## Viscosities of Binary and Ternary Mixtures of Hexadecanoic, Octadecanoic, and *cis*-9-Octadecenoic Acids

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The kinematic viscosity was measured for binary and ternary liquid mixtures for the hexadecanoic, octadecanoic, and *cis*-9-octadecenoic acids, at temperatures ranging from above the solidification point up to 373 K using a Cannon Fenske three-capillary viscosimeter. The measurements were correlated with Andrade's equation for pure components, with McAllister's equation for binary and ternary mixtures, and with Teja and Rice's equation for ternary mixtures. A nearly lineal behavior of the kinematic viscosity with regard to composition was observed in the above-mentioned equations for all the tested mixtures. The equations gave a satisfactory fit to the kinematic viscosity of the liquid mixtures studied. For ternary mixtures, Teja and Rice's equation permitted their estimation over a higher temperature range than McAllister's equation.

#### Introduction

In the refining of edible oils, gas distillates are obtained that are of great interest to the food and pharmaceutical industries. The majority of the components of the distillates are fatty acids (Ghosh and Bhattacharyya, 1996; Ruiz et al., 1995a). The fatty acids that are present in the raw oils and in the soya, sunflower, and olive refined oils are essentially hexadecanoic, octadecanoic, *cis*-9-octadecenoic, and 9,12-octadecadienoic acids (Ruiz, 1993b).

In Gracianni et al. (1994), a procedure is currently being tested to recover these compounds in tubes and shell exchangers. As heat- and mass-transfer phenomena are involved in the design of these heat exchangers, certain information concerning the kinematic viscosities of each compound and its mixtures is required.

This study presents the results of the measurements of the kinematic viscosity for binary and ternary mixtures of hexadecanoic (palmitic), octadecanoic (stearic), and *cis*-9-octadecenoic (oleic) fatty acids. The measurements were carried out every 5 K between temperatures close to solidification of each mixture and 373 K.

The binary mixtures (palmitic + stearic), (palmitic + oleic), and (oleic + stearic) and the ternary mixture (palmitic + stearic + oleic) were studied. In this last mixture, the presence of oleic acid was increased within the range of compositions so as to reproduce those obtained in raw and deodorized oils, to ascertain the effect of the viscosity as a function of the composition of the mixture.

The experimental values of kinematic viscosity for the pure substances obtained in a previous study (Cedeño et al., 1999) were fitted to Andrade's equation. The experimental data for the binary mixtures were fitted to McAllister's equation, and for the experimental data for the

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ternary mixtures were fitted to McAllister's and Teja and Rice's equations.

#### **Experimental Section**

Measurements of kinematic viscosity were carried out for the binary mixtures (palmitic + stearic), (palmitic + oleic), and (oleic + stearic) and the ternary mixture (palmitic + stearic + oleic). The mixtures were prepared in an analytical balance Mettler AE 240, accurate to 0.1 mg. The mass ratios used for the first and second components for the binary mixtures were respectively (1:1), (1: 3), and (3:1). (1:1) means 50% of the mass fraction comes from the first component and 50% of the mass fraction comes from the second, (1:3) means 25% of the mass fraction comes from the first component and 75% of the mass fraction comes from the second, and (3:1) means 75% of the mass fraction comes from the first component and 25% of the mass fraction comes from the second. The first component corresponded to the one with the lower molecular mass. Under the supposition that the compositions of the fatty acids in raw and deodorized oils are practically the same, we employed the same values for the compositions of the ternary mixtures. The mass ratios used for the first, second, and third components were respectively (1: 1:1), (3:1:1), (3:1:3), (3:1:6), (3:1:12), (3:1:18), (3:1:24), and (3:1:30). The pure free fatty acids were provided by Merck, their purities for palmitic, stearic, and oleic fatty acids being 99.3 mass %, 97 mass %, and 99.9 mass %, respectively. All the measurements of kinematic viscosity were carried out according to ASTM test methods D 445 and D 2515 using two Canon-Fenske-type Ostwald capillary viscosimeters for transparent liquids, supplied by PROTON (Spain), of sizes 75, 150, and 200. These viscosimeters were used because of the type of fatty acid and the range of working temperature. The kinematic viscosity was determined by the expression

$$v = c\tau$$
 (1)

where *c* is the calibration constant in  $(mm^2 \cdot s^{-1}) \cdot s^{-1}$  for the two viscosimeters used, given by the manufacturer for

