | 1.3641 | -0.6206 | -50 | -0.0265 |
| 0.0248 | 0.2330 | 0.7460 | 1060 | 1192 | 1.3652 | -0.5347 | -41 | -0.0223 |
| 0.0184 | 0.1731 | 0.7433 | 1055 | 1210 | 1.3658 | -0.4433 | -32 | -0.0180 |
| 0.2000 | 0.8000 | 0.7926 | 1144 | 965 | 1.3510 | 0.0623 | 5 | 0.0022 |
| 0.1771 | 0.7086 | 0.7835 | 1132 | 995 | 1.3564 | -0.2551 | -35 | -0.0069 |
| 0.1567 | 0.6267 | 0.7761 | 1121 | 1026 | 1.3598 | -0.4575 | -54 | -0.0130 |
| 0.1403 | 0.5612 | 0.7707 | 1111 | 1051 | 1.3618 | -0.5705 | -60 | -0.0167 |
| 0.1199 | 0.4796 | 0.7645 | 1099 | 1082 | 1.3636 | -0.6560 | -63 | -0.0196 |
| 0.1035 | 0.4141 | 0.7599 | 1090 | 1107 | 1.3647 | -0.6833 | -62 | -0.0206 |
| 0.0883 | 0.3531 | 0.7559 | 1083 | 1129 | 1.3654 | -0.6767 | -59 | -0.0205 |
| 0.0668 | 0.2671 | 0.7506 | 1072 | 1160 | 1.3662 | -0.6157 | -51 | -0.0186 |
| 0.0531 | 0.2124 | 0.7473 | 1065 | 1180 | 1.3665 | -0.5444 | -43 | -0.0164 |
| 0.0299 | 0.1198 | 0.7421 | 1053 | 1216 | 1.3667 | -0.3626 | -27 | -0.0108 |
| 0.3131 | 0.6869 | 0.7954 | 1164 | 928 | 1.3614 | 0.0738 | 5 | 0.0035 |
| 0.2758 | 0.6050 | 0.7859 | 1148 | 965 | 1.3643 | -0.2540 | -34 | -0.0086 |
| 0.2463 | 0.5403 | 0.7791 | 1135 | 996 | 1.3658 | -0.4490 | -52 | -0.0160 |
| 0.2240 | 0.4914 | 0.7743 | 1125 | 1020 | 1.3666 | -0.5593 | -59 | -0.0202 |
| 0.1893 | 0.4153 | 0.7673 | 1111 | 1057 | 1.3674 | -0.6689 | -64 | -0.0246 |
| 0.1616 | 0.3546 | 0.7620 | 1099 | 1086 | 1.3678 | -0.7031 | -64 | -0.0261 |
| 0.1356 | 0.2976 | 0.7573 | 1089 | 1113 | 1.3679 | -0.6928 | -60 | -0.0259 |
| 0.0995 | 0.2184 | 0.7511 | 1075 | 1152 | 1.3678 | -0.6119 | -50 | -0.0231 |
| 0.0787 | 0.1726 | 0.7477 | 1067 | 1175 | 1.3677 | -0.5302 | -43 | -0.0201 |
| 0.0733 | 0.1608 | 0.7468 | 1065 | 1181 | 1.3676 | -0.5051 | -40 | -0.0192 |
| 0.3907 | 0.6093 | 0.7971 | 1176 | 908 | 1.3676 | 0.0742 | 4 | 0.0035 |
| 0.3464 | 0.5402 | 0.7884 | 1160 | 943 | 1.3690 | -0.2460 | -33 | -0.0079 |
| 0.3087 | 0.4814 | 0.7814 | 1146 | 975 | 1.3696 | -0.4469 | -53 | -0.0171 |
| 0.2696 | 0.4204 | 0.7746 | 1130 | 1010 | 1.3698 | -0.5919 | -63 | -0.0256 |
| 0.2304 | 0.3594 | 0.7682 | 1116 | 1046 | 1.3698 | -0.6769 | -66 | -0.0323 |
| 0.2041 | 0.3183 | 0.7640 | 1106 | 1070 | 1.3696 | -0.7018 | -66 | -0.0354 |
| 0.1662 | 0.2592 | 0.7583 | 1093 | 1104 | 1.3693 | -0.6932 | -62 | -0.0376 |
| 0.1280 | 0.1997 | 0.7528 | 1080 | 1139 | 1.3688 | -0.6313 | -54 | -0.0364 |
| 0.1011 | 0.1576 | 0.7490 | 1071 | 1163 | 1.3684 | -0.5545 | -47 | -0.0332 |
| 0.0685 | 0.1068 | 0.7446 | 1060 | 1194 | 1.3679 | -0.4235 | -35 | -0.0264 |
| 0.4812 | 0.5188 | 0.7988 | 1189 | 886 | 1.3738 | 0.0686 | 2 | 0.0024 |
