

# Thermodynamic Properties of Aqueous Poly(vinylpyrrolidone) Solutions from Laser-Light-Scattering, Membrane Osmometry, and Isopiestic Measurements

Hans-Peter Kany,<sup>†</sup> Hans Hasse,<sup>‡</sup> and Gerd Maurer\*

Lehrstuhl für Technische Thermodynamik, Universität Kaiserslautern, D-67653 Kaiserslautern, Germany

Thermodynamic properties of poly(vinylpyrrolidone) (PVP) were studied by laser-light-scattering, membrane osmometry, and isopiestic measurements. Four polymer samples of weight-average molecular mass between about 9000 and 1 200 000 were investigated at temperatures from (278 to 333) K. The experimental results are described with application of the osmotic virial equation and compared to literature data.

## Introduction

In previous work thermodynamic properties of aqueous solutions of poly(ethylene glycol) (PEG)<sup>1</sup> and of dextran (DEX)<sup>2</sup> were investigated by laser-light-scattering, membrane osmometry, and isopiestic measurements. With the present contribution this work is extended to aqueous solutions of poly(vinylpyrrolidone) (PVP). Figure 1 shows the structural formula of PVP. Despite the importance of aqueous solutions of PVP, only a few experimental investigations of their thermodynamic properties have been carried out before. Table 1 gives a survey of that literature data. Most of the experimental work has been limited to 298 K and has been given in graphical form or as correlations. Only Vink<sup>3</sup> reported numerical data. In the present study, as in our previous work on PEG and DEX solutions, three different methods were applied: laser-light-scattering, membrane osmometry, and isopiestic measurements. The experimental results are presented together with the second and third osmotic virial coefficients of PVP(aq) which were determined by simultaneously evaluating the experimental data with an expanded osmotic virial equation.

## Experimental Section

The experimental methods applied in the present studies are similar to those used in previous investigations on aqueous solutions of PEG<sup>1</sup> and of DEX.<sup>2</sup> Experimental details described in these earlier publications are not repeated here.

**Materials.** Aqueous solutions of four different PVP samples were investigated. All samples were described by the suppliers as non-cross-linked PVP. Two samples were from BASF, AG, Ludwigshafen, Germany [PVP 10 (producer's nomenclature PVP 17PF) and PVP 1000 (producer's nomenclature PVP 90F)], one was from Aldrich, Steinheim, Germany [PVP 50 (producer's nomenclature PVP K30)], and one from Fluka, Neu-Ulm, Germany [PVP 1000FL

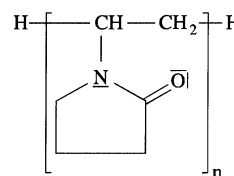


Figure 1. Structure of poly(1-vinyl-2-pyrrolidone).

Table 1. Previous Experimental Work on Aqueous Solutions of Poly(pyrrolidone)

exp method	molecular mass	<i>T</i> /K	ref
membrane osmometry	$1.6 \times 10^5, 1.2 \times 10^6$	295	11
	$1.1 \times 10^4, 2.3 \times 10^4$	298	15
	$1.2 \times 10^4$ to $7.5 \times 10^4$ <sup>a</sup>	298	10
	$5 \times 10^4, 10^6$	298	3 <sup>c</sup>
	$10^5$ <sup>b</sup>	298	16
light-scattering	$7.5 \times 10^5$	283, 293, 303, 313, 323	17
	$1.1 \times 10^4$	298	15
sedimentation	$2.3 \times 10^4, 3.8 \times 10^5$	298	15

<sup>a</sup> 10 samples. <sup>b</sup> 15 samples. <sup>c</sup> Numerical data reported.

(producer's nomenclature PVP K90)]. The number following the abbreviation PVP gives the approximate weight-average molecular mass (e.g., PVP 10:  $M_w \approx 10\,000$ ). All polymer samples were furthermore characterized with a gel permeation chromatograph (GPC) coupled with a multiangle laser-light-scattering photometer and an interferometric refractometer. Experimental details were similar to those described for DEX samples by Kany et al.<sup>2</sup> The numerical results have been reported by Kany.<sup>4</sup> Figure 2 gives the differential molecular weight distributions  $d\xi/d \log M$ . The results for the molecular mass distribution were evaluated to determine the number-average molecular mass  $M_n$  and the weight-average molecular mass  $M_w$  (cf. Table 2 and the explanation below). The ratio of  $M_w$  to  $M_n$  is called the polydispersity  $P$ . The polydispersities of the samples varied between 1.8 (PVP 10) and 9.32 (PVP 1000FL). The rather large numbers for the polydispersities of the high molecular weight PVP samples reveal their broad molecular mass distributions.

HPLC water (Merck, Darmstadt, Germany; impurities below 5 mg/kg) was used for the preparation of all aqueous solutions. Table 3 gives a survey of the experimental work.

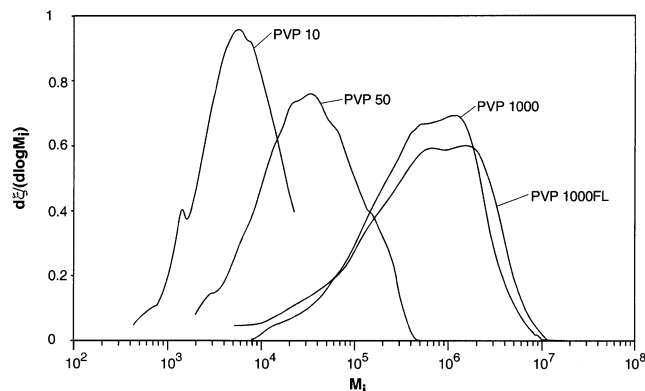
\* To whom all correspondence should be addressed. Fax: +49 631 205 3835. E-mail: gmaurer@rhrk.uni-kl.de.

<sup>†</sup> Present address: Großhandels- und Lagerei-Berufsgenossenschaft, M 5,7 D-68161 Mannheim, Germany.

<sup>‡</sup> Present address: Institut für Technische Thermodynamik und Thermische, Verfahrenstechnik, Universität Stuttgart, D-70550 Stuttgart, Germany.

**Table 2. Poly(pyrrolidone) Samples**

abbrev	supplier's abbrev	supplier	supplier's charge no.	$M_w$			$M_n$		
				GPC	LLS + ISO + MO		GPC	LLS + ISO + MO	
					method I	method II		method I	method II
PVP 10	PVP 17PF	BASF	93-0024	9 411	9 377	8 894	3 882	4 856	4 606
PVP 50	PVP K30	Aldrich	73-095	57 980	54 090	48 480	17 750	22 690	22 610
PVP 1000	PVP 90F	BASF	73-3990	973 500	1 045 600	1 189 300	210 400	162 900	169 400
PVP 1000FL	PVP K90	Fluka	336382/1495	1 146 000	1 028 000	1 171 000	138 600	125 600	127 000

**Figure 2.** Differential molecular weight distribution of poly(vinylpyrrolidone) samples from gel permeation chromatography.**Table 3. Survey of the Experimental Work**

polymer	$T/K$	polymer mass fraction ( $100\xi_s/g\cdot g^{-1}$ )			
		LLS	MO	ISO	density
PVP 10	278	0.40–5.1		35–42	0.50–30
	293	0.30–1.5		25–40	1.2–37
	333	0.38–4.8		44–54	1.2–37
PVP 50	278	0.40–1.5		38–42	0.61–29
	293	0.81–2.0		26–40	0.10–39
	303		0.52–2.8		
PVP 1000	333	0.40–1.0		45–54	0.10–39
	278	0.017–0.17			0.51–4.8
	293	0.015–0.14			0.61–20
PVP 1000FL	303		2.0–4.0		
	333	0.032–0.12	0.63–2.1		0.61–9.5
	278	0.0092–0.16			
PVP 1000FL	293	0.020–0.15			
	303		0.48–3.9		
	333	0.033–0.12	0.58–3.0		

**Laser-Light-Scattering.** Laser-light-scattering experiments were performed with aqueous solutions of all PVP samples at temperatures between (278 and 333) K and polymer mass fractions of about (0.3 to 5) mass % (for PVP 10) and (0.015 to 0.17) mass % (for PVP 1000). The experimental results are given in Tables 4–6. The uncertainty of these investigations was checked by repeating some experiments, as indicated, for example, in Table 5.

