# Vapor-Liquid and Chemical Reaction Equilibria in the Synthesis of 2-Methoxy-2-methylbutane (TAME)

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Isobaric vapor–liquid equilibrium (VLE) data (T-x-y) for the binary systems methanol/2-methoxy-2methylbutane (TAME), methanol/2-methyl-2-butene, and methanol/2-methylbutane were obtained at 101.3 kPa. All systems showed a positive deviation from ideality with a minimum-boiling-point azeotrope. The activity coefficients were calculated with the use of the Wilson equation where the parameters of the binary systems were determined on the basis of the experimental data. Other VLE data relevant to TAME synthesis were collected from the literature, and the respective parameters were adjusted. Earlier reported results of the reaction equilibrium experiments on the liquid-phase formation of TAME were reanalyzed. On the basis of the experimental reaction equilibrium, a value of  $-109.6 \text{ kJ} \cdot \text{mol}^{-1}$  is presented for the Gibbs energy of formation for TAME in the gas phase at 298 K.

#### Introduction

Tertiary ethers are used as octane-enhancing components in gasoline. Because of the relatively high solubility of 2-methoxy-2-methylpropane (methyl *tert*-butyl ether, MTBE) in water, a search is being made for substitutes posing less threat to the environment. Possible replacements are higher ethers, for example, 2-methoxy-2-methylbutane (*tert*-amyl methyl ether, TAME). Recently, several vapor—liquid equilibria (VLEs) studies of these ethers have been published.<sup>1-4</sup>

TAME is synthesized in an acid-catalyzed equilibrium reaction of isoamylenes (2-methyl-1-butene (2M1B) and 2-methyl-2-butene (2M2B)) with methanol (MEOH).<sup>5</sup> The third equilibrium in the system is that between the isoamylene isomers, 2M1B and 2M2B. Typical side reactions are the dehydration of methanol to form methoxymethane (dimethyl ether, DME), the hydration of isoamylene to yield 2-methyl-2-butanol (*tert*-amyl alcohol, TAOH), and the dimerization of isoamylenes to form branched  $C_{10}$  alkenes (DIP).<sup>6</sup>

In our previous publication<sup>5</sup> we measured the reaction equilibrium and calculated the reaction equilibrium constants for the formation of TAME. At the temperatures investigated, the equilibrium constants, having the activities calculated by the UNIQUAC method, were found to depend on the methanol mole fraction. The equilibrium constants were higher in experiments where the mole fraction of methanol in the equilibrium was below 0.02 than they were when the methanol mole fraction was above 0.02.

The aim of the present study was to measure the VLEs for the most important binary component pairs (MEOH/ TAME, MEOH/2M2B) present in the TAME synthesis. The VLE of MEOH/IPEN (2-methylbutane, isopentane) was measured as well, because 2-methylbutane can be seen to

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represent the C<sub>5</sub>-inert in the TAME synthesis process. The available binary VLE data for 2M1B and for the side products (DME, TAOH, DIP) were taken from the literature. The parameters for the Wilson method were adjusted for our experimental data as well as for the data from the literature. The Wilson method was selected because it is particularly suitable for alcohol/hydrocarbon mixtures.<sup>7,8</sup> In the second part of the work, the results of the reaction equilibrium experiments<sup>5</sup> for the liquid-phase formation of TAME were recalculated using the Wilson method for the calculation of activity coefficients.

#### **Experimental Section**

*Materials.* The following chemicals were used in the VLE experiments: methanol (>99.95 mass %), 2-methyl-2-butene (>99.0 mass %, originating from 2-methylbutane dehydrogenation), 2-methylbutane (99.8 mass %), and TAME (>99.9 mass %, synthesized from methanol and isoamylenes). All chemicals were dried using molecular sieves. The water content was checked by the Fischer method, and it did not exceed 0.02 mass %.

**Analysis.** The samples were analyzed with a gas-liquid chromatograph LHM-80 equipped with a FID detector and a squalan capillary column (100 m, diameter 0.3 mm). The accuracy of the GC analysis was  $\pm 0.5$  mass %. The response factors of the compounds were determined with samples of known compositions.