| 0.4259 | 0.4592 | 0.7904 | 1171 | 922 | 1.3740 | -0.2650 | -35 | -0.0101 |
| 0.3660 | 0.3946 | 0.7815 | 1151 | 966 | 1.3737 | -0.5152 | -57 | -0.0201 |
| 0.3259 | 0.3514 | 0.7758 | 1137 | 997 | 1.3732 | -0.6247 | -64 | -0.0247 |
| 0.2927 | 0.3155 | 0.7712 | 1126 | 1023 | 1.3728 | -0.6834 | -67 | -0.0273 |
| 0.2561 | 0.2761 | 0.7664 | 1114 | 1051 | 1.3722 | -0.7157 | -67 | -0.0287 |
| 0.2005 | 0.2161 | 0.7592 | 1097 | 1095 | 1.3712 | -0.7023 | -63 | -0.0283 |
| 0.1751 | 0.1888 | 0.7561 | 1089 | 1115 | 1.3707 | -0.6714 | -59 | -0.0270 |
| 0.1134 | 0.1223 | 0.7486 | 1071 | 1164 | 1.3694 | -0.5297 | -45 | -0.0211 |
| 0.0789 | 0.0850 | 0.7446 | 1061 | 1193 | 1.3686 | -0.4073 | -34 | -0.0161 |
| 0.5975 | 0.4025 | 0.8010 | 1204 | 862 | 1.3807 | 0.0547 | 1 | -0.0007 |
| 0.5301 | 0.3571 | 0.7926 | 1184 | 900 | 1.3796 | -0.2542 | -31 | -0.0117 |
| 0.4872 | 0.3282 | 0.7874 | 1171 | 925 | 1.3788 | -0.4044 | -46 | -0.0172 |
| 0.4356 | 0.2934 | 0.7813 | 1156 | 958 | 1.3777 | -0.5418 | -58 | -0.0223 |
| 0.3600 | 0.2425 | 0.7726 | 1133 | 1008 | 1.3760 | -0.6648 | -65 | -0.0269 |
| 0.2820 | 0.1900 | 0.7641 | 1111 | 1060 | 1.3741 | -0.6999 | -64 | -0.0279 |
| 0.2414 | 0.1626 | 0.7598 | 1100 | 1087 | 1.3731 | -0.6818 | -61 | -0.0269 |
| 0.1816 | 0.1223 | 0.7536 | 1085 | 1128 | 1.3716 | -0.6086 | -53 | -0.0236 |
| 0.1204 | 0.0811 | 0.7474 | 1069 | 1171 | 1.3700 | -0.4729 | -41 | -0.0179 |
| 0.0699 | 0.0471 | 0.7424 | 1056 | 1208 | 1.3686 | -0.3099 | -27 | -0.0115 |
| 0.6763 | 0.3237 | 0.8021 | 1212 | 848 | 1.3846 | 0.0429 | 0 | -0.0033 |
| 0.5980 | 0.2862 | 0.7939 | 1192 | 887 | 1.3830 | -0.2791 | -33 | -0.0132 |
| 0.5326 | 0.2549 | 0.7871 | 1174 | 921 | 1.3814 | -0.4795 | -51 | -0.0194 |
| 0.4640 | 0.2221 | 0.7801 | 1155 | 960 | 1.3797 | -0.6279 | -63 | -0.0238 |
| 0.4061 | 0.1944 | 0.7742 | 1140 | 994 | 1.3782 | -0.7060 | -67 | -0.0260 |
| 0.3501 | 0.1676 | 0.7687 | 1125 | 1028 | 1.3767 | -0.7413 | -68 | -0.0267 |
| 0.2835 | 0.1357 | 0.7622 | 1108 | 1068 | 1.3749 | -0.7317 | -66 | -0.0258 |
| 0.2227 | 0.1066 | 0.7564 | 1093 | 1107 | 1.3732 | -0.6728 | -59 | -0.0232 |
| 0.1603 | 0.0767 | 0.7505 | 1078 | 1147 | 1.3714 | -0.5601 | -49 | -0.0189 |
| 0.1104 | 0.0528 | 0.7459 | 1065 | 1181 | 1.3700 | -0.4297 | -37 | -0.0142 |
| 0.7765 | 0.2235 | 0.8036 | 1223 | 832 | 1.3891 | 0.0269 | -0 | -0.0060 |
| 0.6771 | 0.1949 | 0.7946 | 1199 | 876 | 1.3865 | -0.3113 | -34 | -0.0169 |
| 0.5846 | 0.1683 | 0.7863 | 1176 | 920 | 1.3840 | -0.5335 | -54 | -0.0240 |
| 0.5239 | 0.1508 | 0.7809 | 1160 | 951 | 1.3823 | -0.6341 | -62 | -0.0270 |