**Membrane Osmometry.** Membrane osmometry experiments were carried out with commercially available equipment (membrane osmometer type Osmomat 090, Gonotec, Berlin, Germany). Experiments could not be carried out for the low molecular weight PVPs due to the lack of suitable membranes. With the exception of a single data point, the experimental results for the osmotic pressure could be reproduced within  $\pm 5\%$ , which is also the estimated experimental uncertainty. The experimental results are given in Tables 7 and 8.

**Isopiestic Method.** The apparatuses and the experimental procedures used for the isopiestic investigations have been described before.<sup>5</sup> Isopiestic investigations were performed with aqueous solutions of PVP 10 and PVP 50 at polymer mass fractions up to about 50%. Experimental

work was not possible for the high molecular weight PVPs, as the aqueous solutions were too viscous and equilibration could not be achieved within a reasonable period of time. The experimental results are summarized in Table 9. The maximum uncertainty of that data is  $\pm 0.1$  K in temperature,  $\pm 0.002$   $g\cdot g^{-1}$  in polymer concentration, and  $\pm 0.001$  in water activity.

**Density.** For the conversion of polymer mass fractions  $\xi_s (=m_s/(m_s + m_w))$  into mass density  $c_s (=m_s/V)$ , the specific density  $\rho^* (= (m_s + m_w)/V)$  of the aqueous PVP solution has to be known:

$$c_s = \rho^* \xi_s$$

The specific densities of the aqueous solutions of PVP 10, PVP 50, and PVP 1000 were measured at (278, 293, and 333) K with a vibrating tube densimeter. The experimental results are given in Table 10.

## Correlation

**Model.** The osmotic virial equation is used to describe the thermodynamic properties of aqueous solutions of PVP in a similar way as it was used before for describing aqueous solutions of PEG<sup>1</sup> and DEX,<sup>2</sup> respectively. For a better understanding, the basic ideas are repeated here. It is common practice to use that equation also for solutions of polydisperse polymers, but neglecting any polydispersity. However, this can result in serious deficiencies when the osmotic virial coefficients depend on the polymer molecular mass. In the present work two different evaluations of the experimental data (from light-scattering, membrane osmometry, and isopiestic measurements) were applied. In one evaluation, the influence of polydispersity on the osmotic virial coefficients is taken into account (method I) whereas, in the other one (method II), it is neglected. The polydispersity of the polymer samples was approximated by assuming that the polydisperse polymer consists of ( $i = 2, \dots, N$ ), that is, ( $N - 1$ ), monodisperse polymers. The distribution is characterized by the mass fraction  $\xi_i$  of (each) monodisperse polymer in the polydisperse polymer sample. The osmotic virial equation is based on a Taylor series expansion of the activity coefficients of the solutes,  $\ln \gamma_i$ , in concentration  $c_i$ , that is, mass of polymer per volume, around the ideal solution ( $\ln \gamma_i = 0$  at  $c_i = 0$  in pure solvent), where the chemical potential  $\mu_i$  of solute  $i$  is normalized according to Henry's law ( $c_i \rightarrow 0$  for interactions and  $c_i \rightarrow 1$   $g\cdot cm^{-3}$  for concentration, both in pure solvent):

$$\ln \gamma_i = \sum_{j=2}^N \left( \frac{\partial \ln \gamma_i}{\partial c_j} \right)_{\text{pure solvent}} c_j + \frac{1}{2} \sum_{j=2}^N \sum_{k=2}^N \left( \frac{\partial^2 \ln \gamma_i}{\partial c_j \partial c_k} \right)_{\text{pure solvent}} c_j c_k + \dots \quad (1)$$

Introducing abbreviations for partial derivatives similar to

**Table 4. Experimental Results for the Excess Rayleigh Ratio at 278.15 K**

$100c_s/\text{g}\cdot\text{cm}^{-3}$	$10^4(Kc_s/R_\Theta^E)/\text{mol}\cdot\text{g}^{-1}$										
	$\Theta = 44.5^\circ$	$\Theta = 54.0^\circ$	$\Theta = 64.9^\circ$	$\Theta = 77.1^\circ$	$\Theta = 90.0^\circ$	$\Theta = 102.9^\circ$	$\Theta = 115.1^\circ$	$\Theta = 126.0^\circ$	$\Theta = 135.5^\circ$	$\Theta = 143.8^\circ$	$\Theta = 151.3^\circ$
PVP 10											
0.403	1.1079	1.1114		1.1009	1.0906		1.0975	1.0739	1.0839		
0.758	1.2038	1.2038		1.1907	1.1738		1.1822	1.1634	1.1696		
1.50	1.3804	1.3789		1.3616	1.3392		1.3489	1.3365	1.3365		
2.27	1.5751	1.5763		1.5564	1.5299		1.5406	1.5299	1.5275		
3.03	1.7845	1.7821		1.7607	1.7272		1.7409	1.7317	1.7294		
3.72	1.9826	1.9826		1.9574	1.9190		1.9339	1.9190	1.9032		
4.56	2.2495	2.2495		2.2192	2.1778		2.1934	2.1826	2.1778		
5.07	2.3859	2.3872		2.3616	2.3193		2.3390	2.3291	2.3267		
PVP 50											
0.400	2.1665	2.1651		2.1387	2.1143		2.1076	2.0865	2.0710	2.0697	2.0506
0.400	2.2228	2.2213		2.1764	2.1567		2.1401	2.1103	2.1010	2.0891	2.0839
0.604	2.5237	2.5148		2.4692	2.4369		2.4229	2.3918	2.3782	2.3771	2.3682
0.604	2.4986	2.5073		2.4560	2.4287		2.4078	2.3715	2.3626	2.3494	2.3374
0.800	2.7579	2.7499		2.7009	2.6621		2.6462	2.6120	2.5947	2.5917	2.5777
0.800	2.7218	2.7218		2.6642	2.6358		2.6079	2.5678	2.5599	2.5404	2.5317
1.00	3.1255	3.1231		3.0634	3.0158		2.9984	2.9580	2.9340	2.9392	2.9084
1.00	3.0691	3.0668		3.0006	2.9664		2.9361	2.8873	2.8714	2.8362	2.7214
1.50	3.7798	3.7912		3.7168	3.6721		3.6384	3.5592	3.5211	3.4693	3.1622
PVP 1000											
0.0149	1.0428	1.0955	1.1527	1.2736	1.3265	1.3968	1.4857	1.5306	1.5804	1.5521	
0.0284	1.0933	1.1436	1.2012	1.3228	1.3730	1.4423	1.5311	1.5749	1.6235	1.6022	
0.0546	1.2031	1.2529	1.3155	1.4399	1.4821	1.5481	1.6358	1.6778	1.7246	1.7015	
0.0546	1.2129	1.2636	1.3214	1.4488	1.4941	1.5601	1.6504	1.6918	1.7408	1.7186	
0.0837	1.3588	1.4064	1.4673	1.6017	1.6359	1.7012	1.7872	1.8280	1.8752	1.8513	
0.0837	1.3518	1.3986	1.4569	1.5920	1.6288	1.6944	1.7826	1.8221	1.8727	1.8453	
0.112	1.5009	1.5480	1.6088	1.7505	1.7778	1.8438	1.9293	1.9667	2.0181	1.9851	
0.112	1.5105	1.5580	1.6148	1.7573	1.7879	1.8507	1.9392	1.9770	2.0311	1.9977	
0.140	1.6540	1.7486	1.7567	1.9062	1.9274	1.9900	2.0777	2.1131	2.1657	2.1289	
0.140	1.6555	1.7546	1.7638	1.9126	1.9327	1.9949	2.0811	2.1159	2.1682	2.1246	
PVP 1000FL											
0.00920	0.9916		1.1304	1.2391	1.3432	1.4272	1.5311	1.5952			
0.0169	0.9484		1.1147	1.2379	1.3569	1.4507	1.5602	1.6294			
0.0323	1.1443		1.2931	1.4072	1.5159	1.6016	1.7057	1.7725			
0.0457	1.1798		1.3331	1.4494	1.5630	1.6500	1.7574	1.8245			
0.0654	1.3566		1.4967	1.6076	1.7149	1.7968	1.9014	1.9693			
0.0817	1.4367		1.5832	1.6963	1.8064	1.8881	1.9953	2.0638			
0.121	1.7012		1.8431	1.9556	2.0647	2.1443	2.2533	2.3225			
0.162	1.9965		2.1333	2.2434	2.3494	2.4239	2.5334	2.6032			

those for a binary system

$$a_{ij} = \left( \frac{\partial \ln \gamma_i}{\partial c_j} \right)_{\text{pure solvent}} \quad (2)$$

$$a_{ijk} = \left( \frac{\partial^2 \ln \gamma_i}{\partial c_j \partial c_k} \right)_{\text{pure solvent}} \quad (3)$$

leads to the osmotic virial equation for the activity coefficient of the polydisperse polymer  $i$

$$\ln \gamma_i = \sum_{j=2}^N a_{ij} c_j + \frac{1}{2} \sum_{j=2}^N \sum_{k=2}^N a_{ijk} c_j c_k + \dots \quad (4)$$