**Apparatus.** The vapor–liquid equilibria of the binary pairs were measured in a glass still with vapor-phase circulation (modified Othmer-type still). A detailed description of the apparatus is given elsewhere.<sup>9</sup> The still was operated under atmospheric pressure for about 1.5 to 2.0 h until the conditions were stabilized and the equilibrium was reached. The samples were analyzed every 15 min until no further change was observed in the compositions. The pressure was measured with a mechanical precision barometer with an accuracy of  $\pm 0.13$  kPa, and the tem-

Table 1. Isobaric VLE Data, Temperature *T*, Liquid Phase  $x_1$  and Vapor Phase  $y_1$  Mole Fractions, and Experimental Activity Coefficients  $\gamma_i$  for Methanol (1)/TAME (2) Systems

<i>T</i> /K	<i>X</i> <sub>1</sub>	$y_1$	$\gamma_1$	Y2
337.55	100.00	100.00	1.002	
336.65	95.54	92.41	1.004	3.500
336.55	95.09	92.77	1.016	3.039
336.30	90.33	86.79	1.011	2.842
336.25	89.88	86.48	1.014	2.784
335.55	78.92	79.76	1.095	2.047
335.40	76.39	76.39	1.090	2.143
335.25	76.21	76.21	1.096	2.154
335.25	76.04	76.04	1.096	2.154
335.35	75.31	75.31	1.092	2.146
336.10	58.75	69.15	1.248	1.563
336.15	58.32	66.37	1.205	1.683
337.30	40.30	59.74	1.501	1.352
337.50	39.33	62.39	1.594	1.235
338.45	29.11	56.83	1.892	1.174
338.65	28.94	56.24	1.869	1.179
340.90	18.69	52.74	2.492	1.033
345.25	9.33	38.95	3.139	1.039
350.25	4.76	29.66	3.917	0.974
350.55	4.07	24.80	3.792	1.024
359.15	0.00	0.00		1.013

Table 2. Isobaric VLE Data, Temperature *T*, Liquid Phase  $x_1$  and Vapor Phase  $y_1$  Mole Fractions, and Experimental Activity Coefficients  $\gamma_i$  for Methanol (1)/2M2B (2) Systems

<i>T</i> /K	<i>X</i> 1	$y_1$	$\gamma_1$	γ2
337.55	100.00	100.00	1.002	
334.70	99.44	87.58	0.986	11.221
334.65	99.31	87.14	0.985	9.442
325.40	97.05	58.38	0.984	9.289
325.25	96.84	60.15	1.023	8.340
317.65	93.68	40.00	0.978	7.907
317.75	93.37	40.40	0.987	7.464
312.75	88.41	32.95	1.066	5.634
312.70	88.09	33.66	1.096	5.434
308.20	74.17	24.70	1.180	3.302
308.25	73.82	25.95	1.243	3.198
307.40	61.49	23.56	1.411	2.310
307.30	61.14	23.21	1.404	2.307
307.00	48.21	21.40	1.666	1.790
306.85	34.22	22.15	2.447	1.403
306.85	33.84	24.43	2.729	1.354
306.75	21.43	21.10	3.741	1.195
306.75	21.26	20.98	3.749	1.194
306.70	20.82	20.48	3.746	1.197
306.70	20.58	20.33	3.762	1.196
306.70	18.72	20.57	4.185	1.165
306.65	18.44	19.89	4.118	1.173
307.00	11.24	18.77	6.269	1.080
306.90	10.81	17.23	6.012	1.098
307.25	5.43	16.48	11.258	1.033
307.35	5.16	17.07	12.212	1.019
307.35	5.07	15.99	11.642	1.032
311.80	0.00	0.00		1.004

perature was measured with a mercury thermometer with an accuracy of  $\pm 0.2$  K. The description of the apparatus which was used for the reaction equilibrium measurements can be found elsewhere.<sup>5</sup>