Table 3 (Continued)

| $\mathrm{x}_{1}$ | $\mathrm{x}_{2}$ | $\rho /\left(\mathrm{g} \cdot \mathrm{cm}^{-3}\right)$ | $\mathrm{u} /\left(\mathrm{m} \cdot \mathrm{s}^{-1}\right)$ | $\kappa_{s} /$ ( $\mathrm{Pa}^{-1}$ ) | $\mathrm{n}_{\mathrm{D}}$ | $\mathrm{V}^{\mathrm{E}} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | $\Delta \kappa_{s}$ T $\mathrm{Pa}^{-1}$ ) | $\Delta \mathrm{R} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.4437 | 0.1277 | 0.7737 | 1141 | 994 | 1.3800 | -0.7143 | -67 | -0.0290 |
| 0.3772 | 0.1086 | 0.7679 | 1125 | 1030 | 1.3780 | -0.7356 | -67 | -0.0290 |
| 0.3015 | 0.0868 | 0.7614 | 1107 | 1072 | 1.3758 | -0.7093 | -63 | -0.0271 |
| 0.2322 | 0.0668 | 0.7554 | 1091 | 1112 | 1.3738 | -0.6358 | -56 | -0.0237 |
| 0.1763 | 0.0508 | 0.7506 | 1078 | 1146 | 1.3721 | -0.5404 | -47 | -0.0197 |
| 0.1177 | 0.0339 | 0.7456 | 1065 | 1183 | 1.3703 | -0.4028 | -35 | -0.0143 |
| 0.8960 | 0.1040 | 0.8049 | 1233 | 818 | 1.3938 | 0.0099 | -0 | -0.0059 |
| 0.7902 | 0.0917 | 0.7968 | 1210 | 858 | 1.3909 | -0.2979 | -30 | -0.0118 |
| 0.7041 | 0.0817 | 0.7900 | 1190 | 893 | 1.3884 | -0.4761 | -47 | -0.0154 |
| 0.6112 | 0.0709 | 0.7828 | 1169 | 935 | 1.3856 | -0.6144 | -58 | -0.0179 |
| 0.5190 | 0.0602 | 0.7757 | 1148 | 978 | 1.3829 | -0.7022 | -64 | -0.0190 |
| 0.4476 | 0.0519 | 0.7702 | 1133 | 1012 | 1.3807 | -0.7351 | -65 | -0.0189 |
| 0.3429 | 0.0398 | 0.7622 | 1111 | 1064 | 1.3776 | -0.7197 | -62 | -0.0173 |
| 0.2696 | 0.0313 | 0.7566 | 1095 | 1101 | 1.3753 | -0.6571 | -57 | -0.0152 |
| 0.1811 | 0.0210 | 0.7498 | 1077 | 1150 | 1.3725 | -0.5173 | -45 | -0.0115 |
| 0.1146 | 0.0133 | 0.7446 | 1063 | 1189 | 1.3704 | -0.3630 | -32 | -0.0079 |