The activity of the solvent follows from an integration of the Gibbs–Duhem equation, taking into account the symmetry of the virial coefficients as well as assuming  $\rho_{\text{solution}} \approx \rho_{\text{pure solvent}}$ :

$$\ln a_1 = - \frac{c_s}{\rho_1} \left( \frac{1}{M_n} + A_2^{\text{osm}} c_s + A_3^{\text{osm}} c_s^2 + \dots \right) \quad (5)$$

where

$$A_2^{\text{osm}} = \sum_{i=2}^N \sum_{j=2}^N \xi_i \xi_j A_{ij} \quad (6)$$

$$A_3^{\text{osm}} = \sum_{i=2}^N \sum_{j=2}^N \sum_{k=2}^N \xi_i \xi_j \xi_k A_{ijk} \quad (7)$$

$$c_s = \sum_{i=2}^N c_i \quad (8)$$

$c_s$  is the total concentration of the polymer.  $A_2^{\text{osm}}$  and  $A_3^{\text{osm}}$  are the second and third osmotic virial coefficients of the polydisperse polymer in the solvent, respectively. The mixed virial coefficients  $A_{ij}$  and  $A_{ijk}$  ( $i \neq j \neq k$ ) are directly related to the partial derivatives in eqs 2 and 3:

$$A_{ij} = \frac{a_{ij}}{2M_{n,i}} \quad (9)$$

$$A_{ijk} = \frac{a_{ijk}}{3M_{n,i}} \quad (10)$$

$M_n$  is the number-average molecular mass of the polydis-

**Table 5. Experimental Results for the Excess Rayleigh Ratio at 293.15 K**

$100c_s/\text{g}\cdot\text{cm}^{-3}$	$10^4(Kc_s/R_\Theta^E)/\text{mol}\cdot\text{g}^{-1}$											
	$\Theta = 36.2^\circ$	$\Theta = 44.5^\circ$	$\Theta = 54.0^\circ$	$\Theta = 64.9^\circ$	$\Theta = 77.1^\circ$	$\Theta = 90.0^\circ$	$\Theta = 102.9^\circ$	$\Theta = 115.1^\circ$	$\Theta = 126.0^\circ$	$\Theta = 135.5^\circ$	$\Theta = 143.8^\circ$	$\Theta = 151.3^\circ$
PVP 10												
0.304	1.1839	1.1320	1.1270	1.1029	1.1173	1.1124	1.1077	1.0754	1.1029			
0.611	1.2063	1.1709	1.1579	1.1502	1.1579	1.1527	1.1527	1.1131	1.1502			
0.611	0.6728	0.9787	1.0151	1.1037	1.1228	1.1179	1.1228	1.0852	1.0608			
0.899	1.2330	1.2095	1.2019	1.2000	1.2076	1.2038	1.2019	1.1925	1.2038			
0.899	0.8000	1.0648	1.0985	1.1622	1.1801	1.1711	1.1783	1.1379	1.1362			
1.20	1.2687	1.2454	1.2409	1.2409	1.2485	1.2454	1.2439	1.2319	1.2470			
1.20	0.8937	1.1383	1.1577	1.2186	1.2319	1.2186	1.2304	1.1750	1.1915			
1.50	1.3251	1.3101	1.3074	1.3034	1.3088	1.3034	1.3048	1.2928	1.3048			
1.50	0.9773	1.2082	1.2257	1.2773	1.2902	1.2811	1.2902	1.2621	1.2559			
PVP 50												
0.404		2.2434	2.2465	2.1357	2.2572	2.2388	2.2697	2.2373	2.2728	2.2886		
0.617		2.4931	2.5006	2.4003	2.5144	2.4993	2.5257	2.4981	2.5207	2.5295		
0.809		2.7154	2.7232	2.7368	2.7459	2.7459	2.7551	2.7402	2.7459	2.7551		
0.809		2.7482	2.7505	2.6552	2.7655	2.7471	2.7737	2.7448	2.7784	2.7621		
1.01		3.0017	3.0061	3.0171	3.0249	3.0271	3.0360	3.0160	3.0338	3.0484		
1.01		3.0260	3.0304	2.9353	3.0461	3.0293	3.0552	3.0260	3.0586	3.0405		
1.51		3.6961	3.7129	3.7219	3.7365	3.7434	3.7491	3.7365	3.7434	3.7537		
1.51		3.7860	3.7709	3.6784	3.7883	3.7582	3.7977	3.7525	3.8130	3.7698		
2.02		4.6340	4.6236	4.5145	4.6379	4.6054	4.6471	4.5964	4.6642	4.6158		
2.02		4.5331	4.5658	4.5646	4.5862	4.5964	4.5977	4.5926	4.5952	4.6171		
PVP 1000												
0.0149		1.0428	1.0955	1.1527	1.2736	1.3265	1.3968	1.4857	1.5306	1.5804	1.5521	
0.0284		1.0933	1.1436	1.2012	1.3228	1.3730	1.4423	1.5311	1.5749	1.6235	1.6022	
0.0546		1.2031	1.2529	1.3155	1.4399	1.4821	1.5481	1.6358	1.6778	1.7246	1.7015	
0.0546		1.2129	1.2636	1.3214	1.4488	1.4941	1.5601	1.6504	1.6918	1.7408	1.7186	
0.0837		1.3588	1.4064	1.4673	1.6017	1.6359	1.7012	1.7872	1.8280	1.8752	1.8513	
0.0837		1.3518	1.3986	1.4569	1.5920	1.6288	1.6944	1.7826	1.8221	1.8727	1.8453	
0.112		1.5009	1.5480	1.6088	1.7505	1.7778	1.8428	1.9293	1.9667	2.0181	1.9851	
0.112		1.5105	1.5580	1.6148	1.7573	1.7879	1.8507	1.9392	1.9770	2.0311	1.9977	
0.140		1.6540	1.7486	1.7567	1.9062	1.9274	1.9900	2.0777	2.1131	2.1657	2.1289	
0.140		1.6555	1.7546	1.7638	1.9126	1.9327	1.9949	2.0811	2.1159	2.1682	2.1246	
PVP 1000FL												
0.0201		1.0786		1.1780	1.2471	1.3226	1.3818		1.4912	1.5175	1.5374	1.5729
0.0401		1.1721		1.2696	1.3432	1.4147	1.4734		1.5811	1.6052	1.6252	1.6573
0.0600		1.2815		1.3757	1.4491	1.5174	1.5757		1.6825	1.7060	1.7259	1.7601
0.0600		1.2883		1.3795	1.4538	1.5226	1.5787		1.6895	1.7036	1.7320	1.7690
0.0800		1.4109		1.5006	1.5772	1.6424	1.7002		1.8088	1.8239	1.8514	1.8873
0.0800		1.4015		1.4927	1.5700	1.6354	1.6936		1.7998	1.8229	1.8420	1.8754
0.0999		1.5194		1.6058	1.6828	1.7452	1.8008		1.9081	1.9243	1.9488	1.9854
0.0999		1.5110		1.5717	1.6773	1.7396	1.7965		1.9005	1.9239	1.9427	1.9757
0.149		1.8030		1.8441	1.9625	2.0166	2.0702		2.1686	2.1905	2.2065	2.2390
0.149		1.8162		1.8942	1.9717	2.0257	2.0770		2.1787	2.1969	2.2174	2.2557

perse polymer, and  $\xi_i$  is the mass fraction of (monodisperse) component  $i$  of the polydisperse polymer.