## **Results and Discussion**

**Vapor**–*Liquid Equilibrium.* For the binary systems MEOH/TAME, MEOH/2M2B, and MEOH/IPEN, the T-x-y values were measured at atmospheric pressure. The liquid and vapor phase mole fractions of methanol along with the boiling points are presented in Tables 1–3. Figures 1–3 show the respective diagrams. The data were found to be thermodynamically consistent when they were tested by the method of Fredenslund.<sup>10</sup> Second-order Legendre poly-



**Figure 1.** Temperature–composition diagram for the methanol (1)/TAME (2) system: experimental liquid-phase mole fraction of methanol  $x_1$  ( $\Box$ ); vapor phase mole fraction of methanol  $y_1$  ( $\triangle$ ); calculated by the Wilson method (–).

Table 3. Isobaric VLE Data, Temperature *T*, Liquid Phase  $x_1$  and Vapor Phase  $y_1$  Mole Fractions, and Experimental Activity Coefficients  $\gamma_i$  for Methanol (1)/2-Methylbutane (2) Systems

	•		
<i>X</i> 1	<i>Y</i> 1	$\gamma_1$	$\gamma_2$
100.00	100.00	1.002	
97.57	43.15	0.956	13.503
97.39	44.32	0.977	12.261
93.59	27.53	1.077	9.188
93.11	28.53	1.139	8.510
86.34	18.83	1.100	5.953
85.88	16.36	0.971	5.974
76.39	16.84	1.231	3.772
61.75	16.92	1.590	2.386
61.18	15.12	1.441	2.410
50.30	14.20	1.663	1.916
35.31	14.57	2.450	1.473
35.05	15.21	2.570	1.454
24.69	14.55	3.508	1.268
14.78	14.78	5.969	1.119
14.32	14.32	5.984	1.121
14.12	14.12	5.969	1.119
14.08	14.08	5.969	1.119
10.10	12.03	7.110	1.095
9.33	12.27	7.830	1.081
4.58	11.01	14.130	1.033
4.09	12.15	17.371	1.011
0.00	0.00		1.012
	$\begin{array}{r} x_1 \\ \hline 100.00 \\ 97.57 \\ 97.39 \\ 93.59 \\ 93.11 \\ 86.34 \\ 85.88 \\ 76.39 \\ 61.75 \\ 61.18 \\ 50.30 \\ 35.31 \\ 35.05 \\ 24.69 \\ 14.78 \\ 14.32 \\ 14.12 \\ 14.08 \\ 10.10 \\ 9.33 \\ 4.58 \\ 4.09 \\ 0.00 \\ \end{array}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

nomials were obtained for the three binary systems. The mean deviations between the experimental and calculated vapor-phase mole fraction compositions were 0.0082 (MEOH/TAME), 0.0083 (MEOH/2M2B), and 0.0090 (MEOH/IPEN). The Antoine equation and the coefficients from Table 4 for TAME and the Wagner equation for MEOH, 2M2B, and 2-methylbutane<sup>7</sup> were used in the calculation of vapor pressures.

All the measured systems showed positive deviations from ideality, having a minimum-boiling-point azeotrope. The azeotropic compositions and boiling points are summarized in Table 5. The azeotropic boiling points and the mole fractions of the binary systems obtained in the experiments were in good agreement with the values found in the literature (see Table 5). The azeotropic point for MEOH/2M2B was estimated also from the results of Budantseva et al.,<sup>17</sup> the agreement with our results being satisfactory.



**Figure 2.** Temperature–composition diagram for the methanol (1)/2M2B (2) system: experimental liquid-phase mole fraction of methanol  $x_1$  ( $\Box$ ); vapor-phase mole fraction of methanol  $y_1$  ( $\triangle$ ); calculated by the Wilson method (–).



**Figure 3.** Temperature–composition diagram for the methanol (1)/isopentane (2) system: experimental liquid-phase mole fraction of methanol  $x_1$  ( $\Box$ ); vapor-phase mole fraction of methanol  $y_1$  ( $\triangle$ ); calculated by the Wilson method (–).