# e calibration constant in $(mm^2 \cdot e^{-1}) \cdot e^{-1}$

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 Table 1. Kinematic Viscosity Measurements of Pure Components

		$10^6 \nu/m^2 \cdot s^{-1}$						
$T/\mathbf{K}$	palmitic	stearic	oleic					
298			32.948					
303			27.343					
308			22.990					
313			19.588					
318			16.778					
323			14.455					
328			12.537					
333			11.017					
338	9.956		9.735					
343	8.867		8.598					
348	7.856	10.127	7.560					
353	7.039	8.989	6.774					
358	6.322	8.022	5.998					
363	5.703	7.188	5.419					
368	5.158	6.485	4.926					
373	4.694	5.868	4.499					

 Table 2. Kinematic Viscosity Measurements of Binary

 Mixtures

	$10^6 \nu_{ m m}/{ m m}^2 \cdot { m s}^{-1}$								
		palmitic +		oleic +		palmitic +			
T/K	$X_1^a$	stearic	<i>X</i> 1	stearic	<i>X</i> 1	oleic			
333					0.2686	11.514			
338	0.2700	12.302	0.2513	12.358	0.2686	10.101			
343	0.2700	10.751	0.2513	10.845	0.2686	8.817			
348	0.2700	9.538	0.2513	9.617	0.2686	7.834			
353	0.2700	8.470	0.2513	8.424	0.2686	7.000			
358	0.2700	7.558	0.2513	7.541	0.2686	6.286			
363	0.2700	6.860	0.2513	6.767	0.2686	5.655			
368	0.2700	6.118	0.2513	6.091	0.2686	5.123			
373	0.2700	5.608	0.2513	5.528	0.2686	4.645			
323					0.5241	15.294			
328					0.5241	13.253			
333	0.5259	12.884	0.5018	13.416	0.5241	11.554			
338	0.5259	11.269	0.5018	11.709	0.5241	10.139			
343	0.5259	9.922	0.5018	10.287	0.5241	8.949			
348	0.5259	8.801	0.5018	9.105	0.5241	7.923			
353	0.5259	7.774	0.5018	8.040	0.5241	7.077			
358	0.5259	7.006	0.5018	7.188	0.5241	6.356			
363	0.5259	6.259	0.5018	6.440	0.5241	5.714			
368	0.5259	5.703	0.5018	5.818	0.5241	5.179			
373	0.5259	5.180	0.5018	5.263	0.5241	4.702			
333	0.7690	12.303							
338	0.7690	10.767	0.7255	10.464	0.7430	10.927			
343	0.7690	9.528	0.7255	9.247	0.7430	8.793			
348	0.7690	8.475	0.7255	8.166	0.7430	7.848			
353	0.7690	7.576	0.7255	7.301	0.7430	7.011			
358	0.7690	6.780	0.7255	6.540	0.7430	6.308			
363	0.7690	6.071	0.7255	5.901	0.7430	5.695			
368	0.7690	5.509	0.7255	5.341	0.7430	5.089			

 $^a$   $x_1\colon$  mole fraction of the component with lower molecular mass of the binary mixtures (first component).

310.93 K, 323.15 K, and 372.04 K, and  $\tau$  is the flow average time of the three times measured, with an accuracy of 0.01 s.