A similar derivation with fixed temperature and fixed chemical potential  $\mu_1$  of the solvent (instead of a fixed or neglected pressure) leads to an expression for the osmotic pressure  $\pi^*$  of a solution of a polydisperse polymer (cf. Kurata<sup>6</sup>):

$$\frac{\pi^*}{RT} = c_s \left( \frac{1}{M_n} + A_2^{\text{osm}} c_s + A_3^{\text{osm}} c_s^2 + \dots \right) \quad (11)$$

The basic equation for the evaluation of laser-light-scattering data in multicomponent systems is (cf. Stockmayer;<sup>7</sup> Kirkwood and Goldberg;<sup>8</sup> Kurata<sup>6</sup>)

$$\frac{Kc_s}{R_\Theta^E} = \frac{1}{M_w P_\Theta} + 2A_2^{\text{LS}} c_s + 3A_3^{\text{LS}} c_s^2 + \dots \quad (12)$$

$K$  is the optical constant:

$$K = \frac{4\pi^4 n_1^2 \left( \frac{\partial n}{\partial c_s} \right)^2}{N_A \lambda^4} \quad (13)$$

$R_\Theta^E$  is the excess Rayleigh ratio, which accounts primarily for the difference between the intensity of light scattered

at an angle  $\theta$  from the polymer solution and the intensity of that scattered from the pure solvent, and  $M_w$  is the mass-average molecular mass of the polymer. The particle scattering function  $P_\theta$  describes the angular dependence of the Rayleigh ratio.  $P_\theta$  is the ratio of the excess Rayleigh ratios at the angle of observation  $\theta$ , that is,  $R_\Theta^E$ , and at  $\theta = 0$ , that is,  $R_{\Theta=0}^E$  (cf. Kratochvil<sup>9</sup>):

$$P_\theta = \frac{R_\Theta^E}{R_{\Theta=0}^E} \quad (14)$$

As discussed before by Kany et al.,<sup>2</sup>  $P_\theta$  was approximated by

$$P_\theta = 1 + \Lambda_1 \sin^4(\Theta/2) \quad (15)$$

where  $\Lambda_1$  was considered to be an adjustable parameter characterizing each polydisperse polymer sample. However, eq 15 was only used to extrapolate the experimental laser-light-scattering results to  $\theta = 0$ . Therefore, the parameters  $\Lambda_1$  are not given here; they are available elsewhere.<sup>4</sup>  $M_w$ ,  $A_2^{\text{LS}}$ , and  $A_3^{\text{LS}}$  were determined from the experimental (i.e. extrapolated) numbers for  $R_{\Theta=0}^E$  using eq 12.  $A_2^{\text{LS}}$  and  $A_3^{\text{LS}}$  are the light-scattering second and third virial coefficients, respectively. These virial coefficients are related to  $A_{ij}$  and

**Table 6. Experimental Results for the Excess Rayleigh Ratio at 333.15 K**

$100c_s/\text{g}\cdot\text{cm}^{-3}$	$10^4(K_{C_s}/R_C^E)/\text{mol}\cdot\text{g}^{-1}$											
	$\Theta = 44.5^\circ$	$\Theta = 54.0^\circ$	$\Theta = 64.9^\circ$	$\Theta = 77.1^\circ$	$\Theta = 90.0^\circ$	$\Theta = 102.9^\circ$	$\Theta = 115.1^\circ$	$\Theta = 126.0^\circ$	$\Theta = 135.5^\circ$	$\Theta = 143.8^\circ$	$\Theta = 151.3^\circ$	$\Theta = 158.2^\circ$
PVP 10												
0.378	1.0312	1.0276	1.0383	1.0529	1.0312	1.0276	1.0206	1.0312	1.0103	0.9741	1.0069	0.9145
0.727	1.0592	1.0572	1.0670	1.0852	1.0651	1.0592	1.0514	1.0651	1.0438	1.0161	1.0592	0.9043
1.44	1.2437	1.2263	1.2356	1.2423	1.2276	1.2119	1.2106	1.2171	1.2042	1.1684	1.2289	1.1212
2.16	1.3054	1.2829	1.2896	1.2965	1.2829	1.2639	1.2639	1.2686	1.2602	1.2197	1.2781	1.1891
3.62	1.5201	1.4931	1.5002	1.5065	1.4923	1.4679	1.4709	1.4731	1.4664	1.4212	1.4854	1.3709
4.35	1.6426	1.6119	1.6179	1.6263	1.6111	1.5844	1.5866	1.5895	1.5837	1.5363	1.6043	1.5100
4.83	1.7204	1.6900	1.6952	1.7051	1.6870	1.6599	1.6620	1.6664	1.6584	1.6122	1.6811	1.6021
PVP 50												
0.206	2.0712	2.0414	2.0022	2.0256	1.9920	2.0177		2.0203	2.0203	2.1450		2.2565
0.397	2.1759	2.2224	2.2290	2.2676	2.2778	2.2917		2.2727	2.2917	2.2143		1.9037
0.397	2.3599	2.2987	2.2761	2.2813	2.2625	2.2727		2.2830	2.3110	2.4186		2.8592
0.611	2.5911	2.5248	2.4949	2.4989	2.4723	2.4829		2.4909	2.5179	2.6383		2.9411
0.611	2.4069	2.4347	2.4424	2.4697	2.4922	2.4922		2.4816	2.5221	2.4194		2.0486
0.812	2.7480	2.6683	2.6398	2.6409	2.6196	2.6263		2.6364	2.6776	2.7803		3.0865
0.812	2.5481	2.5672	2.5822	2.6063	2.6409	2.6352		2.6319	2.6823	2.5651		2.1803
1.02	3.0459	2.9564	2.9152	2.9163	2.8762	2.8880		2.9010	2.9552	3.0921		3.1968
1.02	2.8645	2.8709	2.8773	2.8837	2.9196	2.9010		2.8891	2.9575	2.8155		2.3729
2.03	3.8835	3.8747	3.9081	3.8913	3.9573	3.9200		3.9061	4.0087	3.8048		3.1910
PVP 1000												
0.0322	1.0897	1.1085	1.1395	1.2264	1.2632	1.3349		1.4628	1.4950	1.6113		1.6482
0.0322	1.0586	1.0878	1.1306	1.2240	1.2764	1.3408		1.4584	1.5051	1.5628		1.6018
0.0458	1.1698	1.1910	1.2229	1.3129	1.3538	1.4156		1.5262	1.5746	1.6392		1.6619
0.0458	1.1730	1.1890	1.2190	1.3085	1.3439	1.4167		1.5452	1.5824	1.6976		1.7383
0.0644	1.2632	1.2831	1.3148	1.4117	1.4510	1.5182		1.6372	1.6898	1.7667		1.8200
0.0816	1.3480	1.3584	1.3829	1.4752	1.5064	1.5697		1.6860	1.7429	1.8207		1.8573
0.0816	1.3608	1.3668	1.3907	1.4819	1.5089	1.5785		1.7040	1.7473	1.8612		1.8902
0.122	1.5753	1.5755	1.5937	1.6906	1.7083	1.7768		1.9024	1.9480	2.0662		2.1076
0.122	1.5681	1.5691	1.5879	1.6826	1.7049	1.7650		1.8819	1.9452	2.0278		2.0502
PVP 1000FL												
0.0165	1.1921	1.2053	1.2467	1.2937	1.4051	1.4376	1.5321	1.5651	1.6296	1.5880		1.5429
0.0328	1.2858	1.3020	1.3543	1.4064	1.5121	1.5400	1.6381	1.6666	1.7264	1.6795		1.6433
0.0328	1.2910	1.3192	1.3810	1.4569	1.5409	1.5822	1.6741	1.7128	1.7568	1.7150		1.6817
0.0489	1.3349	1.3626	1.4249	1.5023	1.5867	1.6268	1.7193	1.7584	1.8018	1.7584		1.7371
0.0489	1.3895	1.4026	1.4576	1.5123	1.6186	1.6455	1.7434	1.7745	1.8325	1.7819		1.7576
0.0654	1.4352	1.4497	1.5045	1.5621	1.6641	1.6913	1.7896	1.8211	1.8773	1.8276		1.8122
0.0654	1.4040	1.4312	1.4936	1.5712	1.6551	1.6936	1.7872	1.8256	1.8698	1.8237		1.8040
0.0825	1.5011	1.5125	1.5681	1.6264	1.7266	1.7526	1.8510	1.8809	1.9390	1.8847		1.8717
0.0825	1.4630	1.4898	1.5517	1.6308	1.7139	1.7507	1.8452	1.8825	1.9287	1.8787		1.8717
0.123	1.6381	1.6611	1.7216	1.8040	1.8839	1.9166	2.0134	2.0485	2.0962	2.0404		2.0238