**Table 4. Coefficients of the Antoine Equation for TAME** 

compound	$A^a$	В	С
TAME	5.976 31 <sup>b</sup>	1208.391	-55.243

 $^a$  Equation: log  $P\left({\bf kPa}\right)=A-B/((T/{\bf K})+C).$   $^b$  Cervenkova and Boublik.  $^{11}$ 

The experimental activity coefficient of the liquid phase,  $\gamma_b$  was calculated by the following equation:

$$\frac{y_i}{x_i} = \frac{\gamma_i p_i^S \phi_i^S PF}{\phi_i^V P} \tag{1}$$

where  $x_i$  and  $y_i$  are the measured mole fractions of the liquid and vapor phases,  $\phi_i^S$  and  $\phi_i^V$  are the fugacity coefficients of the liquid and vapor phases, *PF* is the Poynting factor,  $p_i^S$  is the vapor pressure of component *i*, and *P* is the total pressure. The fugacity coefficients of the vapor and liquid phases were calculated with the Soave–Redlich–Kwong (SRK) equation of state.

Table 5. Boiling Points and Mole Fraction of Methanol,  $x_1$ , of the Azeotropes

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system	₽⁄kPa	<i>T</i> /K	<i>X</i> <sub>1</sub>
MEOH-TAME	101.3	335.25	0.7613
	101.3	335.45	0.7613 <sup>a</sup>
	101.3	335.41	$0.7710^{b}$
	101.3	335.37	0.7674 <sup>c</sup>
	101.3	335.34	$0.749^{d}$
MEOH-2M2B	101.3	306.7	0.2058
	101.3	306.25	$0.22^{e}$
	101.3	306.25	$0.216^{f}$
MEOH-IPEN	101.3	297.65	0.1432
	101.3	297.35	$0.1440^{f}$

 $^a$  Evans and Edlund.  $^{12}$   $^b$  Cervenkova and Boublik.  $^{11}$   $^c$  Palczewska-Tulinska et al.  $^{13}$   $^d$  Arce et al.  $^{14}$   $^e$  Kudryavtseva et al.  $^{15}$   $^f$  Ogorodnikov et al.  $^{16}$ 

The activity coefficients were calculated by the Wilson method.<sup>18</sup> The molar volume for each component was estimated from the density and molar mass. The adjustable parameters in the Wilson method are the differences in the parameters  $\lambda_{ij}$  and  $\lambda_{ii}$  for each binary component pair. The program VLEFIT was used in the optimization.<sup>19</sup> The differences ( $\lambda_{ij} - \lambda_{ij}$ ) were adjusted for the T-x-y or P-x-y data by using the Davidon method to minimize the objective function:

$$OF = (\gamma_{L}^{meas} - \gamma_{L}^{calc})^{2}$$
(2)

For the sets of isothermic P-x data, the differences between measured and calculated total pressures were minimized as follows:

$$OF = (P^{meas} - P^{calc})^2$$
(3)

The lines in Figures 1-3 represent vapor-phase mole fractions calculated by the Wilson method using the parameters obtained in the optimization. As can be seen, the method describes the activities of the studied systems well.

The Wilson parameters  $(\lambda_{ij} - \lambda_{ii})$  obtained for MEOH/ 2M2B, MEOH/TAME, and MEOH/IPEN are summarized in Table 6. To be able to calculate the component activities for the reaction equilibrium results in the next section, the parameters for the other compounds present in the TAME synthesis are included. T-x-y type data were available for MEOH/2M1B<sup>16</sup> and MEOH/DIP;<sup>20</sup> P-x-y type data were available for MEOH/DME<sup>21</sup> and TAME/DIP;<sup>22</sup> and P-x type data were available for MEOH/TAOH.<sup>23</sup> For 2M1B/TAME, 2M2B/TAME, and TAME/IPEN, P-x type data of TAME/pentane<sup>24</sup> and, for 2M1B/TAOH, 2M2B/ TAOH, and TAOH/IPEN, P-x type data of TAOH/pentane<sup>24</sup> were used. The parameters for the nearly ideal binary pair 2M1B/2M2B, 2M1B/IPEN, or 2M2B/IPEN are based on P-x type data of *n*-pentane/2M2B.<sup>25</sup> For some component pairs (e.g. TAME/DME, 2M2B/DME, 2M2B/ DIP), no VLE data were found, and ideal behavior between the components was assumed. The Wilson parameters were adjusted for the above data and are summarized in Table 6.