A thermostat model Summer & Runge D 1000 (Germany), with a temperature range of 283 to 373 K and a temperature accuracy of  $\pm 0.1$  K, was also employed, the thermometers used having subdivisions of 0.1 K.

#### **Results and Discussion**

Applications for Andrade's equation for fatty acids appear in Noureddini and Clements (1992b) and Valeri and Meirelles (1997). The equation is as follows:

$$\ln \nu = A + \frac{B}{T} \tag{2}$$



**Figure 1.** Estimated kinematic viscosity and the measurements for the binary mixtures as a function of the mole fraction, from McAllister's equation. Solid lines are correlations, and the points are experimental data. ( $\Box$ ) 373 K; ( $\diamond$ ) 368 K; ( $\triangle$ ) 363 K; ( $\times$ ) 358 K; (\*) 353 K; (-) 348 K; ( $\bigcirc$ ) 343 K.

where  $\nu$  is the kinematic viscosity, *A* and *B* are the constants obtained by fitting to the experimental data, and *T* is the thermodynamic temperature.

McAllister's method for the estimation of the kinematic viscosities of binary mixtures of fatty acids is reported in Valeri and Meirelles (1997), Irving (1977), and Barata and Serrano (1994). The resulting equation has the following form:

$$\ln v_{\rm m} = x_1^3 \ln v_1 + (1 - x_1)^3 \ln v_2 + 3x_1^2 (1 - x_1) \ln v_{12} + 3x_1 (1 - x_1)^2 \ln v_{21} + r^{\circ} (3)$$

with

Table 3.	Kinematic	Viscosity	Measurements of	<b>Ternary Mixtures</b>
		./		

			$10^{6}$ v <sub>m</sub> /m <sup>2</sup> ·s <sup>-1</sup>							
mixture <sup>a</sup>	$X_1^b$	$X_2^b$	303 K	308 K	313 K	318 K	323 K	328 K	333 K	338 K
1:1:1	0.3560	0.3209					16.669	14.411	12.552	11.002
3:1:1	0.6238	0.1874						13.771	12.063	10.502
3:1:3	0.4528	0.1361					15.459	13.340	11.631	10.209
3:1:6	0.3209	0.0964				17.917	15.419	13.358	11.675	10.297
3:1:12	0.2027	0.0609		25.023	21.018	17.887	15.326	13.379	11.642	10.277
3:1:18	0.1482	0.0445		24.052	20.286	17.434	15.015	13.028	11.440	10.042
3:1:24	0.1168	0.0351	28.035	23.511	19.830	17.049	14.686	12.780	11.161	9.844
3:1:30	0.0963	0.0290	28.135	23.630	20.021	17.142	14.812	12.899	11.269	9.946
			$10^6 v_{ m m}/{ m m}^2 \cdot { m s}^{-1}$							
mixture <sup>a</sup>	$x_1^b$	$X_2^b$	343 K	. 3	348 K	353 K	358 K	363 K	368 K	373 K
1:1:1	0.3560	0.3209	9.740	5	8.604	7.659	6.888	6.181	5.583	5.096
3:1:1	0.6238	0.1874	9.288	8	8.232	7.348	6.590	5.948	5.373	4.881
3:1:3	0.4528	0.1361	9.018	8	8.013	7.162	6.424	5.782	5.242	4.756
3:1:6	0.3209	0.0964	9.082	8	8.026	7.161	6.433	5.835	5.258	4.796
3:1:12	0.2027	0.0609	9.180	8	8.213	7.126	6.374	5.753	5.251	4.709
3:1:18	0.1482	0.0445	8.866		7.946	7.101	6.377	5.735	5.196	4.734
3:1:24	0.1168	0.0351	8.721		7.765	6.992	6.248	5.637	5.136	4.661
3:1:30	0.0963	0.0290	8.815		7.860	7.019	6.313	5.709	5.181	4.715

<sup>*a*</sup> Mixture: mass ratios used in the ternary mixtures. <sup>*b*</sup>  $x_1$ ,  $x_2$ : mole fraction for the palmitic and stearic fatty acids in the ternary mixtures.