the 1-butanol, MTBE, and methanol (determined with a Metrohm 737 KF coulometer) were 0.1, 0.02 , and 0.03 mass $\%$, respectively. All three were used without further purification. During the experiments these purities were checked by gas chromatography and by measurements of the density and refractive index. Table 1 lists the densities, refractive indices, and speeds of sound measured for the pure components, together with published values for these properties (Daubert and Danner, 1989; Riddick et al., 1986; Aminabhavi et al., 1993).

The densities and the speeds of sound both in pure liquids and in the binary and ternary systems were measured using an Anton Paar densimeter DSA (density and sound analyzer), and the refractive indices, with a digital refractometer ATAGO RX1000. The accuracies of the measurements were $0.0001 \mathrm{~g} \cdot \mathrm{~cm}^{-3}, 1 \mathrm{~m} \cdot \mathrm{~s}^{-1}$, and 0.0001 , respectively. A Hetotherm thermostat was used to maintain the temperature at $(298.15 \pm 0.02) \mathrm{K}$. The mixtures were prepared by mass using a Metler AE 240 balance that measured to within 0.0001 g .

## Results

Tables 2 and 3 list the experimental values of densities $(\rho)$, speeds of sound $(u)$, and refractive indices ( $n_{D}$ ) for the binary system 1-butanol + methanol and for the ternary system, respectively, obtained at 298.15 K and atmospheric pressure. These tables also include the calculated values of the isentropic compressibilities $\left(\kappa_{\mathrm{s}}\right)$, excess molar volumes $\left(V^{E}\right)$, and deviations in molar refraction ( $\Delta \mathrm{R}$ ) and in isentropic compressibility $\left(\Delta \kappa_{s}\right)$, calculated by means of the following expressions:

Excess Molar Volumes:

$$
\begin{equation*}
V^{E}=\frac{1}{\rho} \sum_{i=1}^{n} x_{i} M_{i}-\sum_{i=1}^{n} \frac{x_{i} M_{i}}{\rho_{i}}=V-\sum_{i=1}^{n} x_{i} V_{i} \tag{1}
\end{equation*}
$$

where $\rho$ is the density, $M$ is the molecular weight, $x$ is the mole fraction, i is related to each component, and n is the number of components in the mixture. The molar refractions were calculated using the Lorentz-Lorenz equation

$$
\begin{equation*}
\mathrm{R}=\mathrm{V} \frac{\mathrm{n}_{\mathrm{D}}^{2}-1}{\mathrm{n}_{\mathrm{D}}^{2}+2} \tag{2}
\end{equation*}
$$

Molar Refraction Deviations:

$$
\begin{equation*}
\Delta R=R-\sum_{i=1}^{n} x_{i} R_{i} \tag{3}
\end{equation*}
$$

Isentropic Compressibilities:

$$
\begin{equation*}
\kappa_{\mathrm{s}}=\mathrm{u}^{-2} \rho^{-1} \tag{4}
\end{equation*}
$$