**Chemical Reaction Equilibrium.** The equilibrium constants for the reactions of MEOH and 2M1B to TAME (R1) and of MEOH and 2M2B to TAME (R2) are the following:

R*i*: 
$$K_{ai} = \frac{\alpha_{TAME}}{\alpha_{MeOH}\alpha_{2M/B}} = \frac{\gamma_{TAME}}{\gamma_{MEOH}\gamma_{2M/B}} \frac{X_{TAME}}{X_{MEOH}X_{2M/B}}$$
 (4)

For isomerization of 2M1B to 2M2B, the equilibrium

Table 6.	Wilson	<b>Parameters</b>	$(\lambda_{ii} -$	$\lambda_{ii}$ )/J·mol <sup>-1</sup>
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i	MEOH	2M1B	2M2B	TAME	DME	TAOH	DIP	IPEN
MEOH	0.0	12510.2	9030.9	6556.5	4630.6	104.7	11216.4	9822.2
2M1B	935.7	0.0	-94.2	584.9		85.8		-94.2
2M2B	1490.9	504.9	0.0	584.9		85.8		-94.2
TAME	-1660.9	-218.1	-218.1	0.0		-775.3	-432.1	-218.1
DME	-701.7				0.0			
TAOH	528.4	3479.2	3479.2	3509.9		0.0		3479.2
DIP	1658.0			1150.1			0.0	
IPEN	2221.9	504.9	504.9	584.9		85.8		0.0

 Table 7. Experimental Reaction Conditions (Initial Mole Ratio of Methanol/Isoamylene, Temperature), Mole Fractions of Methanol (1), 2-Methyl-1-butene (2), 2-Methyl-2-butene (3), TAME (4), Dimethyl Ether (5), *tert*-Amyl Alcohol (6), and Diisopentane (7) in Equilibrium, Acitivity Coefficients by Wilson for Methanol (1), 2-Methyl-1-butene (2), 2-Methyl-2-butene (3), and TAME (4), and the Reaction Equilibrium Constants