 Table 4. Constants A and B Obtained for Andrade's Equation

pure substances	Α	В	<i>r</i> /%	$10^6\sigma/m^2\cdot s^{-1}$	<i>T/</i> K
palmitic	-19.558	2718.3	0.3	0.02	338-373
stearic	-19.647	2835.0	0.2	0.02	348 - 373
oleic	-20.241	2945.4	1.5	0.42	303-373
$r^{\circ} = -\ln \bigg[ x_1 + 1 \bigg] + 1$	$(1-x_1)\frac{N}{N}$	$\left[\frac{d_2}{d_1}\right] + 3x$	$(x_1^2)^2$	$-x_{1}$ ) $\ln\left(\frac{2}{3}+\right)$	$\left(\frac{M_2}{3M_1}\right) +$
$3x_1^2(1)$	$(-x_1)^2 \ln(x_1)^2$	$\frac{1}{3} + \frac{2N}{3N}$	$\left(\frac{l_2}{l_1}\right) +$	$(1-x_1)^3 \ln x_1$	$\left(\frac{M_2}{M_1}\right)$ (4)

where  $v_m$ ,  $v_1$ , and  $v_2$  are the kinematic viscosities of the mixture and the pure components, respectively,  $v_{12}$  and  $v_{21}$  are the pseudokinematic viscosities of McAllister's method, M is the molecular mass, and  $x_i$  is the mole fraction of component *i*. The term  $r^{\rho}$  is approximately zero when the molecular mass ratio is approximately unity.

The temperature dependence of the two pseudokinematic viscosities  $v_{12}$  and  $v_{21}$  is also given by Andrade's equation:

$$\ln v_{ij} = A_{ij} + \frac{B_{ij}}{T} \tag{5}$$

-18.1505

For each binary system, the Andrade parameters of eq 5,  $A_{ij}$  and  $B_{ij}$  (*i* and  $j = 1, 2; i \neq j$ ), are obtained using the method of least-squares, from measurements of kinematic viscosity at several temperatures and compositions and eq 3.

McAllister's equation can be applied for the ternary mixture (Serrano et al., 1990). The equation has the following form:

$$\ln v_{\rm m} = x_1^{3} \ln v_1 + x_2^{3} \ln v_2 + x_3^{3} \ln v_3 + 3x_1^{2}x_2 \ln v_{12} + 3x_1^{2}x_3 \ln v_{13} + 3x_2^{2}x_1 \ln v_{21} + 3x_2^{2}x_3 \ln v_{23} + 3x_3^{2}x_1 \ln v_{31} + 3x_3^{2}x_2 \ln v_{32} + 6x_1x_2x_3 \ln v_{123} + r^{\circ}$$
(6)

To determine the pseudokinematic viscosity of the ternary interaction  $\nu_{123}$ , the procedure explained according to eq 5 was also applied, and  $r^{\circ}$  was set to zero for the same reason as that for binary mixtures.

Teja and Rice's method for estimating the kinematic viscosities of liquid mixtures, which is based on the model of General Corresponding States (GCS), is reported by Reid et al. (1987) and Teja and Rice (1981). The equation has the following form:

$$\ln(\nu\xi) = \ln(\nu\xi)^{r_1} + \frac{\omega - \omega^{r_1}}{\omega^{r_1} - \omega^{r_1}} [\ln(\nu\xi)^{r_2} - \ln(\nu\xi)^{r_1}] \quad (7)$$

where  $\nu$  is the kinematic viscosity of the mixture or of the reference substances 1 and 2,  $\omega$  is the acentric factor of the mixture or of the reference substances 1 and 2, and  $\xi$  is a parameter, defined as  $\xi = V_c^{2/3}/(T_c M)^{1/2}$  for the mixture or for the reference substances 1 and 2.  $V_c$  and  $T_c$  are the critical mole volume and temperature for the mixture or for the reference substances 1 and 2. The numbers 1 and 2 refer to the two fluids that need to be defined and that have known temperature-dependent properties.