Isentropic Compressibility Deviations:

$$
\begin{equation*}
\Delta \kappa_{\mathrm{s}}=\kappa_{\mathrm{s}}-\sum_{\mathrm{i}=1}^{\mathrm{n}} \phi_{\mathrm{i}} \kappa_{\mathrm{si}} \tag{5}
\end{equation*}
$$

where $\phi$ is the volume fraction defined by

$$
\begin{equation*}
\phi_{\mathrm{i}}=\mathrm{x}_{\mathrm{i}} \mathrm{~V}_{\mathrm{i}} / \sum_{\mathrm{j}} \mathrm{x}_{\mathrm{j}} \mathrm{~V}_{\mathrm{j}} \tag{6}
\end{equation*}
$$

and j refers to all the components in the mixture.
Figure 1 shows the comparative values of the excess volume for the binary 1-butanol + methanol obtained at 298.15 K by different authors (I glesias et al., 1996, 1998; Plug and Benson, 1967). For the 1-butanol + methanol + MTBE system Figures 2, 3, and 5 show the density isolines, the refractive indices, and the excess volumes obtained, plotted versus the mole fraction of the mixture. Figures 4 and 6 show the isolines of the speed of sound and the isentropic compressibility deviations plotted versus the volume fraction of the mixture.

## Correlation

The cal culated values of $\mathrm{V}^{\mathrm{E}}, \Delta \mathrm{R}$, and $\Delta \kappa_{\mathrm{s}}$ were correl ated to the composition by means of the Redlich-Kister (1948) expansion, which for binary mixtures is

$$
\begin{equation*}
\Delta \mathrm{N}=\mathrm{x}_{\mathrm{i}} \mathrm{x}_{\mathrm{j}} \sum_{\mathrm{n}} \mathrm{~A}_{\mathrm{n}}\left(\mathrm{x}_{\mathrm{i}}-\mathrm{x}_{\mathrm{j}}\right)^{\mathrm{n}} \tag{7}
\end{equation*}
$$

where $\Delta N$ is $V E$ or $\Delta R$ and $x_{i}$ is the mole fraction of component $i$ in the mixture, or $\Delta N$ is $\Delta \kappa_{s}$ and $x_{i}$ is the volume fraction of component $i$ in the mixture, $A_{n}$ is the polynomial coefficient, and $n$ is the number of polynomial coefficients. For ternary systems the corresponding equation is

$$
\begin{align*}
& \Delta N_{123}=\Delta N_{12}+\Delta N_{23}+\Delta N_{13}+ \\
& \quad x_{1} x_{2} x_{3}\left(A+B\left(x_{1}-x_{2}\right)+C\left(x_{2}-x_{3}\right)+D\left(x_{1}-x_{3}\right)+\ldots\right) \tag{8}
\end{align*}
$$

where $\Delta \mathrm{N}_{123}$ is $\mathrm{V}^{\mathrm{E}}, \Delta \kappa_{\mathrm{s}}$, or $\Delta \mathrm{R}, \mathrm{x}_{\mathrm{i}}$ is the mole fraction or


Figure 1. Excess molar volume for the system 1-butanol + methanol: (O) this work; ( $\square$ ) Pflug, H. D., et al. (1968); ( $\nabla$ ) I glesias, M., et al. (1996); (土) Iglesias, M., et al. (1998).


Figure 2. Density isolines for 1-butanol + methanol + MTBE mixtures at 298.15 K and atmospheric pressure (system compositions in mole fractions).
volume fraction of component $i$, according to the correlated parameter (as previously indicated), and $\Delta \mathrm{N}_{\mathrm{ij}}$ is the value of the Redlich-Kister coefficient for the same property, as obtained by fitting the Redlich-Kister polynomial to the data for the binary system ( $\mathrm{i}, \mathrm{j}$ ).

Equations 7 and 8 were fitted to the appropriate param-eter-composition data for the binary and ternary systems by the least-squares regression, applying Fisher's F-test to establish the number of coefficients. These coefficients and their mean standard deviations are listed in Table 4 for the binary system 1-butanol + methanol (data for the binaries methanol + MTBE and 1-butanol + MTBE were taken from Arce et al., 1997 and 1999) and in Table 5 for the ternary system 1-butanol + methanol + MTBE.


Figure 3. Refractive index isolines for 1-butanol + methanol + MTBE mixtures at 298.15 K and atmospheric pressure (system compositions in mole fractions).


Figure 4. Speed of sound isolines for 1-butanol + methanol + MTBE mixtures at 298.15 K and atmospheric pressure (system compositions in volume fractions).