init ratio	Т	<i>X</i> <sub>1</sub>	<i>X</i> <sub>2</sub>	<i>X</i> 3	<i>X</i> 4	<i>X</i> 5	X <sub>6</sub>	<i>X</i> <sub>7</sub>	γ1	Y2	γ3	$\gamma_4$	K <sub>a1</sub>	$K_{a2}$
а	323	0.195	0.015	0.166	0.604	0.009	0.010	0.001	2.629	1.416	1.351	1.069	59.14	5.62
1.0	323	0.202	0.014	0.152	0.618	0.000	0.013	0.000	2.530	1.436	1.373	1.077	64.72	6.23
а	333	0.220	0.019	0.194	0.557	0.000	0.010	0.000	2.471	1.448	1.371	1.076	39.90	4.15
0.1	333	0.003	0.071	0.736	0.133	0.000	0.013	0.045	12.853	1.103	1.008	1.092	55.91	5.86
0.5	333	0.047	0.041	0.416	0.481	0.000	0.014	0.001	5.505	1.154	1.083	1.013	39.60	4.15
1.0	333	0.221	0.021	0.187	0.560	0.000	0.011	0.000	2.444	1.452	1.377	1.079	36.78	4.33
2.5	333	0.636	0.005	0.054	0.298	0.001	0.005	0.000	1.190	3.082	3.012	1.710	41.33	4.14
5.0	333	0.794	0.003	0.026	0.174	0.001	0.003	0.000	1.059	4.646	4.696	2.241	37.28	3.84
10	333	0.900	0.001	0.011	0.085	0.001	0.001	0.000	1.014	6.571	6.906	2.802	37.97	3.38
а	343	0.242	0.023	0.207	0.510	0.000	0.018	0.000	2.280	1.482	1.399	1.092	30.12	3.49
1.0	343	0.271	0.021	0.204	0.491	0.003	0.009	0.001	2.173	1.537	1.447	1.105	27.99	3.13
а	353	0.267	0.029	0.247	0.447	0.002	0.007	0.001	2.243	1.505	1.405	1.085	18.64	2.34
0.1	353	0.007	0.072	0.646	0.127	0.000	0.012	0.135	11.430	1.080	1.005	1.089	23.32	2.81
0.13	353	0.011	0.071	0.634	0.172	0.004	0.010	0.097	10.352	1.088	1.010	1.072	20.94	2.53
0.5	353	0.080	0.051	0.447	0.403	0.004	0.011	0.004	4.663	1.181	1.098	1.008	18.02	2.22
1.0	353	0.274	0.027	0.243	0.446	0.001	0.008	0.000	2.192	1.523	1.422	1.093	19.38	2.35
2.5	353	0.634	0.009	0.081	0.268	0.004	0.004	0.000	1.207	2.943	2.829	1.639	20.75	2.50
5.0	353	0.804	0.005	0.038	0.147	0.004	0.002	0.000	1.058	4.599	4.577	2.206	18.36	2.16
10	353	0.900	0.002	0.017	0.078	0.003	0.001	0.000	1.016	6.332	6.525	2.729	18.97	2.16
а	363	0.290	0.032	0.257	0.400	0.009	0.011	0.001	2.109	1.541	1.433	1.098	14.70	1.95

<sup>a</sup> Initial feed TAME.

constant can be calculated from  $K_{a1}$  and  $K_{a2}$ ,

R3: 
$$K_{a3} = \frac{a_{2M2B}}{a_{2M1B}} = \frac{K_{a1}}{K_{a2}}$$
 (5)

The mole fractions of the main components MEOH, 2M1B, 2M2B, and TAME in the equilibrium measurements were reported earlier.<sup>5</sup> To allow a closer analysis, Table 7 presents the results of the equilibrium measurements in detail, including the mole fractions of the side products DME, TAOH, and DIP. The Wilson method using the parameters  $(\lambda_{ij} - \lambda_{ii})$  from Table 6 was used in the calculation of the activity coefficients for MEOH, 2M1B, 2M2B, and TAME in a multicomponent system. The mole fractions of the side products (Table 7) and the respective Wilson parameters in Table 6 were included in the calculation. The effect of the side products on the activity of methanol was significant in experiments where the methanol mole fraction was low. In the case when the methanol activity is high (over 10), it is sensitive to the mole fractions of the other compounds present in the system or to the parameters  $(\lambda_{ij} - \lambda_{ii})$  used in the calculation. In Table 7 the activity coefficients and equilibrium constants  $K_{a1}$  and  $K_{a2}$  for each experiment are presented. After applying the *r*-criterion<sup>26</sup> to the experimental data, the equilibrium constants calculated from the experiment with the methanol equilibrium mole fraction 0.003 at 333 K were omitted. At 333 K the average equilibrium constant  $K_{a1}$  by the Wilson method was 38.8 with standard deviation 1.72 and  $K_{a2}$  was 4.00 with standard deviation 0.3. For comparison,

the respective equilibrium constants by the UNIQUAC method were 44.7 ( $K_{a1}$ ) and 4.3 ( $K_{a2}$ ) with standard deviations of 4.0 and 0.2.