**Table 7. Osmotic Pressure  $\pi^*$  at 303.15 K from Membrane Osmometry**

PVP 50		PVP 1000		PVP 1000FL	
$100\xi_s$	$\pi^*$	$100\xi_s$	$\pi^*$	$100\xi_s$	$\pi^*$
$\text{g}\cdot\text{g}^{-1}$	Pa	$\text{g}\cdot\text{g}^{-1}$	Pa	$\text{g}\cdot\text{g}^{-1}$	Pa
0.524	$601_{-13}^{+11}$	1.955	$684_{-12}^{+12}$	0.478	$107^a$
0.894	$1052_{-15}^{+16}$	2.076	$819_{-17}^{+16}$	0.969	$198_{-4}^{+3}$
2.116	$2873_{-5}^{+4}$	2.912	$1536_{-17}^{+16}$	0.982	$272^a$
2.801	$4244_{-44}^{+49}$	2.955	$1637^a$	1.076	$302_{-8}^{+10}$
		4.001	$3296_{-26}^{+25}$	1.918	$799^a$
				1.966	$817_{-25}^{+17}$
				2.070	$893_{-25}^{+17}$
				2.943	$1792^a$
				3.116	$1897^a$
				3.915	$3027^a$

<sup>a</sup> Only a single data point.**Table 8. Osmotic Pressure  $\pi^*$  at 333.15 K from Membrane Osmometry**

PVP 1000		PVP 1000FL	
$100\xi_s$	$\pi^*$	$100\xi_s$	$\pi^*$
$\text{g}\cdot\text{g}^{-1}$	Pa	$\text{g}\cdot\text{g}^{-1}$	Pa
0.626	$127_{-4}^{+3}$	0.582	$154_{-17}^{+10}$
1.027	$250_{-1}^{+2}$	0.948	$264_{-6}^{+7}$
2.076	$723_{-11}^{+11}$	2.088	$819_{-33}^{+32}$
		2.961	$1567_{-47}^{+47}$

 $A_{ijk}$  of eqs 9 and 10 through

$$A_2^{\text{LS}} = \frac{1}{M_w^2} \sum_{i=2}^N \sum_{j=2}^N \xi_i \xi_j M_i M_j A_{ij} \quad (16)$$

and

$$A_3^{\text{LS}} = \frac{1}{M_w^3} \sum_{i=2}^N \sum_{j=2}^N \sum_{k=2}^N \xi_i \xi_j \xi_k M_i M_j A_{ijk} - \frac{4}{3M_w^3} \sum_{i=2}^N \sum_{j=2}^N \sum_{k=2}^N \sum_{l=2}^N \xi_i \xi_j \xi_k \xi_l M_i M_j M_k M_l (A_{ij} A_{jk} - A_{ik} A_{jl}) \quad (17)$$

Light-scattering virial coefficients  $A_2^{\text{LS}}$  and  $A_3^{\text{LS}}$  differ from osmotic virial coefficients  $A_2^{\text{osm}}$  and  $A_3^{\text{osm}}$  only for polydisperse polymers, whereas there is no such difference for monodisperse polymers.

**Pseudocomponents.** The molecular mass distribution of each PVP sample was approximated by eight pseudocomponents. The molecular mass and the mass fraction of each pseudocomponent were determined applying the same method as in previous investigations on DEX.<sup>2</sup> The results are given in Table 11.

**Simultaneous Evaluation of Laser-Light-Scattering, Membrane Osmometric, and Isopiestic Data.** Experimental data from laser-light-scattering experiments,

**Table 9. Activity of Water  $a_1$  from Isopiestic Investigations**

$a_1$	278.15 K		$a_1$	293.15 K		$a_1$	333.15 K	
	$\xi_s/g \cdot g^{-1}$			$\xi_s/g \cdot g^{-1}$			$\xi_s/g \cdot g^{-1}$	
	PVP 10	PVP 50		PVP 10	PVP 50		PVP 10	PVP 50
0.9825	0.3506		0.9942	0.2489	0.2639	0.9829	0.4435	0.4498
0.9813	0.3736	0.3826	0.9888	0.3363	0.3464	0.9811		0.4505
0.9789	0.3998	0.3989	0.9884	0.3500		0.9791		0.4670
0.9774	0.4000		0.9883	0.3356	0.3362	0.9783		0.4961
0.9797		0.4017	0.9874		0.3466	0.9772	0.4934	0.4931
0.9769		0.4237	0.9868	0.3526	0.3577	0.9753	0.5029	
0.9735	0.4098	0.4146	0.9865		0.3579	0.9751		0.5170
0.9731	0.4202	0.4233	0.9823	0.3917	0.3990	0.9716	0.5398	
			0.9818		0.3874			

**Table 10. Density of Aqueous Solutions of Poly(pyrrolidone)**

	$\xi_a/g \cdot g^{-1}$	$\rho^*/g \cdot cm^{-3}$			
		278.15 K	293.15 K	333.15 K	
PVP 10	0.0052	1.0011			
	0.0103	1.0022			
	0.0124		1.0005	0.9865	
	0.0252	1.0055			
	0.0288		1.0044	0.9945	
	0.0484	1.0107			
	0.0563		1.0106	0.9946	
	0.0918	1.0205			
	0.0940		1.0187	1.0025	
	0.1884		1.0399	1.0223	
	0.1957	1.0446			
	0.2979	1.0705			
	0.3728		1.0859	1.0652	
	0.0010		1.004	0.9854	
	PVP 50	0.0061	1.0013		
0.0128		1.0028			
0.0200		1.0044			
0.0295			1.0047	0.9895	
0.0436			1.0081	0.9926	
0.0491		1.0109			
0.0993			1.0208	1.0047	
0.1034		1.0234			
0.1886		1.0441			
0.1975			1.0432	1.0261	
0.2899		1.0701			
0.3890			1.0919	1.0734	
PVP 1000		0.0051	1.0012		
		0.0061		0.9996	
		0.0100	1.0023		
	0.0113		1.0007	0.9557	
	0.0201	1.0041			
	0.0263		1.0040	0.9889	
	0.0483	1.0113			
	0.0513		1.0084	0.9947	
	0.0945		1.0204	1.0044	
	0.2000		1.0453		

membrane osmometry (both at low polymer concentrations), and isopiestic measurements (at high polymer concentrations) were simultaneously evaluated to determine the number- and weight-average molecular masses as well as the second and third virial coefficients of PVP in aqueous solution. In a procedure similar to that described before for DEX,<sup>2</sup> the pure component virial coefficients  $A_{ii}$  and  $A_{iii}$  were expressed by two-parametric empirical expressions:

$$A_{ii} = \alpha_2 M_i^{\beta_2} \quad (18)$$

and

$$A_{iii} = \alpha_3 M_i^{\beta_3} \quad (19)$$

where  $\alpha_j$  and  $\beta_j$  ( $j = 2$  or  $3$ ) are constants. Thus, it is possible to describe solutions of polydisperse polymers either in the

common way (i.e. neglecting the influence of polydispersity by setting  $\beta_2 = \beta_3 = 0$ ) or by taking that influence into account. When the influence of polydispersity is taken into account, mixed virial coefficients (between polymers differing only in molecular weight) are required. These mixed virial coefficients were approximated using geometric mixing rules:

$$A_{ij} = (A_{ii}A_{jj})^{1/2} \quad (20)$$

$$A_{ijk} = (A_{iii}A_{jjj}A_{kkk})^{1/3} \quad (21)$$

The experimental results were evaluated using two different methods. Method I assumes that  $A_{ii}$  and  $A_{iii}$  depend on the molecular mass of PVP, whereas method II assumes that  $A_{ii}$  and  $A_{iii}$  do not depend on the molecular mass of PVP. As shown before,<sup>1,2</sup> in an evaluation with method II, the number-average and weight-average molecular masses of each polymer sample should not be taken from the GPC experiments (cf. Figure 2) but have to be treated as unknown adjustable parameters. In an evaluation according to method I, the molecular mass distribution has to be known a priori. In such evaluations the pseudocomponent mass fractions were taken from Table 11 and used in eqs 6 and 7 as well as in eqs 16 and 17. The influence of temperature on  $A_{ii}$  and  $A_{iii}$  was expressed by the following empirical equation for  $\alpha_2$  and  $\alpha_3$ :