## Prediction

An interesting practice in solution thermodynamics is to estimate the properties of the multicomponent systems from the properties of their pure components; however, this practice is often inaccurate due to the effects of mixing. An attractive alternative that reduces the experimental work to binary mixtures is to evaluate the mixing changes of the multicomponent system from the properties of its constituent binary subsystems. To assess the viability of this approach for the ternary systems studied here, their $V^{\mathrm{E}}, \Delta \mathrm{R}$, and $\Delta \kappa_{\mathrm{s}}$ were predicted from these properties of their constituent binary subsystems by means of empirical equations available in the literature. These were the equations of Radojkovic et al. (1977), Rastogi et al. (1977), J acob and Fitzner (1977), Colinet (1967), Toop (1965), K ohler (1960), and Tsao and Smith (1953) and the equation of Scatchard et al. (1952) among others. These expressions are common in the bibliography and have been used in a


Figure 5. Excess molar volume isolines for 1-butanol + methanol + MTBE mixtures at 298.15 K and atmospheric pressure (system compositions in mole fractions).


Figure 6. I solines for the deviation in isentropic compressibility for 1-butanol + methanol + MTBE mixtures at 298.15 K and atmospheric pressure (system compositions in volume fractions).
previous paper (Arce et al., 1997) and are therefore not repeated unnecessarily.

Table 6 shows the standard deviations of the excess molar volumes and the refraction and isentropic compressibility deviations when they are predicted using the above equations. Some of these equations handle the components of different forms; the asymmetrical component of the mixture is indicated in Table 6.

## Conclusions

At present there are few measurements of $\mathrm{V}^{\mathrm{E}}$ and isentropic compressibilities for mixtures of ethers and alcohols. The ternary mixture 1-butanol + methanol + MTBE exhibits negative values of $\mathrm{V}^{\mathrm{E}}$ at 298.15 K and atmospheric pressure for the range of compositions; only the binary system 1-butanol + methanol shows positive but very low values of this property. The deviations in $\Delta R$ and $\Delta \kappa_{s}$ were also negative except for some compositions of the binary system butanol + methanol. This behavior may be

Table 4. Polynomial Coefficients $A_{n}$, and Standard Deviations $\boldsymbol{\sigma}$ Obtained for the Fits of Eq 7 to the $\mathrm{V}^{\mathrm{E}}-$, $\Delta \kappa_{s^{-}}$, and $\Delta \mathbf{R}$-Composition Data for the Binary Systems (for $\Delta \kappa_{\mathrm{s}}$, System Compositions Were in Volume Fraction $\left.\phi_{i}\right)$

| property | $\mathrm{A}_{0}$ | $\mathrm{A}_{1}$ | $\mathrm{A}_{2}$ | $\mathrm{A}_{3}$ | $\sigma$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1-Butanol + Methanol |  |  |  |  |  |
| $\mathrm{V}^{\mathrm{E}} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | 0.2673 | -0.2032 |  |  | 0.001 |
| $\Delta \kappa_{s} /\left(\mathrm{T} \mathrm{Pa}^{-1}\right)$ | 18.9 | -19.7 | -7.2 |  | 0.1 |
| $\Delta \mathrm{R} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | 0.0079 | 0.0445 | -0.0582 |  | 0.001 |
| Methanol + MTBE |  |  |  |  |  |
| $\mathrm{V}^{\mathrm{E}} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | -2.4651 |  | -0.1678 | -0.3632 | 0.001 |
| $\Delta \kappa_{s} /\left(\mathrm{T} \mathrm{Pa}^{-1}\right)$ | -214.7 | 72.0 | -86.4 | 130.0 | 0.4 |
| $\Delta \mathrm{R} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | -0.0885 |  |  |  | 0.001 |
| 1-Butanol + MTBE |  |  |  |  |  |
| $\mathrm{V}^{\mathrm{E}} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | -2.9144 | 0.0886 | -0.2546 |  | 0.001 |
| $\Delta \kappa_{s} /\left(\mathrm{T} \mathrm{Pa}^{-1}\right)$ | -253.5 | 53.1 | -63.2 | 52.6 | 0.1 |
| $\Delta \mathrm{R} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | -0.0627 | -0.0314 | -0.1725 |  | 0.001 |