Parts a and b of Figure 4 show the reaction equilibrium constants  $K_{a1}$  and  $K_{a2}$  obtained by the Wilson method as a function of methanol mole fraction at equilibrium. For comparison, the equilibrium constants calculated by the UNIQUAC<sup>5</sup> method are included. As can be seen, at MEOH mole fractions above 0.05, the equilibrium constants obtained by the Wilson method are on the same level as the values obtained by the UNIQUAC method. At the point where the methanol mole fraction was 0.0026 (at 333 K), the equilibrium constants calculated with the Wilson method were closer to the average than the ones calculated with the UNIQUAC method. Our results reinforce the view of the Wilson method being a good estimation method for hydrocarbon/alcohol mixtures.<sup>7.8</sup>

*Equilibrium Constants.* The equilibrium constant  $K_a$  at temperature *T* is defined by the equation

$$K_{\rm a} \equiv \exp\left(\frac{-\Delta G_{\rm R}^{\rm L}(T)}{RT}\right) = \prod_{i=1}^{N} a_i^{\rm v}$$
(6)

where  $-\Delta G_{\rm R}^{\rm L}(T)$  is the Gibbs energy change for the liquidphase reaction at the temperature *T*. We wanted to calculate the respective value for the Gibbs energy change of TAME formation in the liquid phase at 298 K,  $\Delta G_{\rm TAME}^{\rm L}$ , and the corresponding value in the gas phase,  $\Delta G_{\rm TAME}^{\rm C}$ , that would agree with our experimental results. From the Gibbs–Helmholtz equation the temperature dependence of

quantity	units	MEOH	2M1B	2M2B	TAME
$\Delta H_i$ (gas) <sup>a</sup>	kJ⋅mol <sup>-1</sup>	$-201.3^{\circ}$	$-36.34^{\circ}$	$-42.58^{\circ}$	$-305.4^{h}$
$\Delta G_i(gas)^a$	kJ∙mol <sup>−1</sup>	$-162.6^{\circ}$	65.65 <sup>c</sup>	59.7 <sup>c</sup>	
$\Delta H_i(\text{vap})^a$	$kJ\cdot mol^{-1}$	$37.53^{d}$	$25.8^{f}$	$27.1^{f}$	$35.3^{h}$
T <sub>c</sub>	K	512.6 <sup>c</sup>	465 <sup>c</sup>	470 <sup>c</sup>	$531.2^{i}$
$P_{\rm c}$	kPa	8090 <sup>c</sup>	3450 <sup>c</sup>	3450 <sup>c</sup>	$3250^{i}$
ω		$0.556^{c}$	0.236 <sup>c</sup>	0.244 <sup>c</sup>	$0.246^{i}$
$c_{\rm p}({\rm lig})^a$	kJ⋅mol <sup>-1</sup> ⋅K <sup>-1</sup>	$0.0816^{d}$	$0.1569^{d}$	$0.1523^{d}$	0.2192 <sup>g</sup>
$c_{\rm p}({\rm lig})^b$	$a imes 10^2$	$10.76^{e}$	14.951 <sup>e</sup>	$15.4^{e}$	$7.83^{e}$
1 .	$b imes 10^5$	$-38.06^{e}$	$-24.763^{e}$	$-29.335^{e}$	$44.92^{e}$
	$c  imes 10^7$	$9.79^{e}$	$9.1849^{e}$	$9.794^{e}$	

<sup>*a*</sup> At 298.15 K. <sup>*b*</sup> The equation of temperature dependence for  $c_p = a + bT + cT^2$ . <sup>*c*</sup> Reid et al., 1988.<sup>7</sup> <sup>*d*</sup> CRC, 1983.<sup>27</sup> <sup>*e*</sup> Daubert and Danner, 1992.<sup>28</sup> <sup>*f*</sup> Smith and Srivastava, 1986.<sup>29</sup> <sup>*g*</sup> TRC, 1986.<sup>30</sup> <sup>*h*</sup> Rozhnov et al., 1991.<sup>31</sup> <sup>*i*</sup> Palczewska-Tulinska et al., 1990.<sup>13</sup>