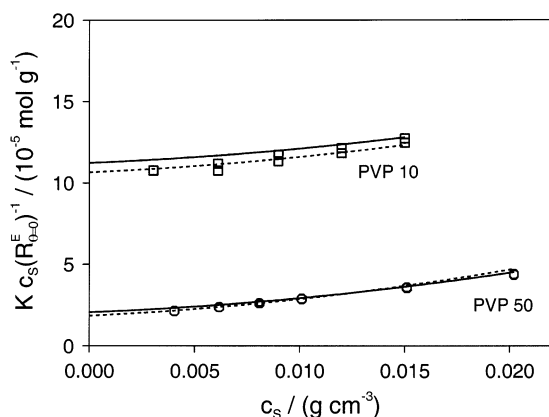
$$\alpha_j = \alpha_j(T) = \alpha_j^{(0)} \left( \frac{1}{T} - \frac{1}{T_\Theta} \right) \quad (j = 2, 3) \quad (22)$$

where  $T_\Theta$  is the temperature where all osmotic virial coefficients are zero.

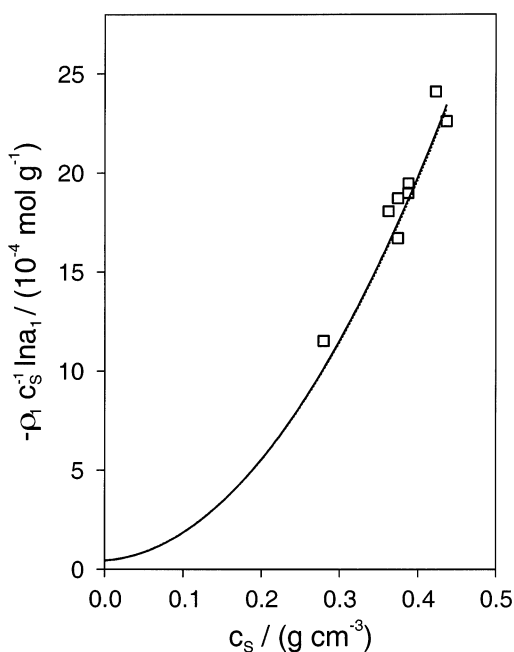
The remaining unknown parameters ( $\alpha_2^{(0)}$ ,  $\alpha_3^{(0)}$ ,  $\beta_2$ ,  $\beta_3$ ,  $T_\Theta$ , and  $\Lambda_{1,j}$  ( $j = \text{PVP10, PVP 50, PVP 1000, and PVP 1000FL}$ )) were fitted to the experimental data by minimizing an objective function as described by Kany et al.<sup>2</sup> The results of both evaluations confirm the previously published results for aqueous solutions of PEG<sup>1</sup> and of DEX.<sup>2</sup> Both methods allow for an equally good description of the experimental data. Typical comparisons between experimental data and both correlations are shown in Figures 3–5. Figure 3 shows a comparison for laser-light-scattering data (Rayleigh ratios  $Kc_s/R_\Theta^E$  extrapolated to zero scattering angle) for PVP 10 and PVP 50. Figures 4 and 5 show similar comparisons for the reduced water activity ( $-\rho_1 \ln a_1/c_s$ ) in aqueous solutions of PVP 50 at 293.15 K and 303.15 K from isopiestic investigations (Figure 4) and from membrane osmometry, respectively. Table 2 gives the mass-average and number-average molecular masses determined with a GPC as well as from the laser-light-scattering and (isopiestic experiments and membrane osmometry) applying both evaluation methods. The polydispersity of the samples increases with increasing molec-

**Table 11. Pseudocomponents for Poly(vinylpyrrolidone) Samples**

PVP 10		PVP 50		PVP 1000		PVP 1000FL	
$M_i$	$\xi/\text{g}\cdot\text{g}^{-1}$	$M_i$	$\xi/\text{g}\cdot\text{g}^{-1}$	$M_i$	$\xi/\text{g}\cdot\text{g}^{-1}$	$M_i$	$\xi/\text{g}\cdot\text{g}^{-1}$
446	0.0055	2 291	0.0137	37 120	0.0176	6 403	0.0079
748	0.0289	3 810	0.0492	61 370	0.0527	12 810	0.0248
1 582	0.1289	8 850	0.1608	137 200	0.1331	37 790	0.0734
4 041	0.3482	23 410	0.3248	362 300	0.2718	144 000	0.1890
10 180	0.3405	64 200	0.2917	999 200	0.3251	540 000	0.3280
24 740	0.1255	169 900	0.1415	2 362 000	0.1704	1 836 000	0.2949
51 550	0.0209	324 600	0.0182	5 081 000	0.0275	4 576 000	0.0767
82 350	0.0016	606 600	0.0001	8 256 000	0.0018	8 803 000	0.0052

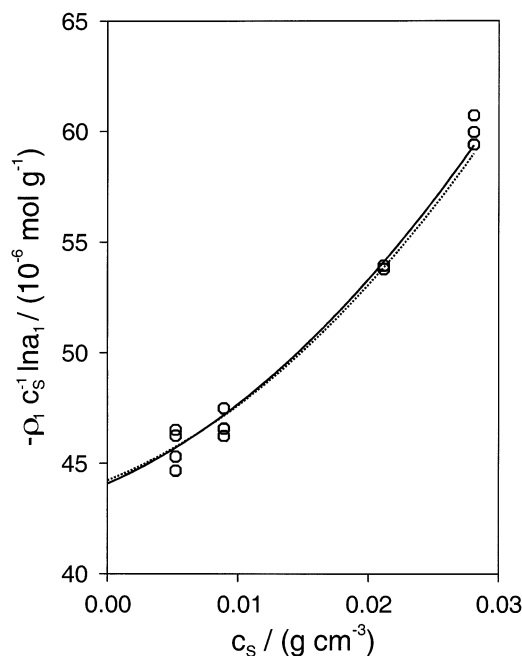


**Figure 3.** Experimental results of laser-light-scattering experiments of aqueous solutions of poly(vinylpyrrolidone) samples at 293.15 K:  $\square$ , PVP 10;  $\circ$ , PVP 50; dashed line, correlation by “method I”; full line, correlation by “method II”. Both correlations give nearly the same results.



**Figure 4.** Reduced activity of water in aqueous solutions of PVP 50 at 293.15 K:  $\square$ , from isopiestic investigations; dashed line, correlation by “method I”; full line, correlation by “method II”. Both correlations give nearly the same results.

ular mass from about 1.8 (for PVP 10) to 9.3 (for PVP 1000). The experimental results for the mass-average molecular mass scatter by about  $\pm 10\%$ . For 293 K, the numerical evaluation by “method I” (i.e. assuming that the virial coefficients depend on molecular mass) gives for the second virial coefficient  $2.33 \leq (A_{22}/(10^{-4} \text{ mol}\cdot\text{cm}^3\cdot\text{g}^{-2})) \leq 2.97$  and for the third virial coefficient  $0.51 \leq (A_{222}/(10^{-2} \text{ mol}\cdot\text{cm}^6\cdot\text{g}^{-3}))$



**Figure 5.** Reduced activity of water in aqueous solutions of PVP 50 at 303.15 K:  $\square$ , from isopiestic investigations; dashed line, correlation by “method I”; full line, correlation by “method II”.