The variables related to the composition of the mixture are defined by the terms  $V_{\rm cm}$ ,  $T_{\rm cm}$ ,  $M_{\rm m}$ , and  $\omega_{\rm m}$ . The rules suggested by several authors for these parameters of the mixture are

0.09

348-373

**Table 5. Parameters Obtained for McAllister's Equation** 

palmitic + stearic + oleic

		-					
binary mixtures	$A_{12}$	$B_{12}$	$A_{21}$	$B_{21}$	<i>r</i> /%	$10^6 \sigma/m^2 \cdot s^{-1}$	<i>T/</i> K
palmitic + stearic oleic + stearic palmitic + oleic	$-19.6040 \\ -18.6589 \\ -19.8169$	2766.3045 2413.3122 2801.6949	$-19.3798 \\ -20.4441 \\ -19.3978$	2709.7740 3102.6215 2677.2858	0.8 0.9 0.6	0.07 0.01 0.05	343-373 348-373 338-373
Table 6. Parameters Obtained for McAllister's Equation							
ternary mixtu	re	$A_{123}$	B <sub>123</sub>	<i>r</i> /%	106	$\sigma/m^2 \cdot s^{-1}$	T∕K

2227.2146

1.1



**Figure 2.** Estimated kinematic viscosity and the measurements for the ternary mixture from McAllister's equation when the oleic acid was increased with mass ratios from 3:1:1 to 3:1:30. Solid lines are correlations, and the points are experimental data. ( $\Box$ ) 373 K; ( $\diamond$ ) 368 K; ( $\diamond$ ) 363 K; ( $\star$ ) 358 K; ( $\star$ ) 353 K; (-) 348 K.

 Table 7. Constants A and B Obtained for Andrade's

 Equation

fatty acid	Α	В	<i>r</i> /%	$10^6\sigma/m^2 \cdot s^{-1}$	<i>T</i> /K
erucic	-19.750	2956.6	0.2	0.62	310-383

$$V_{\rm cm} = \sum_{i} \sum_{j} x_i x_j V_{\rm cij} \tag{8}$$

$$V_{c_{ij}} = \frac{(V_{ci}^{1/3} + V_{cj}^{1/3})^3}{8}$$
(9)

$$T_{\rm cm} = \frac{\sum_{i} \sum_{j} x_i x_j T_{\rm cij} V_{\rm cij}}{V_{\rm cm}}$$
(10)

$$T_{\rm cij}V_{\rm cij} = \varphi_{ij}(T_{\rm ci}T_{\rm cj}V_{\rm ci}V_{\rm cj})^{1/2}$$
(11)

$$M_{\rm m} = \sum_{i} X_i M_i \tag{12}$$

$$\omega_{\rm m} = \sum_{i} x_i \omega_i \tag{13}$$

In eq 11,  $\varphi_{ij}$  is an interaction parameter close to unity, which is determined by the kinematic viscosity experimental data.

To estimate the kinematic viscosity of the mixture at a certain temperature using eq 7, knowledge of the kinematic viscosity values of the reference substances is required. These values are determined according to Andrade's equation, using the reference temperature  $T(T_c^{r_1}/T_{cm})$  for reference substance 1 and  $T(T_c^{r_2}/T_{cm})$  for reference substance 2. The choice of the reference substances is preferably carried out from among the components of the mixture, although they may also be arbitrary (Teja and Rice, 1981).