**Figure 4.** (a)  $K_{a1}$  as a function of MEOH mole fraction x in the equilibrium state:  $K_{a1}$  at 333 K ( $\blacktriangle$ ) and at 353 K ( $\blacksquare$ ) calculated by the Wilson method;  $K_{a1}$  at 333 K ( $\triangle$ ) and at 353 K ( $\square$ ) calculated by UNIQUAC method taken from Rihko et al.<sup>5</sup> (b)  $K_{a2}$  as a function of MEOH mole fraction x in the equilibrium state:  $K_{a2}$  at 333 K ( $\bigtriangleup$ ) and at 353 K ( $\blacksquare$ ) calculated by the Wilson method;  $K_{a2}$  at 333 K ( $\triangle$ ) and at 353 K ( $\blacksquare$ ) calculated by the UNIQUAC method taken from Rihko et al.<sup>5</sup>

the equilibrium constants is derived

$$\ln \frac{K_{\rm a}}{K_{\rm a0}} = \int_{T_0}^{T} \frac{\Delta H_{\rm R}^{\rm L}(T)}{RT^2} \, {\rm d} \, T \tag{7}$$

The  $\Delta H_{\rm R}^{\rm L}(T)$  was calculated with the  $\Delta H_i^{\rm G}(298 \text{ K})$ , the heat of vaporization,  $\Delta H_i^{\rm VAP}(298 \text{ K})$ , and the liquid-phase

heat capacities of each compound (Table 8). The experimental  $K_{\rm ai}$  values at 323 to 363 K were compared to the values that were calculated with eqs 6 and 7. The  $\Delta G_{\rm TAME}^{\rm L}$ was adjusted minimizing the difference between the experimental equilibrium constants and the ones from thermodynamic data.

The gas-phase Gibbs energies  $\Delta G_i^{\text{G}}$  for the formation of TAME were calculated from the liquid-phase values  $\Delta G_i^{\text{L}}$  by the equation

$$\Delta G_i^{\rm G} = \Delta G_i^{\rm L} - RT \ln \left( \frac{\phi_i^{\rm s} p_i^{\rm s} PF}{P} \right) \tag{8}$$

where  $\phi_i^s$  is the component fugacity coefficient at the vapor pressure  $p_i^s$  of component *i* and *P* is the atmospheric pressure. The Poynting factor, *PF*, was assumed to have a value of 1 under these conditions. The fugacity coefficients were calculated with the SRK equation of state using the critical temperatures and acentric factors for the components from Table 8. A value of  $-115.5 \pm 0.1 \text{ kJ} \cdot \text{mol}^{-1}$  was obtained for  $\Delta G_{\text{TAME}}^{\text{L}}$ , corresponding by eq 7 to a gas-phase value  $\Delta G_{\text{TAME}}^{\text{G}}$  of  $-109.6 \pm 0.1 \text{ kJ} \cdot \text{mol}^{-1}$  at 298 K.

Our experimental value of  $\Delta G_{\text{TAME}}^{\text{G}}$  is 5.4% lower than the value  $-104.0 \text{ kJ} \cdot \text{mol}^{-1}$  reported in the literature.<sup>30</sup> Our value for  $\Delta G_{\text{TAME}}^{\text{L}}$  agrees with the values -114.65kJ·mol<sup>-1</sup> <sup>32</sup> and with the value  $-113.8 \text{ kJ} \cdot \text{mol}^{-1}$ , published recently by Syed et al. (2000).<sup>33</sup> The differences are likely due to the different thermodynamic data used in the calculation.

#### Conclusions

The isobaric vapor-liquid equilibrium data (T-x-y) were measured for three binary mixtures: methanol/2-methoxy-2-methylbutane (TAME), methanol/2-methyl-2-butene, and methanol/2-methylbutane. On the basis of experimental findings, we adjusted the binary parameters for the Wilson method of activity coefficient estimation. The reaction equilibrium constants were recalculated for the liquid-phase synthesis of TAME by using the Wilson method. The nonideality was well described with the Wilson method, and the equilibrium constants remained more invariable than those calculated earlier with the UNIQUAC method. On the basis of the experimental equilibrium results, a value of  $-109.6 \text{ kJ} \cdot \text{mol}^{-1}$  is proposed for the formation of TAME in the gas phase,  $\Delta G_{\text{TAME}}^{\text{G}}$ , at 298 K.

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Received for review September 8, 1999. Accepted July 10, 2000.

JE990245V