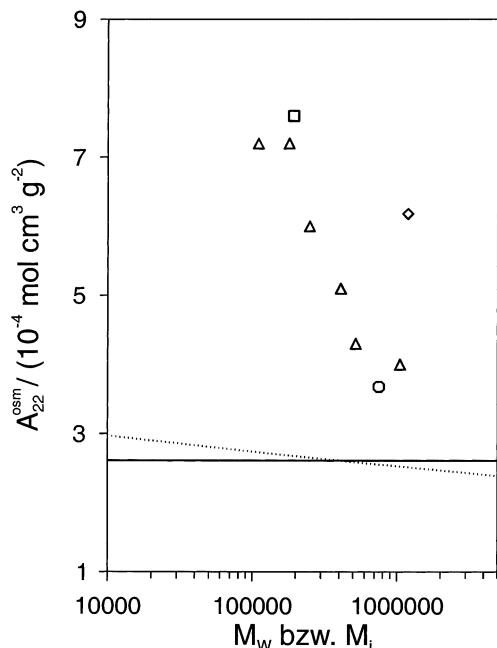
$\leq 0.74$  for  $10^4 \leq M \leq 10^7$ , where with increasing molecular mass  $A_{22}$  as well as  $A_{222}$  decreases. The influence of the molecular mass on  $A_{22}$  as well as on  $A_{222}$  is rather small. Therefore, it is not surprising that the evaluation by “method II” (i.e. assuming that the virial coefficients do not depend on molecular mass) represents the experimental data as well. Therefore, there is no need to assume that neither  $A_{22}$  nor  $A_{222}$  depend on molecular mass. These results are in accordance with previous findings for aqueous solutions of PEG<sup>1</sup> and DEX.<sup>2</sup> It is furthermore confirmed by the finding that both methods give nearly the same number for  $T_\Theta$  (method I,  $T_\Theta = 446$  K; method II,  $T_\Theta = 442.5$  K). Neglecting the influence of molecular mass on  $A_{22}$  and  $A_{222}$  gives for temperatures between 278 and 333 K

$$A_2^{\text{osm}} = A_{22}; \quad A_2^{\text{osm}}/\text{mol}\cdot\text{cm}^3\cdot\text{g}^{-2} = 0.227\left(\frac{1}{T/\text{K}} - \frac{1}{442.5}\right) \quad (23)$$

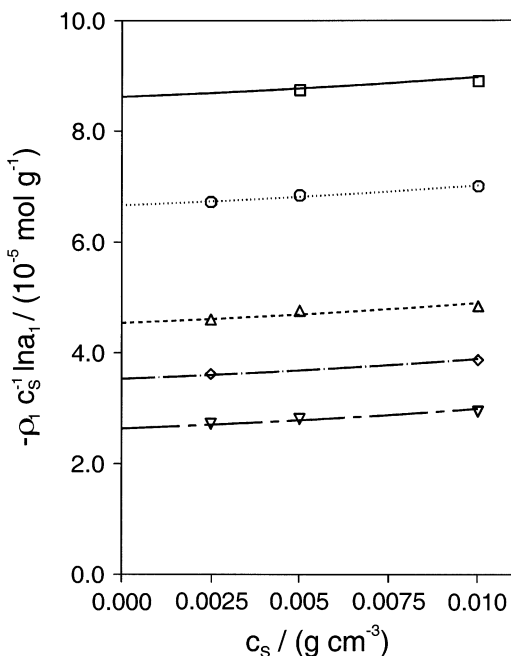
and

$$A_3^{\text{osm}} = A_{222}; \quad A_3^{\text{osm}}/\text{mol}\cdot\text{cm}^6\cdot\text{g}^{-3} = 9.949\left(\frac{1}{T/\text{K}} - \frac{1}{442.5}\right) \quad (24)$$

resulting, for example, for 293 K in  $A_2^{\text{osm}} = 2.62 \times 10^{-4} \text{ mol}\cdot\text{cm}^3\cdot\text{g}^{-2}$  and  $A_3^{\text{osm}} = 1.15 \times 10^{-2} \text{ mol}\cdot\text{cm}^6\cdot\text{g}^{-3}$ .



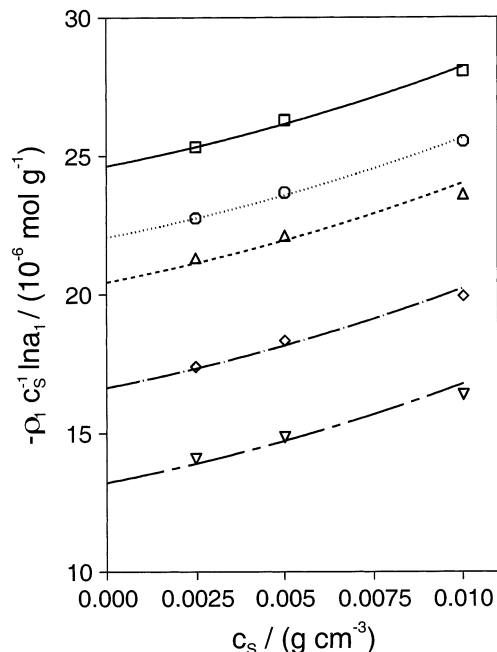
**Figure 6.** Second osmotic virial coefficient  $A_2^{\text{osm}}$  of poly(vinylpyrrolidone) in water at around 300 K:  $\diamond$ , at 295.15 K from Edsman and Sundelöf;<sup>11</sup>  $\square$ , at 303.15 K from Hefford;<sup>12</sup>  $\triangle$ , at 298.15 K from Nakayama;<sup>13</sup>  $\circ$ , at 293.15 K from Nordmeier;<sup>14</sup> dashed line, this work applying "method I"; full line, this work applying "method II. Both methods are performed at 293.15 K.



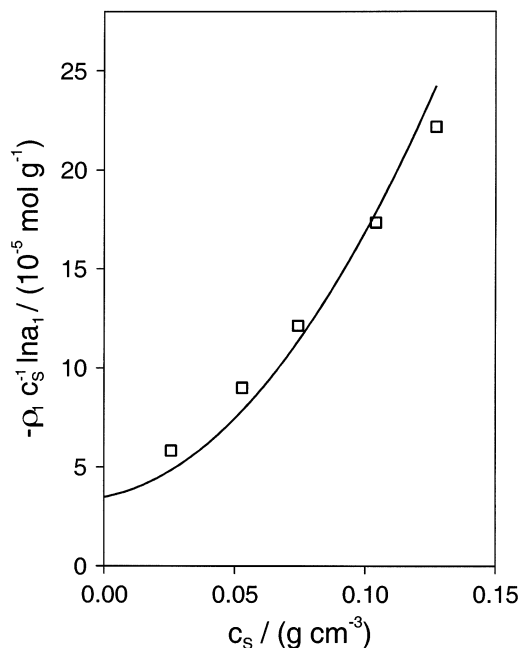
**Figure 7.** Reduced activity of water in aqueous solutions of poly(vinylpyrrolidone) at 298.15 K. Experimental results by Hengstenberg and Schuch<sup>10</sup> for PVP 12 ( $\square$ ), PVP 15 ( $\circ$ ), PVP 22 ( $\triangle$ ), PVP 28 ( $\diamond$ ), and PVP 38 ( $\nabla$ ). Lines are predictions assuming that the osmotic virial coefficients do not depend on molecular mass.

### Comparison with Literature Data

Figure 6 shows a comparison between literature data for the second osmotic virial coefficient of PVP in water at temperatures around 300 K and the results of the present work (for 293 K). This comparison is very similar to that for PEG<sup>1</sup> and for DEX:<sup>2</sup> the very limited literature data scatter extremely and reveal a strong influence of the polymer molecular mass. However, and as already stated



**Figure 8.** Reduced activity of water in aqueous solutions of poly(vinylpyrrolidone) at 298.15 K. Experimental results by Hengstenberg and Schuch<sup>10</sup> for PVP 41 ( $\square$ ), PVP 46 ( $\circ$ ), PVP 49 ( $\triangle$ ), PVP 60 ( $\diamond$ ), and PVP 75 ( $\nabla$ ). Lines are predictions assuming that the osmotic virial coefficients do not depend on molecular mass.