Table 5. Polynomial Coefficients and Standard Deviations $\sigma$ Obtained for the Fits of Eq 8 to the $\mathrm{V}^{\mathrm{E}}-$, $\Delta k_{s^{-}}$, and $\Delta \mathbf{R}$-Composition Data for the Ternary System 1-Butanol (1) + Methanol (2) + MTBE (3) (for $\Delta \kappa_{\mathrm{s}}$, System Compositions Were in Volume Fraction $\phi_{i}$ )

| property | A | B | C | D | $\sigma$ |
| :--- | :--- | :---: | :---: | :---: | :---: |
| $\mathrm{V}^{\mathrm{E}} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | -1.129 | 0.3058 | -0.7373 | -0.4315 | 0.009 |
| $\Delta \kappa \mathrm{~s} /\left(\mathrm{T} \mathrm{Pa}^{-1}\right)$ | 17.60 | -78.62 | 37.44 | -4.18 | 0.74 |
| $\Delta \mathrm{R} /\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | -0.1289 | -0.2374 | 0.5471 | 0.3097 | 0.003 |

Table 6. Standard Deviations in the Excess Molar Volumes and Deviations in Molar Refraction and Isentropic Compressibility Predicted for Ternary Mixtures at 298.15 K and Atmospheric Pressure

|  | $\mathrm{VE}_{123 /}$ <br> $\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | $\Delta \kappa_{\text {s123 }} /$ <br> $\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ | $\Delta \mathrm{R}_{123} /$ <br> $\left(\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}\right)$ |
| :--- | :---: | :---: | :---: |
| Radojkovic | 0.025 | 2 | 0.007 |
| Rastogi | 0.210 | 19 | 0.011 |
| Kohler | 0.023 | 3 | 0.007 |
| J acob and Fitzner | 0.063 | 5 | 0.008 |
| Tsao and Smitha | 0.092 | 11 | 0.007 |
| Tsao and Smith | 0.099 | 12 | 0.006 |
| Tsao and Smith | 0.109 | 10 | 0.010 |
| Colinet | 0.299 | 30 | 0.013 |
| Toop $^{\text {c }}$ | 0.044 | 8 | 0.007 |
| Toop $^{\text {b }}$ | 0.047 | 7 | 0.006 |
| Toop $^{\text {c }}$ | 0.104 | 10 | 0.010 |
| Scatchard $^{\text {a }}$ | 0.234 | 24 | 0.011 |
| Scatchard $^{\mathrm{b}}$ | 0.264 | 21 | 0.009 |
| Scatchard $^{\mathrm{c}}$ | 0.131 | 12 | 0.010 |

${ }^{\text {a }} 1$-Butanol is the asymmetric component. ${ }^{\text {b }}$ Methanol is the asymmetric component. ${ }^{\text {c MTBE }}$ is the asymmetric component.
considered regular, taking into account that these components are open-chain, relatively flexible molecules, whose orientation order increases with the increase of the chain length of the alkyl group. This would reveal the tendency of interstitial accommodation of the al cohols into the ethers leading to a negative $\mathrm{V}^{\mathrm{E}}$, as can be see in the obtained values. The properties $V \mathrm{E}, \Delta \mathrm{R}$, and $\Delta \kappa_{\mathrm{s}}$ were satisfactorily correlated by the polynomial expansion of Redlich-Kister. The equations of Radojkovic and Kohler, followed by those of Jacob and Fitzner, are the most adequate for the prediction of the properties considered in this paper and usable in the absence of ternary data. The equations of Colinet, Rastogui, and Scatchard produce high deviations and are not recommended. Limitations are found using the equations of Toop and Tsao and Smith.
The conclusions obtained for the prediction of the property variations from the constituent binary systems (and therefore for the direct physical properties also) can be generalized for mixtures of ethers and alcohols. This can
be asserted from the results of this and other previous work (Arce et al., 1997, 1999b).

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