The values of kinematic viscosity estimated for each equation are compared using the average deviation r and the standard deviation  $\sigma$ , by means of the expressions

$$r = \left[\frac{\sum(\nu - \nu_{\rm est}|/\nu)}{n}\right] 100 \tag{14}$$

$$\sigma = \left[\frac{\sum (\nu - \nu_{\rm est})^2}{(n - p)}\right]^{1/2}$$
(15)

where  $\nu$  and  $\nu_{est}$  are the kinematic viscosity measurement and the estimated one, *n* is the number of experimental points, and *p* is the number of adjustment parameters.

Starting from the measurement, the values of the kinematic viscosity for pure components are presented in Table 1; these were obtained from the dynamic viscosity  $\mu$ and density  $\rho$  measurements reported by Cedeño et al. (1999). The results of the measurements for binary and ternary mixtures are presented in Tables 2 and 3. In previous works, kinematic viscosities for the palmitic, stearic, and oleic acids and some binary mixtures were measured with a similar experimental technique. Although in the present work the measurements obtained by other authors are not compared, the results obtained were similar to the values published by Noureddini et al. (1992b) and Valeri and Meirelles (1997) (palmitic, stearic, and oleic acids and (palmitic + stearic) and (oleic + stearic) binary mixtures), the minimum average deviation being  $r \simeq 0.6\%$ for the case of stearic acid and the maximum average deviation being  $r \simeq 4.8\%$  for the case of the binary mixture (oleic + stearic).

The constants *A* and *B* of eq 2 for the palmitic, stearic, and oleic acids are presented in Table 4. The average deviation values *r* are <0.3%, except for oleic acid. The highest standard deviation value  $\sigma$  corresponds to oleic acid, being  $0.42 \times 10^{-6} \text{ m}^2 \cdot \text{s}^{-1}$ .



**Figure 3.** Estimated kinematic viscosity and the measurements for the ternary mixture from Teja and Rice's equation when the oleic fatty acid was increased with mass ratios from 3:1:1 to 3:1:30. Solid lines are correlations, and the points are experimental data. ( $\Box$ ) 373 K; ( $\diamond$ ) 363 K; ( $\triangle$ ) 353 K; ( $\times$ ) 343 K; ( $\ast$ ) 333 K; (-) 323 K; (-) 313 K; ( $\bigcirc$ ) 303 K.

**Table 8.** Interaction Parameter  $\varphi_{ii}$  Obtained for Teja and Rice's Equation

	arphipalmitic-stearic	arphipalmitic-oleic	$arphi_{ ext{stearic-oleic}}$	<i>r</i> /%	$10^6\sigma/m^2$ ·s <sup>-1</sup>	<i>T</i> /K
palmitic + stearic + oleic	1.0916	1.0387	0.9771	2.0	0.23	303-308

The constants  $A_{ij}$  and  $B_{ij}$  of eq 3 for the binary mixtures are presented in Table 5. Once the constants are substituted in the equation, r does not exceed 1% in any case. The estimated kinematic viscosity and the measurements for the binary mixtures as a function of the mole fraction are presented in Figure 1. A nearly lineal behavior of the kinematic viscosity is observed for the three binary mixtures, although small deviations are observed for the mixtures (palmitic + stearic) and (oleic + stearic). The values of the kinematic viscosity remain nearly constant with the mole fraction for mixtures (palmitic + oleic). The values of  $r^{\circ}$  were found to be around  $1.0 \times 10^{-3}$  in all the cases. The use of McAllister's equation is limited when the temperature is higher than the melting point of any component of the mixture. However, the mixture may be liquid at a lower temperature.

The interaction parameters  $A_{123}$  and  $B_{123}$  for the ternary mixtures (eq 6) are presented in Table 6. In the determination of these coefficients, the term  $r^{\circ}$  was given the value zero. The estimated kinematic viscosity and the measurements for the ternary mixtures as a function of the oleic mole fraction are presented in Figure 2 for the mass ratios (3:1:1), (3:1:3), (3:1:6), (3:1:12), (3:1:18), (3:1:24), and (3:1: 30). A nearly lineal behavior is also observed when the oleic mole fraction increases. For the same reason as for the binary mixtures, the estimation of the viscosity by McAllister's equation is limited and cannot be applied when the temperature is lower than those of the solidification of the pure components.