**Figure 9.** Reduced activity of water in aqueous solutions of PVP 90 at 298.15 K:  $\square$ , experimental results by Vink;<sup>3</sup> line, prediction assuming that the osmotic virial coefficients do not depend on molecular mass.

previously, the reliability of the literature data is questionable mainly for two reasons. First, second virial coefficients were determined from measurements using a single experimental procedure in a rather limited concentration range, and second, in the evaluation of the experimental data both the polydispersity of the polymer samples and the third virial coefficient were neglected. Therefore, it is more reasonable to compare direct experimental data (instead of derived properties such as the second osmotic virial coefficient) with the correlation of the present work. Such a comparison is possible with the experimental



results for the activity of water in aqueous solutions of several poly(vinylpyrrolidone) samples by Hengstenberg and Schuch<sup>10</sup> and by Vink.<sup>3</sup> Hengstenberg and Schuch<sup>10</sup> reported results of experimental investigations of ten PVP samples by membrane osmometry at 298 K at polymer mass fractions up to 0.01 g·cm<sup>-3</sup>. For comparison with the correlation of the present work, the molecular mass of the polymer samples was taken from ref 10 and the activity of water was calculated with osmotic virial coefficients as given by eqs 23 and 24 (i.e.,  $A_2^{\text{osm}} = 2.48 \times 10^{-4} \text{ mol}\cdot\text{cm}^3\cdot\text{g}^{-2}$  and  $A_3^{\text{osm}} = 1.09 \times 10^{-2} \text{ mol}\cdot\text{cm}^6\cdot\text{g}^{-3}$ ). As shown in Figures 7 and 8, the predictions based on the correlation of the present work agree excellently with the experimental data. A similar comparison (cf. Figure 9) with the experimental data by Vink<sup>3</sup> for aqueous solutions of PVP 90 (at polymer concentrations up to nearly 0.15 g·cm<sup>-3</sup>) also reveals a good agreement (adopting Vink's numerical value for the molecular mass of the PVP sample:  $M_n = 28\,600$ ), although the experimental data (for the reduced water activity) do not depend as strongly on the polymer concentration as the predictions.

### Conclusions

The results of experimental investigation of aqueous solutions of several polydisperse PVP samples varying in the mass-average molecular mass between about 9 000 and 1 200 000 by laser-light-scattering, membrane osmometry, and isopiestic measurements at temperatures between (278 and 333) K were simultaneously evaluated to determine the second and third osmotic virial coefficients of poly(vinylpyrrolidone) in pure water. The results confirm the previous findings for aqueous solutions of the single polymers poly(ethylene glycol) and dextran, that the thermodynamic properties of such solutions can be accurately described by the osmotic virial equation neglecting the influence of the polymer molecular mass on the osmotic virial coefficients.

### Nomenclature

$A_{ij}$  = second virial coefficient for interactions between species  $i$  and  $j$   
 $A_{ijk}$  = third virial coefficient for interactions between species  $i$ ,  $j$ , and  $k$   
 $A_2^{\text{osm}}$  = second osmotic virial coefficient of solute 2  
 $A_3^{\text{osm}}$  = third osmotic virial coefficient of solute 2  
 $A_2^{\text{LS}}$  = light-scattering second osmotic virial coefficient of solute 2  
 $A_3^{\text{LS}}$  = light-scattering third osmotic virial coefficient of solute 2  
 $a_1$  = activity of water  
 $a_{ij}$  = partial derivative of  $\ln \gamma_i$  with respect to  $c_j$   
 $a_{ijk}$  = partial derivative of  $\ln \gamma_i$  with respect to  $c_j$  and  $c_k$   
 $c$  = mass density  
 DEX = dextran  
 GPC = gel permeation chromatography  
 ISO = isopiestic experiment  
 $K$  = optical constant  
 LLS = laser-light-scattering  
 $M_n$  = number-average molecular mass  
 $M_w$  = mass-average molecular mass  
 $m$  = amount of mass  
 MO = membrane osmometry  
 $N$  = number of components  
 $N_A$  = Avogadro's number  
 $n$  = refractive index of the solution  
 $n_1$  = refractive index of water

$P$  = polydispersity  
 $P_\Theta$  = normalized Rayleigh ratio  
 PEG = poly(ethylene glycol)  
 PVP = poly(vinylpyrrolidone)  
 PVP(aq) = aqueous solution of poly(vinylpyrrolidone)  
 $R$  = universal gas constant  
 $R_\Theta^E$  = excess Rayleigh ratio  
 $T$  = absolute temperature  
 $T_\Theta$  =  $\Theta$ -temperature ( $A_2^{\text{osm}} = A_3^{\text{osm}} = 0$ )  
 $V$  = volume

### Greek Letters

$\alpha_2, \alpha_3$  = parameters describing the influence of the molecular mass on the second and third virial coefficients  
 $\alpha_j^{(0)}$  ( $j = 2$  or  $3$ ) = parameters describing the influence of temperature on the second and third virial coefficients  
 $\beta_2, \beta_3$  = parameters describing the influence of the molecular mass on the second and third virial coefficients  
 $\Theta$  = scattering angle  
 $\gamma_i$  = activity coefficient of species  $i$  (on mass density scale)  
 $\Lambda_1$  = adjustable parameter  
 $\lambda$  = laser wavelength (=633 nm)  
 $\mu_1$  = chemical potential of water  
 $\pi^*$  = osmotic pressure  
 $\rho_1$  = density of water  
 $\rho^*$  = specific density of aqueous solution

### Subscripts

$i, j, k$  = components  $i, j, k$   
 $s$  = total solute (polymer)  
 $w$  = water

### Literature Cited

- (1) Hasse, H.; Kany, H.-P.; Tintinger, R.; Maurer, G. Osmotic virial coefficients of aqueous poly(ethylene glycol) from laser-light scattering and isopiestic measurements. *Macromolecules* **1995**, *28*, 3540–3552.
- (2) Kany, H.-P.; Hasse, H.; Maurer, G. Thermodynamic properties of aqueous dextran solutions from laser-light-scattering, membrane osmometry, and isopiestic measurements. *J. Chem. Eng. Data* **1999**, *44*, 230–242.
- (3) Vink, H. Precision measurements of osmotic pressure in concentrated polymer solutions. *Eur. Polym. J.* **1971**, *13*, 1411–1419.
- (4) Kany, H.-P. Thermodynamische Eigenschaften wässriger Polymerlösungen. Ph.D. Thesis, Universität Kaiserslautern, Kaiserslautern, 1998.
- (5) Großmann, C.; Tintinger, R.; Zhu, J.; Maurer, G. Aqueous two-phase systems of poly(ethylene glycol) and dextran—experimental results and modelling of thermodynamic properties. *Fluid Phase Equilib.* **1995**, *106*, 111–138.
- (6) Kurata, M. *Thermodynamics of Polymer Solutions*; Harwood Academic Publishers: Chur, Switzerland, 1982.
- (7) Stockmayer, W. H. Light scattering in multicomponent systems. *J. Chem. Phys.* **1949**, *18*, 58–61.
- (8) Kirkwood, J. G.; Goldberg, R. J. Light scattering arising from composition fluctuations in multicomponent systems. *J. Chem. Phys.* **1950**, *18*, 54–57.
- (9) Kratochvil, P. *Classical Light Scattering from Polymer Solutions*; Elsevier: Amsterdam, 1987.
- (10) Hengstenberg, J.; Schuch, E. Molekulargewichtsbestimmung von Polyvinylpyrrolidon (PVP) mittels des osmotischen Drucks und der Lichtstreuung ihrer Lösungen. *Makromol. Chem.* **1951**, *7*, 236–258.
- (11) Edsman, K.; Sundelöf, L.-O. Interaction virial coefficients in some mixed polymer solutions. *Polymer* **1988**, *29*, 535–540.
- (12) Hefford, R. J. Polymer mixing in aqueous solution. *Polymer* **1984**, *25*, 979–984.

- (13) Nakayama, H. Temperature dependence of heats of solution of poly(ethylene glycol) and related compounds. *Bull. Chem. Soc. Jpn.* **1970**, *43*, 1683–1687.
- (14) Nordmeier, E. Static and dynamic light-scattering solution behavior of Pullulan and Dextran in comparison. *J. Phys. Chem.* **1993**, *97*, 5770–5785.
- (15) Elias, H.-G. Konstitution und Lösungseigenschaften von Makromolekülen. Ermittlung von  $\Theta$ -Lösungen. *Anal. Chem.* **1961**, *33*, 1–19.
- (16) Nakagaki, M.; Shimabayashi, S.; Yoshida, S.; Saito, M. Light scattering studies of aqueous solutions of poly(vinylpyrrolidone). *Yakugaku Zasshi* **1976**, *96*, 757–763.
- (17) Nordmeier, E.; Lechner, M. D. Light scattering from polymer-mixed systems. 1. Selective adsorption phenomena of poly(N-vinylpyrrolidone). *Macromolecules* **1991**, *24*, 2529–2537.

Received for review November 18, 2002. Accepted February 13, 2003. Financial support by Deutsche Forschungsgemeinschaft, Bad Godesberg, Germany, is gratefully acknowledged.

JE020203Y