One alternative to McAllister's equation is Teja and Rice's equation (eq 7), but reference substances must be selected. Oleic acid and erucic acid were chosen as reference substances. Measurements of density and dynamic viscosity for erucic acid are reported by Noureddini et al. (1992a,b). The values of the constants *A* and *B* for erucic acid, which were obtained according to eq 2, are presented in Table 7. The interaction parameters  $\varphi_{ij}$  for the ternary mixtures are presented in Table 8.

The estimated kinematic viscosity (eq 7) and the measurements for the ternary mixtures as a function of the oleic mole fraction are presented in Figure 3 for the mass ratios (3:1:1), (3:1:3), (3:1:6), (3:1:12), (3:1:18), (3:1:24), and (3:1:30). As in the application of McAllister's equation, a nearly lineal behavior can be observed, and furthermore, Teja and Rice's equation allows a wider temperature range than McAllister's equation.

#### **Literature Cited**

- Barata, P. A.; Serrano, M. L. Densities and Viscosities of Thymol + 1,8-Cineole. 2. J. Chem. Eng. Data 1994, 39, 298–301.
- Cedeño, F. O.; Prieto, M.; Alonso, R.; Bada, J. C. Study of the Density and the Viscosity of Some Pure Fatty Acids. *Grasas Aceites (Seville)* **1999** (in press).
- Ghosh, S.; Bhattacharyya, D. K. Isolation of Tocopherol and Sterol Concentrate from Sunflower Oil Deodorizer Distillate. J Am. Oil Chem. Soc. 1996, 73, 1271–1274.
- Gracianni, E.; Bada, J. C.; Berbel, F. R.; Méndez, M. V. R. Physical refining of edible oils using nitrogen as stripping gas. Process optimization. 3. *Grasas Aceites (Seville)* **1994**, *45*, 132–146.
- Irving, J. B. Viscosities of Binary Liquid Mixtures: A Survey of Mixtures Equations. Natl. Eng. Lab. Rept. 630; East Kilbride, Glasgow, Scotland, Feb. 1977.
- Noureddini, H.; Teoh, B. C.; Clements, L. D. Densities of Vegetable Oils and Fatty Acids. J. Am. Oil Chem. Soc. **1992a**, 69, 1184–1188.
- Noureddini, H.; Teoh, B. C.; Clements, L. D. Viscosities of Vegetable Oils and Fatty Acids. J. Am. Oil Chem. Soc. 1992b, 69, 1189–1191.
- Reid, R. C.; Prausnitz, J. M.; Poling, B. E. The Properties of Gases & Liquids, 4th ed.; McGraw-Hill: New York, 1987.
- Ruiz, M. V. Modifications Produced During the Process of the Edible Oils Refining. Ph.D. Thesis, University of Seville, Spain, 1993b.

- Ruiz, M. V.; Marquéz, V. G.; Dobarganes, M. C. Quantitative Determination of Majority Components present in Distilled Obtained in the Deodorization of Oils and Fats. 1. *Grasas Aceites (Seville)* **1995a**, *46*, 21–25.
- Serrano, L.; Silva, A. J.; Farelo, F. Densities and Viscosities of Binary and Ternary Liquid Systems Containing Xylenes. J. Chem. Eng. Data 1990, 35 (5), 288–291.
- Teja, A. S.; Rice, P. Generalized Corresponding states Method for the Viscosities of Liquid Mixtures. 1. Ind. Eng. Chem. Fundam. 1981, 20, 77–81.
- Valeri, D.; Meirelles, A. J. A. Viscosities of Fatty Acids, Triglycerides, and Their Binary Mixtures. 10. J. Am. Oil Chem. Soc. 1997, 74, 1221–1226.

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